

The problems on this worksheet are for in-class practice during tutorial. You are free to collaborate and to ask for help. They don't count for course credit, but it's a good idea to make sure you know how to do everything before you leave tutorial – similar problems may show up on a test or assignment.

Evaluate the following integrals:

1.  $\int \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$

2.  $\int \frac{\frac{1}{x} + 1}{x^2} dx$

3. The substitution for the last integral should have been clear. Note that the numerator can be written as  $\frac{x+1}{x}$ , so the whole integral can be re-written as  $\int \frac{x+1}{x^3} dx$ . Do you still want to do the integral by substitution, or is there a “better way”? Do your answers agree?

4.  $\int \tan^2(x) \sec^2(x) dx$

5.  $\int \tan^2(x) dx$

6.  $\int_0^1 2x(1-x^2)^4 dx$

7.  $\int x^3 e^x dx$

8.  $\int e^{2x} \sin(3x) dx$

9.  $\int x \sec^2(x) dx$

10.  $\int x\sqrt{x-2} dx$ . (Try this once using substitution, and again using integration by parts.)

11.  $\int e^{\ln x} dx$ . (With a bit of work you can do this by substituting  $u = \ln x$  and noting that  $x = e^u$ . Why is this a bad idea?)

12.  $\int \sin^5(x) \cos^6(x) dx$

13.  $\int \sin(x) \sin(2x) dx$

14.  $\int \sec^3(x) dx$ .

15.  $\int \sec^5(x) dx$

16.  $\int \sqrt{9-x^2} dx$

17.  $\int \frac{8}{\sqrt{x^2+2}} dx$

18.  $\int \frac{5x^2}{\sqrt{x^2-10}} dx$ . (This can be done with a secant substitution, but you might want to try hyperbolic functions instead.)