

# Programming Language Concepts

## Syntax and Parsing

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# Outline

## 1 Describing Syntax

- Introduction
- Backus-Naur Form and CFGs
- Context Free Grammar
- Ambiguous Grammars
- Associativity
- An Assignment Grammar

## 2 Parsing

- if-then-else ambiguity
- Compilation
- Lexical Analysis
- Parsing
- Top-down Parsing
- Recursive Descent Parser
- LL Parsers
- Bottom-up Parsing

# Introduction

- **Syntax**: the form and structure of a program.
- **Semantics**: meaning of a program
- Language definitions are used by:
  - Programmers
  - Implementors of the language processors
  - Language designers

# Definitions

- A **sentence** is a string of characters over some alphabet
- A **language** is a set of sentences
- A **lexeme** is the lowest level syntactic unit of the language (i.e. `++`, `int`, `total`)
- A **token** is a category of lexemes (i.e. *identifier*)

# Definitions

- **syntax recognition**: read input strings of the language and verify the input belonging to the language
- **syntax generation**: generate sentences of the language (i.e. from a given data structure)
- Compilers and interpreters recognize syntax and convert it into machine understandable form.

# Backus-Naur Form and CFGs

- CFG's introduced by Noam Chomsky (mid 1950s)
- Programming languages are usually in **context free language** class
- BNF introduced by John Bakus and modified by Peter Naur for describing Algol language
- BNF is equivalent to CFGs. It is a **meta-language** that describes other languages
- Extended BNF improves readability of BNF

# A Grammar Rule

$\langle \text{while\_stmt} \rangle \rightarrow \text{while} ( \langle \text{logic\_expr} \rangle ) \langle \text{stmt} \rangle$

- LHS is a non-terminal denoting an intermediate phrase
- LHS can be defined (rewritten) as the RHS sequence which can contain terminals (lexems and tokens) of the language and other non-terminals
- Non-terminals are denoted as strings enclosed in angle brackets.
- $::=$  may be used in BNF notation instead of the arrow
- $|$  is used to combine multiple rules with same LHS in a single rule

$$\begin{array}{lcl} \langle \text{lgc\_cons} \rangle ::= \text{true} & \equiv & \langle \text{lgc\_cons} \rangle ::= \text{true} \mid \text{false} \\ \langle \text{lgc\_cons} \rangle ::= \text{false} & & \end{array}$$

# Context Free Grammar

- A **grammar**  $G$  is defined as  $G = (N, \Sigma, R, S)$ :
  - $N$ , finite set of non terminals
  - $\Sigma$ , finite set of terminals
  - $R$  is a set of grammar rules. A relation from  $N$  to  $(N \cup \Sigma)^*$ .
  - $S \in N$  the start symbol
- Application of a rule maps one sentential form into the other by replacing a non-terminal element in sentential form with its right handside sequence in the rule,  $u \mapsto v$ .
- Language of a grammar  $L(G) = \{w \mid w \in \Sigma^*, S \xrightarrow{*} w\}$



- Recursive or list like structures can be represented using recursion

$$\langle \text{expr\_list} \rangle \rightarrow \langle \text{expr} \rangle , \langle \text{expr\_list} \rangle$$

$$\langle \text{btree} \rangle \rightarrow \langle \text{head} \rangle ( \langle \text{btree} \rangle , \langle \text{btree} \rangle )$$

- A **derivation** starts with a starting non-terminal and rules are applied repeatedly to end with a sentence containing only terminal symbols.
- **leftmost derivation**: always leftmost non-terminal is chosen for replacement
- **rightmost derivation**: always rightmost non-terminal is chosen for replacement
- Same sentence can be derived using leftmost, rightmost, or other derivations.

# Sample Grammar

$$\begin{aligned}\langle \text{stmt} \rangle &\rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle \\ \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mid \langle \text{id} \rangle \\ \langle \text{op} \rangle &\rightarrow + \mid * \\ \langle \text{id} \rangle &\rightarrow a \mid b \mid c\end{aligned}$$

- Leftmost derivation of  $a = a * b$  :

$$\begin{aligned}\langle \text{stmt} \rangle &\mapsto \langle \text{id} \rangle = \langle \text{expr} \rangle \mapsto a = \langle \text{expr} \rangle \\ &\mapsto a = \langle \text{id} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mapsto a = a \langle \text{op} \rangle \langle \text{expr} \rangle \\ &\mapsto a = a * \langle \text{expr} \rangle \mapsto a = a * \langle \text{id} \rangle \mapsto a = a * b\end{aligned}$$

- Rightmost derivation of  $a = a * b$  :

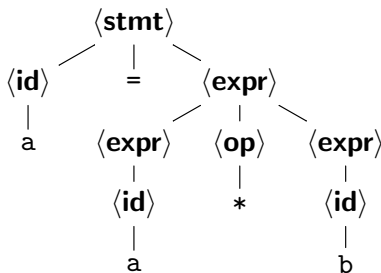
$$\begin{aligned}\langle \text{stmt} \rangle &\mapsto \langle \text{id} \rangle = \langle \text{expr} \rangle \mapsto \langle \text{id} \rangle = \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \\ &\mapsto \langle \text{id} \rangle = \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{id} \rangle \mapsto \langle \text{id} \rangle = \langle \text{expr} \rangle \langle \text{op} \rangle b \\ &\mapsto \langle \text{id} \rangle = \langle \text{expr} \rangle * b \mapsto \langle \text{id} \rangle = \langle \text{id} \rangle * b \\ &\mapsto \langle \text{id} \rangle = a * b \mapsto a = a * b\end{aligned}$$

# Parse Tree

- Steps of a derivation gives the structure of the sentence. This structure can be represented as a tree.
- All non-terminals used in derivation are **intermediate nodes**. Each grammar rule replaces the non-terminal node with its children. Root node is the start symbol.
- Terminal nodes are the **leaf nodes**.
- preorder traversal of leaf nodes gives the resulting sentence.
- leftmost and rightmost derivations can be retrieved by traversal of the tree.

# Parse Tree Example

a = a \* b

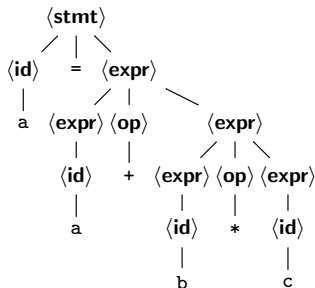


# Parse Tree Generation

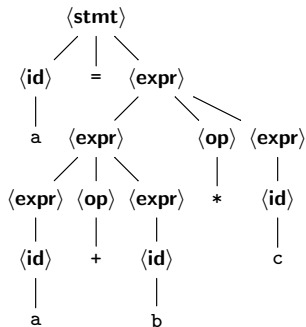
- A parse tree gives the structure of the program so semantics of the program is related to this structure.
- For example local scopes, evaluation order of expressions etc.
- During compilation, parse trees might be required for code generation, semantic analysis and optimization phases.
- After a parse tree generated, it can be traversed to do various tasks of compilation.
- The processing of parse tree takes too long, so creation of parse trees is usually avoided.
- Approaches like [syntax directed translation](#) combines parsing with code generation, semantic analysis etc..

# Ambiguous Grammars

- Consider  $a = a + b * c$  in our grammar:



VS



- Both can be derived by the grammar!

- A grammar is called **ambiguous** if same sentence can be derived by following different set of rules, thus resulting in a different parse tree
- If structure changes semantic meaning of the program, ambiguity is a serious problem.
- Even if not, which one is the result?
- i.e. Precedence of operators affects the value of the expression.
- Programming languages enforces precedence rules to resolve ambiguity.
- Solution:
  - 1 design grammar not to be ambiguous, or
  - 2 during parsing, choose rules to generate the correct parse tree

# Precedence and Grammar

- Operators with different precedence levels should be treated differently
- Higher precedence operations should be deep in the parse tree  
→ their rules should be applied later.
- Lower precedence operations should be closer to root → applied earlier in derivation.
- For each precedence level, define a non-terminal
- One rewritten on the other based on the precedence lower to higher



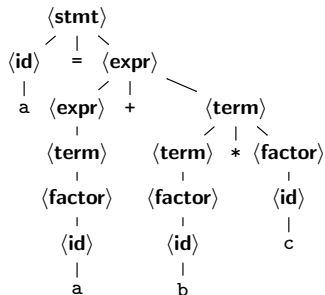
# Rewritten Grammar

$$\langle \text{stmt} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$$

$$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$$

$$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{factor} \rangle$$

$$\langle \text{factor} \rangle \rightarrow \langle \text{id} \rangle \mid ( \langle \text{expr} \rangle )$$

$$\langle \text{id} \rangle \rightarrow a \mid b \mid c$$


- `<term>` and `<expr>` has different precedence.
- Once inside of `<term>`, there is no way to derive `+`
- Only one parse possible

# Associativity

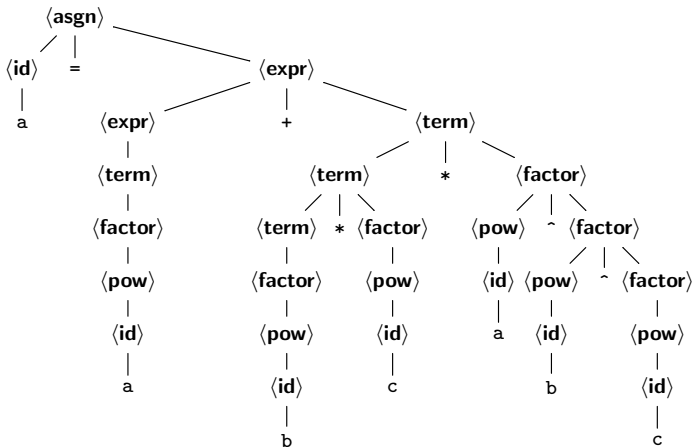
- Associativity of operators is another issue  
 $a - b - c \equiv (a - b) - c \quad \text{or} \quad a - (b - c)$
- Recursion of grammar defines how tree is constructed for operators in the same level.
- If left recursive, later operators in the sentence will be closer to root, if right recursive earlier operators will be closer to root
- **left recursion** implies left associativity, **right recursion** implies right associativity.
- Consider  $a + b + c$  in these grammars:  

$$\begin{array}{l} \langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{id} \rangle \mid \langle \text{id} \rangle \\ \langle \text{id} \rangle \rightarrow a \mid b \mid c \end{array} \quad \text{VS} \quad \begin{array}{l} \langle \text{expr} \rangle \rightarrow \langle \text{id} \rangle + \langle \text{expr} \rangle \mid \langle \text{id} \rangle \\ \langle \text{id} \rangle \rightarrow a \mid b \mid c \end{array}$$

# Sample Grammar

$$\begin{aligned}
 \langle \text{asgn} \rangle &\rightarrow \langle \text{id} \rangle = \langle \text{asgn} \rangle \mid \langle \text{id} \rangle = \langle \text{expr} \rangle \\
 \langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle \\
 \langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{factor} \rangle \\
 \langle \text{factor} \rangle &\rightarrow \langle \text{pow} \rangle ^ \langle \text{factor} \rangle \mid \langle \text{pow} \rangle \\
 \langle \text{pow} \rangle &\rightarrow \langle \text{id} \rangle \mid ( \langle \text{expr} \rangle ) \\
 \langle \text{id} \rangle &\rightarrow a \mid b \mid c
 \end{aligned}$$

- $\langle \text{asgn} \rangle$  is right recursive like right associative C assignments.
- $\langle \text{expr} \rangle$  and  $\langle \text{term} \rangle$  are left recursive,  $*$  and  $+$  left associative
- $\langle \text{factor} \rangle$  is right recursive for power operation  $^$  to be right associative.
- precedence order is  $(\dots) \prec ^ \prec * \prec + \prec =$

$$a = a + b * c * a \wedge b \wedge c$$


# if-then-else ambiguity

- Following grammar is ambiguous:

$\langle \text{stmt} \rangle \rightarrow \langle \text{if-stmt} \rangle$

$\langle \text{if-stmt} \rangle \rightarrow \text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{stmt} \rangle \mid$   
 $\text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

- Consider if a then if b then x=1 else x=0:

# if-then-else ambiguity

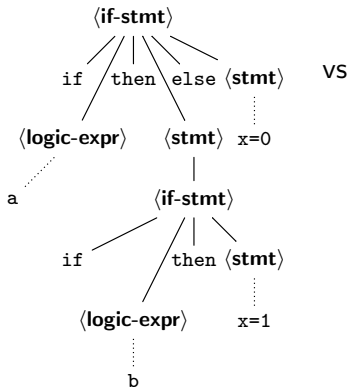
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$$\text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$$

- Consider if a then if b then x=1 else x=0:



# if-then-else ambiguity

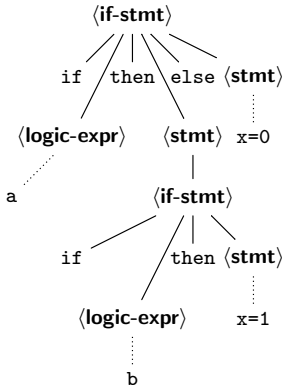
- Following grammar is ambiguous:

$$\langle \text{stmt} \rangle \rightarrow \langle \text{if-stmt} \rangle$$

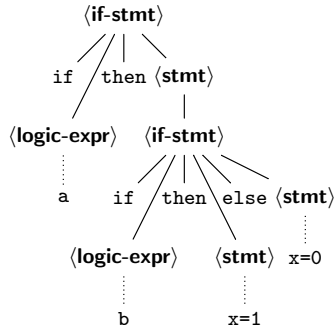
$$\langle \text{if-stmt} \rangle \rightarrow \text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{stmt} \rangle \mid$$

$$\text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$$

- Consider if a then if b then x=1 else x=0:



VS



# Solution

- Distinguish categories of statements. if's matched with else and unmatched:

```

<stmt> → <matched> | <unmatched>
<matched> → if <logic-expr> then <matched> else <matched> |
            <other-stmt>
<unmatched> → if <logic-expr> then <stmt> |
              if <logic-expr> then <matched> else <unmatched>

```

- if a then if b then x=1 else x=0:



# Solution

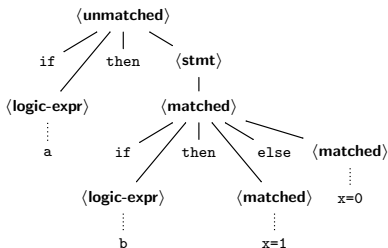
- Distinguish categories of statements. if's matched with else and unmatched:

$$\langle \text{stmt} \rangle \rightarrow \langle \text{matched} \rangle \mid \langle \text{unmatched} \rangle$$

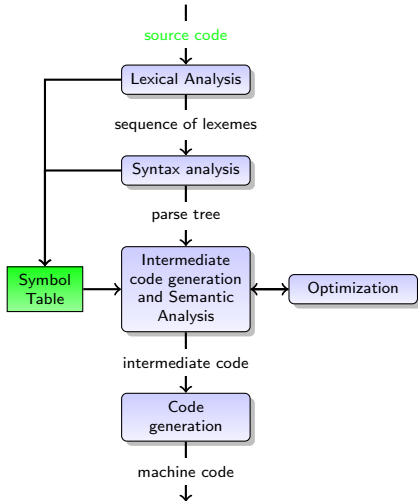
$$\langle \text{matched} \rangle \rightarrow \text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{matched} \rangle \text{ else } \langle \text{matched} \rangle \mid \langle \text{other-stmt} \rangle$$

$$\langle \text{unmatched} \rangle \rightarrow \text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{stmt} \rangle \mid \text{if } \langle \text{logic-expr} \rangle \text{ then } \langle \text{matched} \rangle \text{ else } \langle \text{unmatched} \rangle$$

- if a then if b then x=1 else x=0:

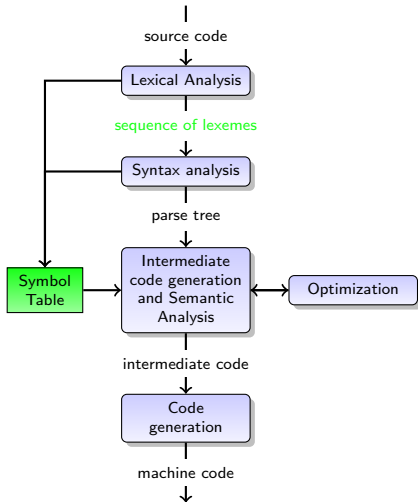


# Compilation



```
while (counter < 12341) {  
    f() ;  
    counter += 12;  
}
```

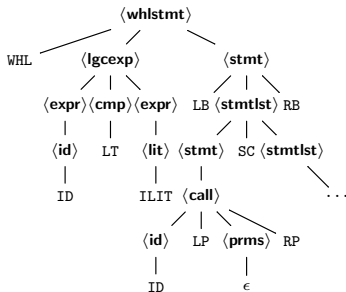
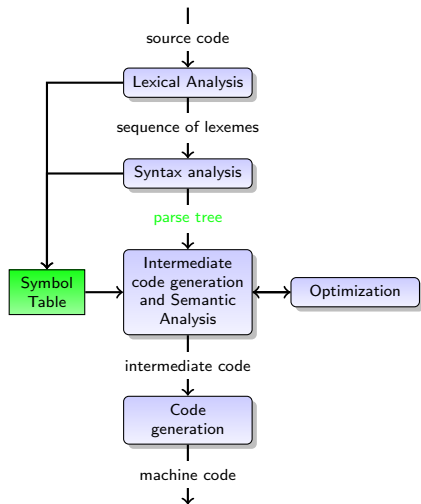
# Compilation



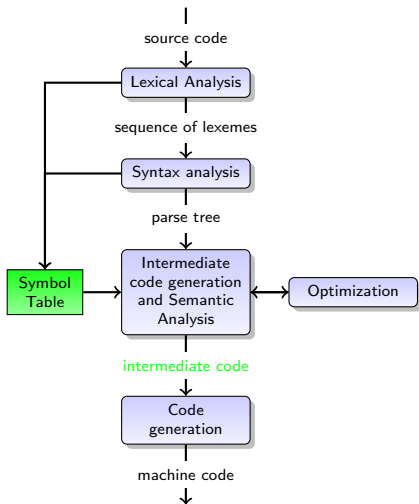
```

WHL LP ID LT ILIT RP LB
      ID LP RP SC
      ID PLEQ ILIT SC
RB
  
```

# Compilation



# Compilation

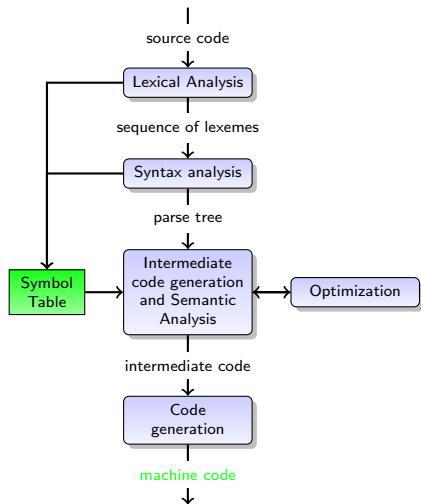


```

.L3:      movl    $0, %eax
          call    f
          addl    $12, -4(%rbp)

.L2:      cmpl    $12340, -4(%rbp)
          jle     .L3
          leave   .L3
          ret
  
```

# Compilation



```

001 f 0001 0006 0000
0034 0021 0000 0000
0004 0000 001 b 0009
0000 0000 02 f4 0008
0008 0001 0004 0008
0025 0001 0003 0000
0058 0000 0000 0000
0004 0000 002 b 0008
  
```

# Lexical Analysis

- **input**: sequence of characters, source code.
- **output**: sequence of lexemes
- Worst case complexity of parsing is  $\mathcal{O}(n^3)$ . Depending on algorithm type, recursion type and number of grammar rules, this might change.  $n$  is the length of the string.
- Regular language processing complexity is  $\mathcal{O}(n)$ . Grammars can be defined in terms of lexemes.
- # of chars vs # of lexemes?
- Lexical analysis convert character sequences into lexemes.  
Identifiers registered on symbol table

# Parsing

- **input**: sequence of lexemes (output of lexical analysis) or characters.
- **output**: parse tree, intermediate code, translated code, or sometimes only if document is valid or not.
- Two main classes of parser:
  - Top down parsing
  - Bottom up parsing



# Top-down Parsing

- Start from the starting non-terminal, apply grammar rules to reach the input sentence

$$\begin{aligned}
 \langle assign \rangle &\mapsto a = \langle expr \rangle \mapsto a = \langle expr \rangle + \langle term \rangle \mapsto \\
 &a = \langle term \rangle + \langle term \rangle \mapsto a = \langle fact \rangle + \langle term \rangle \mapsto \\
 &a = a + \langle term \rangle \mapsto a = a + \langle term \rangle * \langle fact \rangle \mapsto \\
 &a = a + \langle fact \rangle * \langle fact \rangle \mapsto a = a + b * \langle fact \rangle \mapsto \\
 &a = a + b * a
 \end{aligned}$$

- Simplest form gives leftmost derivation of a grammar processing input from left to right.
- Left recursion in grammar is a problem. Elimination of left recursion needed.
- Deterministic parsing:** Look at input symbols to choose next rule to apply.
- recursive descent parsers, LL family parsers** are top-down parsers

# Recursive Descent Parser

```

typedef enum {ident, number, lparen, rparen, times,
             slash, plus, minus} Symbol;
int accept(Symbol s) { if (sym == s) { next(); return 1; }
                      return 0;
}
void factor(void) {
    if (accept(ident)) ;
    else if (accept(number)) ;
    else if (accept(lparen)) { expression(); expect(rparen);}
    else { error("factor: syntax error at ", currsym); next(); }
}
void term(void) {
    factor();
    while (accept(times) || accept(slash))
        factor();
}
void expression(void) {
    term();
    while (accept(plus) || accept(minus))
        term();
}

```

- Each non-terminal realized as a parsing function
- Parsing functions calls the right handside functions in sequence
- Rule choices are based on the current input symbol. accept checks a terminal and consumes if matches.
- Cannot handle direct or indirect left recursion. A function has to call itself before anything else.
- Hand coded, not flexible.

# LL Parsers

- First L is 'left to right input processing', second is 'leftmost derivation'
- Checks next  $N$  input symbols to decide on which rule to apply:  $LL(N)$  parsing.
- For example  $LL(1)$  checks the next input symbol only.
- $LL(N)$  parsing table: A table for  $V \times \Sigma^N \mapsto R$
- for expanding a nonterminal  $NT \in V$ , looking at this table and the next  $N$  input symbols,  $LL(N)$  parser chooses the grammar rule  $r \in R$  to apply in the next step.

- Grammar and lookup table for a LL(1) parser:

$$1 \quad S \rightarrow E$$

$$2 \quad S \rightarrow -E$$

$$3 \quad E \rightarrow N + E$$

$$4 \quad E \rightarrow (E)$$

$$5 \quad N \rightarrow a$$

$$6 \quad N \rightarrow b$$

	a	b	-	(
S	1	1	2	1
E	3	3		4
N	5	6		

- What if we add  $E \rightarrow N$  to grammar?
- You need an LL(2) grammar. What if  $N$  is recursive?

- Grammar and lookup table for a LL(1) parser:

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see LL(\*) parser

# Bottom-up Parsing

- Start from input sentence and merge parts of sentential form matching RHS of a rule into LHS at each step. Try to reach the starting non-terminal. reach the input sentence

$$\begin{aligned}
 a = a + b * a &\mapsto a = \langle fact \rangle + b * a \mapsto a = \langle term \rangle + b * a \mapsto \\
 a = \langle expr \rangle + b * a &\mapsto a = \langle expr \rangle + \langle fact \rangle * a \mapsto \\
 a = \langle expr \rangle + \langle term \rangle * a &\mapsto a = \langle expr \rangle + \langle term \rangle * \langle fact \rangle \mapsto \\
 a = \langle expr \rangle + \langle term \rangle &\mapsto a = \langle expr \rangle \mapsto \langle assign \rangle
 \end{aligned}$$

- Simplest form gives rightmost derivation of a grammar (in reverse) processing input from left to right.
- Shift-reduce parsers are bottom-up:
  - **shift**: take a symbol from input and push to stack.
  - **reduce**: match and pop a RHS from stack and reduce into LHS.

# Shift-Reduce Parser in Prolog

```

% Grammar is E-> E-T/E+T/T  T -> a/b
rule(e,[e,-,t]).
rule(e,[e,+,t]).
rule(e,[t]).
rule(t,[a]).
rule(t,[b]).

parse([], [S]) :- S = e .  % starting symbol alone in the stack
% reduce: find RHS of a rule on stack, reduce it to LHS
parse(Input, Stack) :- match(LHS, Stack, Remainder),
                        parse(Input, [LHS|Remainder]).

% shift: nonterminals are removed from input added on stack
parse([H|Input], Stack) :- member(X, [a,b,-,+]),
                           parse(Input, [H|Stack]).

% check if RSH of a rule is a prefix of Stack (reversed).
match(LHS, List, L) :- rule(LHS, RHS),  reverse(RHS, NRHS),
                      prefix(NRHS, List, L).

```



- Shift reduce parser tries all non-deterministic shift combinations to get all parses.
- For deterministic parsing states based on input lookahead or precedence required
- Deterministic bottom up parsers: LALR, SLR(1).