$$\zeta = \rho e^{i\phi}$$

$$z = re^{i\theta}$$

$$\frac{z}{\zeta} = \frac{r}{\rho} e^{i(\theta-\phi)}$$