Neural Codes for Image Retrieval

David Stutz

July 22, 2015

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1. Introduction

Image retrieval:

Problem. Given a large database of images and a query image, find images showing the same object or scene.

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Today, content-based image retrieval:

Techniques based on the Bag of Visual Words [SZ03] model.

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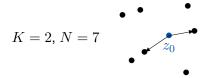
Sparse-Coded Features
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- 3 Convolutional Neural Networks Multi-layer Perceptrons Convolutional Neural Networks Architectures Training
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2. Image Retrieval

Formalization of content-based image retrieval:

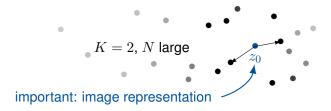
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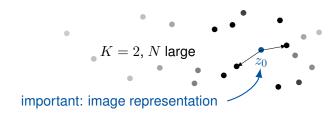
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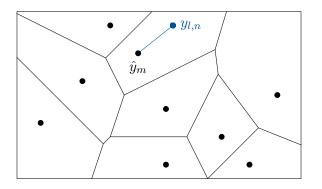
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Examples for image representations from the "Computer Vision" lecture:

- Histograms;
- Bag of Visual Words [SZ03].

Intuition: assign local descriptors $y_{l,n}$ of image x_n to visual words $\hat{y}_1,\ldots,\hat{y}_M$ previously obtained using clustering.



- 1. Extract local descriptors Y_n for each image x_n .
- 2. Cluster all local descriptors $Y = \bigcup_{n=1}^{N} Y_n$ to obtain visual words

$$\hat{Y} = \{\hat{y}_1, \dots, \hat{y}_M\}.$$

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3. Assign each $y_{l,n} \in Y_n$ to nearest visual word (embedding step):

$$f(y_{l,n}) = \left(\delta(\mathsf{NN}_{\hat{Y}}(y_{l,n}) = \hat{y}_1), \ldots\right).$$

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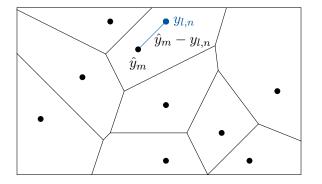
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$$f(y_{l,n}) = \left(\delta(\mathsf{NN}_{\hat{Y}}(y_{l,n}) = \hat{y}_1), \ldots\right).$$

4. Count visual word occurrences (aggregation step):

$$F(Y_n) = \sum_{l=1}^{L} f(y_{l,n}).$$

Intuition: consider the residuals $y_{l,n} - \hat{y}_m$ instead of counting visual words.



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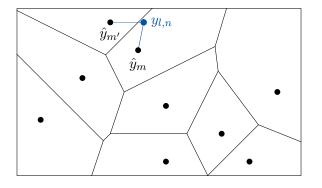
$$f(y_{l,n}) = (\delta(\mathsf{NN}_{\hat{Y}}(y_{l,n}) = \hat{y}_1)(y_{l,n} - \hat{y}_1), \ldots).$$

3. Aggregate residuals (aggregation step):

$$F(Y_n) = \sum_{l=1}^{L} f(y_{l,n}).$$

4. L_2 -normalize $F(Y_n)$.

Intuition: soft-assign local descriptors to visual words.



1. Extract and cluster local descriptors.

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- 2. Compute sparse codes (embedding step):

$$f(y_{l,n}) = \underset{r_l}{\operatorname{argmin}} \|y_{l,n} - \hat{Y}r_l\|_2^2 + \lambda \|r_l\|_1.$$
 contains \hat{y}_m as columns

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3. Pool sparse codes (aggregation step):

$$F(Y_n) = \left(\max_{1 \leq l \leq L} \{f_1(y_{l,n})\}, \ldots\right)$$
 first component of $f(y_{l,n})$

2.4. Compression, Nearest-Neighbor Search

Until now: image representation.

Additional aspects of image retrieval:

- compression of image representations;
- efficient indexing and nearest-neighbor search [JDS11];
- query expansion [CPS+07] and spatial verification [PCI+07].

2.4. Compression, Nearest-Neighbor Search

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Additional aspects of image retrieval:

- compression of image representations;
- efficient indexing and nearest-neighbor search [JDS11];
- query expansion [CPS+07] and spatial verification [PCI+07].

For example, compression can be accomplished using:

- Unsupervised methods, e.g. Principal Component Analysis (PCA);
- or discriminate methods, e.g. Joint Subspace and Classifier Learning [GRPV12] or Large Margin Dimensionality Reduction [SPVZ13].



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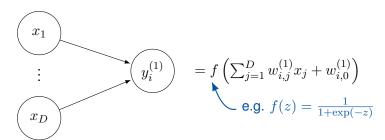
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3.1. Multi-layer Perceptrons

The prototypical neural network is the L-layer perceptron.

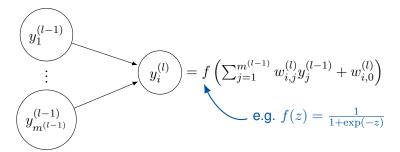
Given input $x \in \mathbb{R}^D$, layer l = 1 computes for $1 \le i \le m^{(l)}$:



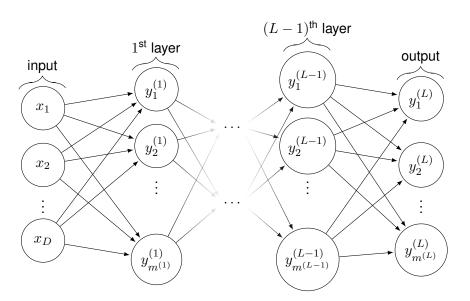
3.1. Multi-layer Perceptrons

The prototypical neural network is the L-layer perceptron.

Given input $y^{(0)} := x \in \mathbb{R}^{m^{(0)}}$, layer l computes for $1 \le i \le m^{(l)}$:



3.1. Multi-layer Perceptrons



3.2. Convolutional Neural Networks

Motivation:

- Multi-layer perceptrons do not naturally accept images as input;
- however, spatial information is important.

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Motivation:

- Multi-layer perceptrons do not naturally accept images as input;
- however, spatial information is important.

Solution: convolutional neural networks.

Intuition: apply learned filters on the input image to compute a set of feature maps.

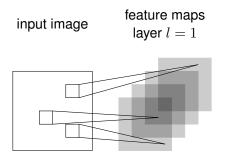
Repeat: normalize and pool feature maps before applying another set of learned filters.

Apply a multi-layer perceptron on the obtained (small) feature maps.

3.2. Convolutional Layer

General architecture:

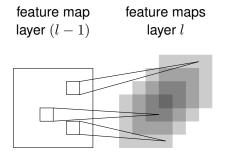
convolutional layer - contrast normalization layer - pooling layer



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Given $m_1^{(l-1)}$ feature maps $Y_j^{(l-1)}$, layer l computes

$$Y_i^{(l)} = f\left(B_i^{(l)} + \sum_{j=1}^{m_1^{(l-1)}} W_{i,j}^{(l)} * Y_j^{(l-1)}\right), \quad 1 \le i \le m_1^{(l)}$$

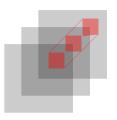
where $B_i^{(1)}$ are bias matrices and $W_{i,j}^{(1)}$ are filters.

3.2. Local Contrast Normalization Layer

General architecture:

convolutional layer - contrast normalization layer - pooling layer

 $\begin{array}{l} \text{feature maps} \\ \text{layer} \; (l-1) \end{array}$



ensure that values are comparable

3.2. Local Contrast Normalization Layer

General architecture:

convolutional layer - contrast normalization layer - pooling layer

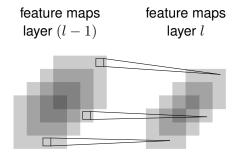
Given $m_1^{(l-1)}$ feature maps $Y_j^{(l-1)}, \mbox{ brightness normalization [KSH12] computes}$

$$(Y_i^{(l)})_{r,s} = \frac{(Y_i^{(l-1)})_{r,s}}{1 + \sum_{j=1}^{m_1^{(l-1)}} (Y_j^{(l-1)})_{r,s}^2}, \quad 1 \le i \le m_1^{(l)} = m_1^{(l-1)}.$$

3.2. Pooling Layer

General architecture:

convolutional layer – contrast normalization layer – **pooling layer**



3.2. Pooling Layer

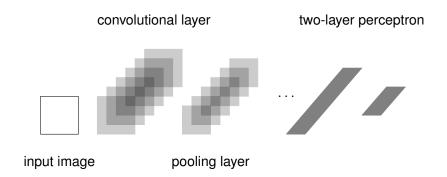
General architecture:

convolutional layer - contrast normalization layer - pooling layer

Given feature maps $Y_j^{(l-1)}$ of size $m_2^{(l-1)} \times m_3^{(l-1)}$, it computes feature maps $Y_i^{(l)}$ of reduced size by

- computing the average value within (non-overlapping) windows (average pooling);
- or keeping the maximum value of (non-overlapping) windows (max pooling).

3.3. Schematic Architecture



3.3. ImageNet Architecture "AlexNet"

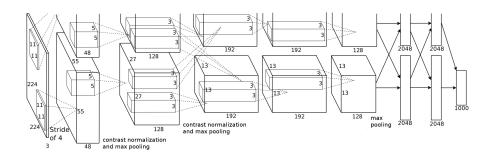


Figure: Architecture used by Krizhevsky et al. [KSH12], L=13.

3.4. Training

For classification, use softmax activation function in layer L:

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Given a training set $\{(x_n, t_n)\}$ with $t_n = i$ iff x_n belongs to class i, minimize multinomial loss

all weights of the network
$$E(W) = -\frac{1}{m^{(L)}} \sum_{n=1}^{N} \log \left(y_{t_n}^{(L)} \right)$$

using gradient descent.

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4. Neural Codes - Motivation



Figure: Back-projection of a single feature activation in the fourth convolutional layer [ZF14].

4. Neural Codes for Image Retrieval

Motivation: Intermediate feature activations are rich representations of image content.

For application in image retrieval, Babenko et al. [BSCL14] use

- layer l = 10: last convolutional layer, including subsequent max pooling;
- ▶ layer l = 11 and l = 12: first and second layer of the three-layer perceptron.

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- ▶ layer l = 11 and l = 12: first and second layer of the three-layer perceptron.

Two models:

- ▶ pre-trained on ImageNet¹ (~ 3.2 million images, > 1000 classes);
- ▶ and re-trained on the Landmark dataset (213, 678 images of 672 popular landmarks).

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¹Available at http://www.image-net.org/.

4. Neural Codes for Image Retrieval

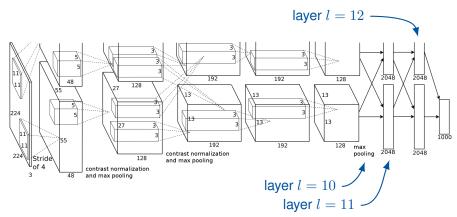


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4. Compressed Neural Codes

Compression using PCA and Large Margin Dimensionality Reduction.

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Compression using PCA and Large Margin Dimensionality Reduction.

Large Margin Dimensionality Reduction:

- 1. Match images such that $t_{n,n'} = 1$ iff images x_n and $x_{n'}$ are related.
- 2. Compute linear dimensionality reduction $P \in \mathbb{R}^{C' \times C}$ by minimizing

$$E(P) = \sum_{n,n'}^{N} \max\{0, 1 - t_{n,n'} \left(b - (x_n - x_{n'})^T P^T P(x_n - x_{n'})\right)\}$$
 large margin condition

using gradient descent.

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5. Datasets and Metric

Datasets:

- ➤ Oxford 5k [PCI⁺07]: 5,062 images of eleven different landmarks in Oxford; 5 queries with ground truth per landmark.
- ▶ INRIA Holidays [JDS08]: 1,491 holiday images with 500 distinct queries including ground truth.







Figure: Example images from the Oxford 5k dataset showing the All Souls College of the University of Oxford.

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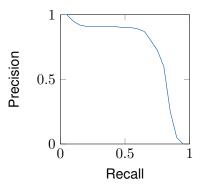


Figure: Example images from the INRIA Holidays dataset.

5. Precision-Recall Framework

Precision-Recall curves:

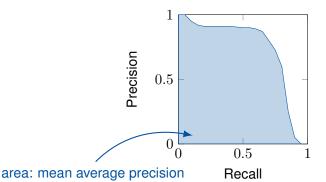
- Recall: ratio of true positives to all related images;
- Precision: ratio of true positives to number of retrieved images.



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5. Experiments

	Oxford 5k	Holidays	
Fisher Vectors [GRPV12]	_	0.774	
Vector of Locally Aggregated Descriptors [AZ13]	0.555	0.646	
Sparse-Coded Features [GKS13]	_	0.767	
Triangulation Embedding [JZ14]	0.676	0.771	
Pre-Trained on ImageNet			
l = 10	0.389	0.69	
l = 11	0.435	0.749	
l=12	0.430	0.736	
Re-Trained			
l = 10	0.387	0.674	
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Table: Mean average precision for the Oxford 5k dataset and the Holidays dataset.

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Fisher Vectors* [GRPV12]	_	0.764
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Triangulation Embedding [JZ14]	0.433	0.617
Pre-Trained on ImageNet		
l=11 (PCA)	0.433	0.747
l=11 (Large-Margin)	0.439	_
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5. Experiments – Examples



Figure: Qualitative examples provided by Babenko et al. [BSCL14]: left-most image is the query; correctly retrieved images are marked.

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5. Experiments – Conclusion

Notes on Experiments:

- no experiments using Large Margin Dimensionality Reduction on the re-trained model;
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Conclusion:

- fully learned features are interesting alternative to hand-crafted features;
- and convolutional neural networks may be explicitly trained for the image retrieval task.

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Summary and takeaways:

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 - Sparse-Coded Features [GKS13].

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 - Excellent performance on ImageNet;
 - but difficult to train or implement.

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 - Vector of Locally Aggregated Gradients [AZ13];
 - Sparse-Coded Features [GKS13].
- Convolutional neural networks are powerful, but complex models for classification.
 - Excellent performance on ImageNet;
 - but difficult to train or implement.
- Intermediate feature activations of convolutional neural networks offer rich representations.

A.1. Bag of Visual Words - Discussion

For large Y, k-means clustering may be infeasible:

- hierarchical k-means [NS06];
- or approximate k-means [PCI+07].

Burstiness, that is single large components can strongly affect performance [AZ13]:

- term frequency, inverse document frequency weighting;
- or component-wise square root and L_2 normalization.

A.2. Vector of Locally Aggregated Descriptors

Remember, embedding step:

$$f(y_{l,n}) = (\delta(NN_{\hat{Y}}(y_{l,n}) = \hat{y}_1)(y_{l,n} - \hat{y}_1),...),$$

and aggregation step:

$$F(Y_n) = \sum_{l=1}^{L} f(y_{l,n}).$$

Further normalization techniques:

• power-law normalization (usually, $\alpha = 0.5$):

$$F_m(Y_n) = \operatorname{sign}(F_m(Y_n)) |F_m(Y_n)|^{\alpha};$$

ightharpoonup intra-normalization: L_2 -normalize sum of residuals for each visual word independently.

B. Training in Practice

Training with gradient descent, in iteration [t+1] compute

$$W[t+1] = W[t] - \gamma \nabla E(W[t])$$

with learning rate γ .

In practice:

- ▶ Compute $\nabla E(W[t])$ in $\mathcal{O}(|W|)$ using Error Backpropagation.
- Add a regularizer of the form

$$\hat{E}(W) = E(W) + \lambda ||W||_1.$$

▶ Use dropout [HSK⁺12] and stochastic gradient descent.

C. Neural Codes – Motivation

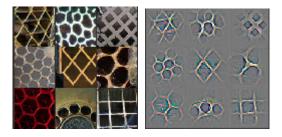


Figure: Back-projection of a single feature activation in layer l=3 [ZF14]².

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²Note that the architecture used by Zeiler et al. [ZF14] does not exactly match the architecture presented previously.

C. Neural Codes – Motivation



Figure: Computed image to maximize posterior for classes "goose" (left) and "husky" (right) [SVZ13].

D. Try it out ...

Unfortunately, Babenko et al. do not provide source code to reproduce their experiments.

However, you can try other state-of-the-art approaches:

- Oxford 5k dataset (including evaluation script): http://www.robots.ox.ac.uk/~vgg/data/oxbuildings/;
- SIFT, Vector of Locally Aggregated Descriptors and Fisher Vectors [PD07] are implemented in the VLFeat library: http://www.vlfeat.org/overview/encodings.html;

... or try to use convolutional neural networks, for example using

► Caffe: http://caffe.berkeleyvision.org/.

Relja Arandjelović and Andrew Zisserman.
All about VLAD.

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