1. Equations of Tangent & Secant Lines

1.1 Essential Questions

Essential Questions 1.1

- 1. How do we find the equation of the tangent line of a given function at the point P(a, b)?
- 2. How do we find the equation of the tangent line of a given function at x = a?

1.2 Finding the Equation of the Tangent Line

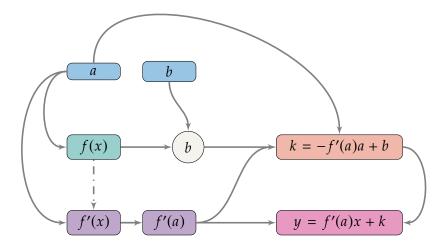


Figure 1.1: Finding the Equation of a Tangent Line Workflow

For a given function, f(x), our goal is to find the equation of the tangent line at the point P(a, b), which can be expressed in slope-intercept form as:

$$y = f'(a)x + k$$

Where f'(a) is the value of the derivative, slope, at x = a and k is the y-intercept. We therefore need to:

- 1. Find the derivative of the function f(x): f'(x)
- 2. Find the value of the derivative at x = a: f'(a)
- 3. Find the value of the *y*-intercept: k = -f'(a) + b:
- 4. If the ordinate b is not explicitly given, then find f(a) = b

Example 1.1 - id:20151011-154209.

Find the equation of the line tangent to the curve of the function $f(x) = 2x^2 + 3x + 7$ at the point P(2, 21).



Solution:

Find the derivative of f(x)

$$f'(x) = 4x + 3$$
 goto ??

Evaluate the derivative at x = 2

$$f'(2) = 4[2] + 3$$
 SPE(??)
 $f'(2) = 8 + 3$ OOM(??)
 $f'(2) = 11$ OOA(??)

Find the y-intercept, k, of the equation of the tangent line.

$$y = f'(x)x + k$$
[21] = [11][2] + k SPE(??)
21 = 22 + k OOM(??)

 $\neg 22 + [[21]] = \neg 22 + [[22]] + k$ SPE+AI

 $\neg 22 + 21 = (\neg 22 + 22) + k$ APA(??)

 $\neg 1 = 0 + k$ OOA(??)

 $\neg 1 = k$ AId(??)

 $-1 = k$ ONeg(??)

 $k = -1$ SyPE(??)

The equation of the tangent line is

$$y = f'(2)x + k$$

 $y = 11x - 1$ SPE(??)