$$z\zeta = (x\xi - y\psi) + i(x\psi + y\xi)$$

$$= r\rho e^{i(\theta + \phi)}$$

$$\zeta = \xi + i\psi = \rho e^{i\phi}$$

$$z = x + iy = re^{i\theta}$$