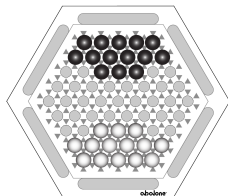


Exploration of Abalone game-playing agents

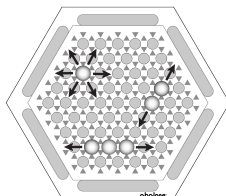
Ture Claussen

2021-06-14

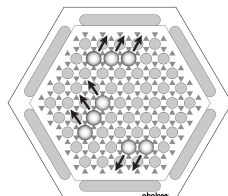
Rules



(a) Starting position



(b) "In-line" moves



(c) "Side-step" moves

Agent design: PEAS

Performance measure Win/loss, number of moves, time to deliberate

Environment Digital playing board

Actuators Move marbles, display text to CLI

Sensors Position of marbles

Agent design: Environment

- ▶ fully observable
- ▶ two-agent
- ▶ competitive
- ▶ sequential
- ▶ static and discrete

State space complexity

$$\sum_{k=8}^{14} \sum_{m=9}^{14} \frac{61!}{k!(61-k)!} \times \frac{(61-k)!}{m!((61-k)-m)!}$$

Game tree complexity

- ▶ Average branching factor b of 60
- ▶ Average length of game d of 87 [?]

$$b^d = 60^{87}$$

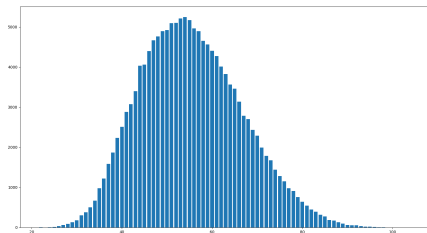
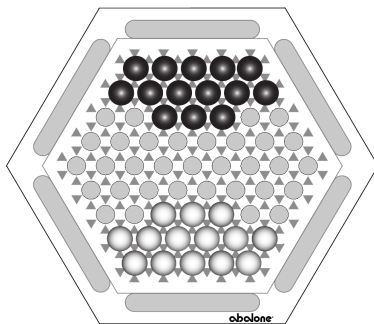


Figure: Counts of moves available for random for random player in 5 games

Complexity Comparison

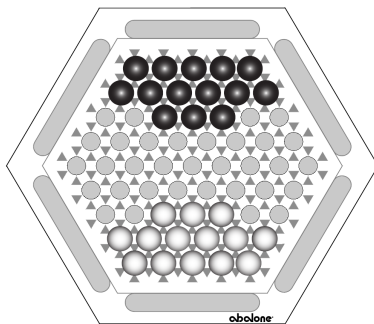
| Game | state-space complexity (log) | game-tree complexity (log) |
|-------------|------------------------------|----------------------------|
| Tic-tac-toe | 3 | 5 |
| Reversi | 28 | 58 |
| Chess | 46 | 123 |
| Abalone | 24 | 154 |
| Go | 172 | 360 |

Heuristics: Adjacency



$$\text{adjacency} = n_{\text{self}} - n_{\text{opponent}}$$

Heuristics: Distance



$$\text{distance} = n_{\text{self}} - n_{\text{opponent}}$$

Heuristics: Marble ratio

$$\text{marbleRatio} = n_{\text{won}} - n_{\text{lost}}$$

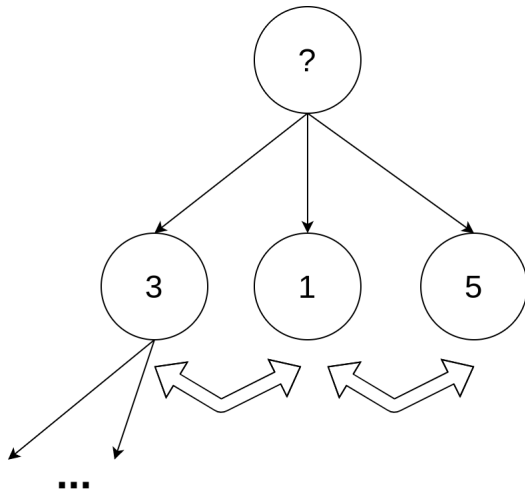
Heuristics: Win and loss

$$\text{winLoss} = \begin{cases} 1 & \text{if game won} \\ -1 & \text{otherwise} \end{cases}$$

| Heuristic | weight |
|-------------|--------|
| adjacency | 1 |
| distance | -1.5 |
| marbleRatio | 100 |
| winLoss | 100000 |

Table: Weights for the linear combination

Alpha-beta pruning agent: Move ordering



Alpha-beta pruning agent: Move ordering

- ▶ Move capturing marble: +3
- ▶ Move pushing marble: +1
- ▶ Move involving 2/3 marbles: +1/+2

Alpha-beta pruning agent: Move ordering

| Depth | Without ordering | Evaluation 1 | Evaluation 2 | $\sqrt{b^d}$ |
|-------|------------------|--------------|--------------|--------------|
| 1 | 45 | 45 | 45 | 8 |
| 2 | 1594 | 304 | 132 | 60 |
| 3 | 9755 | 4971 | 2423 | 464 |
| 4 | 457309 | 94650 | 6918 | 3600 |

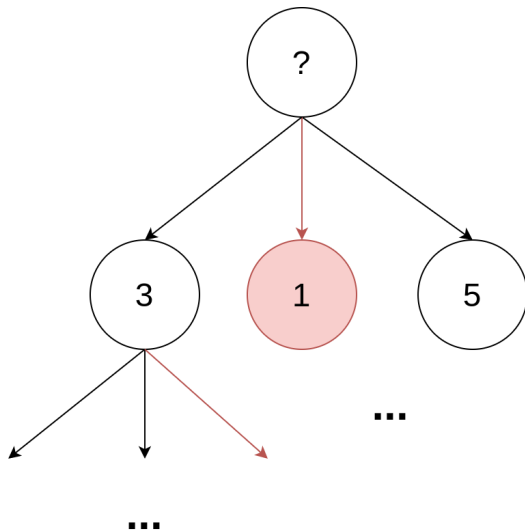
Table: Nodes visited with/without move ordering and the optimal case

Alpha-beta pruning agent: Transposition table

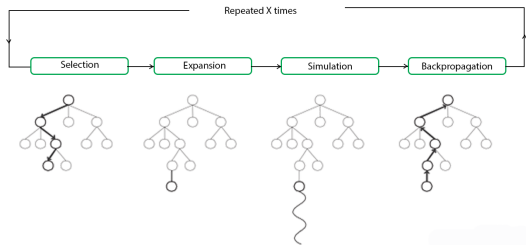
| | 1 | 2 | ... |
|-----|--------------|--------------|-----|
| 1 | 129310293812 | 929310293912 | ... |
| 2 | 889394293012 | 426317297917 | ... |
| ... | ... | ... | ... |

Table: Zobrist hash table

Alpha-beta pruning agent: Branch cutting



Monte carlo search agent



Monte carlo search agent: UCB

$$UCB(n) = \frac{U(n)}{N(n)} + C \times \sqrt{\frac{\log N(\text{Parent}(n))}{N(n)}}$$

Monte carlo search agent: Playout policy

- ▶ Random moves bad as branching factor is high
- ▶ Choose moves based on evaluation function

Face-off

| Black player | White player | Marbles lost b | |
|----------------------------|---------------------|----------------|--|
| AlphaBeta (d=3) | Random | 0.2 | |
| AlphaBeta (d=4) | Random | 0.0 | |
| AlphaBeta (d=3) | AlphaBetaFast (d=3) | 6.0 | |
| MonteCarloPure (t=20s) | RandomPlayer | 5.0 | |
| MonteCarloImproved (t=20s) | RandomPlayer | 0.0 | |
| MonteCarloImproved (t=20s) | AlphaBetaFast (d=3) | 0.0 | |

Table: Face-off results

Conclusion

- ▶ Implementation simple, improvement requires a lot of engineering
- ▶ MCTS performed badly but with more time still promising