Programming Language Concepts Syntax and Parsing

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Introduction

- Syntax: the form and structure of a program.
- Semantics: meaning of a program
- Language definitions are used by:
 - Programmers
 - Implementors of the language processors
 - Language designers

Definitions

- A sentence is a string of characters over some alphabet
- A language is a set of sentences
- A lexeme is the lowest level syntactic unit of the language (i.e. ++, int, total)
- A token is a category of lexemes (i.e. *identifier*)

Definitions

- syntax recognition: read input strings of the language and verify the input belonging to the language
- syntax generation: generate sentences of the language (i.e. from a given data structure)
- Compilers and interpreters recognize syntax and convert it into machine understandable form.

Backus-Naur Form and CFGs

- CFG's introduced by Noam Chomsky (mid 1950s)
- Programming languages are usually in context free language class
- BNF introduced by John Bakus and modified by Peter Naur for describing Algol language
- BNF is equivalent to CFGs. It is a meta-language that decribes other languages
- Extended BNF improves readability of BNF

A Grammar Rule

```
\langle while\_stmt \rangle \rightarrow while (\langle logic\_expr \rangle) \langle stmt \rangle
```

- LHS is a non-terminal denoting an intermediate phrase
- LHS can be defined (rewritten) as the RHS sequence which can contain terminals (lexems and tokens) of the language and other non-terminals
- Non-terminals are denoted as strings enclosed in angle brackets.
- ::= may be used in BNF notation instead of the arrow
- is used to combine multiple rules with same LHS in a single rule

```
\begin{array}{lll} \langle lgc\_cons \rangle \ ::= \ true & \equiv & \langle lgc\_cons \rangle \ ::= \ true \ | \ false \\ \langle lgc\_cons \rangle \ ::= \ false \end{array}
```

Context Free Grammar

- A grammar G is defined as $G = (N, \Sigma, R, S)$:
 - N. finite set of non terminals
 - \blacksquare Σ , finite set of terminals
 - R is a set of grammar rules. A relation from N to $(N \cup \Sigma)^*$.
 - $S \in N$ the start symbol
- Application of a rule maps one sentential form into the other by replacing a non-terminal element in sentential form with its right handside seugence in the rule, $u \mapsto v$.
- Language of a grammar $L(G) = \{ w \mid w \in \Sigma^*, S \stackrel{*}{\mapsto} w \}$

 Recursive or list like structures can be represented using recursion

```
\begin{array}{l} \langle expr\_list \rangle \ \rightarrow \ \langle expr \rangle \ \ \text{,} \ \ \langle expr\_list \rangle \\ \langle btree \rangle \ \rightarrow \ \langle head \rangle \ \ ( \ \langle btree \rangle \ \ \text{,} \ \ \langle btree \rangle \ \ ) \end{array}
```

- A derivation starts with a starting non-terminal and rules are applied repeteadly to end with a sentence containing only terminal symbols.
- leftmost derivation: always leftmost non-terminal is chosen for replacement
- rightmost derivation: always rightmost non-terminal is chosen for replacement
- Same sentence can be derived using leftmost, rightmost, or other derivaionts.

Sample Grammar

```
\langle \mathsf{stmt} \rangle \to \langle \mathsf{id} \rangle = \langle \mathsf{expr} \rangle
\langle expr \rangle \rightarrow \langle expr \rangle \langle op \rangle \langle expr \rangle \mid \langle id \rangle
\langle \mathsf{op} \rangle \to + \mid *
\langle id \rangle \rightarrow a \mid b \mid c
```

I eftmost derivation of a = a * b : $\langle \mathbf{stmt} \rangle \mapsto \langle \mathbf{id} \rangle = \langle \mathbf{expr} \rangle \mapsto \mathbf{a} = \langle \mathbf{expr} \rangle$ \mapsto a = $\langle id \rangle \langle op \rangle \langle expr \rangle \mapsto$ a = a $\langle op \rangle \langle expr \rangle$

$$\mapsto \quad \mathsf{a} = \mathsf{a} \ ^* \langle \mathbf{expr} \rangle \quad \mapsto \quad \mathsf{a} = \mathsf{a} \ ^* \langle \mathbf{id} \rangle \quad \mapsto \quad \mathsf{a} = \mathsf{a} \ ^* \mathsf{b}$$

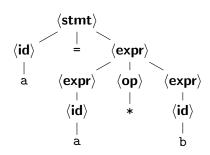
Rightmost derivation of a = a * b : $\langle \mathsf{stmt} \rangle \mapsto \langle \mathsf{id} \rangle = \langle \mathsf{expr} \rangle \mapsto \langle \mathsf{id} \rangle = \langle \mathsf{expr} \rangle \langle \mathsf{op} \rangle \langle \mathsf{expr} \rangle$ \mapsto $\langle id \rangle = \langle expr \rangle \langle op \rangle \langle id \rangle \mapsto \langle id \rangle = \langle expr \rangle \langle op \rangle b$ \mapsto $\langle id \rangle = \langle expr \rangle * b \mapsto \langle id \rangle = \langle id \rangle * b$ \mapsto $\langle id \rangle = a * b \mapsto a = a * b$

Parse Tree

- Steps of a derivation gives the structure of the sentence. This structure can be represented as a tree.
- All non-terminals used in derivation are intermediate nodes. Each grammar rule replaces the non-terminal node with is children. Root node is the start symbol.
- Terminal nodes are the leaf nodes.
- preorder traversal of leaf nodes gives the resulting sentence.
- leftmost and rightmos derivations can be retrieved by traversal of the tree.

Parse Tree Example

$$a = a * b$$

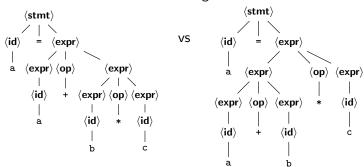


Parse Tree Generation

- A parse tree gives the structure of the program so semantics of the program is related to this structure.
- For example local scopes, evaluation order of expressions etc.
- During compilation, parse trees might be required for code generation, semantic analysis and optimization phases.
- After a parse tree generated, it can be traversed to do various tasks of compilation.
- The processing of parse tree takes too long, so creation of parse trees is usually avoided.
- Approaches like syntax directed translation combines parsing with code generation, semantic analysis etc...

Ambigous Grammars

■ Consider a = a + b * c in our grammar:



■ Both can be derived by the grammar!

- A grammar is called ambigous if same sentence can be derived by following different set of rules, thus resulting in a different parse tree
- If structure changes semantic meaning of the program, ambiguity is a serious problem.
- Even if not, which one is the result?
- i.e. Precedence of operators affects the value of the expression.
- Programming languages enforces precedence rules to resolv ambiguity.
- Solution:
 - 1 design grammar not to be ambigous, or
 - 2 during parsing, choose rules to generate the correct parse tree

Precedence and Grammar

- Operators with different precedence levels should be treated differently
- Higher precedence operations should be deep in the parse tree
 → their rules should be applied later.
- Lower precedence operations should be closer to root \rightarrow applied earlier in derivation.
- For each precedence level, define a non-terminal
- One rewritten on the other based on the precedence lower to higher

Rewritten Grammar

$$\begin{split} \langle \text{stmt} \rangle &\rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle \\ \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle \\ \langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{factor} \rangle \\ \langle \text{factor} \rangle &\rightarrow \langle \text{id} \rangle \mid (\langle \text{expr} \rangle) \\ \langle \text{id} \rangle &\rightarrow \text{a} \mid \text{b} \mid \text{c} \end{split}$$

- ⟨**term**⟩ and ⟨**expr**⟩ has different precedence.
- Once inside of (**term**), there is no way to derive +
- Only one parse possible

Associativity

Associativity of operators is another issue

$$a - b - c \equiv (a - b) - c \text{ or } a - (b - c)$$

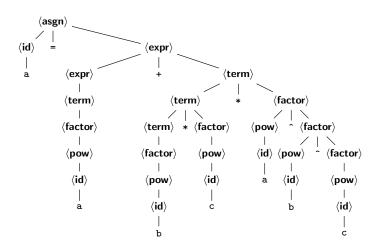
- Recursion of grammar defines how tree is constructed for operators in the same level.
- If left recursive, later operators in the sentence will be closer to root, if right recursive earlier operators will be closer to root
- left recursion implies left associativity, right recursion implies right associativity.
- Consider a + b + c in these grammars: $\begin{array}{l} \langle expr \rangle \, \rightarrow \, \langle id \rangle \, + \, \langle expr \rangle \, \mid \, \langle id \rangle \\ \langle id \rangle \, \rightarrow \, a \, \mid \, b \, \mid \, c \end{array}$ $\langle expr \rangle \rightarrow \langle expr \rangle + \langle id \rangle \mid \langle id \rangle$ $\langle id \rangle \rightarrow a \mid b \mid c$

Sample Grammar

```
\langle \mathsf{asgn} \rangle \to \langle \mathsf{id} \rangle = \langle \mathsf{asgn} \rangle \mid \langle \mathsf{id} \rangle = \langle \mathsf{expr} \rangle
 \langle expr \rangle \rightarrow \langle expr \rangle + \langle term \rangle \mid \langle term \rangle
\langle term \rangle \rightarrow \langle term \rangle * \langle factor \rangle \mid \langle factor \rangle
\langle factor \rangle \rightarrow \langle pow \rangle \hat{\ } \langle factor \rangle \mid \langle pow \rangle
\langle \mathsf{pow} \rangle \, 	o \, \langle \mathsf{id} \rangle \mid (\langle \mathsf{expr} \rangle)
\langle id \rangle \rightarrow a \mid b \mid c
```

- (asgn) is right recursive like right associative C assignments.
- (expr) and (term) are left recursive, * and + left associative
- (factor) is right recursive for power operation ^ to be right associative.
- \blacksquare precedence order is (...) \prec $^{\land}$ \prec * \prec + \prec =

$$a = a + b * c * a ^ b ^ c$$

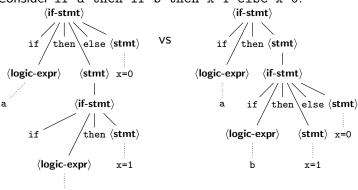


if-then-else ambiguity

■ Following grammar is ambigous:

```
\begin{split} \langle \mathsf{stmt} \rangle &\to \langle \mathsf{if\text{-}stmt} \rangle \\ \langle \mathsf{if\text{-}stmt} \rangle &\to \mathsf{if} \ \langle \mathsf{logic\text{-}expr} \rangle \ \mathsf{then} \ \langle \mathsf{stmt} \rangle \ | \\ & \mathsf{if} \ \langle \mathsf{logic\text{-}expr} \rangle \ \mathsf{then} \ \langle \mathsf{stmt} \rangle \ \mathsf{else} \ \langle \mathsf{stmt} \rangle \end{split}
```

 \blacksquare Consider if a then if b then x=1 else x=0:

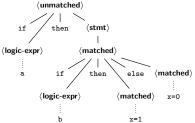


Solution

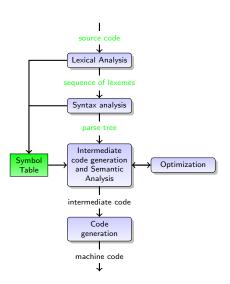
Distinguish categories of statements. if's matched with else and unmatched:

```
\begin{tabular}{lll} $\langle stmt \rangle & \to & \langle matched \rangle & | & \langle unmatched \rangle & | & \langle matched \rangle & | & \langle unmatched \rangle & | & \langle unmatched
```

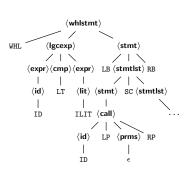
 \blacksquare if a then if b then x=1 else x=0:



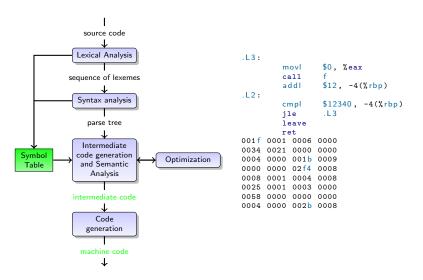
Compilation



```
while (counter < 12341) {
        f():
        counter += 12:
WHL LP ID LT ILIT RP LB
        ID LP RP SC
        ID PLEQ ILIT SC
RB
```



Compilation



Lexical Analysis

- input: sequence of characters, source code.
- output: sequence of lexemes
- Worst case complexity of parsing is $\mathcal{O}(n^3)$. Depending on algorithm type, recursion type and number of grammar rules, this might change. *n* is the length of the string.
- Regular language processing complexity is $\mathcal{O}(n)$. Grammars can be defined in terms of lexemes.
- # of chars vs # of lexemes?
- Lexical analysis convert character sequences into lexemes. Identifiers registered on symbol table

- input: sequence of lexemes (output of lexical analysis) or characters.
- output: parse tree, intermediate code, translated code, or sometimes only if document is valid or not.
- Two main classes of parser:
 - Top down parsing
 - Tottom up parsing

Top-down Parsing

■ Start from the starting non-terminal, apply grammar rules to reach the input sentence

- Simplest form gives leftmost derivation of a grammar processing input from left to right.
- Left recursion in grammar is a problem. Elimination of left recursion needed.
- Deterministic parsing: Look at input symbols to choose next rule to apply.
- recursive descent parsers, LL family parsers are top-down parsers

Recursive Descent Parser

```
typedef enum {ident, number, lparen, rparen, times,
        slash, plus, minus} Symbol;
int accept(Symbol s) { if (sym == s) { next(); return 1; }
        return 0:
void factor(void) {
   if (accept(ident));
    else if (accept(number));
    else if (accept(|paren)) { expression(); expect(rparen);}
    else { error("factor:usyntaxuerroruatu",currsym); next(); }
void term(void) {
   factor();
    while (accept(times) || accept(slash))
        factor();
void expression(void) {
   term():
    while (accept(plus) || accept(minus))
        term();
```

- Each non-terminal realized as a parsing function
- Parsing functions calls the right handside functions in sequence
- Rule choices are based on the current input symbol. accept checks a terminal and consumes if matches
- Cannot handle direct or indirect left recursion. A function has to call itself before anything else.
- Hand coded, not flexible.

LL Parsers

- First L is 'left to right input processing', second is 'leftmost derivation'
- Checks next *N* input symbols to decide on which rule to apply: LL(*N*) parsing.
- For example LL(1) checks the next input symbol only.
- LL(N) parsing table: A table for $V \times \Sigma^N \mapsto R$
- for expanding a nonterminal $NT \in V$, looking at this table and the next N input symbols, LL(N) parser chooses the grammar rule $r \in R$ to apply in the next step.

■ Grammar and lookup table for a LL(1) parser:

1
$$S \rightarrow E$$

$$2 \quad S \rightarrow -E$$

$$3\quad \textit{E} \rightarrow \textit{N} + \textit{E}$$

4
$$E \rightarrow (E)$$

$$5\quad {\it N}\rightarrow {\it a}$$

$$6 \quad N \to b$$

, ,				
	а	b	-	(
S	1	1	2	1
Ε	3	3		4
N	5	6		

- What if we add $E \rightarrow N$ to grammar?
- You need an LL(2) grammar. What if N is recursive? see LL(*) parser

Bottom-up Parsing

Start from input sentence and merge parts of sentential form matching RHS of a rule into LHS at each step. Try to reach the starting non-terminal. reach the input sentence

- Simplest form gives rightmost derivation of a grammar (in reverse) processing input from left to right.
- Shift-reduce parsers are bottom-up:
 - shift: take a symbol from input and push to stack.
 - reduce: match and pop a RHS from stack and reduce into LHS.

Shift-Reduce Parser in Prolog

```
% Grammar is E \rightarrow E - T/E + T/T T \rightarrow a/b
rule(e,[e,-,t]).
rule(e,[e,+,t]).
rule(e,[t]).
rule(t,[a]).
rule(t,[b]).
parse([],[S]): - S = e . % starting symbol alone in the stack
% reduce: find RHS of a rule on stack, reduce it to LHS
parse(Input, Stack) :- match(LHS, Stack, Remainder),
                        parse(Input,[LHS|Remainder]).
% shift: nonterminals are removed from input added on stack
parse([H|Input], Stack) :- member(X,[a,b,-,+]),
                            parse(Input,[H|Stack]).
% check if RSH of a rule is a prefix of Stack (reversed).
match (LHS, List, L) :- rule (LHS, RHS), reverse (RHS, NRHS),
                       prefix (NRHS, List, L).
```

- Shift reduce parser tries all non-deterministic shift combinations to get all parses.
- For deterministic parsing states based on input lookahead or precedence required
- Deterministic bottom up parsers: LALR, SLR(1).