$$\zeta = \rho e^{i\phi}$$

$$z = re^{i\theta}$$

$$\zeta = \frac{r}{\zeta} e^{i(\theta - \phi)}$$