

The problems on this worksheet are for in-class practice during tutorial. You are free to collaborate and to ask for help. They don't count for course credit, but it's a good idea to make sure you know how to do everything before you leave tutorial – similar problems may show up on a test or assignment.

1. Evaluate the improper integral, or explain why it does not exist:

(a) $\int_0^{\infty} e^{4-3x} dx$

(b) $\int_{-\infty}^{\infty} \frac{1}{4+x^2} dx$

(c) $\int_{-\infty}^{\infty} \frac{x}{1+x^2} dx$

(d) $\int_1^{\infty} \frac{\ln x}{x^2} dx$

2. Find the area between the given curves:

(a) $y = x^2 - 3x + 2$, and $y = -3x + 3$

(b) $y = \sqrt{x}$, $y = -2x + 3$, and $y = -\frac{1}{2}x$.

3. Find the volume of the solid of revolution:

- (a) Generated by revolving the region bounded by $y = x^2 - 2x + 2$ and $y = 2x - 1$ about the x -axis.
- (b) Generated by revolving the region bounded by $y = x^2 - 2x + 2$ and $y = 2x - 1$ about the line $y = 1$.
- (c) Generated by revolving the triangle with vertices $(1, 1)$, $(1, 2)$, and $(2, 1)$ about the y -axis.
- (d) Generated by revolving the triangle with vertices $(1, 1)$, $(1, 2)$, and $(2, 1)$ about the x -axis.

4. Find the length of the curve $y = 2x^{3/2} - \frac{1}{\sqrt{6}}\sqrt{x}$, for $0 \leq x \leq 9$.

5. Find the area of the surface generated by revolving the the curve $y = x^2$, for $0 \leq x \leq 1$, about the y -axis.

6. Find the area enclosed by the following regions:

- (a) The region above the x -axis and below the spiral $r = \theta$, for $0 \leq \theta \leq \pi$.
- (b) The region given by the part of the first quadrant inside the curve $r = 1 + \sin \theta$.
- (c) One loop of the curve $r = \sin 4\theta$.
- (d) The inner loop of the curve $r = 1 + 2 \sin \theta$.