

# TTK4130 Modeling and Simulation

## Lecture 1

# TTK4130 Modeling and Simulation

## To learn:

- Formulate mathematical models from first principles
- Simulate models using computer

Main purpose: Control system design/testing/validation,  
hence *dynamic* modeling

## Instructors:

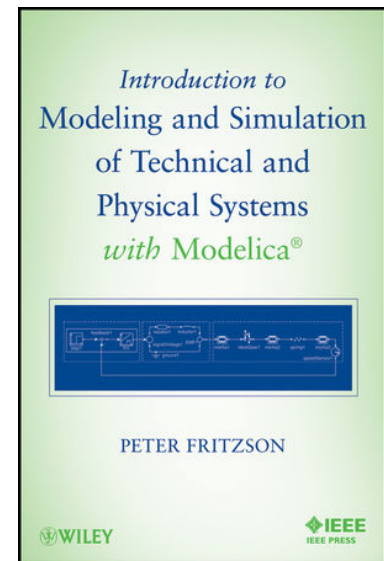
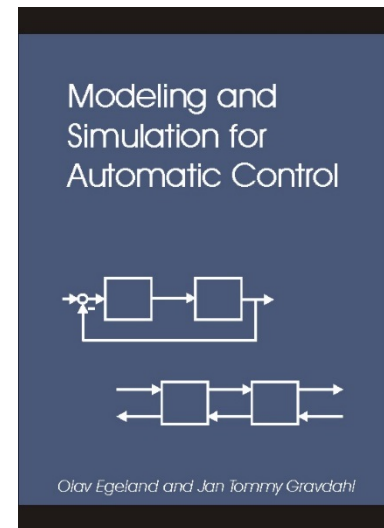
- Lecturer: Leif Erik Andersson
- Teaching assistant: Mikkel Eske Nørgaard Sørensen (D351 A)
  - 4 student assistants

# Course Information

- All course information is provided on Itslearning. There will be no handout of material
- We will not cover the complete curriculum in our lectures; rather focus on the most important and/or difficult parts
- Lectures:
  - Tuesdays 10:15-12:00 (KJL5)
  - Thursdays 8:15-10:00 (EL3)
- Exam:
  - May 15<sup>th</sup>, 2017
  - Examination support code: A (Open book)
- Grading: Exam counts 100%

# Syllabus

- Books:
  - “Modeling and Simulation for Automatic Control”, 2002, by O.Egeland and J.T. Gravdahl (ISBN 82-92356-00-2) **(E)**
    - Errata in itslearning
  - “Introduction to Modeling and Simulation of Technical and Physical Systems with Modelica, 2011, by Peter Fritzson **(F)**



# Lecture schedule

Week	Date	Theme	Literature
2	10.01	Introduction to Modelica	F: 1, 2
	12.01	More introduction. State-space models, transfer functions. Modeling software, network models.	E: 1.1-1.3, 2.1-2.2 (E:1.4-1.5)
3	17.01	Energy functions, passivity	E: 2.3-2.4
	19.01	More passivity	E: 2.4
4	24.01	Modeling of complex systems. Simulation: Order, test system	F: 3, 4, E: 14.1-14.2
	26.01	Explicit Runge-Kutta methods	E: 14.3-14.4
5	31.01	Electrical motors	E: 3.1-3.4
	02.02	Implicit Runge-Kutta methods	E: 14.5
6	07.02	Stability, Padé approximations	E: 14.6
	09.02	Stability, frequency properties, automatic step size adjustment Implementation, BDF and differential-algebraic systems	E: 14.6-14.7 E: 14.8, 14.11, 14.12
7	14.02	Hydraulic motors, transmission lines	E: 4.1-4.6
	16.02	Friction	E: 5
8	21.02	Vectors, dyadics, rotation matrices	E: 6.1-6.4
	23.02	Euler angles, angle axis	E: 6.5-6.6
9	28.02	Euler parameters, angular velocities	E: 6.7-6.8
	02.03	Kinematic differential equations	E: 6.9
10	07.03	Kinematics of a rigid body, Newton-Euler equations of motion	E: 6.12-6.13, 7.3
	09.03	Newton-Euler equations of motion, Modelica.Multibody	E: 7.3
11	14.03	Lagrange equations of motion	E: 7.7, 8.1-8.2
	16.03	Lagrange equations of motion, recap, examples	
12	21.03	Process modelling and balance laws, I	E: 10.4, 11.1-4 (+ slides)
	23.03	Process modelling and balance laws, II	E: 10.4, 11.1-4 (+ slides)
13	28.03	Guest lecture: Erlend Kristiansen, Comsol Multiphysics	
	30.03	No lecture (excursion)	
14	04.04	No lecture (excursion)	
	06.04	No lecture (excursion)	
15	11.04	No lecture (Easter)	
	13.04	No lecture (Easter)	
16	18.04	No lecture (Easter)	
	20.04	Topic: Not decided yet	
17	25.04	Topic: Not decided yet	
	27.04	No lecture (TTK4135 lab.rapport)	
18	02.05	Topic: Not decided yet	
	04.05	Topic: Not decided yet	

E: "Modeling and Simulation for Automatic Control" by O. Egeland and J.T. Gravdahl  
 F: "Introduction to Modeling and Simulation of Technical and Physical Systems with Modelica" by P. Fritzson

# Course information, assignments

- A minimum number of exercises (8 of 11) must be approved to enter the final examination
- The deadlines for all assignments are absolute
  - Schedule:
    - Out: Latest Wednesdays (week before delivery)
    - In: Tuesdays 7 days later – 12:00

# Exercise Schedule

Assignments	Upload	Deadline
<b>1</b>	11/1-17 at 12.00 (noon)	17/1-17 at 12.00 (noon)
<b>2</b>	18/1-17 at 12.00 (noon)	24/1-17 at 12.00 (noon)
<b>3</b>	25/1-17 at 12.00 (noon)	31/1-17 at 12.00 (noon)
<b>4</b>	1/2-17 at 12.00 (noon)	7/2-17 at 12.00 (noon)
<b>5</b>	8/2-17 at 12.00 (noon)	14/2-17 at 12.00 (noon)
<b>6</b>	15/2-17 at 12.00 (noon)	21/2-17 at 12.00 (noon)
<b>7</b>	22/2-17 at 12.00 (noon)	7/3-17 at 12.00 (noon)
<b>8</b>	1/3-17 at 12.00 (noon)	8/3-17 at 12.00 (noon)
<b>9</b>	8/3-17 at 12.00 (noon)	14/3-17 at 12.00 (noon)
<b>10</b>	15/3-17 at 12.00 (noon)	28/3-17 at 12.00 (noon)
<b>11</b>	29/3-17 at 12.00 (noon)	25/4-17 at 12.00 (noon)

Exercise class:

Exercise	Exercise hours	Room
<b>1</b>	16/1-17 8.00-12.00	G124-G128 and G134
<b>2</b>	23/1-17 8.00-12.00	G124-G128 and G134
<b>3</b>	30/1-17 8.00-12.00	G124-G128 and G134
<b>4</b>	6/2-17 8.00-12.00	G124-G128 and G134
<b>5</b>	13/2-17 8.00-12.00	G124-G128 and G134
<b>6</b>	20/2-17 8.00-12.00	G124-G128 and G134
<b>7</b>	27/2-17 8.00-12.00	G124-G128 and G134
<b>8 (7)</b>	6/3-17 8.00-12.00	G124-G128 and G134
<b>9</b>	13/3-17 8.00-12.00	G124-G128 and G134
<b>10</b>	20/3-17 8.00-10.00	KJL2
<b>10</b>	27/3-17 8.00-10.00	KJL2
<b>11</b>	24/4-17 8.00-10.00	KJL2

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5	13/2-17 8.00-12.00	G124-G128 and G134
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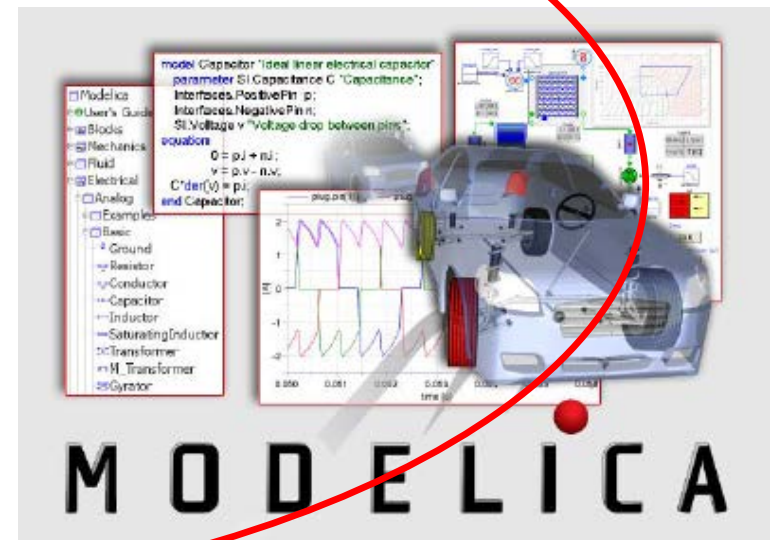
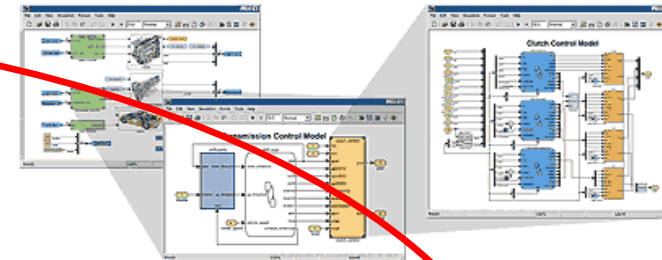
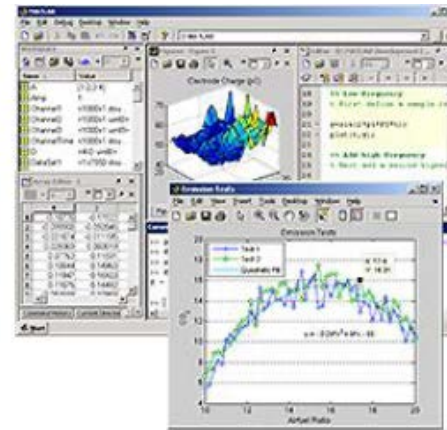


# Course information, assignments

- A minimum number of exercises (8 of 11) must be approved to enter the final examination
- The deadlines for all assignments are absolute
  - Schedule:
    - Out: Latest Wednesdays (week before delivery)
    - In: Tuesdays 7 days later – 12:00
  - One exercise class with assistants present ahead of the deadline for every assignment (Mondays 8:00-12:00, G124-G128 & G134)
  - Several exercises require computers
    - Matlab/Simuling & Dymola
    - Computer lab G124-128 & G134 reserved Mondays 8-12

# Software

- Matlab/Simulink
  - Computer labs
  - Your own computer
  - Some familiarity with Matlab/Simulink is assumed
- Dymola
  - Based on the Modelica modelling language
  - Installed on computer labs, but you can also use your PCs (Windows and Linux)
  - License:
    - License sever (via VPN), but limited number of licenses (50)
    - Much can be done with demo license



# Introduction to Modelica

Slides taken/adapted from Peter Fritzson

# History

- Development from autumn 1996 through person from industry and academics

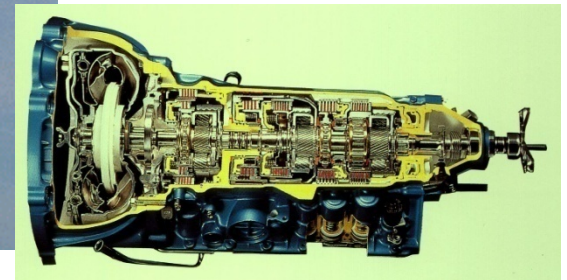
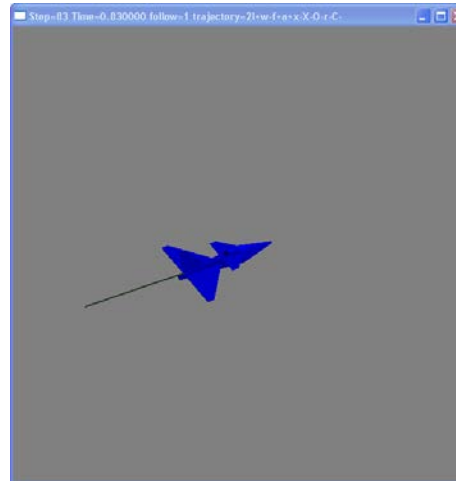


- Modelica 1.0 in September 1997
- At the moment: Modelica 3.3 (2012)

# What is Modelica?

A language for modeling of complex physical systems

- Robotics
- Automotive
- Aircrafts
- Satellites
- Process systems
- Power plants
- Systems biology



# What is Modelica?

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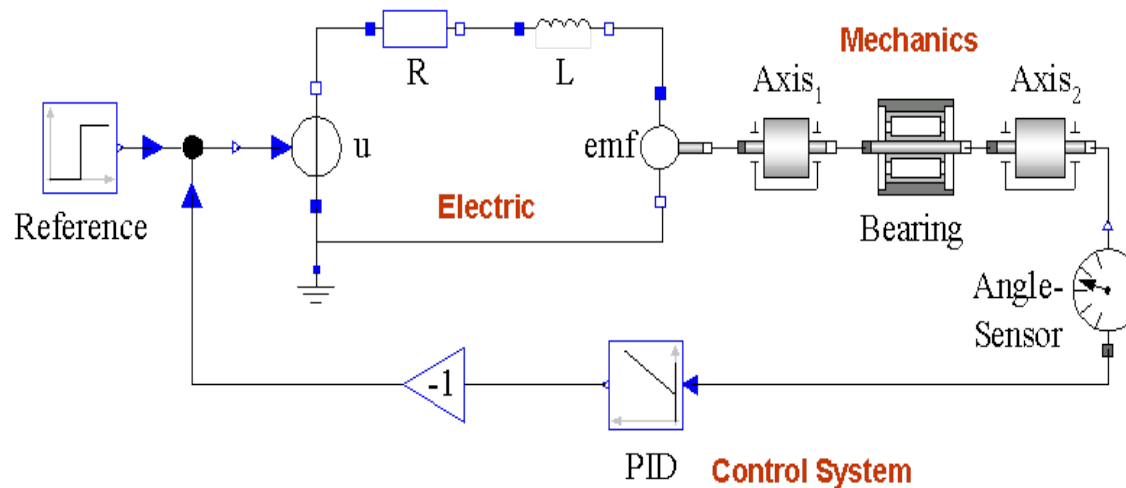
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M O D



# What is Modelica?

A language for modeling of complex physical systems



Primary designed for **simulation**, but there are also other usages of models, e.g. optimization.

# What is Modelica?

A language for modeling of complex physical systems  
i.e., Modelica is not a tool

Free, open language  
specification:



There exist several free and commercial tools, for example:

- OpenModelica from OSMC
- Dymola by Dassault systems / Dynasim
- SimulationX by ITI
- MapleSim by MapleSoft
- SystemModeler by Wolfram

Available at: <http://www.modelica.org/>



# Modelica technology

- Modelica is primarily an *equation-based* language

# The Form – Equations

- Equations were used in the third millennium B.C.
- Equality sign was introduced by Robert Recorde in 1557

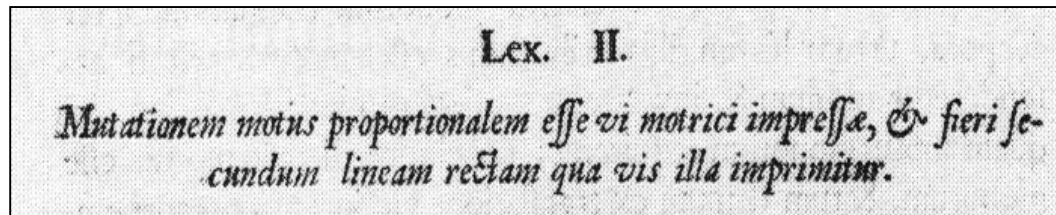
$$14.ze. + 15.9 = 71.9.$$

# The Form – Equations

- Equations were used in the third millennium B.C.
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14.ze. — + — . 15.9 — — — — — 71.9.

Newton still wrote text (Principia, vol. 1, 1686)



*“The change of motion is proportional to the motive force impressed”*

or

$$m \cdot a = \sum F$$



# Do other programming languages not also use equations?

- Difference between *equation* and *assignment*


# Do other programming languages not also use equations?

- Difference between *equation* and *assignment*
- Equations do not prescribe a certain data flow direction or execution order

Equation	Assignment
$R * i = v;$	$i := v/R;$ $v := R * i;$ $R := v/i;$

# Do other programming languages not also use equations?

- Difference between *equation* and *assignment*
- Equations do not prescribe a certain data flow direction or execution order

Equation	Assignment
$R * i = v;$  Causality unspecified	$i := v/R;$ $v := R * i;$ $R := v/i;$ Output  Input

- → *Acausal modeling*

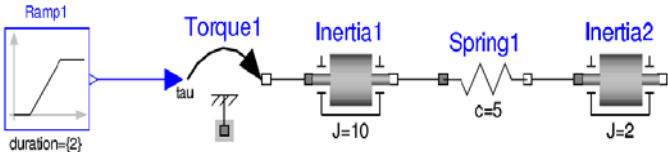
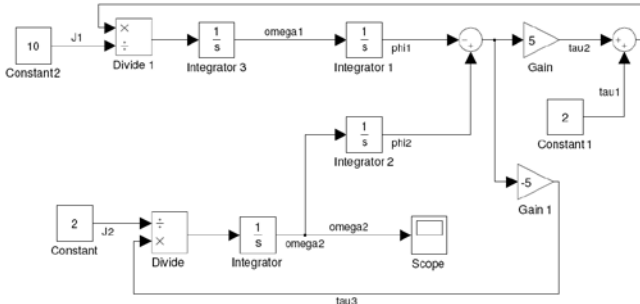
# Advantages of Equations

- More flexible than assignments
- Key to physical modeling capabilities
- Increases reuse potential of Modelica classes/models



# Acausal modeling

The order of computations is not decided at modeling time

	Acausal	Causal
Visual Component Level	 <p>A diagram of an acausal mechanical system. It starts with a 'Ramp1' component (duration={2}) producing a torque 'tau'. This torque is applied to a mass 'Inertia1' (J=10). 'Inertia1' is connected to a spring 'Spring1' (c=5), which is then connected to another mass 'Inertia2' (J=2). The diagram uses standard mechanical symbols: a motor for torque, a mass for inertia, and a spring for elasticity.</p>	 <p>A block diagram of the same mechanical system, rendered causal. The input is a 'Constant2' (10) which is divided by 'J1' (10) in a 'Divide 1' block. The result is integrated by 'Integrator 3' to produce 'omega1'. 'omega1' is integrated by 'Integrator 1' to produce 'phi1'. 'phi1' is summed with a feedback signal from 'Gain 1' (5) and 'tau1' (2) to produce the torque 'tau'. 'tau' is divided by 'J2' (2) in a 'Divide' block, integrated by 'Integrator 2' to produce 'omega2', which is then summed with a feedback signal from 'Gain 1' (-5) to produce the displacement 'phi2'. 'phi2' is integrated by 'Integrator 3' to produce 'tau1'. The displacement 'phi2' is also monitored by a 'Scope'.</p>
Equation Level	<p>A resistor <i>equation</i>:</p> $R \cdot i = v;$	<p>Causal possibilities:</p> $i := v/R;$ $v := R \cdot i;$ $R := v/i;$

# Example – Simple differential equation

- Equation (ODE):

$$-\frac{dx}{dt} = ax ; x(0) = 1;$$

# Example – Simple differential equation

Equation (ODE):

$$\frac{dx}{dt} = -x, \quad x(0) = 1$$

Name of model

Initial condition

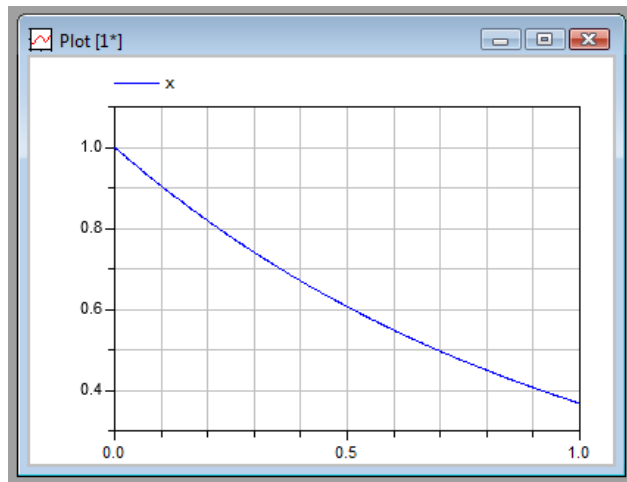
Continuous-time  
variable

Parameter, constant  
during simulation

```
model FirstOrder "A simple equation"
  Real x(start=1);
  parameter Real a = -1;
  equation
    der(x) = a*x;
end FirstOrder;
```

Differential equation

Simulation in Dymola:



# Modelica Variables and Constants

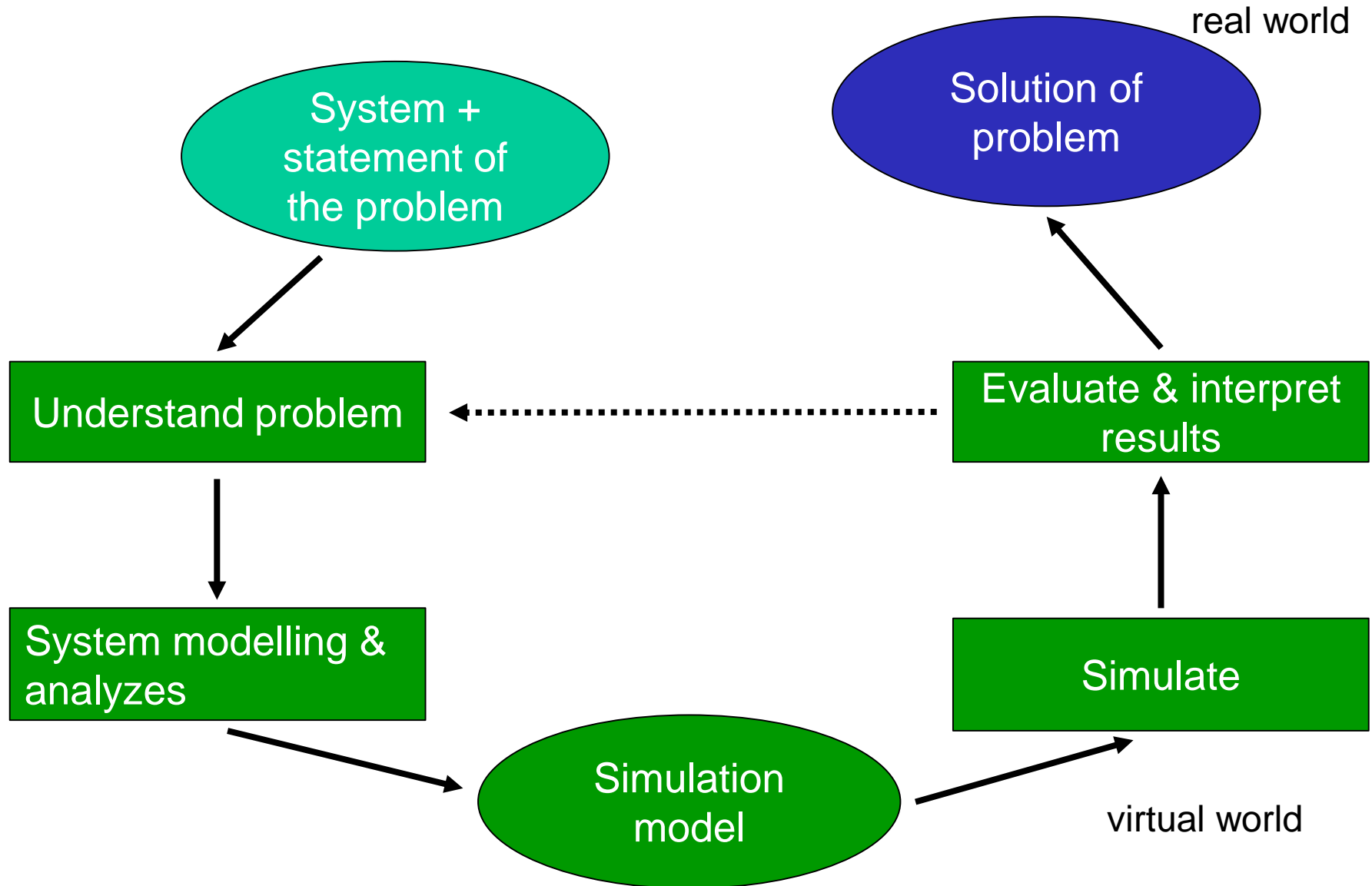
- Built-in primitive data types

<b>Boolean</b>	<b>true</b> or <b>false</b>
<b>Integer</b>	Integer value, e.g. <b>42</b> or <b>-3</b>
<b>Real</b>	Floating point value, e.g. <b>2.4e-6</b>
<b>String</b>	String, e.g. <b>"Hello world"</b>
<b>Enumeration</b>	Enumeration literal e.g. <b>ShirtSize.Medium</b>

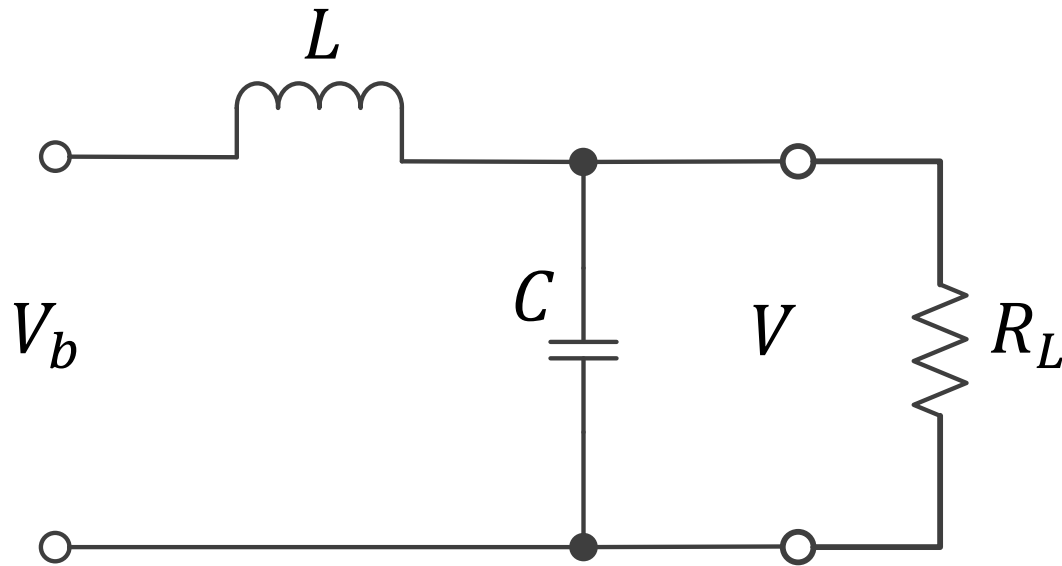
- Parameters are constant during simulation
- Two types of constants in Modelica
  - constant
  - parameter

```
constant Real    PI=3.141592653589793;  
constant String  redcolor = "red";  
constant Integer one = 1;  
parameter Real   mass = 22.5;
```

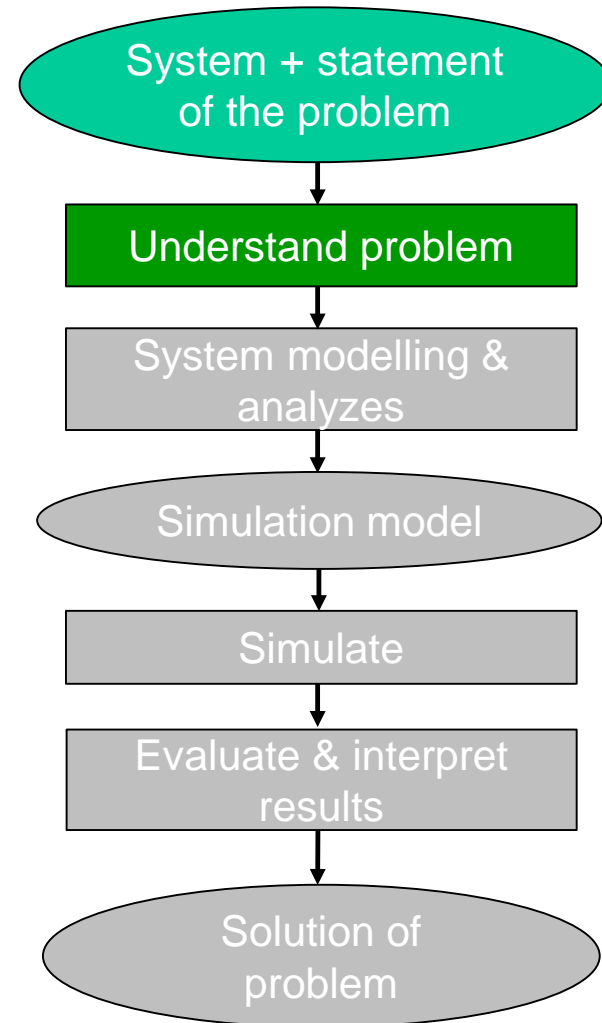
# Modelling and Simulation Process



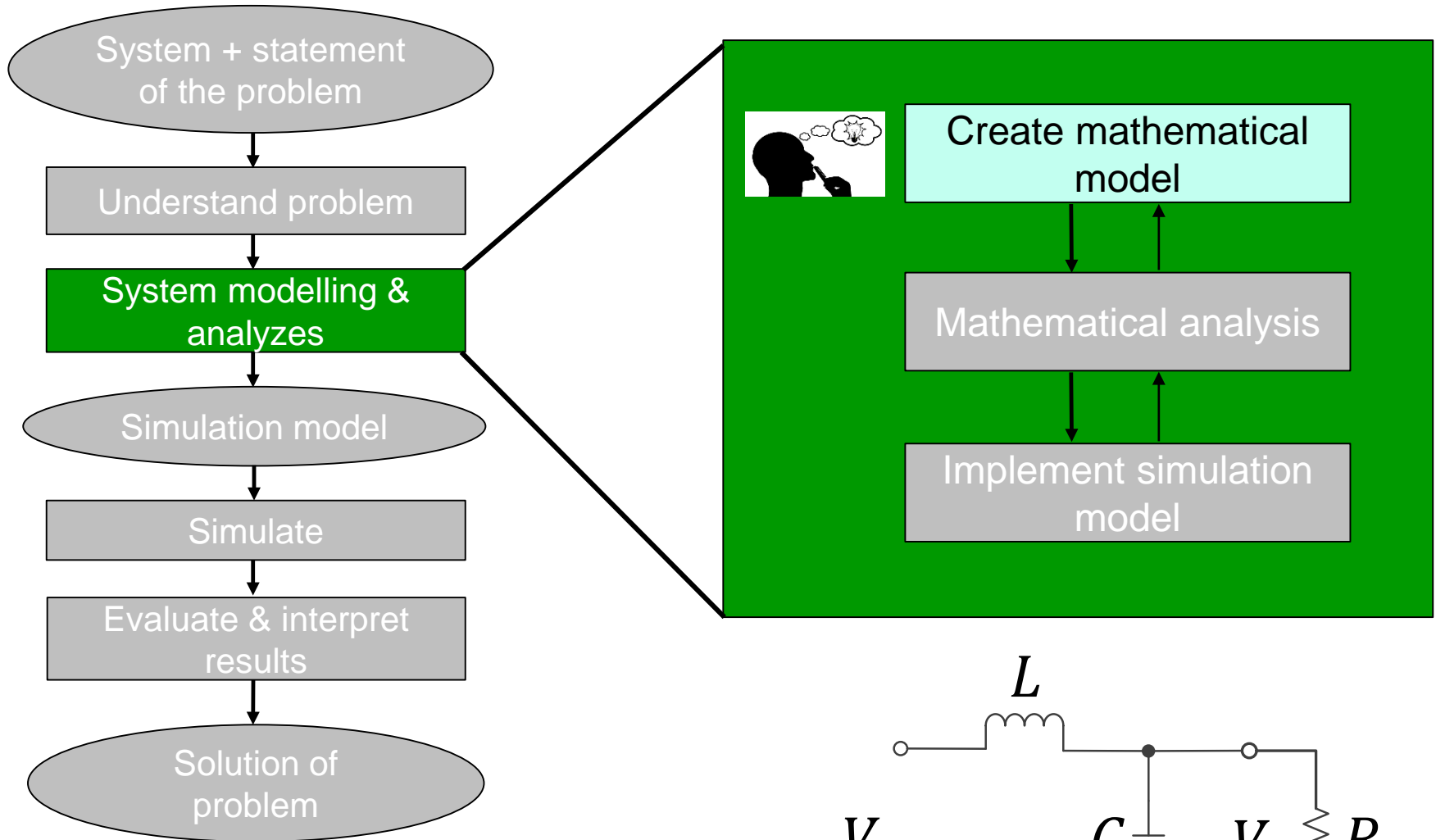
## 2<sup>nd</sup> Example – Low-Pass RLC Filter



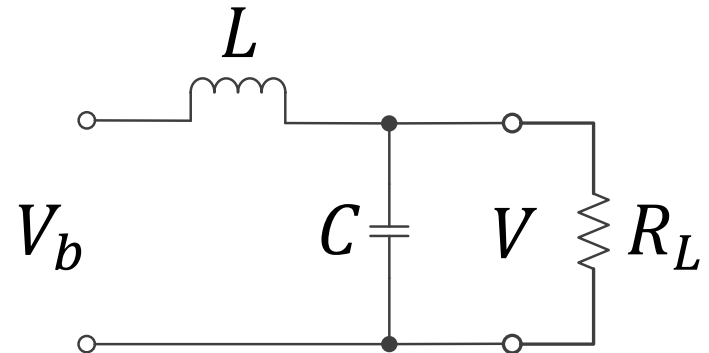
Solve for:  $V$ ,  $i_L$ ,  $i_R$  and  $i_C$



# Create mathematical model



Solve for:  $V$ ,  $i_L$ ,  $i_R$  and  $i_C$

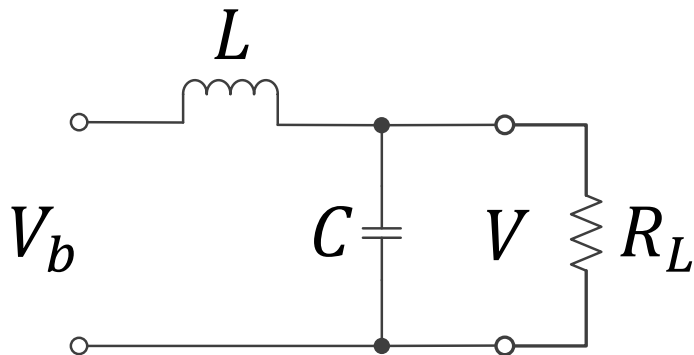


# Equations:

- Type equation here.



## 2<sup>nd</sup> Example – Low-Pass RLC Filter

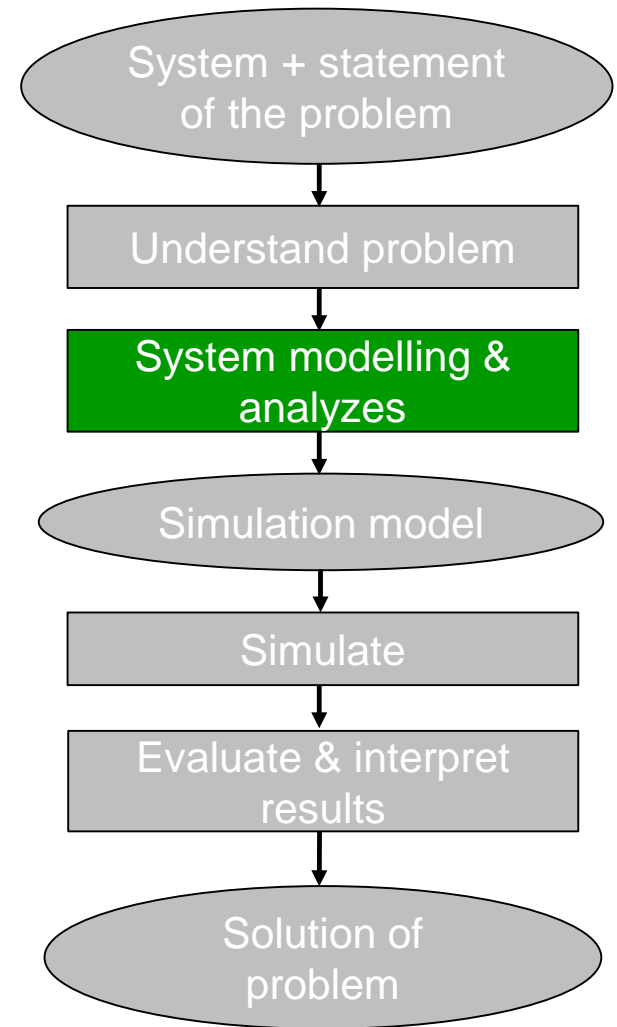


$$V = i_R R$$

$$C \frac{dV}{dt} = i_C$$

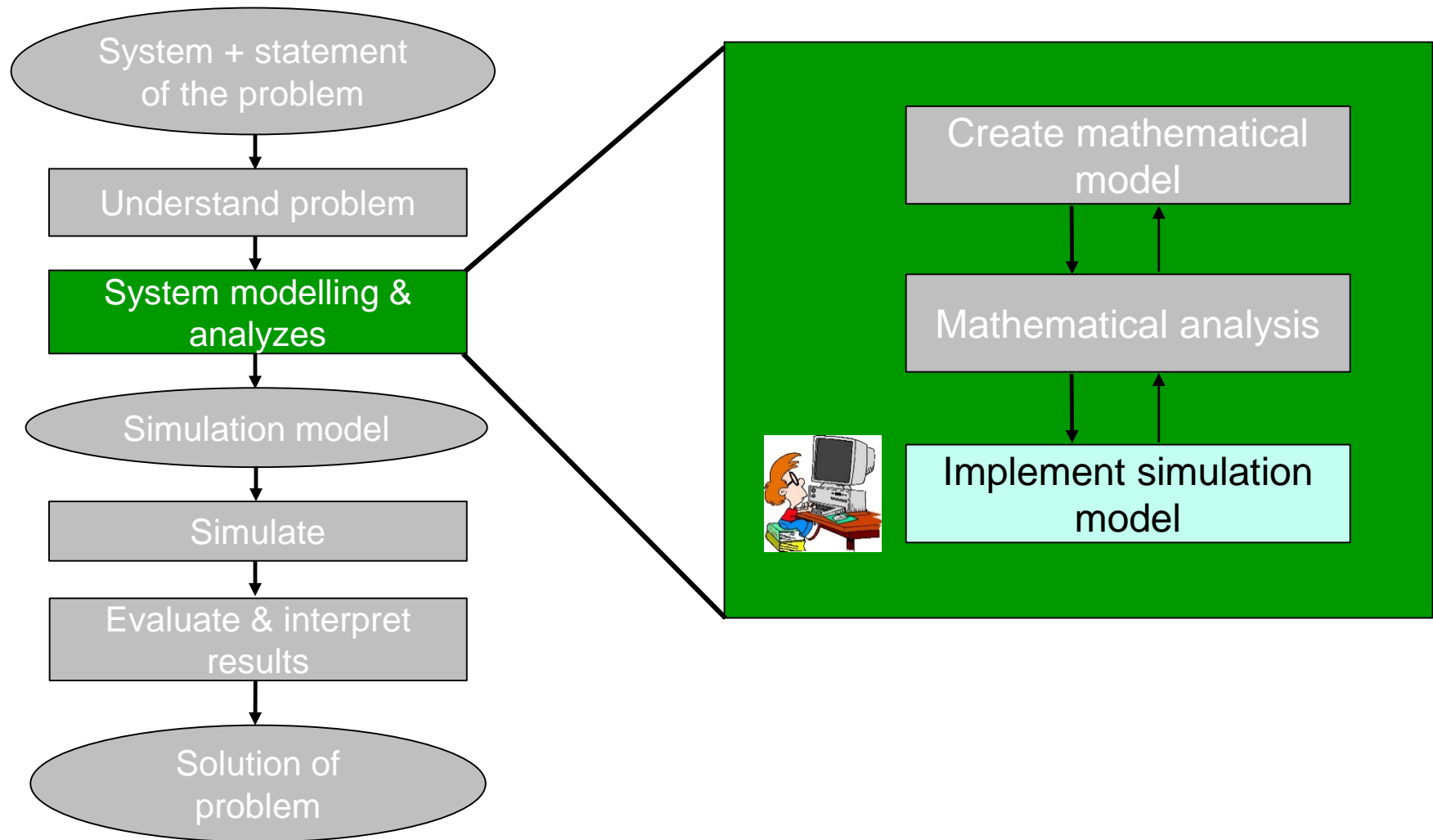
$$L \frac{di_L}{dt} = (V_b - V)$$

$$i_L = i_R + i_C$$



Example taken from: <http://book.xogeny.com/>

## 2<sup>nd</sup> Example – Low-Pass RLC Filter



# 2<sup>nd</sup> Example – Code

Name of model

Import of SIunits package

```
model RLC5 "A resistor-inductor-capacitor circuit model"

  import SI = Modelica.SIunits "imports SIunits from Modelica package";
  // import Modelica.SIunits.* "other way to import package. Here top-level";
```

New type definition

```

a
type Voltage = Real(unit="V");
type Current = Real(unit="A");
```

Parameter, constant during simulation

```

parameter Voltage Vb=24 "Battery voltage";
parameter SI.Inductance L = 1;
parameter SI.Resistance R = 100;
parameter SI.Capacitance C = 1e-03;
```

Continuous-time variable

```

Voltage V;
Current i_L;
Current i_R;
Current i_C;
```

Differential equation

```

equation
  V = i_R*R;
  C*der(V) = i_C;
  L*der(i_L) = (Vb-V);
  i_L = i_R+i_C;

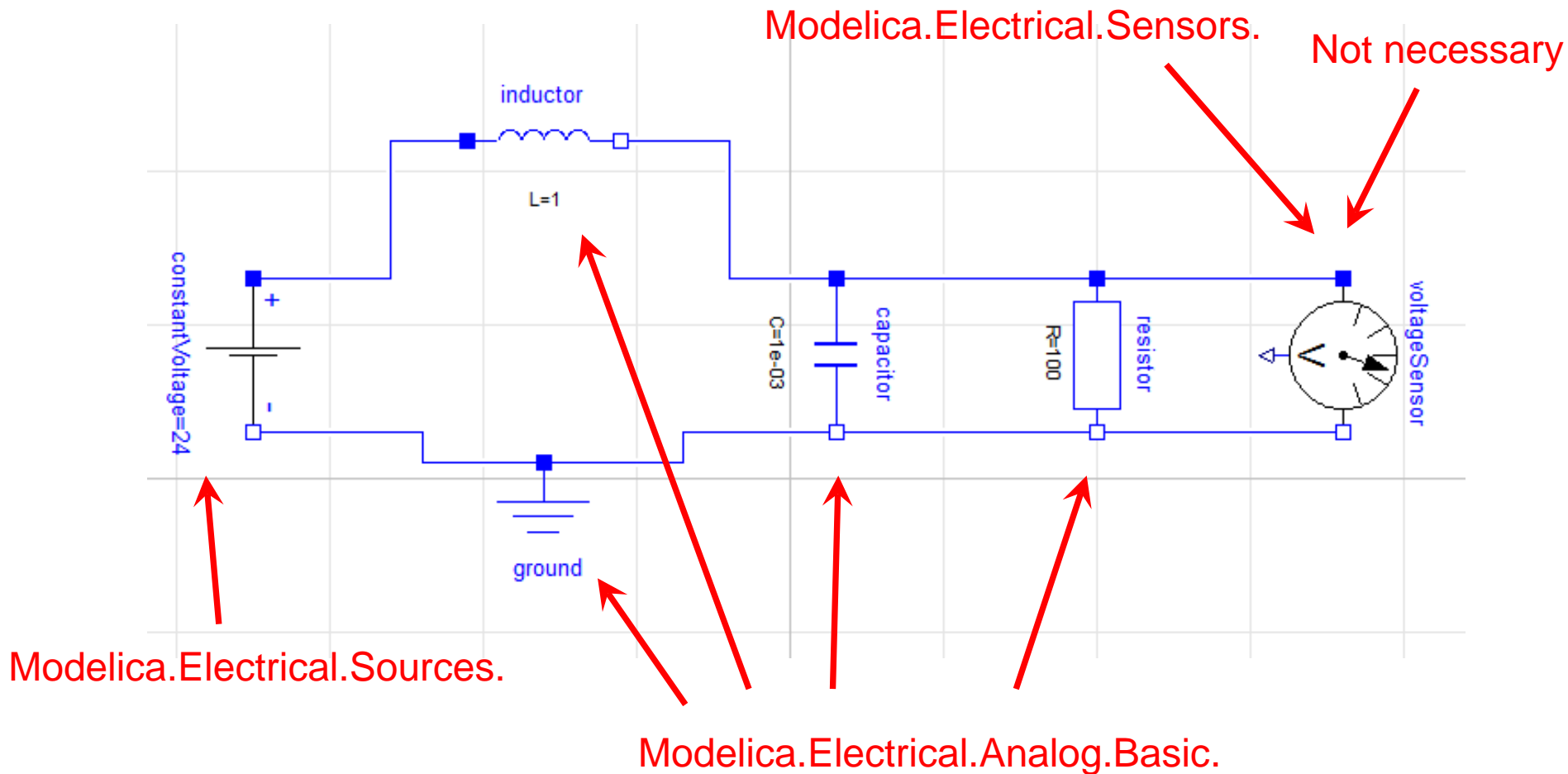
end RLC5;
```

Algebraic equation

# Modelica technology

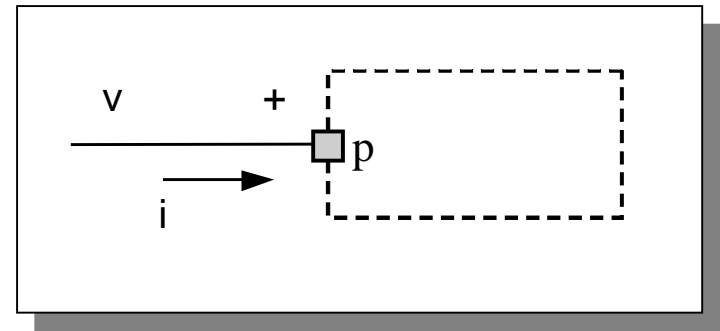
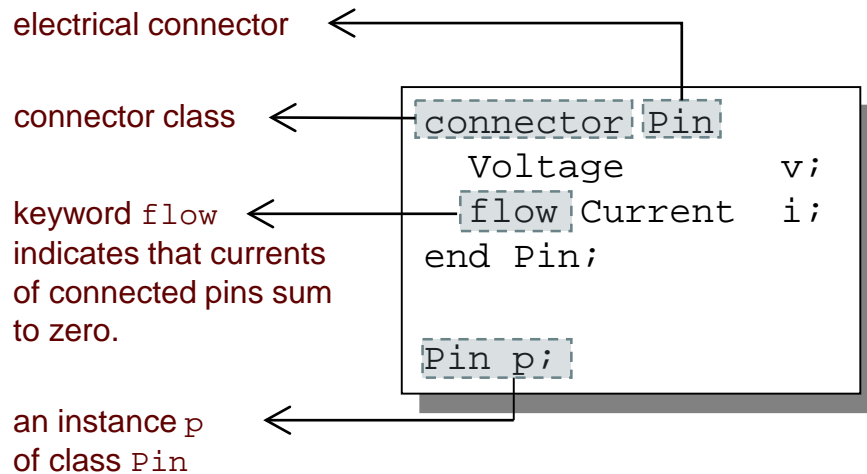
- Modelica includes *graphical* editing for application model design based on predefined components

## 2<sup>nd</sup> Example – Graphical solution with the help of Dymola standard packages



# Connectors and Connector Classes

Connectors are instances of *connector classes*



# The **f**low prefix

Two kinds of variables in connectors:

- *Non-flow variables* **potential** or energy level
- *Flow variables* represent some kind of **flow**

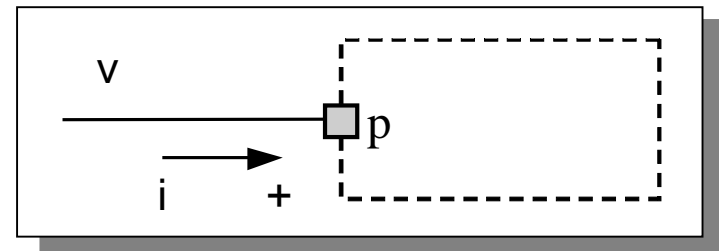
# The `flow` prefix

## Coupling

- *Equality coupling*, for non-`flow` variables
  - In electrics:  $v_1 = v_2 = \dots = v_n$  (Kirchhoff's 2<sup>nd</sup> law)
- *Sum-to-zero coupling*, for `flow` variables
  - In electrics:  $i_1 + i_2 + \dots + i_n = 0$  (Kirchhoff's 1<sup>st</sup> law)

The value of a `flow` variable is *positive* when the current or the flow is *into* the component

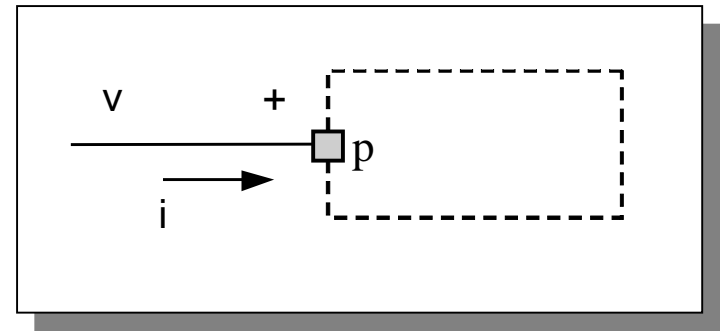
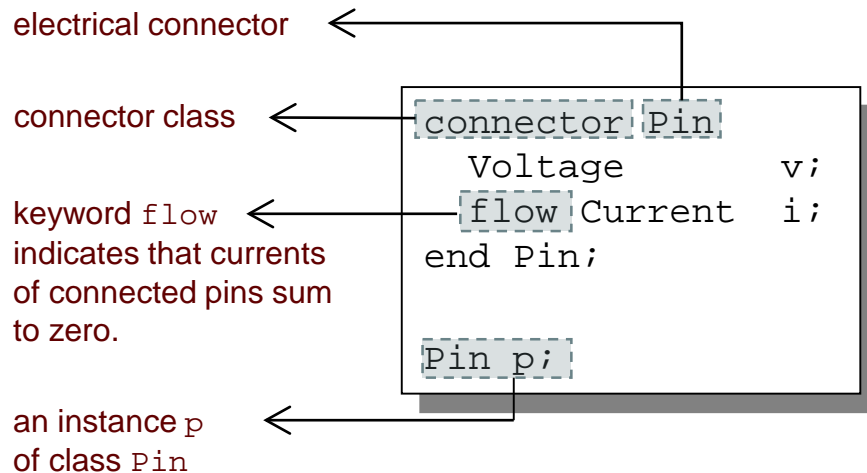
positive flow direction:





# Connectors and Connector Classes

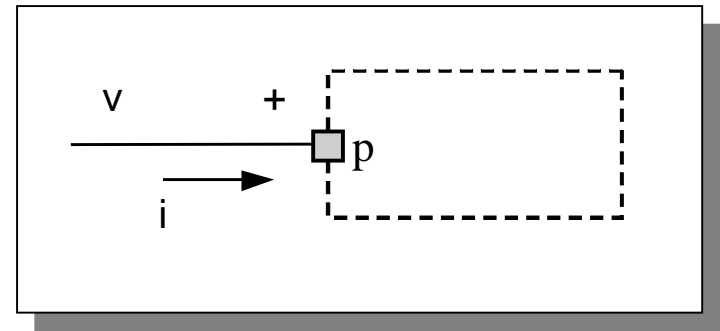
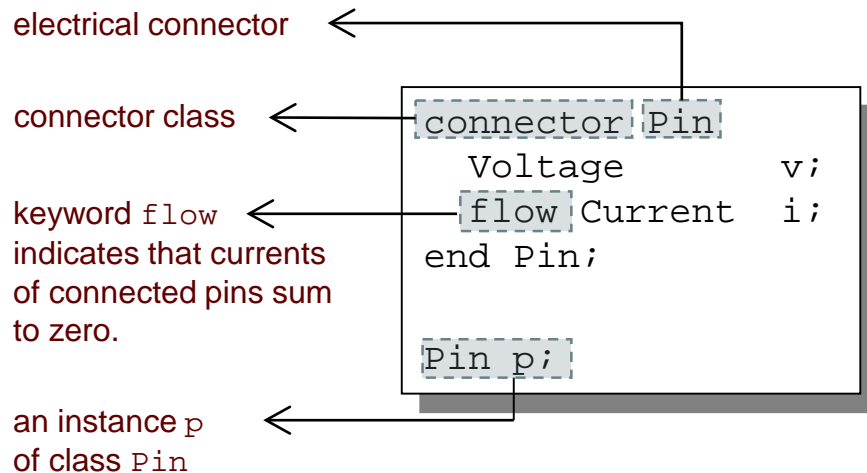
Connectors are instances of *connector classes*



What does the product of the electric pair of connector variables represent?

# Connectors and Connector Classes

Connectors are instances of *connector classes*

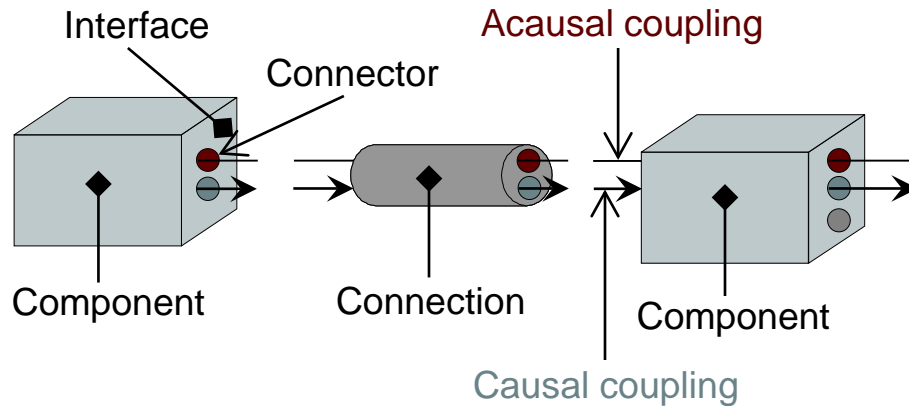


What does the product of the electric pair of connector variables represent?

- $$v \left[ \frac{Nm}{C} \right] \cdot i \left[ \frac{C}{s} \right] = p \left[ \frac{Nm}{s} = W \right]$$

→ Flow of energy

# Software Component Model

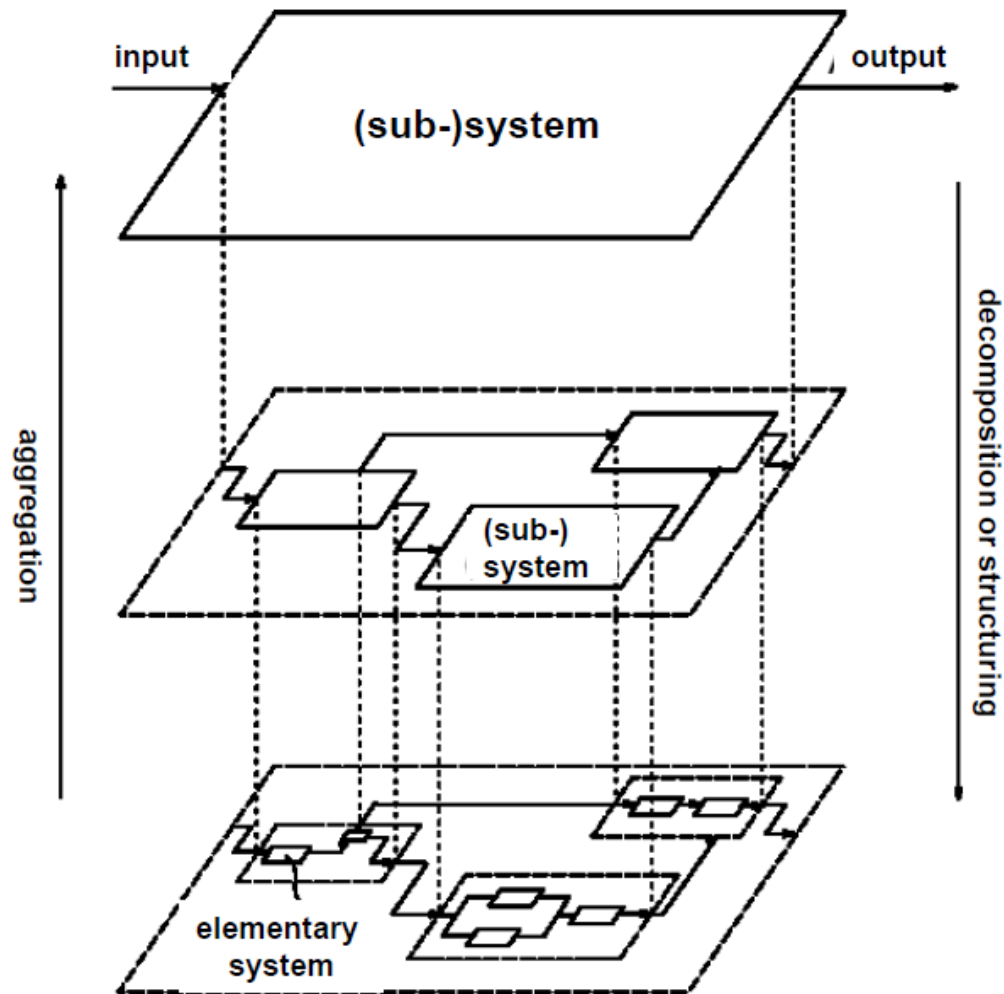


A component class should be defined *independently of the environment*, very essential for *reusability*

A component may internally consist of other components, i.e. *hierarchical* modeling

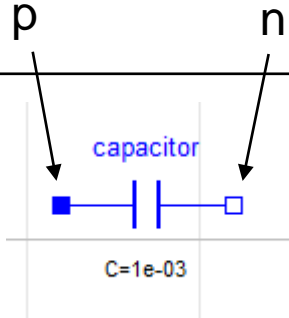
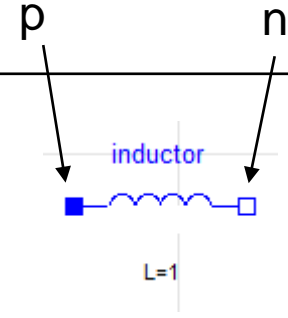
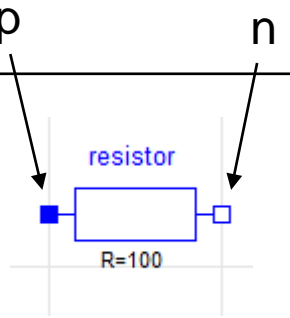
Complex systems usually consist of large numbers of *connected* components

# Decomposition and Aggregation of Systems



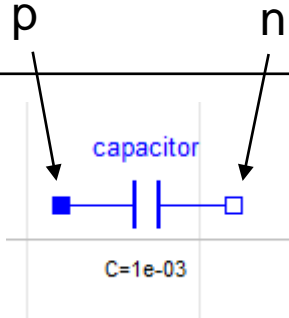
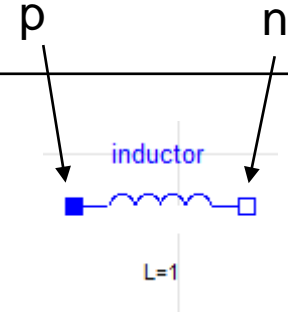
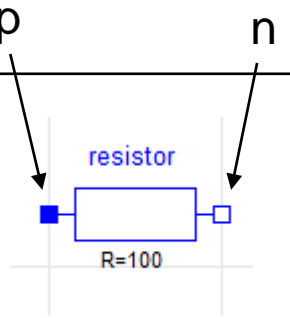
# Use of Inheritance & Connectors

- Connector-Name (Pin): p, n

			
<b>Equations:</b>	$0 = p.i + n.i$ $v = p.v - n.v$ $i = p.i$ $i = C * der(v)$	$0 = p.i + n.i$ $v = p.v - n.v$ $i = p.i$ $v = L * der(i)$	$0 = p.i + n.i$ $v = p.v - n.v$ $i = p.i$ $v = R * i$

# Use of Inheritance & Connectors

- Connector-Name (Pin): p,n

			
<b>Equations:</b>	$0 = p.i + n.i$ $v = p.v - n.v$ $i = p.i$ $i = C * der(v)$	$0 = p.i + n.i$ $v = p.v - n.v$ $i = p.i$ $v = L * der(i)$	$0 = p.i + n.i$ $v = p.v - n.v$ $i = p.i$ $v = R * i$

→ Only one equation different

# Reuse same components

1) Create connector: ■

```
connector Pin
  Modelica.SIunits.Voltage v; //identical at connection
  flow Modelica.SIunits.Current i; //sum-to-0 at connection
end Pin;
```

# Reuse same components

- 1) Create connector: ■

```
connector Pin
  Modelica.SIunits.Voltage v;//identical at connection
  flow Modelica.SIunits.Current i;//sum-to-0 at connection
end Pin;
```

- 2) Create “blueprint” model class TwoPin: ■ □

```
partial model TwoPin "Superclass of elements
with two electrical pins"
  Pin p, n;
  Modelica.SIunits.Voltage v;
  Modelica.SIunits.Current i;
equation
  v = p.v - n.v;
  0 = p.i + n.i;
  i = p.i;
end TwoPin;
```



# Reuse same components

1) Create connector: ■

```
connector Pin
  Modelica.SIunits.Voltage v; //identical at connection
  flow Modelica.SIunits.Current i; //sum-to-0 at connection
end Pin;
```

2) Create “blueprint” model class TwoPin: ■ □

```
partial model TwoPin "Superclass of elements
with two electrical pins"
```

```
  Pin p, n;
```

```
  Modelica.SIunits.Voltage v;
```

```
  Modelica.SIunits.Current i;
```

```
equation
```

```
  v = p.v - n.v;
```

```
  0 = p.i + n.i;
```

```
  i = p.i;
```

```
end TwoPin;
```

partial because:

- Problem is structurally singular
- 6 variables & only 5 equations

# Reuse same components with extends

3) Create model with previous components

```
model Resistor "Ideal electrical resistor"
  extends TwoPin
  parameter Modelica.SIunits.Resistance R;

equation
  R*i = v;
end Resistor;
```

```
model Capacitor "Ideal electrical capacitor"
  extends TwoPin
  parameter Modelica.SIunits.Capacitance C;

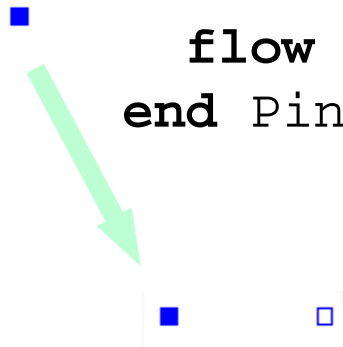
equation
  C*der(v) = i;
end Capacitor;
```

# Use of Modelica connectors

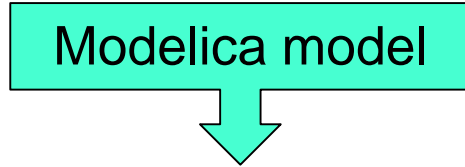
```
connector Pin
  Voltage v; // identical at connection
  flow Current i; // sums to zero at connection
end Pin;
```

```
partial model TwoPin
  Pin p, n; Voltage v; Current i;
equation
  v = p.v - n.v;
  0 = p.i + n.i;
  i = p.i;
end TwoPin;
```

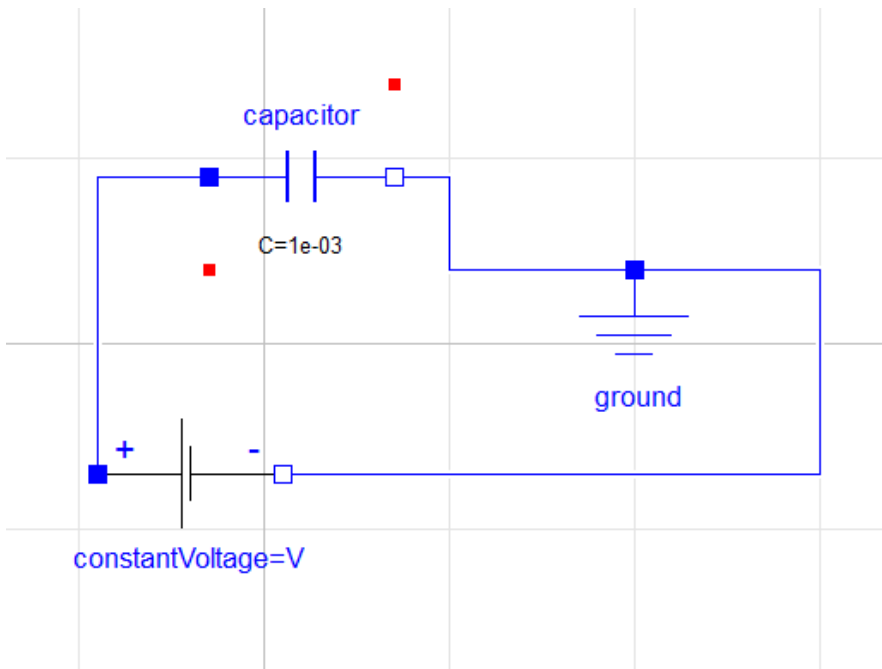
```
model Capacitor
  extends TwoPin;
  parameter Capacitance C;
equation
  C*der(v) = i;
end Capacitor;
```



# Implementation and Execution of Modelica



# Modelica model



```

model Test_Capacitor

// parameter Real i=1;
// parameter Real v=20;
//
// Pin p;

Modelica.Electrical.Analog.Basic.Capacitor capacitor(C=1e-03);
Modelica.Electrical.Analog.Sources.ConstantVoltage constantVoltage;
Modelica.Electrical.Analog.Basic.Ground ground;

equation
connect(constantVoltage.p, capacitor.p);
connect(capacitor.n, ground.p);
connect(ground.p, constantVoltage.n);

end Test_Capacitor;

partial package Modelica.Icons.Package "Icon for standard packages"

end Package;

model Modelica.Electrical.Analog.Basic.Capacitor
  "Ideal linear electrical capacitor"
  extends Interfaces.OnePort;
  parameter SI.Capacitance C(start=1) "Capacitance";

equation
  i = C*der(v);
end Capacitor;

partial package Modelica.Icons.InterfacesPackage
  "Icon for packages containing interfaces"
  //extends Modelica.Icons.Package;
end InterfacesPackage;

partial model Modelica.Electrical.Analog.Interfaces.OnePort
  "Component with two electrical pins p and n and current i from p to n"

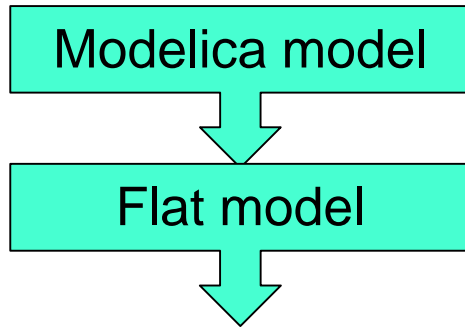
  SI.Voltage v "Voltage drop between the two pins (= p.v - n.v)";
  SI.Current i "Current flowing from pin p to pin n";
  PositivePin p
    "Positive pin (potential p.v > n.v for positive voltage drop v)";
  NegativePin n "Negative pin";

equation
  v = p.v - n.v;
  0 = p.i + n.i;
  i = p.i;
end OnePort;

connector Modelica.Electrical.Analog.Interfaces.PositivePin
  "Positive pin of an electric component"
  Modelica.SIunits.Voltage v "Potential at the pin";
  flow Modelica.SIunits.Current i "Current flowing into the pin";

```

# Implementation and Execution of Modelica



Parsed, preprocessing, flattening

# Flat model

```

model Test_Capacitor
parameter Modelica.SIunits.Capacitance capacitor.C(start = 1) = 0.001
  "Capacitance";
parameter Modelica.SIunits.Voltage constantVoltage.V = 1 "Value of constant voltage";

Modelica.SIunits.Voltage capacitor.v "Voltage drop between the two pins (= p.v - n.v)";
Modelica.SIunits.Current capacitor.i "Current flowing from pin p to pin n";
Modelica.SIunits.Voltage capacitor.p.v "Potential at the pin";
Modelica.SIunits.Current capacitor.p.i "Current flowing into the pin";
Modelica.SIunits.Voltage capacitor.n.v "Potential at the pin";
Modelica.SIunits.Current capacitor.n.i "Current flowing into the pin";
Modelica.SIunits.Voltage constantVoltage.v "Voltage drop between the two pins (= p.v - n.v)";
Modelica.SIunits.Current constantVoltage.i "Current flowing from pin p to pin n";
Modelica.SIunits.Voltage constantVoltage.p.v "Potential at the pin";
Modelica.SIunits.Current constantVoltage.p.i "Current flowing into the pin";
Modelica.SIunits.Voltage constantVoltage.n.v "Potential at the pin";
Modelica.SIunits.Current constantVoltage.n.i "Current flowing into the pin";
Modelica.SIunits.Voltage ground.p.v "Potential at the pin";
Modelica.SIunits.Current ground.p.i "Current flowing into the pin";

// Equations and algorithms

// Component capacitor
// class Modelica.Electrical.Analog.Basic.Capacitor
// extends Modelica.Electrical.Analog.Interfaces.OnePort
equation
  capacitor.v = capacitor.p.v - capacitor.n.v;
  0 = capacitor.p.i + capacitor.n.i;
  capacitor.i = capacitor.p.i;
// end of extends
equation
  capacitor.i = capacitor.C * der(capacitor.v);

// Component constantVoltage
// class Modelica.Electrical.Analog.Sources.ConstantVoltage
// extends Modelica.Electrical.Analog.Interfaces.OnePort
equation
  constantVoltage.v = constantVoltage.p.v - constantVoltage.n.v;
  0 = constantVoltage.p.i + constantVoltage.n.i;
  constantVoltage.i = constantVoltage.p.i;
// end of extends
equation
  constantVoltage.v = constantVoltage.V;

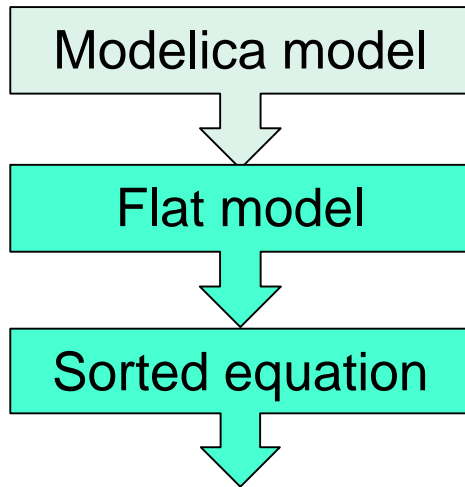
// Component ground
// class Modelica.Electrical.Analog.Basic.Ground
equation
  ground.p.v = 0;

// Component
// class Test_Capacitor
equation
  capacitor.n.i + constantVoltage.n.i + ground.p.i = 0.0;
  constantVoltage.n.v = capacitor.n.v;
  ground.p.v = capacitor.n.v;
  capacitor.p.i + constantVoltage.p.i = 0.0;
  constantVoltage.p.v = capacitor.p.v;

end Test_Capacitor;

```

# Implementation and Execution of Modelica



Parsed, preprocessing, flattening

“make equations causal”, perform BLT transformation



# Lower Triangular Matrix (Example)

	$v_G$	$v_{C1}$	$v_{R1}$	$u_R$	$i_{R1}$	$i_{S1}$	$i_{C1}$	$du_c$	$i_G$
1)	x								
6)	x	x							
2)	x		x						
4)		x	x	x					
3)				x	x				
7)					x	x			
8)					x		x		
5)							x	x	
9)						x	x		x

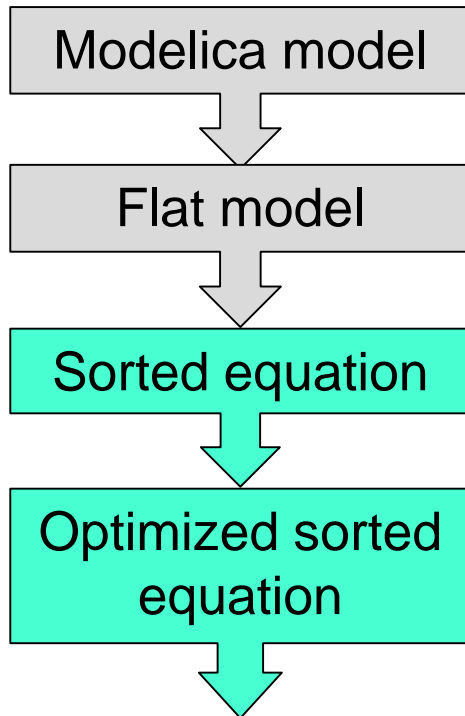
## Causal List:

- 1)  $v_G := 0$
- 6)  $v_{C1} := -u_c + v_G$
- 2)  $v_{R1} := v_G + 10V$
- 4)  $u_R := v_{C1} - v_{R1}$
- 3)  $i_{R1} := u_R/R$
- 7)  $i_{S1} := i_{R1}$
- 8)  $i_{C1} := i_{R1}$
- 5)  $\frac{du_c}{dt} := i_{C1}/C$
- 9)  $i_G := i_{C1} - i_{S1}$

# Block Lower Triangular Matrix (Example)

	x								
	x	x							
	x		x	x					
		x	x	x					
				x	x				
					x	x		x	x
					x		x		x
							x	x	
						x	x		x

# Implementation and Execution of Modelica

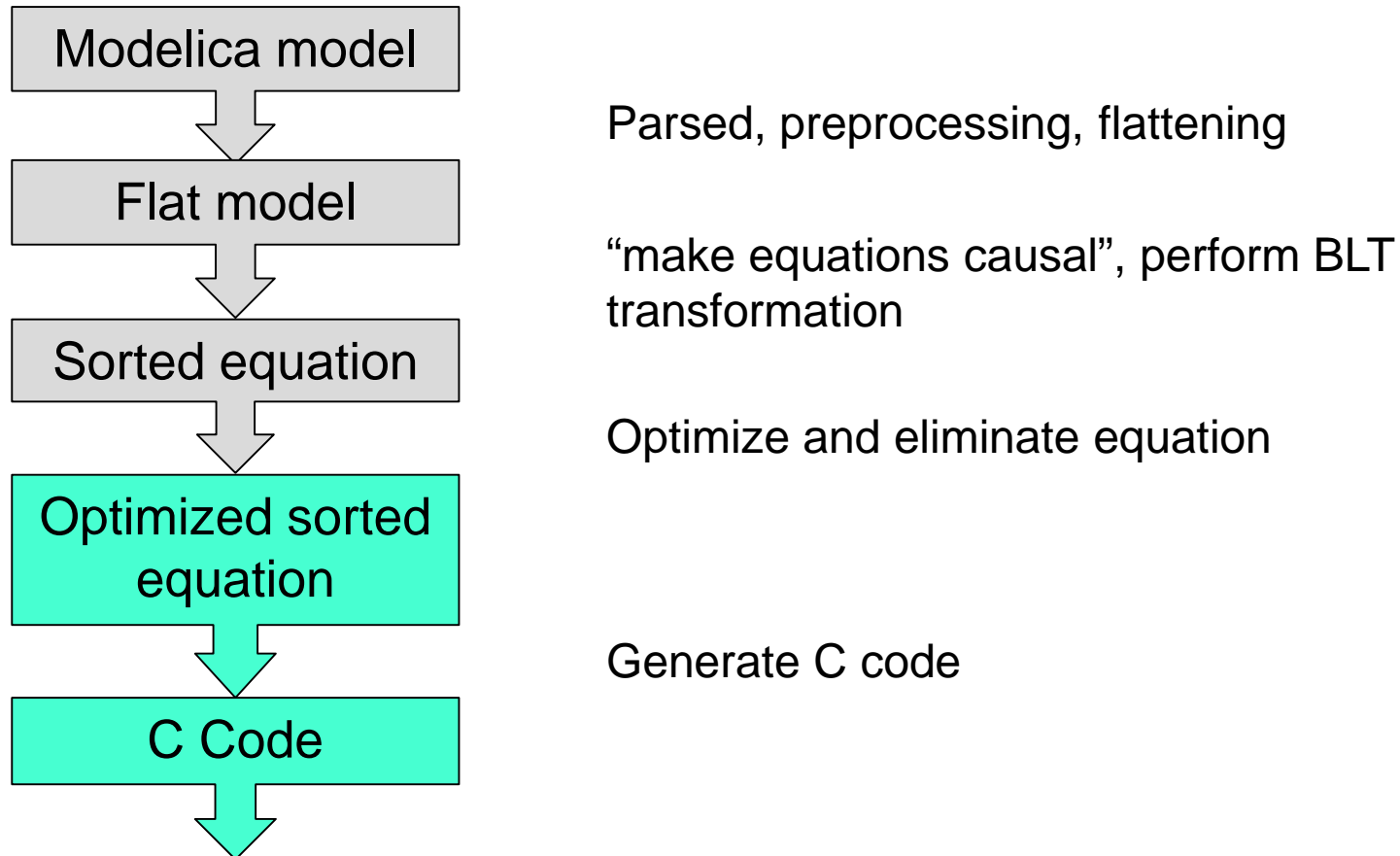


Parsed, preprocessing, flattening

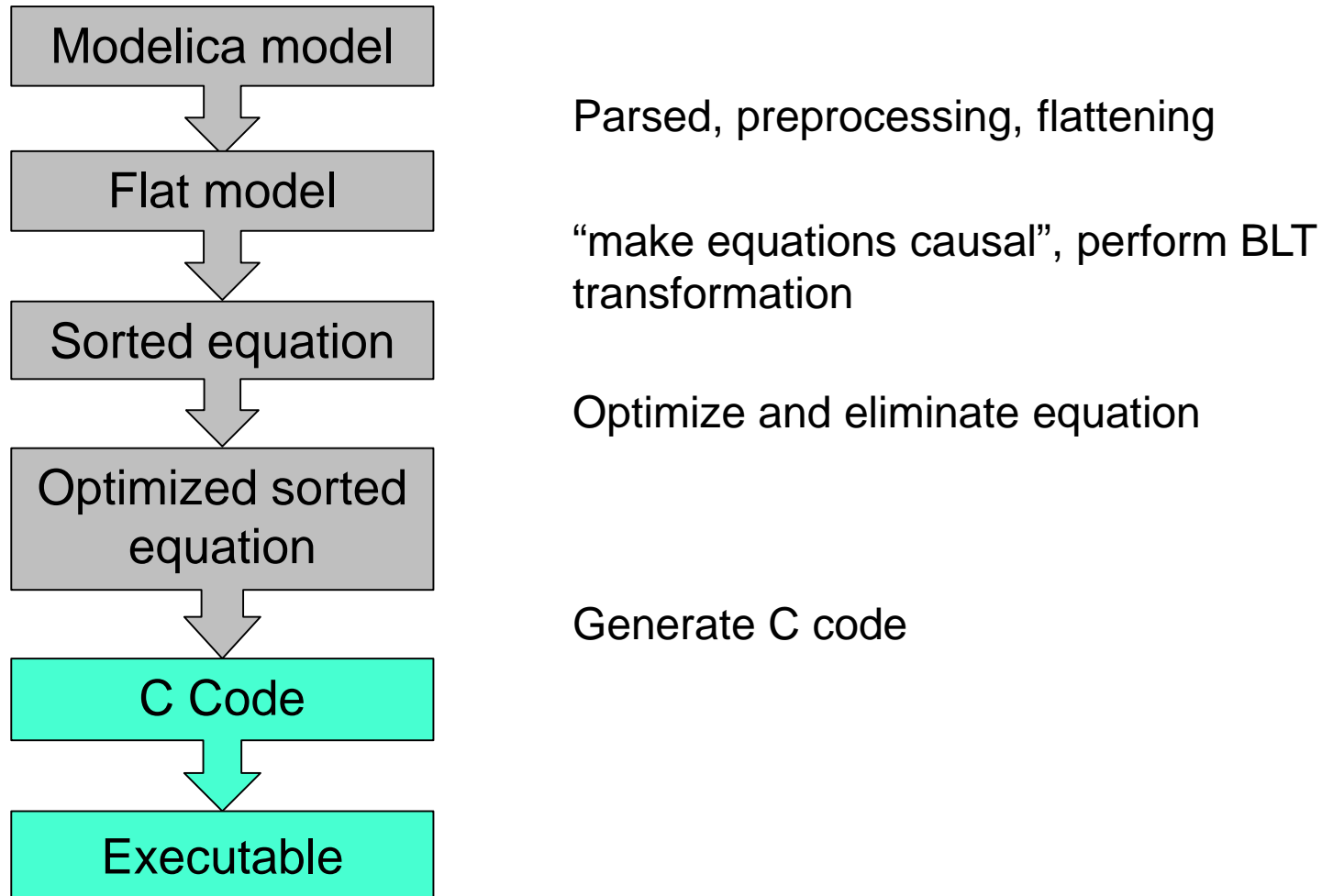
“make equations causal”, perform BLT transformation

Optimize and eliminate equation

# Implementation and Execution of Modelica



# Implementation and Execution of Modelica

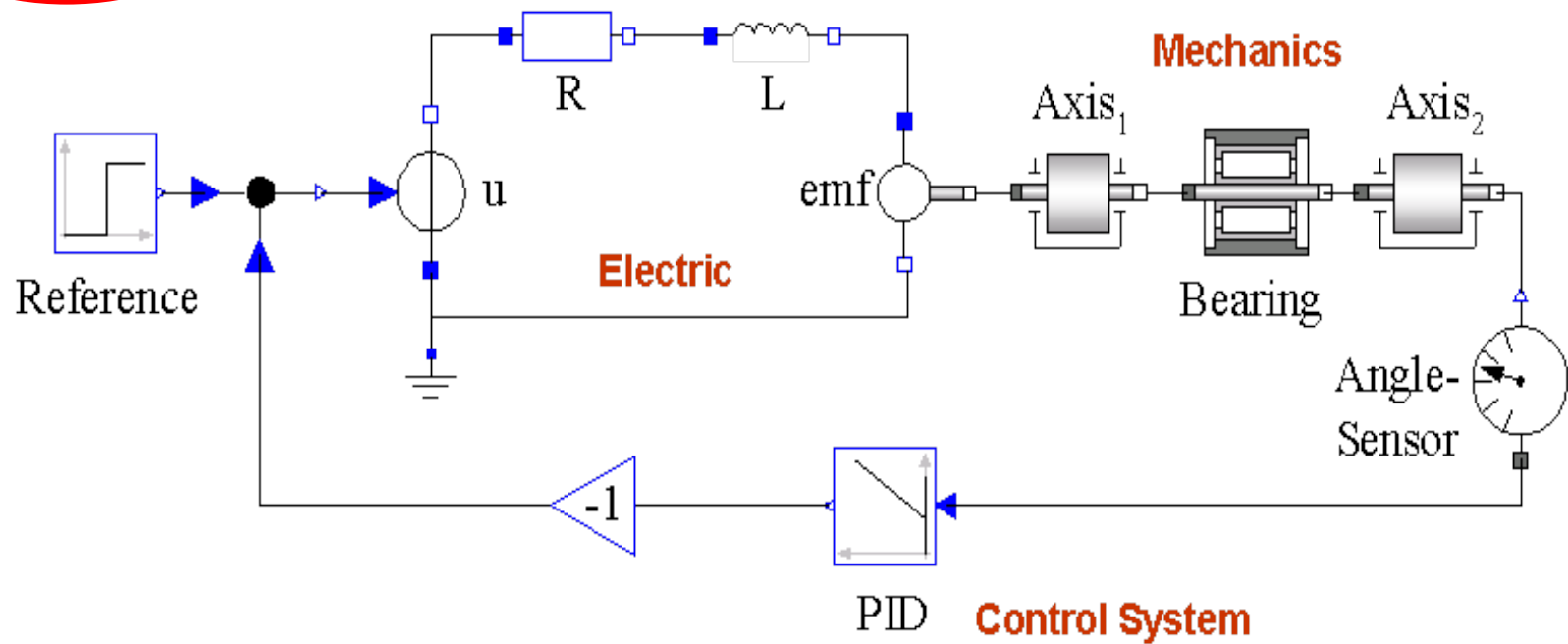


# What is Special about Modelica?

- Multi-Domain Modeling
- Visual acausal hierarchical component modeling
- Typed declarative equation-based textual language
- Hybrid modeling and simulation

# What is Special about Modelica?

Multi-Domain  
Modeling



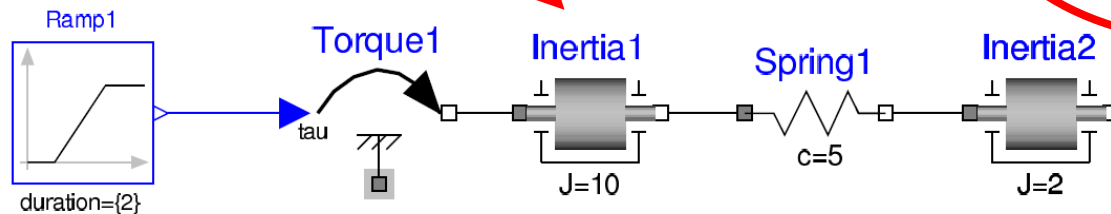
# What is Special about Modelica?

Multi-Domain  
Modeling

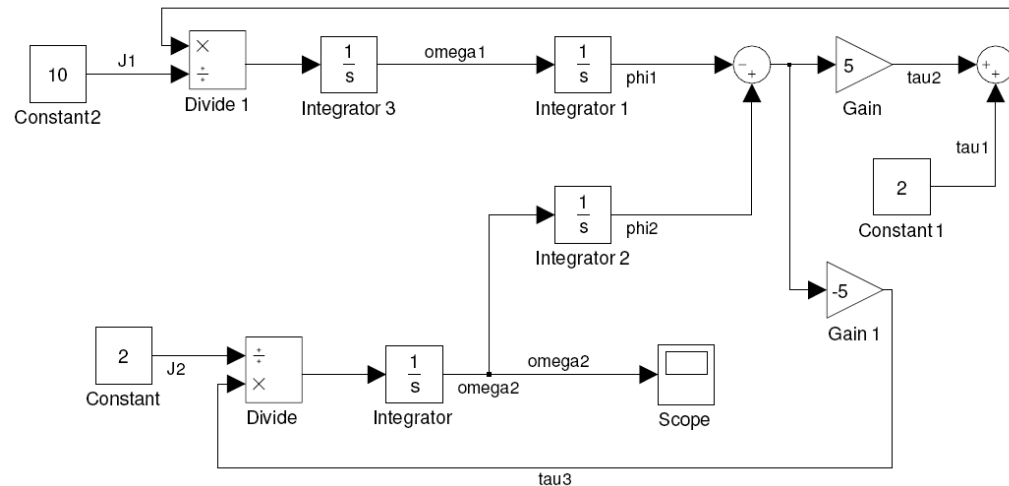
Acausal model  
(Modelica)

Keeps the physical  
structure

Visual Acausal  
Hierarchical  
Component  
Modeling



Causal  
block-based  
model  
(Simulink)





# What is Special about Modelica?

Multi-Domain  
Modeling

A textual *class-based* language  
OO primary used for as a structuring concept

Visual Acausal  
Hierarchical  
Component  
Modeling

Behaviour described declaratively using

- Differential algebraic equations (DAE) (continuous-time)
- Event triggers (discrete-time)

Variable  
declarations

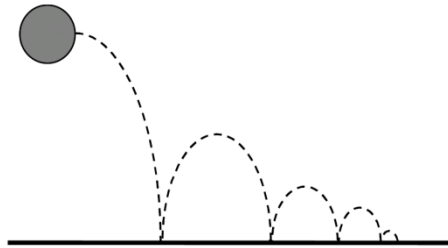
```
model VanDerPol "Van der Pol oscillator model"
  Real x(start = 1) "Descriptive string for x";
  Real y(start = 1) "y coordinate";
  parameter Real lambda = 0.3;
equation
  der(x) = y;
  der(y) = -x + lambda*(1 - x*x)*y;
end VanDerPol;
```

Typed  
Declarative  
Equation-based  
Textual Language

Differential equations

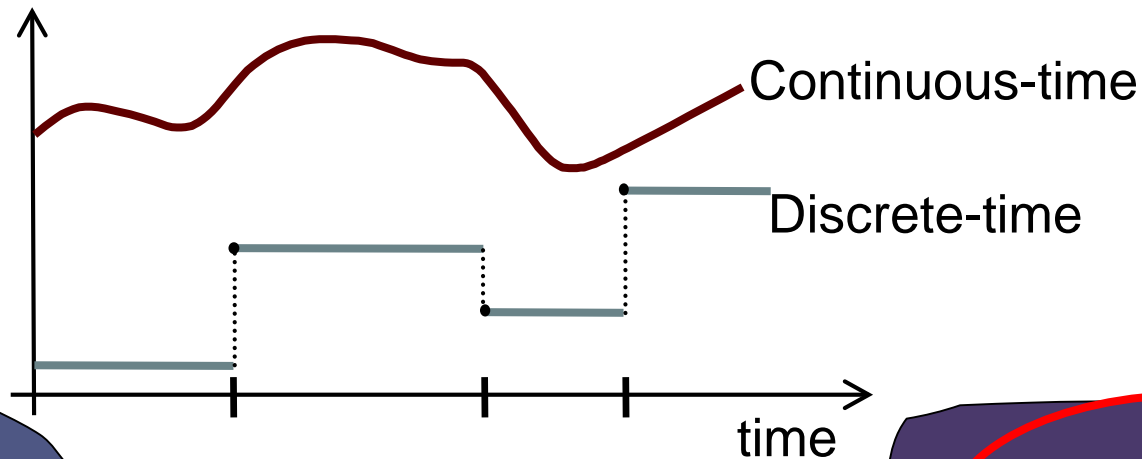
# What is Special about Modelica?

Multi-Domain  
Modeling



Visual Acausal  
Component  
Modeling

Hybrid modeling =  
continuous-time + discrete-time modeling



Typed  
Declarative  
Equation-based  
Textual Language

Hybrid  
Modeling

# Kvalitetssikring

- Fra <http://snl.no/kvalitetssikring>: Kvalitetssikring, planlagte og systematiske aktiviteter som gjøres for å oppnå at et produkt eller en tjeneste vil oppfylle kravene til kvalitet
- På samme måte som industrien tilbyr produkter til sine kunder, så tilbyr NTNU emner til sine studenter
- I så måte ønsker NTNU å tilby best mulig kvalitet på sine emner til studentene:
  - Sikre at emnets læringsmål er oppdaterte og relevante
  - Sikre at læringsaktivitetene i emnet bidrar til at studentene oppnår læringsutbyttet
  - Sikre at det er sammenheng mellom læringsmålene, læringsaktivitetene og vurderingsformene
- NTNU har egne wiki-sider med mye nyttig informasjon for både studenter og ansatte: <https://innsida.ntnu.no/wiki> (her kan man søke seg frem til det meste)
- Direkte lenke til NTNUs sider om kvalitetssikring av utdanning: <https://innsida.ntnu.no/wiki/-/wiki/Norsk/Kvalitetssikring+av+utdanning>
- Hvis ingenting blir gjort kan dere melde inn via NTNUs avvikssystem: <https://innsida.ntnu.no/avvik>

# Referansegruppe

- Hver gang et emne har blitt undervist ved NTNU skal faglærer lage en emnerapport som beskriver tilstanden til emnet, inkludert tilbakemelding fra studenter og handlingsplan med tiltak for forbedringer til neste gang
- **Tilbakemelding fra studenter** innhentes vanligvis gjennom en referansegruppe, som skal **gi faglærer en referanse på hva studentene mener om faget**
- Referansegruppe:
  - Skal bestå av et representativt utvalg av emnets studenter (kjønn, studieprogram)
  - Minimum tre studenter
  - Skal løpende ta imot innspill fra alle studentene som følger emnet
  - Gjennomfører tre møter i løpet av semesteret: Oppstart, midtveis og ved avslutning av emnet
  - Skriver referansegrupperapport som oppsummerer studentenes synspunkter og forbedringsforslag
  - Alle medlemmene får tilbud om de ønsker bekreftelse på at de har deltatt i referansegruppen

# Tilbakekobling for undervisning

