O3_reference_and_sensor_data_with_temp

February 14, 2024

0.0.1 Sensor Constants

```
[]: sensor_name = 'alpha_o3_conc'
sensor_1_name = 'alpha_o3_1_conc'
sensor_2_name = 'alpha_o3_2_conc'
```

0.1 Upload Data from File

0.1.1 Sensor 1

```
directory_path = 'input/'
file_name = sensor_1_name + '_and_temp_valid_1HR.csv'
df_1 = pd.read_csv(directory_path + file_name)
df_1.head()
```

```
[]:
                                                             measuring 1 no Temp \
                   DateTime measuring 1
                                          temperature
                                                      Hour
     0 2022-12-14 14:30:00
                               42.267696
                                                         14
                                                                       56.369783
                                             31.52000
     1 2022-12-14 15:30:00
                               50.822340
                                             30.56750
                                                         15
                                                                       69.328964
     2 2022-12-14 16:30:00
                               67.516902
                                             28.82875
                                                         16
                                                                       94.063829
     3 2022-12-14 17:30:00
                               68.069052
                                             27.91125
                                                         17
                                                                       98.858670
     4 2022-12-14 18:30:00
                               84.294900
                                             27.16250
                                                                      118.546877
                                                         18
```

```
Count 1 Tag
0 3 VALID
1 4 VALID
2 4 VALID
3 4 VALID
4 VALID
```

```
[]: import locale locale.LC_TIME, 'pt_BR')
```

```
[]: 'pt_BR'
```

0.1.2 Create Sensor Dataframe as Pandas Series

```
[]: # Remove the first column with the indexes and save data into web dataframe
     dataframe = df_1.drop(df_1.columns[0], axis='columns')
     dataframe['DateTime'] = (pd.to_datetime(df_1['DateTime'],__
      ⇔infer_datetime_format=True))
     # Resample data with 15 mins period and create sensor dataframe
     sensor 1 dataframe = dataframe.sort values(by='DateTime', ascending=True).
      →reset_index().drop(columns='index')
     sensor_1_dataframe.index = sensor_1_dataframe['DateTime']
     sensor_1_dataframe = sensor_1_dataframe.drop(columns=['DateTime', 'Hour'])
     sensor_1_dataframe = sensor_1_dataframe.rename(columns={'temperature':__
      sensor 1 dataframe
    /var/folders/wc/_83zcrx913j1dqwg4g90kbhh0000gp/T/ipykernel_6358/1180347280.py:3:
    UserWarning: The argument 'infer_datetime_format' is deprecated and will be
    removed in a future version. A strict version of it is now the default, see
    https://pandas.pydata.org/pdeps/0004-consistent-to-datetime-parsing.html. You
    can safely remove this argument.
      dataframe['DateTime'] = (pd.to_datetime(df_1['DateTime'],
    infer_datetime_format=True))
[]:
                         measuring 1 temperature 1 measuring 1 no Temp Count 1 \
    DateTime
    2022-12-14 14:30:00
                            42.267696
                                            31.52000
                                                                56.369783
                                                                                 3
     2022-12-14 15:30:00
                            50.822340
                                            30.56750
                                                                69.328964
                                                                                 4
     2022-12-14 16:30:00
                            67.516902
                                            28.82875
                                                                94.063829
                                                                                 4
     2022-12-14 17:30:00
                           68.069052
                                                                                 4
                                            27.91125
                                                                98.858670
     2022-12-14 18:30:00
                            84.294900
                                            27.16250
                                                               118.546877
     2023-04-19 16:30:00
                            50.962218
                                            28.84750
                                                                77.422442
     2023-04-19 17:30:00
                            56.130342
                                            27.83625
                                                                87.266774
     2023-04-19 18:30:00
                            40.233330
                                            25.86125
                                                                80.502529
                                                                                 4
     2023-04-19 19:30:00
                                                               101.722552
                            51.222342
                                            23.64875
     2023-04-20 20:30:00
                            38.675040
                                            22.74000
                                                                93.377479
                            Tag
    DateTime
     2022-12-14 14:30:00 VALID
     2022-12-14 15:30:00 VALID
     2022-12-14 16:30:00
                         VALID
     2022-12-14 17:30:00
                         VALID
     2022-12-14 18:30:00
                         VALID
     2023-04-19 16:30:00
                         VALID
```

2023-04-19 17:30:00

VALID

```
2023-04-19 18:30:00 VALID
2023-04-19 19:30:00 VALID
2023-04-20 20:30:00 VALID
[1021 rows x 5 columns]
```

0.1.3 Sensor 2

```
[]: import pandas as pd
    directory_path = 'input/'
    file_name = sensor_2_name + '_and_temp_valid_1HR.csv'
    df_2 = pd.read_csv(directory_path + file_name)
    df 2.head()
[]:
                  DateTime measuring 2 temperature Hour measuring 2 no Temp \
    0 2022-11-28 11:30:00
                              53.759778
                                            30.10750
                                                        11
                                                                      11.239952
    1 2022-11-28 12:30:00
                              53.445666
                                            29.88250
                                                        12
                                                                      11.476654
    2 2022-11-28 13:30:00
                              54.100884
                                                        13
                                            30.24125
                                                                      11.253630
    3 2022-11-28 14:30:00
                              53.921742
                                            30.13250
                                                        14
                                                                      11.340715
    4 2022-11-28 15:30:00
                              53.494746
                                            29.89875
                                                        15
                                                                      11.485953
       Count 2
                  Tag
```

0 4 VALID 1 4 VALID 2 4 VALID 3 4 VALID 4 4 VALID

0.1.4 Create Sensor Dataframe as Pandas Series

/var/folders/wc/_83zcrx913j1dqwg4g90kbhh0000gp/T/ipykernel_6358/3647602612.py:3: UserWarning: The argument 'infer_datetime_format' is deprecated and will be removed in a future version. A strict version of it is now the default, see

 ${\tt https://pandas.pydata.org/pdeps/0004-consistent-to-date time-parsing.html.\ You can safely remove this argument.}$

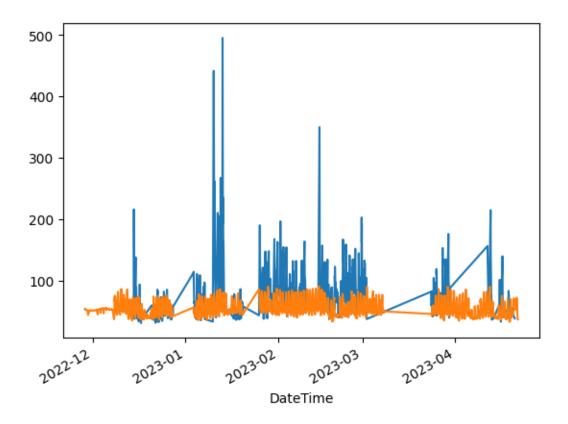
dataframe['DateTime'] = (pd.to_datetime(df_2['DateTime'],
infer_datetime_format=True))

[]:			measuring 2	temperature 2	measuring 2 no Temp	Count 2 \	
	DateTime		G	•	•		
	2022-11-28	11:30:00	53.759778	30.10750	11.239952	4	
	2022-11-28	12:30:00	53.445666	29.88250	11.476654	4	
	2022-11-28	13:30:00	54.100884	30.24125	11.253630	4	
	2022-11-28	14:30:00	53.921742	30.13250	11.340715	4	
	2022-11-28	15:30:00	53.494746	29.89875	11.485953	4	
	•••		•••	•••			
	2023-04-21	17:30:00	50.964672	30.53625	7.395241	4	
	2023-04-21	18:30:00	42.360948	27.13750	7.111857	4	
	2023-04-21	19:30:00	39.303264	25.32750	8.485160	4	
	2023-04-21	20:30:00	37.688532	24.45875	8.997179	4	
	2023-04-21	21:30:00	37.048038	23.90625	9.709237	4	
			Tag				
	DateTime		-46				
	2022-11-28	11:30:00	VALID				
	2022-11-28						
	2022-11-28						
	2022-11-28						
	2022-11-28						
	•••		•••				
	2023-04-21	17:30:00	VALID				
	2023-04-21	18:30:00	VALID				
	2023-04-21	19:30:00	VALID				
	2023-04-21	20:30:00	VALID				
	2023-04-21	21:30:00	VALID				
	[2603 rows	x 5 colum	ns]				

0.1.5 Plot raw data

```
[]: sensor_1_dataframe['measuring 1'].plot()
sensor_2_dataframe['measuring 2'].plot()
```

[]: <Axes: xlabel='DateTime'>



0.2 Compare with original data

0.3 Load reference and sensor data

/var/folders/wc/_83zcrx913j1dqwg4g90kbhh0000gp/T/ipykernel_6358/2986665073.py:4:

UserWarning: The argument 'infer_datetime_format' is deprecated and will be removed in a future version. A strict version of it is now the default, see https://pandas.pydata.org/pdeps/0004-consistent-to-datetime-parsing.html. You can safely remove this argument.

reference_data['DateTime'] = (pd.to_datetime(reference_data['DateTime'],
infer_datetime_format=True))

```
[]: DateTime
2022-01-01 02:30:00
2022-01-01 03:30:00
```

2022-01-01 02:30:00 13.23 2022-01-01 03:30:00 12.07 2022-01-01 04:30:00 13.24

2022-01-01 05:30:00 14.42 2022-01-01 06:30:00 13.30

2022-01-01 06:30:00 13.30

2023-02-08 12:30:00 50.01 2023-02-08 13:30:00 67.43 2023-02-08 14:30:00 72.46

2023-02-08 14:30:00 72.46 2023-02-08 15:30:00 59.65 2023-02-08 16:30:00 NaN

Name: Ozônio, Length: 9687, dtype: float64

0.4 Merge sensor and reference data

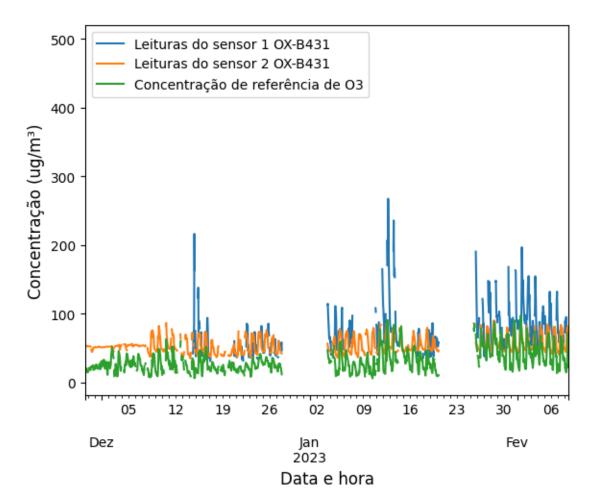
```
[]:
                           measuring 1 measuring 1 no Temp measuring 2 \
     DateTime
     2022-11-28 11:30:00
                                   NaN
                                                          NaN
                                                                 53.759778
     2022-11-28 12:30:00
                                   NaN
                                                          NaN
                                                                 53.445666
     2022-11-28 13:30:00
                                   NaN
                                                          NaN
                                                                 54.100884
     2022-11-28 14:30:00
                                   NaN
                                                          NaN
                                                                 53.921742
     2022-11-28 15:30:00
                                                          NaN
                                                                 53.494746
                                   NaN
     2023-04-21 17:30:00
                                   NaN
                                                          {\tt NaN}
                                                                 50.964672
     2023-04-21 18:30:00
                                   NaN
                                                          NaN
                                                                 42.360948
     2023-04-21 19:30:00
                                                          NaN
                                   NaN
                                                                 39.303264
     2023-04-21 20:30:00
                                   NaN
                                                          NaN
                                                                 37.688532
     2023-04-21 21:30:00
                                   NaN
                                                          NaN
                                                                 37.048038
```

```
DateTime
     2022-11-28 11:30:00
                                     11.239952
                                                    30.10750
     2022-11-28 12:30:00
                                     11.476654
                                                    29.88250
     2022-11-28 13:30:00
                                     11.253630
                                                    30.24125
     2022-11-28 14:30:00
                                     11.340715
                                                    30.13250
     2022-11-28 15:30:00
                                     11.485953
                                                    29.89875
     2023-04-21 17:30:00
                                      7.395241
                                                    30.53625
     2023-04-21 18:30:00
                                      7.111857
                                                    27.13750
     2023-04-21 19:30:00
                                      8.485160
                                                    25.32750
     2023-04-21 20:30:00
                                      8.997179
                                                    24.45875
     2023-04-21 21:30:00
                                      9.709237
                                                    23.90625
     [2616 rows x 5 columns]
[]: sensor_data = pd.concat([sensor_data, reference_data], axis=1, join='inner')
     sensor_data = sensor_data.rename(columns={'Ozônio': 'reference'})
     sensor_data
[]:
                           measuring 1 measuring 1 no Temp measuring 2 \
     DateTime
     2022-11-28 11:30:00
                                   NaN
                                                         NaN
                                                                 53.759778
     2022-11-28 12:30:00
                                   NaN
                                                         NaN
                                                                 53.445666
     2022-11-28 13:30:00
                                   NaN
                                                         NaN
                                                                 54.100884
     2022-11-28 14:30:00
                                   NaN
                                                         NaN
                                                                 53.921742
     2022-11-28 15:30:00
                                   NaN
                                                         NaN
                                                                53.494746
     2023-02-08 12:30:00
                                                                80.255616
                                   NaN
                                                         {\tt NaN}
     2023-02-08 13:30:00
                                   NaN
                                                         NaN
                                                                81.669120
     2023-02-08 14:30:00
                                                         NaN
                                   NaN
                                                                80.498562
     2023-02-08 15:30:00
                                                         NaN
                                                                79.146408
                                   NaN
     2023-02-08 16:30:00
                                   NaN
                                                         NaN
                                                                 71.617536
                           measuring 2 no Temp
                                                temperature reference
     DateTime
     2022-11-28 11:30:00
                                     11.239952
                                                    30.10750
                                                                   21.49
     2022-11-28 12:30:00
                                     11.476654
                                                    29.88250
                                                                     NaN
     2022-11-28 13:30:00
                                     11.253630
                                                    30.24125
                                                                     NaN
     2022-11-28 14:30:00
                                     11.340715
                                                    30.13250
                                                                   20.56
     2022-11-28 15:30:00
                                     11.485953
                                                    29.89875
                                                                   21.15
     2023-02-08 12:30:00
                                     15.204469
                                                    39.31125
                                                                  50.01
     2023-02-08 13:30:00
                                                                   67.43
                                     15.351102
                                                    39.82875
     2023-02-08 14:30:00
                                     13.929618
                                                    39.93125
                                                                   72.46
                                                                   59.65
     2023-02-08 15:30:00
                                     12.788609
                                                    39.84500
                                                    37.96000
     2023-02-08 16:30:00
                                                                     NaN
                                      9.874328
```

measuring 2 no Temp temperature

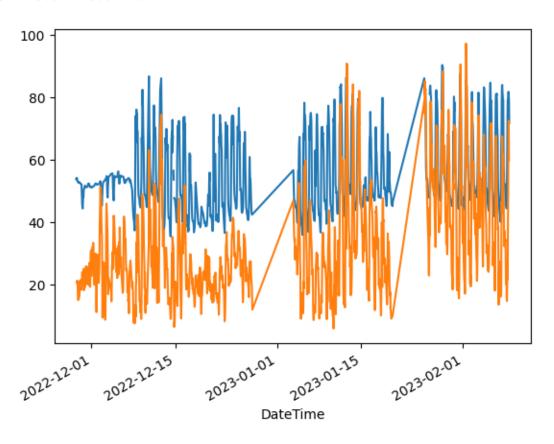
0.4.1 Plot reference and sensor data

[]: Text(0, 0.5, 'Concentração (ug/m³)')



```
[]: sensor_data['measuring 2'].plot() sensor_data['reference'].plot()
```

[]: <Axes: xlabel='DateTime'>



0.5 Plot sensor vs. reference

0.5.1 Sensor 1

```
from scipy.stats import kendalltau, spearmanr, gaussian_kde
import matplotlib.pyplot as plt
import numpy as np

median_reference = sensor_data['reference'].median()
median_measuring = sensor_data['measuring 1'].median()

fig, ax = plt.subplots(figsize=(1.3*5,5))
xy = np.vstack([sensor_data['reference'].fillna(value=median_reference),
sensor_data['measuring 1'].fillna(value=median_measuring)])
```

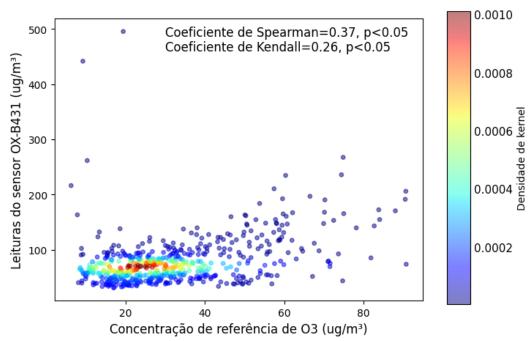
```
z = gaussian_kde(xy)(xy)
plt.scatter(sensor data['reference'], sensor data['measuring 1'], c=z, __
 ⇔cmap='jet', s=15, alpha=.5)
plt.title('Leituras do sensor 1 OX-B431 vs Concentração de referência de O3 \n',
          fontdict={'fontsize':15})
plt.xlabel('Concentração de referência de O3 (ug/m\N{SUPERSCRIPT THREE}))',
           fontsize=12)
plt.ylabel('Leituras do sensor OX-B431 (ug/m\N{SUPERSCRIPT THREE}))',
           fontsize=12)
coef, p = spearmanr(sensor_data['reference'], sensor_data['measuring 1'],
                    nan_policy='omit')
print('Spearmans correlation coefficient: %.2f' % coef)
# interpret the significance
alpha = 0.05
if p > alpha:
        print('Samples are uncorrelated (fail to reject HO) p=%.2f' % p)
else:
       print('Samples are correlated (reject HO) p=%.2f' % p)
kendall, pken = kendalltau(sensor_data['reference'], sensor_data['measuring 1'],
                            nan_policy='omit')
print('Kendall correlation coefficient: %.2f' % coef)
# interpret the significance
alpha = 0.05
if p > alpha:
       print('Samples are uncorrelated (fail to reject HO) p=%.2f' % p)
else:
       print('Samples are correlated (reject HO) p=%.2f' % p)
cax = plt.axes([0.95, 0.1, 0.05, 0.8])
cbar = plt.colorbar(orientation='vertical', cax=cax, label="Densidade de∟
 ⇔kernel")
cbar.ax.tick_params(labelsize=11, length=0)
string = 'Coeficiente de Spearman=%.2f, p<0.05' % coef
plt.text(0.3, 0.95, string, horizontalalignment='left', fontsize=12,
         verticalalignment='center', transform=ax.transAxes)
string = 'Coeficiente de Kendall=%.2f, p<0.05' % kendall
plt.text(0.3, 0.90, string, horizontalalignment='left', fontsize=12,
         verticalalignment='center', transform=ax.transAxes)
```

Spearmans correlation coefficient: 0.37 Samples are correlated (reject H0) p=0.00 Kendall correlation coefficient: 0.37

```
Samples are correlated (reject H0) p=0.00
```

[]: Text(0.3, 0.9, 'Coeficiente de Kendall=0.26, p<0.05')

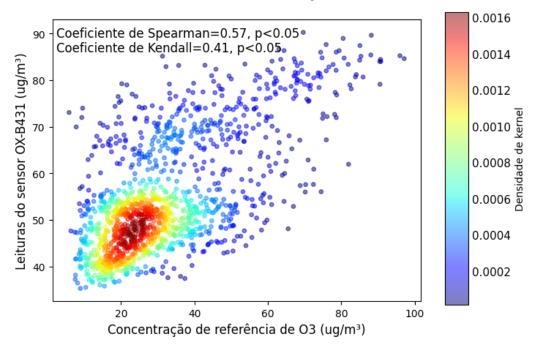
Leituras do sensor 1 OX-B431 vs Concentração de referência de O3



0.5.2 Sensor 2

```
fontsize=12)
     plt.ylabel('Leituras do sensor OX-B431 (ug/m\N{SUPERSCRIPT THREE})',
                fontsize=12)
     coef, p = spearmanr(sensor_data['reference'], sensor_data['measuring 2'],
                         nan_policy='omit')
     print('Spearmans correlation coefficient: %.2f' % coef)
     # interpret the significance
     alpha = 0.05
     if p > alpha:
             print('Samples are uncorrelated (fail to reject HO) p=%.2f' % p)
     else:
             print('Samples are correlated (reject HO) p=%.2f' % p)
     kendall, pken = kendalltau(sensor_data['reference'], sensor_data['measuring 2'],
                                 nan_policy='omit')
     print('Kendall correlation coefficient: %.2f' % coef)
     # interpret the significance
     alpha = 0.05
     if p > alpha:
             print('Samples are uncorrelated (fail to reject HO) p=%.2f' % p)
     else:
             print('Samples are correlated (reject H0) p=%.2f' % p)
     cax = plt.axes([0.95, 0.1, 0.05, 0.8])
     cbar = plt.colorbar(orientation='vertical', cax=cax, label="Densidade dell
      ⇔kernel")
     cbar.ax.tick_params(labelsize=11, length=0)
     string = 'Coeficiente de Spearman=%.2f, p<0.05' % coef
     plt.text(0.01, 0.95, string, horizontalalignment='left', fontsize=12,
              verticalalignment='center', transform=ax.transAxes)
     string = 'Coeficiente de Kendall=%.2f, p<0.05' % kendall
     plt.text(0.01, 0.90, string, horizontalalignment='left', fontsize=12,
              verticalalignment='center', transform=ax.transAxes)
    Spearmans correlation coefficient: 0.57
    Samples are correlated (reject HO) p=0.00
    Kendall correlation coefficient: 0.57
    Samples are correlated (reject HO) p=0.00
[]: Text(0.01, 0.9, 'Coeficiente de Kendall=0.41, p<0.05')
```

Leituras do sensor 2 OX-B431 vs Concentração de referência de O3



0.6 Plot reference vs. temperature

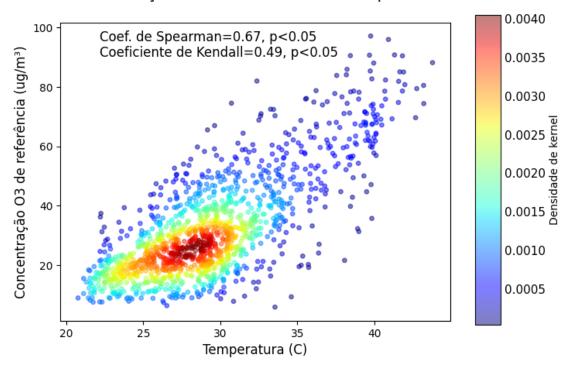
```
[]:|from scipy.stats import kendalltau, spearmanr, gaussian_kde
     import matplotlib.pyplot as plt
     import numpy as np
     median_reference = sensor_data['reference'].median()
     median_temperature = sensor_data['temperature'].median()
     fig, ax = plt.subplots(figsize=(1.3*5,5))
     xy = np.vstack([sensor_data['temperature'].fillna(value=median_temperature),_
      sensor_data['reference'].fillna(value=median_reference)])
     z = gaussian_kde(xy)(xy)
     plt.scatter(sensor_data['temperature'], sensor_data['reference'], c=z,__

cmap='jet', s=15, alpha=.5)
     plt.title('Concentração O3 de referência vs Temperatura\n',
               fontdict={'fontsize':15})
     plt.xlabel('Temperatura (C)',
                fontsize=12)
     plt.ylabel('Concentração O3 de referência (ug/m\N{SUPERSCRIPT THREE}))',
                fontsize=12)
```

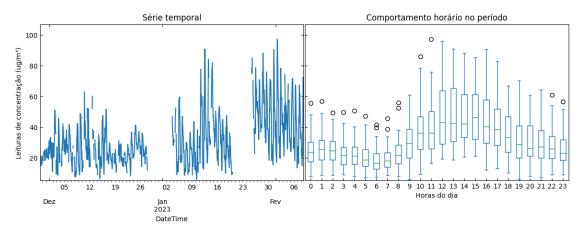
```
coef, p = spearmanr(sensor_data['temperature'], sensor_data['reference'],
                    nan_policy='omit')
print('Spearmans correlation coefficient: %.2f' % coef)
# interpret the significance
alpha = 0.05
if p > alpha:
        print('Samples are uncorrelated (fail to reject HO) p=%.2f' % p)
else:
        print('Samples are correlated (reject HO) p=%.2f' % p)
kendall, pken = kendalltau(sensor_data['temperature'], sensor_data['reference'],
                            nan policy='omit')
print('Kendall correlation coefficient: %.2f' % coef)
# interpret the significance
alpha = 0.05
if p > alpha:
        print('Samples are uncorrelated (fail to reject H0) p=%.2f' % p)
else:
        print('Samples are correlated (reject HO) p=%.2f' % p)
cax = plt.axes([0.95, 0.1, 0.05, 0.8])
cbar = plt.colorbar(orientation='vertical', cax=cax, label="Densidade de⊔
 ⇔kernel")
cbar.ax.tick_params(labelsize=11, length=0)
string = 'Coef. de Spearman=%.2f, p<0.05' % coef
plt.text(0.1, 0.95, string, horizontalalignment='left', fontsize=12,
         verticalalignment='center', transform=ax.transAxes)
string = 'Coeficiente de Kendall=%.2f, p<0.05' % kendall
plt.text(0.1, 0.90, string, horizontalalignment='left', fontsize=12,
         verticalalignment='center', transform=ax.transAxes)
Spearmans correlation coefficient: 0.67
Samples are correlated (reject HO) p=0.00
Kendall correlation coefficient: 0.67
Samples are correlated (reject HO) p=0.00
```

[]: Text(0.1, 0.9, 'Coeficiente de Kendall=0.49, p<0.05')

Concentração O3 de referência vs Temperatura



```
[]: def plot_box(df):
        bottom, height = 0.1, 0.65
        left, width = bottom, height*1.3
         spacing = 0.005
        rect_ser = [left-width-spacing, bottom, width, height]
        rect_box = [left, bottom, width, height]
        plt.figure(figsize=(1.3*5,5))
        ax_ser = plt.axes(rect_ser)
        ax_ser.tick_params(direction='in', top=True, right=True)
        ax_ser.set_title('Série temporal')
        ax_ser.set_xlabel("Data e hora")
        ax_ser.set_ylabel("Leituras de concentração (ug/m\N{SUPERSCRIPT THREE})")
        ax_box = plt.axes(rect_box)
        ax_box.tick_params(direction='in', labelleft=False)
        lim_max = df['reference'].max()+df['reference'].max()*10/100
        lim_min = df['reference'].min()-df['reference'].min()*10/100
```



0.7 Calibrate data

0.7.1 Prepare training and test sets

```
[]: from sklearn.model_selection import train_test_split
from sklearn.model_selection import cross_validate

reference_median = sensor_data['reference'].median()
sensor_1_median = sensor_data['measuring 1'].median()
sensor_2_median = sensor_data['measuring 2'].median()
temperature_mean = sensor_data['temperature'].mean()
trend_1_median = sensor_data['measuring 1 no Temp'].median()
trend_2_median = sensor_data['measuring 2 no Temp'].median()

variables_names = ['measuring 1', 'measuring 2', 'temperature']

y = sensor_data['reference'].fillna(value=reference_median)
```

0.7.2 Grid search with different models and variables combinations

```
[]: from itertools import combinations
              def check_if_list_contains(list1, list2):
                         return [element for element in list1 if element in list2]
              indexes = []
              reference_indexes = [0, 1]
              num_variables = len(variables_names)
              for num_combinations in list(range(num_variables)):
                          contains_reference = False
                          index_list = [list(index_tuple) for index_tuple in_
                 →list(combinations(list(range(num_variables)), r=num_combinations+1))]
                         for sublist in index_list:
                                     contains_reference = check_if_list_contains(sublist, reference_indexes)
                                     if contains_reference:
                                                 indexes.append(sublist)
                                                 contains_reference = False
              feature_subsets = { }
              for index_list in indexes:
                         kev = ""
                         new index list = []
                         for index in index list:
                                     if len(key) < 1:</pre>
                                                 new_index_list.append(index)
                                                key = key + variables_names[index] + " | "
                                     elif not ('measuring 1' in key and 'measuring 1' in
                  ovariables_names[index]) and not ('measuring 2' in key and 'measuring 
                  ⇔variables_names[index]):
                                                new_index_list.append(index)
                                                key = key + variables_names[index] + " | "
                         feature_subsets[key] = new_index_list
              feature subsets
```

```
'measuring 1 | temperature | ': [0, 2],
'measuring 2 | temperature | ': [1, 2],
'measuring 1 | measuring 2 | temperature | ': [0, 1, 2]}
```

Function for plotting observations vs. predictions

```
[]: import matplotlib.pyplot as plt
    from scipy.stats import spearmanr, kendalltau, gaussian_kde
    import numpy as np
    import os
    def plot_predictions_and_observations(X, y, r2, rmse, mae, file_name):
        fig, ax = plt.subplots(figsize=(1.3*5,5))
        xy = np.vstack([X, y])
        z = gaussian kde(xy)(xy)
        ax.scatter(X, y, c=z,s=15,alpha=.5)
        spear_corr, p_value = spearmanr(y, X)
        spearman_text = ''
        alpha = 0.05
        if p_value > alpha:
            spearman_text = 'Coeficiente de Spearman: {:.2f}'.format(spear_corr) + L
      \hookrightarrow', p>0.05'
        else:
            spearman_text = 'Coeficiente de Spearman: {:.2f}'.format(spear_corr) +
      \hookrightarrow', p<0.05'
        kendall_corr, p_value = kendalltau(y, X)
        alpha = 0.05
        kendall_text = ''
        if p_value > alpha:
            kendall_text = 'Coeficiente de Kendall: {:.2f}'.format(kendall_corr) + L
      \hookrightarrow', p>0.05'
        else:
            kendall_text = 'Coeficiente de Kendall: {:.2f}'.format(kendall_corr) +
      9', p<0.05'
        plt.text(0.02, 0.95, spearman_text, ha='left', va='center', transform=plt.
      ⇒gca().transAxes, fontsize=12)
        plt.text(0.02, 0.90, kendall_text, ha='left', va='center', transform=plt.

¬gca().transAxes, fontsize=12)

std())
        rmse_text = 'RMSE = {:.2f} ± {:.2f}'.format(rmse.mean(), rmse.std())
        mae_text = 'MAE = {:.2f} + {:.2f}'.format(mae.mean(), mae.std())
        plt.text(0.02, 0.85, r2_text, ha='left', va='center', transform=plt.gca().
      →transAxes, fontsize=12)
```

```
plt.text(0.02, 0.80, rmse_text, ha='left', va='center', transform=plt.gca().
      ⇔transAxes, fontsize=12)
         plt.text(0.02, 0.75, mae_text, ha='left', va='center', transform=plt.gca().

→transAxes, fontsize=12)
         ax.set_xlim([np.min([y,X]),np.max([y,X])])
         ax.set_ylim([np.min([y,X]),np.max([y,X])])
         ax.set_aspect('equal')
         ax.plot([xy.min(), xy.max()], [xy.min(), xy.max()], 'k-', lw=1,dashes=[2,__
      ⇒2])
         ax.fill_between(np.linspace(xy.min(), xy.max(),y.shape[0]),
                         np.linspace(xy.min(), xy.max(),y.shape[0])*0.5,
                         alpha=0.2,facecolor='gray',edgecolor=None)
         ax.fill_between(np.linspace(xy.min(),xy.max(),y.shape[0]),
                         np.linspace(xy.max(),xy.max(),y.shape[0]),
                         np.linspace(xy.min(),xy.max(),y.shape[0])*2,
                         alpha=0.2,facecolor='gray',edgecolor=None)
         ax.set_xlabel('Concentração de O3 observada (ug/m\N{SUPERSCRIPT THREE})', u
      →fontsize=12)
         ax.set ylabel('Concentração de O3 inferida (ug/m\N{SUPERSCRIPT_11
      ⇔THREE})',fontsize=12)
         if not os.path.exists('images/'):
             os.makedirs('images/')
         plt.savefig('images/' + '03_UNI_' + file_name + '.png')
[]: from sklearn.linear_model import LinearRegression
     from sklearn.neural_network import MLPRegressor
     from sklearn.neighbors import KNeighborsRegressor
     from sklearn.ensemble import RandomForestRegressor
     from sklearn.model_selection import GridSearchCV
     from sklearn.preprocessing import StandardScaler
     from sklearn.pipeline import Pipeline
     from sklearn.metrics import mean_squared_error
     import numpy as np
     models = {
         'MLP Regression': (
```

('mlp_regressor', MLPRegressor(solver="lbfgs", max_iter=1000,_

(4,), (10,), (50,), (100,), (200,), (4,4), (4,10), (4,50), (4,100), (4,200), (10,4), (10,10), (10,50), (10,100), (10,200),

'mlp_regressor__hidden_layer_sizes': [

→random_state=42)), {

```
(50,4), (50,10), (50,50), (50,100), (50,200),
                (100,4),(100,10),(100,50),(100,100),(100,200),
                (200,4),(200,10),(200,50),(200,100),(200,200)],
            'mlp_regressor_alpha': [0.0001, 0.001, 0.01, 0.1, 1, 10]
        }
    ),
    'Multilinear Regression': (
        ('linear_regressor', LinearRegression()), { }
    ),
    'KNN Regression': (
        ('knn_regressor', KNeighborsRegressor()), {
            'knn_regressor__n_neighbors': [3, 5, 7, 9, 11, 13, 15, 17, 20],
            'knn_regressor_weights': ['uniform', 'distance'],
            'knn_regressor__p': [1, 2] # 1 for Manhattan distance, 2 for_
 ⇒Euclidean distance'
        }
    ),
    'Random Forests Regression': (
        ('random forest regressor', RandomForestRegressor()), {
            'random_forest_regressor_n_estimators': [50, 100, 150],
            'random forest regressor max depth': [None, 10, 20, 30],
            'random_forest_regressor__min_samples_split': [2, 5, 10],
            'random_forest_regressor__min_samples_leaf': [1, 2, 4]
        }
    )
}
# Perform grid search for each feature subset
results = {}
rmse by features = {}
r2_by_features = {}
mae by features = {}
for features_set, subset in feature_subsets.items():
    X subset = X[:, subset]
    X_train_subset = X_train[:, subset]
    X_test_subset = X_test[:, subset]
    model_results = {}
    model rmse = {}
    model_r2 = \{\}
    model_mae = {}
    for model_name, (model, param_grid) in models.items():
        print(f"Grid search for features: {features_set} with model:
 →{model_name}...")
        pipeline = Pipeline([
            ('scaler', StandardScaler()),
```

```
model
      ])
      # Perform grid search with cross-validation
      grid_search = GridSearchCV(pipeline, param_grid, cv=3,__
⇒scoring='neg_root_mean_squared_error', n_jobs=-1)
      grid_search.fit(X_train_subset, y_train)
      # Print the best parameters and best score
      best_params = grid_search.best_params_
      # Evaluate the best model on the test set
      best_model = grid_search.best_estimator_
      cross_validation = cross_validate(best_model, X_subset, y, cv=3,__
scoring=['r2', 'neg_root_mean_squared_error', 'neg_mean_absolute_error'])
      y_pred = best_model.predict(X_test_subset)
      # Evaluate the model
      r2 = cross_validation['test_r2']
      rmse = cross_validation['test_neg_root_mean_squared_error']
      mae = cross_validation['test_neg_mean_absolute_error']
      plot_predictions_and_observations(y_test, y_pred, r2=r2, rmse=rmse,_
→mae=mae, file_name=model_name+features_set)
      model_results[model_name] = {
           'Best Model': best model,
           'Best Parameters': best_params,
          'Test R2': r2,
           'Test RMSE': rmse,
           'Test MAE': mae
      }
      model_rmse[model_name] = {
           'Mean': rmse.mean(),
           'Std': rmse.std()
      }
      model_r2[model_name] = {
          'Mean': r2.mean(),
          'Std': r2.std()
      model_mae[model_name] = {
          'Mean': mae.mean(),
          'Std': mae.std()
      }
  results[features_set] = model_results
  rmse_by_features[features_set] = model_rmse
```

1 Save Results

```
[]: output_directory_path = 'output/'
    rmse_file_name = output_directory_path + sensor_name + '_rmse.csv'
    r2_file_name = output_directory_path + sensor_name + '_r2.csv'
    mae_file_name = output_directory_path + sensor_name + '_mae.csv'
    results_file_name = output_directory_path + sensor_name + '_results.csv'

pd.DataFrame(rmse_by_features).transpose().to_csv(rmse_file_name)
    pd.DataFrame(r2_by_features).transpose().to_csv(r2_file_name)
    pd.DataFrame(mae_by_features).transpose().to_csv(mae_file_name)
    pd.DataFrame(results).transpose().to_csv(results_file_name)
```

1.1 Plot Results

```
ax_r2.set_title('R2')
         ax_rmse = plt.axes(rect_rmse)
         ax_rmse.tick_params(direction='in', labelleft=False, labelsize=14)
         ax_rmse.set_title('RMSE')
         ax_mae = plt.axes(rect_mae)
         ax_mae.tick_params(direction='in', labelleft=False, labelsize=14)
         ax_mae.set_title('MAE')
         y_pos = np.arange(len(features))
         ax_r2.barh(y_pos, r2_list, xerr=r2_error_list, align='center')
         min_r2 = r2_list.min() - r2_error_list.max()
         ax_r2.set_xlim([min_r2 - 0.05, 1.0 + 0.05])
         ax_r2.set_yticks(y_pos, labels=features, fontsize=14)
         ax_r2.invert_yaxis() # labels read top-to-bottom
         ax_r2.set_xlabel('R2', fontsize=14)
         ax_rmse.barh(y_pos, rmse_list, xerr=rmse_error_list, align='center')
         max_rmse = rmse_list.max() + rmse_error_list.max()
         min_rmse = rmse_list.min() - rmse_error_list.max()
         if max rmse <= 0: max rmse = -min rmse</pre>
         ax_rmse.set_xlim([min_rmse - 0.05, max_rmse + 0.05])
         ax_rmse.set_yticks(y_pos, labels=features, fontsize=14)
         ax_rmse.invert_yaxis() # labels read top-to-bottom
         ax rmse.set xlabel('RMSE', fontsize=14)
         ax_mae.barh(y_pos, mae_list, xerr=mae_error_list, align='center')
         max_mae = mae_list.max() + mae_error_list.max()
         min_mae = mae_list.min() - mae_error_list.max()
         if max_mae <= 0: max_mae = -min_mae</pre>
         ax_mae.set_xlim([min_mae - 0.05, max_mae + 0.05])
         ax_mae.set_yticks(y_pos, labels=features, fontsize=14)
         ax_mae.invert_yaxis() # labels read top-to-bottom
         ax_mae.set_xlabel('MAE', fontsize=14)
[]: mean r2 by features dataframe = pd.DataFrame()
     std_r2_by_features_dataframe = pd.DataFrame()
     mean rmse by features dataframe = pd.DataFrame()
     std_rmse_by_features_dataframe = pd.DataFrame()
     mean_mae_by_features_dataframe = pd.DataFrame()
     std_mae_by_features_dataframe = pd.DataFrame()
```

ax_r2.tick_params(direction='in', top=True, right=True, labelsize=14)

```
for key in list(feature_subsets.keys()):
        feature_dict = r2_by_features[key]
        for model in list(feature_dict.keys()):
            colum_name = key.replace('measuring', '03')
            colum_name = colum_name.replace(' |', ',')
            colum_name += f': {model[:-11]}'
            mean_r2_by_features_dataframe[colum_name] = ___
      ⇔[feature_dict[model]['Mean']]
            std r2_by_features_dataframe[colum_name] = [feature_dict[model]['Std']]
    for key in list(feature_subsets.keys()):
        feature_dict = rmse_by_features[key]
        for model in list(feature_dict.keys()):
            colum_name = key.replace('measuring', '03')
            colum_name = colum_name.replace(' |', ',')
            colum_name += f': {model[:-11]}'
            mean_rmse_by_features_dataframe[colum_name] =__
      std_rmse_by_features_dataframe[colum_name] =__
      ⇔[feature_dict[model]['Std']]
    for key in list(feature_subsets.keys()):
        feature dict = mae by features[key]
        for model in list(feature_dict.keys()):
            colum name = key.replace('measuring', '03')
            colum_name = colum_name.replace(' |', ',')
            colum name += f': {model[:-11]}'
            mean_mae_by_features_dataframe[colum_name] =__
      std_mae_by_features_dataframe[colum_name] = [feature_dict[model]['Std']]
[]: r2_sorted_dataframe = (mean_r2_by_features_dataframe.
     ⇔sort_values(by=mean_r2_by_features_dataframe.index[0], axis=1,__
     ⇔ascending=False))
    features = r2 sorted dataframe.columns
    mean_r2 = r2_sorted_dataframe.values.flatten()
    error_r2 = std_r2_by_features_dataframe[r2_sorted_dataframe.columns].values.
      →flatten()
    mean rmse = mean rmse by features dataframe[r2 sorted dataframe.columns].values.
      →flatten()
    error rmse = std rmse by features dataframe[r2_sorted dataframe.columns].values.
      →flatten()
```

