How to time a Dispersion Strategy

Canari.dev (www.canari.dev), March-2021

16 # First some setup

The definition of a *dispersion trade* is provided here : https://quantpedia.com/strategies/dispersion-trading/

This project showcases the possibilities offered by the API of Deutsche Boerse's A7 service. You will need a valid A7 subscription to run it. '\ For this, go to: https://www.mds.deutscheboerse.com/mds-en/analytics/A7-analytics-platform

The following git shows how to connect to A7 API, then retrieve intraday quotes and calibrate a volatility surface with the output: https://github.com/canari-dev/Calibrating-implicit-volatility-surface-with-Deutsche-Boerse-A7

The first part of this git reuses large chunks of the code shown in the calibration git but the need here is for "At The Money" volatility only, on a wide range of underlyings so the strikes range is trimmed to fasten the process. None

```
# Indicate here the folders where you want the intraday quotes to be stored (folder1)
    # and the calibration result (folder 2)
   folder1 = 'D:/Users/GitHub/Dispersion Volatility/processed'
   folder2 = 'D:/Users/GitHub/Dispersion Volatility/parameters'
   import os
   os.makedirs(folder1, exist_ok=True)
   os.makedirs(folder2, exist_ok=True)
17 # We are now importing public libraries
   import numpy as np
   import pandas as pd
   import QuantLib as ql
   import math
   import datetime
   import matplotlib.pyplot as plt
   import requests
   import warnings
   from IPython.display import display, HTML
    pd.set option('display.width', 200)
    pd.set_option('display.max_columns', 30)
18 # ...and specific libraries available in this git
    from DateAndTime import DateAndTime
    # uses QuantLib to calculate numbers of business day between dates and generate a list expiration dat
   from PricingAndCalibration import Pricing
    # uses Quantlib to price European and American options with continuous dividend yield and the associa
    from PricingAndCalibration import FittingSpline
    # uses scipy-UnivariateSpline to fit a 2nd degree spline through the implicit vol of bid and ask quot
```

```
19 # Choose here the time frame and the maturity to retrieve
    from date='20200310'
    until date='20200321'
    chosen matu = ['20201218']
    #And now the underlyings with index weight
    # [A7 option code, Spot whern weight in % was observed, Weight in %, Isin code, Underlying future cod
    index_list = [('OESX', 3655.77, '', '', 'FESX')]
    #you can reduce this stock list in ordre to save time...
    udl list = [
        ('SAP', 108.47, 6.17, 'DE0007164600', ''),
        ('ASM', 460, 5.69, 'NL0010273215', ''),
        ('LIN', 257.37, 4.69, 'IE00BZ12WP82', ''),
        ('MOH', 528.7, 4.58, 'FR0000121014', ''),
        ('SNW', 80.01, 4.13, 'FR0000120578', ''),
        ('SIE', 133.06, 3.42, 'DE0007236101', ''),
        ('TOTB', 35.07, 3.16, 'FR0000120271', ''),
        ('ALV', 195.77, 2.89, 'DE0008404005', ''),
        ('LOR', 305.6,2.89, 'FR0000120321', ''),
        ('AIR', 136.25, 2.74, 'FR0000120073', ''),
        ('IBE', 11.26, 2.57, 'ES0144580Y14', ''),
        ('SND', 124.6, 2.52, 'FR0000121972', ''),
        ('ENL5', 8.439, 2.45, 'IT0003128367', ''),
        ('BAY', 56.15, 2.21, 'DE000BAY0017'
         ('ADS', 278, 2.2, 'DE000A1EWWW0', ''),
         ('BAS', 66.86, 2.02, 'DE000BASF111', ''),
        ('ADY', 1884.5, 1.86, 'NL0012969182', ''),
         ('PPX', 549, 1.81, 'FR0000121485', ''),
         ('SQU', 86, 1.71, 'FR0000125486'
         ('ITK', 54.78, 1.64, 'BE0974293251'
         ('DPW', 42.165, 1.63, 'DE0005552004',
         ('DAI', 66.9, 1.61, 'DE0007100000',
         ('PHI1', 47.08, 1.54, 'NL0000009538',
         ('EAD', 93.42, 1.53, 'NL0000235190',
         ('BSN', 53.34, 1.5, 'FR0000120644'
        ('BNP', 53.595, 1.5, 'FR0000131104', ''),
           ('PROSUS', 100.05, 1.44, 'NL0013654783', ''),
           ('ESL', 128.75, 1.44, 'FR0000121667', 'no stock on Xetra'), AXA', 19.204, 1.37, 'FR0000120628', ''),
        ('AXA', 19.204, 1.37, 'FR0000120628',
            ('KONE', 66.03, 1.29, 'FI0009013403',
    #
        ('MUV2', 233.5, 1.58, 'DE0008430026', ''),
        ('SEJ', 112.2, 1.26, 'FR0000073272', 'no stock on Xetra'), ('ANN', 55.53, 1.26, 'DE000A1ML7J1', ''),
         ('IES5', 2.059, 1.22, 'IT0000072618', ''),
         ('DB1', 136.4, 1.21, 'DE0005810055', ''),
         ('AHO', 23.35, 1.18, 'NL0011794037',
         ('PER', 163.2, 1.15, 'FR0000120693', ''),
         ('IXD', 26.115, 1.12, 'ES0148396007',
         ('BSD2', 2.774, 1.11, 'ES0113900J37', ''),
        ('V03', 162.35, 1.07, 'DE0007664039', ''),
('CRG', 35.51, 1.05, 'US12626K2033', 'no stock on Xetra'),
        ('INN', 7.766, 0.99, 'NL0011821202', ''),
           ('AI3A', 56.37, 0.9, 'ES0109067019', 'no stock on Xetra'),
         ('VVU', 25.92, 0.87, 'FR0000127771',
        ('BMW', 70.295, 0.83, 'DE0005190003', ''), ('NOA3', 3.495, 0.8, 'FI0009000681', ''),
         ('ENT5', 8.645, 0.7, 'IT0003132476', '')]
```

```
API_TOKEN = "Bearer " + "your A7 API token here"
# The API token is obtained by clicking on your name in the upper right corner of the A7 Analytics Pl
```

20 #indicate your A7 credentials :
 owner = 'your A7 username here'

```
"http": "", # Enter http Proxy if needed",
       "https": "" # Enter https Proxy if needed",
   }
21 # Select an algo to retrieve quotes on A7.
   # 'minsize_level_tb' allows you to look into the orderbook until finding a minimum number of lots.
   # 'minsize_level_fast' goes faster by looking only at the top level
   # Both algos are given in this git as a .yml file
   # They must be loaded first in your A7 account.
   algo = 'minsize_level_tb'
   # If you have chosen the 'minsize_level' algo :
   min_lots = 1
22 # Filter settings to speed up the process since we are only interested in At The Money volatility
   # Levels are indicated for 1 year maturity option with an adjustment in sqrt(T)
   moneyness_range_call = (-0.025, 0.15)
   moneyness_range_put = (-0.15, 0.025)
   # Create instances of DateAndTime both for italian and other underlyings
   DT = DateAndTime(from_date, until_date, force_matu=chosen_matu)
   DTi = DateAndTime(from_date, until_date, force_matu=chosen_matu, ital_rule=True)
23 <h6>The next function retrieves the intraday quotes given an option code</h6>
   def get guotes(opt): if opt['PutOrCall'] == 'S': market = 'XETR' else: market = 'XEUR'
      url = 'https://a7.deutsche-boerse.com/api/v1/algo/{}/'.format(owner, algo)
      url = url + "run?marketId={}&date={}&marketSegmentId={}&securityId={}&from h=9&from m=1
          market, reference date, opt['SegmentID'], opt['SecurityID'], min lots)
      r = requests.get(url=url, headers={'Authorization': API TOKEN}, proxies=proxies)
      res = r.json()
      if type(res) == list:
          df_opt = pd.DataFrame.from_dict(res[0]['series'][0]['content'])
          df_opt.ts = df_opt.ts.astype(np.int64)
          df_opt.ts = pd.to_datetime(df_opt.ts)
          df opt.set index('ts', inplace=True)
          df_opt[selected_fields_desc] = opt[selected_fields_desc]
          return (df opt)
24 <h6>This function retrieves instruments from A7 in the res* lists, </h6>
   It also gets segment codes in segment*,
   and fills the matu_list* with relevant maturities
   def retrieve instruments from A7():
```

proxies = {

```
global res_u, res_f, res_i
global segmentIDudl, segmentIDfut, segmentIDopt, security
global matu_list_Stk, matu_list_Fut, matu_list_Opt
# stock
if (udl_p not in index_list) and (udl_p[4] != 'no stock on Xetra'):
    lst_ms = np.array([x['MarketSegment'] for x in res_gu['MarketSegments']])
    indx = np.where(lst_ms == isin)[0][0]
    segmentIDudl = res gu['MarketSegments'][indx]['MarketSegmentID']
    url = 'https://a7.deutsche-boerse.com/api/v1/rdi/XETR/{}/?mode=detailed'.format(r
    r = requests.get(url=url, headers={'Authorization': API TOKEN}, proxies=proxies)
    res_u = r.json()
    security = res u['Securities'][0]
    matu list Stk = ['UDL']
else:
    matu list Stk = []
# Futures
if (udl p in index list):
    udl f = udl p[4]
    lst_ms = np.array([x['MarketSegment'] for x in res_go['MarketSegments']])
    indx = np.where(lst_ms == udl_f)[0][0]
    segmentIDfut = res_go['MarketSegments'][indx]['MarketSegmentID']
    url = 'https://a7.deutsche-boerse.com/api/v1/rdi/XEUR/{}}?mode=detailed'.format(
        reference_date,
        segmentIDfut)
    r = requests.get(url=url, headers={'Authorization': API_TOKEN}, proxies=proxies)
    res f = r.json()
    matu list Fut = DT u.get matu list(reference date, trim=True)[:2]
else:
    matu_list_Fut = []
# Options
lst ms = np.array([x['MarketSegment'] for x in res go['MarketSegments']])
indx = np.where(1st ms == udl)[0][0]
segmentIDopt = res go['MarketSegments'][indx]['MarketSegmentID']
url = 'https://a7.deutsche-boerse.com/api/v1/rdi/XEUR/{}/{}?mode=detailed'.format(refer
                                                                                   segme
r = requests.get(url=url, headers={'Authorization': API_TOKEN}, proxies=proxies)
res_i = r.json()
matu_list_Opt = DT_u.get_matu_list(reference_date)
```

```
20200303
20200310
20200317
                               bid PutOrCall StrikePrice ContractMultiplier ExerciseStyle matu udl
                       ask
2020-03-03 10:10:00 177.55 177.50
                                                    None
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2020-03-03 16:25:00 176.20
                            176,10
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                                                          ContractMultiplier ExerciseStyle matu
                       ask
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2020-03-03 14:10:00
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                            177.80
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2020-03-03 16:10:00
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                            177.65
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2020-03-03 14:10:00
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2020-03-03 16:25:00 176.20 176.10
                                                    None
                                                                                      None
                                                                                           UDL
                                                                                                LIN
def build options list():
  global df orderbook
  df u = pd.DataFrame(columns=['SegmentID'] + selected fields + selected fields desc)
  i = 0
  for matu in matu list Stk:
       df_u.loc[i] = [segmentIDudl, security['SecurityDesc'], security['SecurityID'], 'S',
       df_opt = get_quotes(df_u.loc[i])
       df opt['matu'] = matu
       df_opt['udl'] = udl
       df_opt = df_opt.loc[(df_opt.bid > 0) & (df_opt.ask > 0)]
       df orderbook = df orderbook.append(df opt)
       i += 1
  for c, matu in enumerate(matu list Fut):
       for x in [x for x in res_f['Securities'] if (str(x['MaturityDate']) == matu) and (>
           df_u.loc[i] = [segmentIDfut] + [x[elt] for elt in selected_fields] + [
               x['DerivativesDescriptorGroup']['SimpleInstrumentDescriptorGroup'][elt] for
           df_u.loc[i]['PutOrCall'] = 'FUT' + str(c)
           df_opt = get_quotes(df_u.loc[i])
           df_opt['matu'] = matu
```

df opt['udl'] = udl

```
df_opt = df_opt.loc[(df_opt.bid > 0) & (df_opt.ask > 0)]
              df orderbook = df orderbook.append(df opt)
              i += 1
     FVUmin = (df_opt.bid.min() + df_orderbook.ask.min()) / 2
     FVUmax = (df_opt.bid.max() + df_orderbook.ask.max()) / 2
     for matu in matu_list_Opt:
          i = 0
          df = pd.DataFrame(columns=['SegmentID'] + selected fields + selected fields desc)
          for x in [x for x in res i['Securities'] if
                    (str(x['MaturityDate']) == matu) and (x['SecurityType'] == 'OPT')]:
              df.loc[i] = [segmentIDopt] + [x[elt] for elt in selected fields] + \
                          [x['DerivativesDescriptorGroup']['SimpleInstrumentDescriptorGroup']
                           in selected_fields_desc]
              i += 1
          df.sort_values(by=['StrikePrice', 'PutOrCall'], ascending=[True, True], inplace=Tru
          TTM = DT u.time between(pd.Timestamp(reference date), pd.Timestamp(matu))
          df['matu'] = matu
          df['moneyness_T_min'] = df.apply(
              lambda opt: math.log(opt.StrikePrice / FVUmax) / (max(3.0 / 12.0, TTM) ** 0.5),
          # we consider that div max is 8%
          df['moneyness_T_max'] = df.apply(
              lambda opt: math.log(opt.StrikePrice / (FVUmin * 0.92)) / (max(3.0 / 12.0, TTM)
          df['in_range'] = df.apply(lambda opt: (opt.moneyness_T_max > moneyness_range_call[@united]
                  opt.moneyness T min < moneyness range call[1]) \</pre>
              if opt.PutOrCall == '1' else \
              (opt.moneyness T max > moneyness range put[0]) and (
                      opt.moneyness T min < moneyness range put[1]),</pre>
                                     axis='columns')
     return (df.loc[df.in range])
26 <h6>Let's now use these functions to retrieve the intraday quotes data and save them in the df ordebo
   0ESX
   20200304
      20201218
   20200305
      20201218
   20200306
      20201218
   20200309
      20201218
   20200311
      20201218
   20200312
      20201218
   20200313
      20201218
   20200316
```

20201218

SAP

ASM

LIN

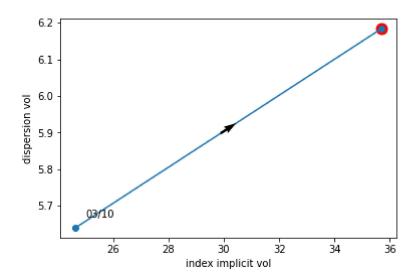
```
20200316
  20201218
20200318
  20201218
20200319
  20201218
20200320
  20201218
                                                                spline bid
                  matu
2020-03-03 10:10:00 20201218 <scipy.interpolate.fitpack2.LSQUnivariateSplin... <scipy.interpolate.fi
2020-03-03 16:25:00 20201218 <scipy.interpolate.fitpack2.LSQUnivariateSplin... <scipy.interpolate.fi
2020-03-10 10:10:00 20201218 <scipy.interpolate.fitpack2.LSQUnivariateSplin... <scipy.interpolate.fi
2020-03-10 12:10:00 20201218 <scipy.interpolate.fitpack2.LSQUnivariateSplin... <scipy.interpolate.fi
2020-03-10 14:10:00 20201218 <scipy.interpolate.fitpack2.LSQUnivariateSplin... <scipy.interpolate.fi
a = datetime.datetime.now() # time check
for reference_date in DT.dates_list: print(reference_date)
  # retrieve all instruments (stocks the options) from A7
  url = 'https://a7.deutsche-boerse.com/api/v1/rdi/XETR/{}?mode=detailed'.format(reference
  r = requests.get(url=url, headers={'Authorization': API TOKEN}, proxies=proxies)
  res_gu = r.json()
  url = 'https://a7.deutsche-boerse.com/api/v1/rdi/XEUR/{}?mode=detailed'.format(reference
  r = requests.get(url=url, headers={'Authorization': API_TOKEN}, proxies=proxies)
  res_go = r.json()
  for udl p in index list + udl list:
      udl = udl p[0]
      isin = udl p[3]
      # Determine which instance of DT class: the normal one (DT)
      # or the one giving thursday expiry dor italian stocks (DTi)
      if isin[:2] == 'IT':
          DT u = DTi
      else:
          DT u = DT
          df_orderbook = pd.read_pickle(folder1 + '/Quotes_' + udl + '.pkl')
      except:
          df_orderbook = pd.DataFrame()
      if df orderbook.shape[0] > 0:
          done_already = [elt.strftime('%Y%m%d') for elt in set([elt.date() for elt in d1
      else:
          done already = []
      if reference_date not in done_already:
          try:
               retrieve_instruments_from_A7()
```

```
# retrieves quotes
                  selected_fields = ['SecurityDesc', 'SecurityID']
                  selected_fields_desc = ['PutOrCall', 'StrikePrice', 'ContractMultiplier', '
                  df = build_options_list()
                  for index, opt in df.iterrows():
                      df opt = get quotes(opt)
                      df opt['matu'] = opt.matu
                      df opt['udl'] = udl
                      df opt = df opt.loc[(df opt.bid > 0) & (df opt.ask > 0)]
                      df orderbook = df orderbook.append(df opt)
              except:
                  print('\n\n fail for : {}, {}\n\n'.format(reference_date, udl))
          df orderbook.to pickle(folder1 + '/Quotes ' + udl + '.pkl')
   for udl_p in index_list + udl_list: print(display(HTML(df_orderbook.head().to_html()))) print('')
27 <h6>At this stage, you have created a df_orderbook dataframe and saved it in folder1.
   We are now going to fit a vol curve on these quotes using the FittingSpline class.</h6>
               udl
                      ATFbid
                                ATFask
                                         Spot
                                                  Error RefSpot
                                                                      W isin info DispVolbid Di
   2020-03-03 OESX 16.503958 17.174238 3414.5 2.375209 3655.77 0.069222
                                                                               FESX
                                                                                    10.444283
   2020-03-10 OESX 24.646138 25.215311 3071.5 1.955628 3655.77 0.139757
                                                                               FESX
                                                                                      5.640720
   2020-03-17 OESX 35.690101 37.699133 2404.5 2.134421 3655.77 0.155439
                                                                              FESX
                                                                                      6.183251
              udl ATFbid ATFask Spot
                                                 Error RefSpot
                                                                      W isin info DispVolbid Di
   2020-03-10 OESX 24.646138 25.215311 3071.5 1.955628 3655.77 0.139757
                                                                              FESX
                                                                                      5.640720
   2020-03-17 OESX 35.690101 37.699133 2404.5 2.134421 3655.77 0.155439
                                                                               FESX
                                                                                      6.183251
   for udl_p in index_list + udl_list: udl = udl_p[0] isin = udl_p[3] print(udl)
     if isin[:2] == 'IT':
          FS = FittingSpline(udl, DTi, folder1, folder2)
     else:
          FS = FittingSpline(udl, DT, folder1, folder2)
     if FS.data_found:
         FS.fit_all()
   print(display(HTML(FS.df_params.head().to_html())))
29 <h6>The partameters have been saved in folder2.</h6>
   We are now going to compute the dispersion volatility defined as :
   Dispersion Vol = ( Sum(i=1..50, Wi * ATFi^2) - (1+Leverage) * ATFindex^2 ) / Normalisation_factor
```

where

- ATFi is the ATM implicit vol of the ith stock in the index
- ATFindex is the ATM implicit vol of the index
- Leverage is the additional notional of index varswap to sell in order to get a vega neutral dispers
- Wi is the weight of the ith component in the index
- Normalisation_factor is a factor to apply to get a vega of 1 on the index so : 2 * (1+Leverage) * A

The index weight are calculated based on a "photo" taken on a specific date. Ref spot have been saved



```
def pick hour(df d):
          i = df d.Error.idxmin()
          return(df.loc[i,:])
def compute_dispvol(df_d):
          W = df d.W.sum()
          res = df_d.loc[df_d.udl == 'OESX']
          res['W'] = W * res.RefSpot / res.Spot
          res['DispVolbid'] = (df_d.DispVolbid.sum() / W - (1+Leverage) * res.ATFbid ** 2) / (2 * (1+Leverage)
          res['DispVolask'] = (df_d.DispVolask.sum() / W - (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * res.ATFask ** 2) / (2 * (1 + Leverage) * 
          return(res)
matu = chosen_matu[0][:-2]
\# udl_dic = dict([(elt[0], (elt[1], elt[2])) for elt in udl_list])
Leverage = 0.2
df = pd.DataFrame()
for udl_p in index_list + udl_list:
          udl = udl_p[0]
          try:
                    df_udl = pd.read_pickle(folder2 + '/Params_' + udl + '.pkl')
          except:
                    df_udl = pd.DataFrame()
          if df udl.shape[0] > 0:
                    df_udl['udl'] = udl
                    df_udl['ATFbid'] = df_udl.spline_bid.apply(lambda x: x(0))
                    df_udl['ATFask'] = df_udl.spline_ask.apply(lambda x: x(0))
                    s = df_udl.index.levels[1].to_series()
                    df_udl.index = df_udl.index.set_levels(s.map(lambda x: x[:-2]).fillna(s), level=1)
                    df_udl = df_udl.xs(matu, level=1, drop_level=True)
                    df_udl = df_udl[['udl', 'ATFbid', 'ATFask', 'Spot', 'Error']]
                    df_udl.index = df_udl.index.map(lambda x: x.date())
                    df_udl.sort_values(by=['ts', 'Error'], inplace=True)
                    df_udl = df_udl.groupby(df_udl.index).first()
                    df = df.append(df_udl)
```

dW = pd.DataFrame(index_list + udl_list, columns=['udl', 'RefSpot', 'W', 'isin', 'info'])

```
df = pd.merge(df, dW, left_on='udl', right_on='udl', how='left').set_index(df.index)
df['W'] = df.apply(lambda x: 0 if x.udl == 'OESX' else x.W / 100 * (x.Spot / x.RefSpot), axis='column
df['DispVolbid'] = df.apply(lambda x: x.W * x.ATFbid ** 2, axis='columns')
df['DispVolask'] = df.apply(lambda x: x.W * x.ATFask ** 2, axis='columns')
df = df.groupby(df.index, group_keys=False).apply(compute_dispvol)
print(df.head())
<h6>Finally, we will graph the DispVol vs the index vol to exhibit circular patterns as describes in .
x = ((df['ATFbid'] + df['ATFask'])/2).values
y = ((df['DispVolbid'] + df['DispVolask'])/2).values
dates = [elt.strftime('%m/%d') for elt in df.index.values]
u = np.diff(x)
v = np.diff(y)
pos_x = x[:-1] + u/2
pos_y = y[:-1] + v/2
norm = np.sqrt(u**2+v**2)
fig, ax = plt.subplots()
ax.plot(x,y, marker="o")
ax.quiver(pos_x, pos_y, u/norm, v/norm, angles="xy", zorder=5, pivot="mid")
for i, txt in enumerate(dates):
   if i%3==0:
       # ax.annotate(txt, (x[i], y[i]))
       ax.annotate(txt, (x[i], y[i]), xytext=(10, 10), textcoords='offset points')
plt.scatter([x[-1]], [y[-1]], c='#ff0000', s=120)
plt.xlabel("index implicit vol")
```

This graph shows the evolution of the Dispersion Volatility (Y) vs the straight Implicit Volatility (X) of the index during the march 2020 market meltdown. It shows a classical example of index vol raising faster than it's components then a catch up. (See the README file of this Git for more details.)

plt.ylabel("dispersion vol")

plt.show()