

1.5

Q10c

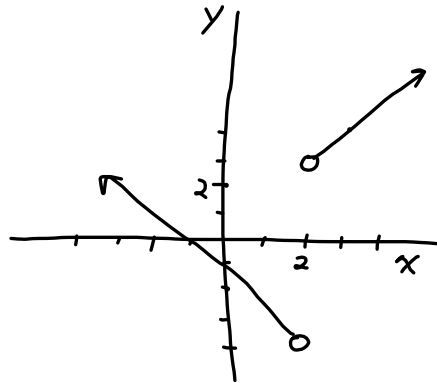
$$y = \frac{x^2 - x - 2}{|x - 2|} = \frac{(x-2)(x+1)}{|x-2|}$$

So, when $x < 2$, $y = -(x+1) = -x-1$

$x > 2$, $y = x+1$

$$\therefore \lim_{x \rightarrow 2^-} y = -2-1 = -3$$

$$\lim_{x \rightarrow 2^+} y = 2+1 = 3$$



So $\lim_{x \rightarrow 2} y$ does NOT exist

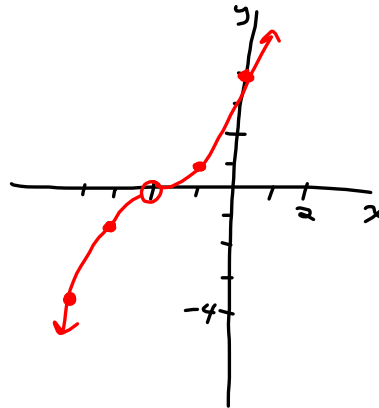
10d

$$y = \frac{(x+2)^3}{|x+2|} = \begin{cases} -(x+2)^2, & x < -2 \\ (x+2)^2, & x > -2 \end{cases}$$

So, $\lim_{x \rightarrow -2^-} y = 0$

$$\lim_{x \rightarrow -2^+} y = 0$$

Thus $\lim_{x \rightarrow -2} y = 0$



$$\textcircled{Q17} \quad y = \frac{x^2 + |x-1| - 1}{|x-1|}$$

$$\text{IF } x < 1$$

$$\begin{aligned} \therefore y &= \frac{x^2 - (x-1) - 1}{-(x-1)} \\ &= \frac{x^2 - x}{-(x-1)} \\ &= \frac{x(x-1)}{-(x-1)} \\ &= -x \end{aligned}$$

$$\text{IF } x > 1$$

$$\begin{aligned} \therefore y &= \frac{x^2 + x - 1 - 1}{x-1} \\ &= \frac{x^2 + x - 2}{x-1} \\ &= \frac{(x+2)(x-1)}{x-1} \\ &= x+2 \end{aligned}$$

$$\text{Well, } \lim_{x \rightarrow 1^-} y = -1 \text{ and } \lim_{x \rightarrow 1^+} y = 1+2 = 3$$

$$\therefore \lim_{x \rightarrow 1} y \text{ does NOT exist}$$

$\textcircled{Q16}$

$$\begin{aligned} &\lim_{x \rightarrow 0} \frac{\sqrt{x+1} - \sqrt{2x+1}}{\sqrt{3x+4} - \sqrt{2x+4}} \cdot \frac{\sqrt{x+1} + \sqrt{2x+1}}{\sqrt{\quad} + \sqrt{\quad}} \cdot \frac{\sqrt{3x+4} + \sqrt{2x+4}}{\sqrt{\quad} + \sqrt{\quad}} \\ &= \lim_{x \rightarrow 0} \frac{(x+1-2x-1)(\sqrt{3x+4} + \sqrt{2x+4})}{(3x+4-2x-4)(\sqrt{x+1} + \sqrt{2x+1})} \\ &= \lim_{x \rightarrow 0} \frac{-x}{x} \cdot \left(\frac{\sqrt{4} + \sqrt{4}}{\sqrt{1} + \sqrt{1}} \right) \\ &= -1 \cdot \left(\frac{\sqrt{4} + \sqrt{4}}{\sqrt{1} + \sqrt{1}} \right) \\ &= -2 \end{aligned}$$

$$(8d) \quad \lim_{x \rightarrow 1} \frac{x^{\frac{1}{6}} - 1}{x^{\frac{1}{3}} - 1}$$

$$= \lim_{y \rightarrow 1} \frac{y - 1}{y^2 - 1}$$

let $y = x^{\frac{1}{6}}$
 $y^6 = x$
 $(y^4)^{\frac{1}{3}} = x^{\frac{1}{3}}$
 $y^2 = x^{\frac{1}{3}}$

As $x \rightarrow 1$
 $y \rightarrow 1$

$$(8c) \quad \lim_{x \rightarrow 1} \frac{x^{\frac{1}{6}} - 1}{x - 1}$$

$$= \lim_{y \rightarrow 1} \frac{y - 1}{y^6 - 1}$$

$$= \lim_{y \rightarrow 1} \frac{y - 1}{(y^3 - 1)(y^3 + 1)}$$

OR

$$\lim_{y \rightarrow 1} \frac{y - 1}{(y^2 - 1)(y^4 + y^2 + 1)}$$

$$= \lim_{y \rightarrow 1} \frac{\cancel{y - 1}}{\cancel{(y - 1)}(y^2 + y + 1)(y^3 + 1)}$$

$$\text{OR} \quad \lim_{y \rightarrow 1} \frac{\cancel{y - 1}}{\cancel{(y - 1)}(y + 1)(y^4 + y^2 + 1)}$$

$$= \frac{1}{(1+1+1)(1+1)}$$

OR

$$= \frac{1}{(1+1)(1+1+1)}$$

$$= \frac{1}{6}$$

$$= \frac{1}{6}$$