Name:

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- 1. Let $T \in \mathcal{L}(V, W)$ be a linear map. Prove that if the vectors v_1, v_2, \ldots, v_m span V, then the vectors Tv_1, Tv_2, \ldots, Tv_m span range T.
- 2. Let $S, T \in \mathcal{V}$ be linear operators. Prove that if ST = TS, then range S is invariant under T.
- 3. (Bonus 2 points) (Correctly) write down the definition of any term introduced in this course.

Total: 10 points