



$$T.F = \frac{X(s)}{P(s)}$$

$$m\ddot{x} + k_1x + k_2(x-y) = p$$

$$k_2(x-y) = b_2\dot{y}$$

$$(ms^2 + k_1 + k_2)X(s) = k_2Y(s) + P(s)$$

$$k_2X(s) = (k_2 + b_2s)Y(s)$$

$$(ms^2 + k_1 + k_2)X(s) = \frac{k_2^2}{k_2 + b_2s} X(s) + P(s)$$

$$(ms^2 + k_1 + k_2)(k_2 + b_2s) - k_2^2 X(s) = (k_2 + b_2s)P(s)$$

$$\frac{X(s)}{P(s)} = \frac{b_2s + k_2}{mb_2s^3 + mk_2s^2 + (k_1 + k_2)b_2s + k_1k_2}$$

$$m = 0.1 \text{ kg}, \quad b_2 = 0.4 \text{ N-s/m}, \quad k_1 = 6 \text{ N/m}, \quad k_2 = 4 \text{ N/m}, \quad p(t) = 10 \text{ N}$$

$$\Rightarrow \frac{Y(s)}{P(s)} = \frac{Y(s)}{X(s)} \frac{X(s)}{P(s)} = \frac{k_2}{mb_2s^3 + mk_2s^2 + (k_1 + k_2)b_2s + k_1k_2}$$

$$\frac{X(s)}{P(s)} = \frac{0.4s + 4}{0.04s^3 + 0.4s^2 + 4s + 24} = \frac{10s + 100}{s^3 + 10s^2 + 100s + 600}$$

$$\frac{Y(s)}{P(s)} = \frac{4}{0.04s^3 + 0.4s^2 + 4s + 24} = \frac{100}{s^3 + 10s^2 + 100s + 600}$$

$p(t) = 10u(t)$, $u(t)$ unit-step input

$$\frac{X(s)}{U(s)} = \frac{100s + 1000}{s^3 + 10s^2 + 100s + 600}s$$

$$\frac{y(s)}{u(s)} = \frac{1000}{s^3 + 10s^2 + 100s + 600}s$$