# Programming Language Concepts Type Systems

Onur Tolga Şehitoğlu

Computer Engineering







#### Outline

- 1 Type Systems
- 2 Polymorphism
  - Inclusion Polymorphism

- Parametric Polymorphism
- 3 Overloading
- Coercion
- 5 Type Inference

Design choices for types:

■ monomorphic vs polymorphic type system.

#### Design choices for types:

- monomorphic vs polymorphic type system.
- overloading allowed?

#### Design choices for types:

- monomorphic vs polymorphic type system.
- overloading allowed?
- coercion(auto type conversion) applied, how?



#### Design choices for types:

- monomorphic vs polymorphic type system.
- overloading allowed?
- coercion(auto type conversion) applied, how?
- type relations and subtypes exist?

Monomorphic types: Each value has a single specific type. Functions operate on a single type. C and most languages are monomorphic.

- Monomorphic types: Each value has a single specific type. Functions operate on a single type. C and most languages are monomorphic.
- Polymorphism: A type system allowing different data types handled in a uniform interface:

- Monomorphic types: Each value has a single specific type. Functions operate on a single type. C and most languages are monomorphic.
- Polymorphism: A type system allowing different data types handled in a uniform interface:
  - **1** Ad-hoc polymorphism: Also called overloading. Functions that can be applied to different types and behave differently.

- Monomorphic types: Each value has a single specific type. Functions operate on a single type. C and most languages are monomorphic.
- Polymorphism: A type system allowing different data types handled in a uniform interface:
  - Ad-hoc polymorphism: Also called overloading. Functions that can be applied to different types and behave differently.
  - 2 Inclusion polymorphism: Polymorphism based on subtyping relation. Function applies to a type and all subtypes of the type (class and all subclasses).

- Monomorphic types: Each value has a single specific type. Functions operate on a single type. C and most languages are monomorphic.
- Polymorphism: A type system allowing different data types handled in a uniform interface:
  - **1** Ad-hoc polymorphism: Also called overloading. Functions that can be applied to different types and behave differently.
  - 2 Inclusion polymorphism: Polymorphism based on subtyping relation. Function applies to a type and all subtypes of the type (class and all subclasses).
  - 3 Parametric polymorphism: Functions that are general and can operate identically on different types



- C types:
  - $char \subseteq short \subseteq int \subseteq long$
- Need to define arithmetic operators on them separately?
- Consider all strings, alphanumeric strings, all strings from small letters, all strings from decimal digits. Ned to define special concatenation on those types?
- $\blacksquare f: T \to V$ ,  $U \subseteq T \Rightarrow f: U \to V$
- Most languages have arithmetic operators operating on different precisions of numerical values.

#### Inheritance

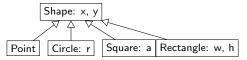
```
■ struct Point { int x, y; };
  struct Circle { int x, y, r; };
  struct Square { int x, y, a; };
  struct Rectangle { int x, y, w, h; };
```

#### Inheritance

```
■ struct Point { int x, y; };
  struct Circle { int x, y, r; };
  struct Square { int x, y, a; };
  struct Rectangle { int x, y, w, h; };
■ void move (Point p, int nx, int ny) {
             p.x=nx; p.y=ny;}
```

#### struct Point { int x, y; }; struct Circle { int x, y, r; }; struct Square { int x, y, a; }; struct Rectangle { int x, y, w, h; };

- void move (Point p, int nx, int ny) { p.x=nx: p.v=nv:
- Moving a circle or any other shape is too different?



Haskell extensible records (only works for Hugs and in 98 mode!!):

```
import Hugs. Trex: -- Only in -98 mode!!!
type Shape = Rec (x::Int, y::Int)
type Circle = Rec (x::Int, y::Int, r::Int)
type Square = Rec (x::Int, y::Int, w::Int)
type Rectangle = Rec (x::Int, y::Int, w::Int, h::Int)
move (x=\_,v=\_|rest) b c = (x=b,v=c|rest)
(a::Shape)=(x=12,y=24)
(b:: Circle) = (x=12, y=24, r=10)
(c::Square)=(x=12,y=24,w=4)
(d::Rectangle)=(x=12,y=24,w=10,h=5)
Main > move b 4 5
(r = 10, x = 4, y = 5)
Main > move c 4 5
(w = 4, x = 4, y = 5)
Main > move d 4 5
(h = 5, w = 10, x = 4, y = 5)
```

#### Haskell Classes

- Subtyping hierarchy based on classes
- An instance implements interface functions of the class
- Functions operating on classes (using interface functions) can be defined

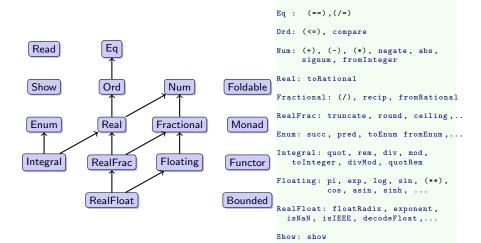
DataStr: insert, get, isempty

A Cuses>>

Stack Queue listinsert

■ Called interface in OO programming

#### Haskell Default Class Hieararchy





```
class DataStr a where
    insert :: (a v) -> v -> (a v)
    get :: (a v)-> Maybe (v,(a v))
    isempty :: (a v) -> Bool
instance DataStr Stack where
    insert \times v = push v \times
    get x = pop x
    isempty Empty = True
    isempty _ = False
instance DataStr Queue where
    insert \times v = enqueue v \times
    get \times = dequeue \times
    isempty EmptyQ = True
    isempty _ = False
insertlist :: DataStr a \Rightarrow (a v) \rightarrow [v] \rightarrow (a v)
insertlist \times \Pi = x
insertlist x (el:rest) = insertlist (insert x el) rest
data Stack a = Empty | St [a] deriving Show
data Queue a = EmptyQ | Qu [a] deriving Show
```

#### Parametric Polymorphism

Polymorphic types: A value can have multiple types.
 Functions operate on multiple types uniformly

### Parametric Polymorphism

- Polymorphic types: A value can have multiple types.
   Functions operate on multiple types uniformly
- identity x = x function. type:  $\alpha \to \alpha$  identity 4: 4, identity "ali": "ali", identity (5,"abc"): (5,"abc") int  $\to$  int, String  $\to$  String, int  $\times$  String  $\to$  int  $\times$  String

- Polymorphic types: A value can have multiple types.
   Functions operate on multiple types uniformly
- identity x = x function. type:  $\alpha \to \alpha$  identity 4: 4, identity "ali": "ali", identity (5,"abc"): (5,"abc") int  $\to$  int, String  $\to$  String, int  $\times$  String  $\to$  int  $\times$  String
- compose f g x = f (g x) function type:  $(\beta \to \gamma) \to (\alpha \to \beta) \to \alpha \to \gamma$  compose square double 3:36,  $(int \to int) \to (int \to int) \to int \to int$ . compose listsum reverse [1,2,3,4]:10  $([int] \to int) \to ([int] \to [int]) \to [int] \to int$



- filter f [] = []

  filter f (x:r) = if (f x) then x:(filter f r) else (filter r)  $(\alpha \to Bool) \to [\alpha] \to [\alpha]$ filter ((<) 3) [1,2,3,4,5,6] : [4,5,6]  $(int \to Bool) \to [int] \to [int]$ filter identity [True, False, True, False] :

  [True,True]  $(Bool \to Bool) \to [Bool] \to [Bool]$
- Operations are same, types are different.
- Types with type variables: polytypes
- Most functional languages are polymorphic
- Object oriented languages provide polymorphism through inheritance



## Overloading

- Overloading: Using same identifier for multiple places in same scope
- Example: Two different functions, two distinct types, same name.
- Polymorphic function: one function that can process multiple types.
- C++ allows overloading of functions and operators.

```
typedef struct Comp { double x, y; } Complex;
double mult(double a, double b) { return a*b; }
Complex mult(Complex s, Complex u) {
    Complex t:
    t.x = s.x*u.x - s.y*u.y;
    t.v = s.x*u.v + s.v*u.x;
   return t:
Complex a,b; double x,y; ...; a=mult(a,b); x=mult(y,2.1);
```

- Binding is more complicated. not only according to name but according to name and type
- Function type:



- Context dependent overloading: \_\_\_\_\_\_\_
   Overloading based on function name, parameter type and return type.
- Context independent overloading : Overloading based on function name and parameter type. No return type!

### Context dependent overloading

Which

type does the expression calling the function expects (context)?

```
int f(double a) { ....(1) }
int f(int a) { ....(2) }
double f(int a) { ....(3) }
double x,y;
int a,b;
```

```
\blacksquare a=f(x);
  a=f(a):
  x=f(a):
  x=2.4+f(a);
  a=f(f(x)):
  a=f(f(a)):
```

Problem gets more complicated. (even forget about coercion)



```
int f(double a) { ....(1) }
int f(int a) { ....(2) }
double f(int a) { ....(3) }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a): x=f(a): x=2.4+f(a): a=f(f(x)): a=f(f(a)):
- Problem gets more complicated. (even forget about coercion)



```
int f(double a) { ....(1) }
int f(int a) { ....(2) }
double f(int a) { ....③ }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a); ② (a int, assign int) x=f(a): x=2.4+f(a): a=f(f(x)): a=f(f(a)):
- Problem gets more complicated. (even forget about coercion)



```
int f(double a) { ....(1) }
int f(int a) { ....(2) }
double f(int a) { ....(3) }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a); ② (a int, assign int) x=f(a); (3) (a int, assign double) x=2.4+f(a): a=f(f(x)): a=f(f(a)):
- Problem gets more complicated. (even forget about coercion)



## Context dependent overloading

Which

```
int f(double a) { ....(1) }
int f(int a) { ....(2) }
double f(int a) { ....(3) }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a); ② (a int, assign int) x=f(a); (3) (a int, assign double) x=2.4+f(a); (3) (a int, mult double) a=f(f(x)): a=f(f(a)):
- Problem gets more complicated. (even forget about coercion)



## Context dependent overloading

Which

```
int f(double a) { ....(1) }
int f(int a) { .... ② }
double f(int a) { ....(3) }
double x,y;
int a,b;
```

- a=f(x); (1)(x double) a=f(a); ② (a int, assign int) x=f(a); (3) (a int, assign double) x=2.4+f(a); (3) (a int, mult double) a=f(f(x)); (2(1)) (x double, f(x):int, assign int)a=f(f(a)):
- Problem gets more complicated. (even forget about coercion)



```
int f(double a) { ....① }
int f(int a) { ....② }
double f(int a) { ....③ }
double x,y;
int a,b;
```

- a=f(x); 1 (x double)
  a=f(a); 2 (a int, assign int)
  x=f(a); 3 (a int, assign double)
  x=2.4+f(a); 3 (a int, mult double)
  a=f(f(x)); 2(1) (x double, f(x):int, assign int)
  a=f(f(a)); 2(2) or 1(3) ???
- Problem gets more complicated. (even forget about coercion)



- Context dependent overloading is more expensive.
- Complex and confusing. Useful as much?
- Most overloading languages are context independent.
- Context independent overloading forbids ② and ③ functions defined together.
- "name: parameters" part should be unique in "name: parameters  $\rightarrow$  result", in the same scope
- Overloading is not much useful. So languages avoid it.

#### Use carefully:

Overloading is useful only for functions doing same operations. Two functions with different purposes should not be given same names. Confuses programmer and causes errors

■ Is variable overloading possible? What about same name for two types?





Making implicit type conversion for ease of programming.

```
double x; int k;
```

- C makes *int* ↔ *double* coercions and pointer coercions (with warning)
- $\blacksquare$  Are other type of coercions are possible? (like A \*  $\rightarrow$  A, A  $\rightarrow$ A \* ). Useful?
- May cause programming errors: x=k=3.25 : x becomes 3.0
- Coercion + Overloading: too complex.
- Most newer languages quit coercion completely (Strict type) checking)



#### Type Inference

- Type system may force user to declare all types (C and most compiled imperative languages), or
- Language processor infers types. How?
- Each expression position provide information (put a constraint) on type inference:
  - Equality  $e = x, x :: \alpha, y :: \beta \Rightarrow \alpha \equiv \beta$
  - Expressions  $e = a + f \times + :: Num \rightarrow Num \rightarrow Num \Rightarrow$  $a :: Num, f :: \alpha \rightarrow Num, e :: Num$
  - Function application  $e = f \times \Rightarrow e :: \beta, x :: \alpha, f :: (\alpha \rightarrow \beta)$
  - Type constructors  $f(x:r) = t \Rightarrow x :: \alpha, t :: \beta, f :: ([\alpha] \rightarrow \beta)$
- Inference of all values start from the most general type (i.e: any type  $\alpha$ )
- Type inference finds the most general type satisfying the constraints.



## Inferring Type from Initializers

- C++11 auto type specifier gets type from initializer or return expression.
- C++11 decltype (varexp) gets type same as the variables declared type

```
auto f(int a) {
    return a/3.0; // double, function becomes double
}
struct P { double x, y;} *pptr;

decltype(pptr->x) xval; // double since pptr->x is double
auto v = (P)({ 2.0, 4.0}); // initializer is P typed
auto t = f(3); // f(3) returns double so t is double
```

■ GCC has typeof(expr), some other dialects have \_\_typeof\_\_ (expr) macro having a similar mechanism in C.



### Summary

- Monomorphic vs Polymorphic types
- Subtyping
- Inheritence
- Overloading
- Parametric polymorphism
- Coercion
- Type Inference