

Name:**Tutorial time:**

1. Evaluate the following limits:

(a) $\lim_{x \rightarrow 2} \frac{2 - \sqrt{x+2}}{x-2}$

(b) $\lim_{\theta \rightarrow 0} \frac{\tan \theta}{\sin \theta + 2\theta}$

(c) $\lim_{x \rightarrow 0} x^2 \cos\left(\frac{1}{x^2}\right)$ (Hint: squeeze theorem)

(d) $\lim_{x \rightarrow 2^+} \frac{x^2 - 9}{x^2 - 4}$.

2. Let $f(x) = \frac{x^2 - 4}{x^2 - 4x + 3}$.

(a) What is the horizontal asymptote for the graph $y = f(x)$?

(b) What are the vertical asymptotes for the graph $y = f(x)$?

(c) What are the left and right-hand limits of $f(x)$ at each vertical asymptote?

3. Find and classify the discontinuities of $f(x) = \begin{cases} \frac{x^2+2x+1}{x+1}, & \text{if } x \leq 0 \\ \frac{1}{x-2}, & \text{if } x > 0 \end{cases}$

4. Using the **definition** of the derivative, find the equation of the tangent line to $y = x^2 + 1$ at the point $(1, 2)$.