

The problems on this worksheet are for in-class practice during tutorial. You are free to collaborate and to ask for help. They don't count for course credit, but it's a good idea to make sure you know how to do everything before you leave tutorial – similar problems may show up on a test or assignment.

1. Eliminate the parameter to obtain an equation for the curve involving only  $x$  and  $y$ :

(a)  $x = \sec t, y = \tan t$

(b)  $x = 4 \sin t + 1, y = 3 \cos t - 2$  (Hint: first solve for  $\cos t$  and  $\sin t$ .)

(c)  $x = \frac{1}{t+1}, y = \frac{3t+5}{t+1}$ . (Hint: try doing long division on the expression for  $y$ .)

(d)  $x = \cosh t, y = \sinh t$

2. Find the length of the parametric curve:

(a)  $x = -3 \sin(2t), y = 3 \cos(2t), t \in [0, \pi]$ .

(b)  $x = e^{t/10} \cos t, y = e^{t/10} \sin t, t \in [0, 2\pi]$ .

3. Find the area enclosed by the astroid  $x = \cos^3 t, y = \sin^3 t, t \in [0, 2\pi]$ . (There is some work involved here to evaluate the integral.)

4. Find the area enclosed by the loop of the “teardrop” curve  $x = t(t^2 - 1), y = t^2 - 1$ . (See Figure 5.34 in the text.)

5. Verify that  $x = Ce^{-t} + De^{2t}$  is a solution to  $x'' - x' - 2x = 0$ .

6. Find the solution from Problem 5 that satisfies  $x(0) = 3$  and  $x'(0) = -2$ .

7. Solve  $y' = y^3$  when  $y(0) = 1$ . (Hint:  $\frac{1}{y'} = \frac{dx}{dy}$ .)

8. Solve  $\frac{dx}{dt} = x \sin(t)$  for  $x(0) = 1$ .