

The problems on this worksheet are for in-class practice during tutorial. You are free to collaborate and to ask for help. They don't count for course credit, but it's a good idea to make sure you know how to do everything before you leave tutorial – similar problems may show up on a test or assignment.

This week I've tried to make my best guess at what your test on Friday might look like.

1. Evaluate the following “immediate integrals”:

(a) $\int (2x + 3)^4 dx =$

(b) $\int \frac{x^2 + 2x}{x^3 + 3x^2 + 5} dx =$

(c) $\int \tan^5(x) \sec^2(x) dx =$

(d) $\int \frac{\ln(\sqrt{x+1})}{\sqrt{x+1}} dx =$

(e) $\int \frac{1}{\sqrt{4-x^2}} dx =$

(f) $\int \frac{x^3 - 4x^2}{\sqrt{x}} dx =$

(g) $\int \frac{e^x + 1}{e^x} dx =$

(h) $\int \frac{\ln(x^3)}{x} dx =$
(Hint: log laws)

(i) $\int x(1 - x^2)^5 dx =$

(j) $\int 3x^2 \cos(x^3) e^{\sin(x^3)} dx =$

2. Evaluate the following integrals:

(a) $\int x \sec^2(x) dx$

(b) $\int e^{\sqrt{x}} dx$

(c) $\int \cos(x) \cos(2x) dx$

(d) $\int \tan^5(x) \sec^4(x) dx$

$$(e) \int \frac{8}{\sqrt{x^2 + 2}} dx$$

$$(f) \int \frac{\sqrt{5 - x^2}}{x^2} dx$$

$$(g) \int \frac{16x^2 - 2x}{(x + 3)(2x - 1)(x - 1)} dx$$

$$(h) \int \frac{2x + 1}{x^3 + x} dx$$

These won't be on your test, but I thought I should give you a couple of practice problems involving improper integrals.

3. Evaluate the following improper integrals, or explain why they do not exist:

(a) $\int_0^4 \frac{1}{\sqrt{x}} dx$

(b) $\int_1^\infty \frac{\ln(x)}{x^2} dx$