

3.2 Q8 $C(t) = \frac{0.1t}{(t+3)^2}$, $1 \leq t \leq 6$

$$C'(t) = \frac{0.1(t+3)^2 - 0.1t[2(t+3)'(1)]}{(t+3)^4}$$

$$= \frac{0.1(t+3)' - 0.1t[2(1)]}{(t+3)^3}$$

$$= \frac{0.1[(t+3) - 2t]}{(t+3)^3}$$

$$= \frac{0.1[3-t]}{(t+3)^2}$$

$\therefore C'(t) = 0$ when $t = 3$

Check

$$C(1) = 0.0063$$

$$C(3) = 0.0083$$

$$C(6) = 0.0074$$

$$\therefore A_{\max} = 0.0083$$

$$A_{\min} = 0.0063$$

Q10 $r(x) = \frac{1}{4} \left[\frac{4900}{x} + x \right] = \frac{1}{4} [4900x^{-1} + x]$

$$r'(x) = \frac{1}{4} [-4900x^{-2} + 1] = 0$$

$$\therefore \frac{4900}{x^2} = 1$$

$$x^2 = 4900$$

$$x = 70 \text{ km/h}$$

$$r(30) = 48.3$$

$$r(70) = 35 \leftarrow \text{BEST!}$$

$$r(120) = 40.2$$

So @ 70 km/h, require 35 L/100 km

Thus 70 L required for 200 km

$$\text{Whence Cost} = 70(1.15)$$

$$= \underline{\underline{\$80.50}}$$

Q14) $u(x) = \frac{C(x)}{x} = 3000x^{-1} + 9 + 0.05x$

$$u'(x) = -3000x^{-2} + 0.05 = 0$$

$$\therefore \frac{3000}{x^2} = \frac{1}{20}$$

$$x^2 = 60000$$

$$x = 245$$

$$u(1) = \$3009.05$$

$$u(245) = \underline{\$33.49}$$

$$u(300) = \$34$$

Thus 245 units of production will minimize unit cost.

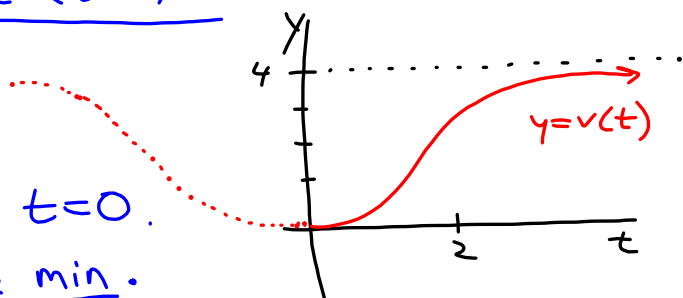
Q5b) $v(t) = \frac{4t^2}{1+t^2}, t \geq 0$

$$v'(t) = \frac{8t(1+t^2) - 4t^2(2t)}{(1+t^2)^2}$$

$$= \frac{8t}{(1+t^2)^2}$$

So $v'(t) = 0$ when $t = 0$.

$\therefore v(0) = 0$ is the min.



$$\lim_{t \rightarrow \infty} v(t) = \lim_{t \rightarrow \infty} \frac{4t^2}{1+t^2}$$

$$= \lim_{t \rightarrow \infty} \frac{4}{\frac{1}{t^2} + 1}$$

$$= \frac{4}{0+1}$$

$$= 4$$

So, NO max but

as $t \rightarrow \infty$

$$v(t) \rightarrow 4.$$
