

3.1 Limites

$$\lim_{x \rightarrow 2} \frac{1+x^2}{1-x^2} = \frac{-5}{3} = -1,667 \quad (1)$$

3.1.1 Limites à esquerda e à direita

$$\lim_{x \rightarrow 3^+} \frac{x}{x-3} = \infty$$
$$\lim_{x \rightarrow 3^-} \frac{x+1}{(x-3)^3} = \frac{-1}{4} = -0,25 \quad (2)$$

3.2 Derivadas

$$f(x) = 2x^2 + 3x$$
$$\frac{\partial f}{\partial x} = 4x + 3$$
$$f(x) = \frac{1}{3-x} \quad (3)$$
$$\frac{\partial f}{\partial x} = \frac{1}{(x-3)^2}$$

3.2.1 Derivadas superiores

$$f(x) = \frac{1}{3-x}$$
$$\frac{\partial^2 f}{\partial x^2} = \frac{-2}{(x-3)^3} \quad (4)$$
$$f(x) = x - \frac{1}{x}$$
$$\frac{\partial^2 f}{\partial x^2} = \frac{-2}{x^3}$$

3.2.2 Derivadas Trigonométricas

$$f(x) = \sin(x)$$

$$\frac{\partial f}{\partial x} = \cos(x)$$

$$f(x) = \cos(2x)$$

$$\frac{\partial f}{\partial x} = -2 \cdot \sin(2x) \quad (5)$$

$$f(x) = \tan(3x+5)$$

$$\frac{\partial f}{\partial x} = 3 \cdot \tan(3x+5)^2 + 3$$

3.3 Integrais

$$\int \sqrt{x}(1-x)^2 dx = \frac{2x^{\frac{3}{2}}(15x^2 - 42x + 35)}{105} \quad (6)$$

$$\int \frac{2x^4 - 3x^3 + 5}{7x^2} dx = \frac{-(-4x^4 + 9x^3 + 30)}{42x}$$

3.3.1 Integrais trigonométricas

$$\int (\cos(2x)) dx = \frac{\sin(2x)}{2}$$

$$\int (\sin(3x+2)) dx = \frac{-\cos(3x+2)}{3} \quad (7)$$

$$\int (3 \cdot \cos(x\pi) + \cos(3x\pi)) dx = \frac{4(3 \cdot \sin(x\pi) - \sin(x\pi)^3)}{3\pi}$$

3.3.2 Integrais definidas

$$\int_0^2 \frac{2x}{(x-3)^2} dx = 4 - \log(9) \quad (8)$$

$$\int_0^1 (1 - 2x - 3x^2) dx = -1$$