Applied Estimation(EL2320) Lab 1 EKF

1 Introduction

This lab consists of two parts:

- 1. A series of preparatory questions that we will go over in class
- 2. Two separate matlab exercises
 - A warm-up case study with a standard Kalman filter where you learn more about the behavior of the Kalman filter. Very little extra code is needed.
 - The main lab 1 problem in which you need to complete an implementation of an Extended Kalman filter based robot localization.

It is a good time to review chapter 1 and 2 to gain more background about what the course is about including Kalman filters, chapter 3(up to the end of 3.3) to do a recap about the (Extended) Kalman filter and chapter 7(up to the end of 7.5) to further familiarize yourself with the EKF localization problem. If you want to dig more, you can also read the section 1 and 2 of An Introduction to the Kalman Filter by Greg Welch and Gary Bishop. You need to keep in mind that you will encounter the same equations with different notations in different literature. Therefore, the best way to not confuse different notations is to make a short list of variables/notations in the literature you are reading and stick with one notation that you feel more comfortable with. We will try to use the book, Probabilitic Robotics, notation as much as possible.

In order to pass this lab you need to upload to the Course Web a pdf with:

- 1. written answers to the preparatory questions, Part I.
- 2. written answers to the questions in Part II
- 3. the plots result on each data set. So that is four runs, one on each of the first two data sets and both the batch and sequential runs on the last. The plots should be analysed in the report with a short text on each that explains why it looks the way it does compared to the other plots.

You must also upload your [working!] code.

Uploading and passing the lab on time gives a bonus point on the exam. Do as much as you can and upload by the deadline. You may then have

to complete sections that don't pass. You need to do the readings and answer the questions (as many as you can) before you start to write the code in order to benefit from this lab.

2 PART I - Preparitory Questions

These questions are intended to encourage you to think about what we have covered so far on the Bayesian filtering, the Kalman filter, the extended Kalman filter and localization.

You should write out your answers to the questions neatly and legibly and bring them to class on the assigned day. Be sure to include your name. These answers will be collected and redistributed randomly in class. You will be grading each others papers while we discuss them in class. The act of grading is part of the process of re-enforcing what you have learned. These grades will be recorded but the value of the grade does not effect your grade for the lab. If you get more than 30% correct you will get a bonus point on the exam. You will then be able to correct the answers before uploading the lab report to the assignement on the course web. In other words getting all the answers correct for class is not necessary, but participation is of great benefit to you. The proper way to do this is come to class with a pdf that you then modify and upload, but as long as you get there in the end any path is ok.

The 30% applies for the bonus point but is not good enough for passing the lab. Upload correct answers for all questions.

Linear Kalman Filter:

- 1. What is the difference between a 'control' \mathbf{u}_t , a 'measurement' \mathbf{z}_t and the state \mathbf{x}_t ? Give examples of each?
- 2. Can the uncertainty in the belief increase during an update? Why (or not)?
- 3. During update what is it that decides the weighing between measurements and belief?
- 4. What would be the result of using a too large a covaraince (Q matrix) for the measurement model?
- 5. What would give the measurements an increased effect on the updated state estimate?
- 6. What happens to the belief uncertainty during prediction? How can you show that?
- 7. How can we say that the Kalman filter is the optimal and minimum least square error estimator in the case of independent Gaussian noise and Gaussian priori distribution? (Just describe the reasoning not a formal proof.)

8. In the case of Gaussian white noise and Gaussian priori distribution, is the Kalman Filter a MLE and/or MAP estimator?

Extended Kalman Filter:

- 9. How does the extended Kalman filter relate to the Kalman filter?
- 10. Is the EKF guaranteed to converge to a consistent solution?
- 11. If our filter seems to diverge often can we change any parameter to try and reduce this?

Localization:

- 12. If a robot is completely unsure of its location and measures the range r to a know landmark with Gaussain noise what does its posterior belief of its location $p(x, y, \theta|r)$ look like? So a formula is not needed but describe it at least.
- 13. If the above measurement also included a bearing how would the posterior look?
- 14. If the robot moves with relatively good motion estimation (prediction error is small) but a large initial uncertainty in heading θ how will the posterior look after traveling a long distance without seeing any features?
- 15. If the above robot then sees a point feature and measures range and bearing to it how might the EKF update go wrong?

3 PART II - Matlab Excercises

3.1 Warm up problem with Standard Kalman Filter

Consider a car example. The acceleration of the car is controlled by the throttle/break. The system is described by:

$$x_{k} = \begin{bmatrix} p_{k} \\ v_{k} \end{bmatrix}$$

$$u_{k} = a_{0}$$

$$A = \begin{bmatrix} 1 & \Delta t \\ 0 & 1 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 \\ \Delta t \end{bmatrix}$$

$$x_{k+1} = Ax_{k} + Bu_{k} + \varepsilon_{k}$$

$$C = \begin{bmatrix} 1 & 0 \\ z_{k} = Cx_{k} + \delta_{k} \end{bmatrix}$$

$$(1)$$

where p_k , v_k and are the position and velocity of the car in the k^{th} time step, a_0 is the (constant) acceleration of the car and ε_k and δ_k are white Gaussians.

• Question 1: What are the dimensions of ε_k and δ_k ? What parameters do you need to define in order to uniquely characterize a white Gaussian?

Download kf_car.m. Read the comments and the code and make sure you understand how the system is defined, how the system is modeled and what are the roles of different variables.

- Question 2: Make a table showing the roles/usages of the variables(x, xhat, P, G, D, Q, R, wStdP, wStdV, vStd, u, PP). To do this one must go beyond simply reading the comments in the code to seeing how the variable is used. (hint some of these are our estimation model and some are for simulating the car motion).
- Question 3: Please answer this question with one paragraph of text that summarizes broadly what you learn/deduce from changing the parameters in the code as described below. Chose two illustrative sets of plots to include as demonstration. What do you expect if you increase/decrease the covariance matrix of the modeled (not the actual simulated) process noise/measurement noise 100 times(one change in the default parameters each time) for the same underlying system? Characterize your expectations. Confirm your expectations using the code (save the corresponding figures so you can analyze them in your report). Do the same analysis for the case of increasing/decreasing both parameters by the same factor at the same time. (Hint: It is the mean and covariance behavior over time that we are asking about.)
- Question 4: How do the initial values for P and xhat affect the rate of convergence and the error of the estimates (try both much bigger and much smaller)?

3.2 Main problem: EKF Localization

Consider the robot localization(tracking) problem. Given a map of the environment (M^1) , some measurements and some control signals, you are to estimate where the robot is located at each time step. Using a first order Markov assumption and Bayesian update, this can be formalized in recursive form as: 2

$$\begin{cases}
p(\mathbf{x_t}|\mathbf{u_{1:t}}, \mathbf{z_{1:t}}, \bar{\mathbf{x_0}}, M) &= \eta p(\mathbf{z_t}|\mathbf{x_t}, M) \int p(\mathbf{x_t}|\mathbf{u_t}, \mathbf{x_{t-1}}) p(\mathbf{x_{t-1}}|\mathbf{z_{1:t-1}}, \mathbf{u_{1:t-1}}, \bar{\mathbf{x_0}}, M) \mathbf{dx_{t-1}} \\
p(\mathbf{x_0}|\bar{\mathbf{x_0}}) &= \delta(\mathbf{x_0} - \bar{\mathbf{x_0}})
\end{cases}$$
(2)

or equivalently

$$\begin{cases} bel(\mathbf{x_t}) &= p(\mathbf{x_t}|\mathbf{u_{1:t}}, \mathbf{\bar{x_0}}, M) = \eta p(\mathbf{z_t}|\mathbf{x_t}, M)\overline{bel}(\mathbf{x_t}) \\ \overline{bel}(\mathbf{x_t}) &= p(\mathbf{x_t}|\mathbf{u_{1:t}}, \mathbf{z_{1:t-1}}, \overline{\mathbf{x_0}}, M) = \int p(\mathbf{x_t}|\mathbf{u_t}, \mathbf{x_{t-1}})bel(\mathbf{x_{t-1}})d\mathbf{x_{t-1}} \\ bel(\mathbf{x_0}) &= p(\mathbf{x_0}|\overline{\mathbf{x_0}}) = \delta(\mathbf{x_0} - \overline{\mathbf{x_0}}) \end{cases}$$
(3)

• Question 5: Which parts of (2) and (3) are responsible for prediction and update steps?

Now, assuming the observation noise and process noise are white Gaussians, it might seem that a standard Kalman filter can be utilized to come up with optimal estimates. However, as it will be pointed out in section 3.2.2, the measurement model in this case is not linear and thus, the standard Kalman filter will be useless for this problem. However, given the initial conditions(initial position: $\mu_0 = \bar{\mathbf{x}}_0$ and initial uncertainty: $\Sigma_0 = \bar{\Sigma}_0$), we can utilize an EKF to perform the prediction and update steps(Alg 1). Note that Alg 1 assumes time invariant models for measurement noise and process noise.

Algorithm 1 The Extended Kalman Filter algorithm

$$\begin{array}{ll} \bar{\boldsymbol{\mu}}_{t} &= \mathbf{g}(\mathbf{u}_{t}, \boldsymbol{\mu}_{t-1}) \\ \bar{\boldsymbol{\Sigma}}_{t} &= G_{t} \boldsymbol{\Sigma}_{t-1} G_{t}^{T} + R \end{array} \} \\ K_{t} &= \bar{\boldsymbol{\Sigma}}_{t} H_{t}^{T} (H_{t} \bar{\boldsymbol{\Sigma}}_{t} H_{t}^{T} + Q)^{-1} \\ \boldsymbol{\mu}_{t} &= \bar{\boldsymbol{\mu}}_{t} + K_{t} (\mathbf{z}_{t} - \mathbf{h}(\bar{\boldsymbol{\mu}}_{t})) \\ \boldsymbol{\Sigma}_{t} &= (I - K_{t} H_{t}) \bar{\boldsymbol{\Sigma}}_{t} \end{array} \}$$
 {Update}

3.2.1 Prediction

The prediction can be performed using the odometry information or control signals to the motors for example. Odometry information is usually computed

¹The units in the EKF Localization problem are meter and radians.

²Note that the definitions for Q and R are reversed in the EKF Localization problem. In the lectures, Q and R correspond to the modeled process and measurement noise covariance matrices respectively, while in the notation in the lab instructions (and also the course literature), Q and R refer to the modeled measurement and process noise covariance matrices.

using sensors like wheel Encoders. In a simple case, the odometry can be computed using (4):

$$\omega_t^R = \frac{2*\pi*E_t^R}{E_T \Delta t}
\omega_t^L = \frac{2*\pi*E_t^L}{E_T \Delta t}
\omega_t = \frac{\omega_t^R R_R - \omega_t^L R_L}{B}
v_t = \frac{\omega_t^R R_R + \omega_t^L R_L}{2}
u_t \approx \begin{bmatrix} v_t \Delta t \cos \mu_{t-1,\theta} \\ v_t \Delta t \sin \mu_{t-1,\theta} \\ \omega_t \Delta t \end{bmatrix}$$
(4)

where E_T is the number of encoder ticks per wheel revolution, E_t^R and E_t^L are the encoder ticks for the right and the left wheel in the t^{th} time step, B is the wheel base (the distance between the contact points of the wheels), R_R and R_L are the radius of the right and the left wheels and ω_t and v_t are the angular and translational velocities of the robot in the t^{th} time step.

Having computed the odometry information, the prediction process is performed using (5).

$$\mathbf{g}(\mathbf{u_t}, \boldsymbol{\mu_{t-1}}) = \boldsymbol{\mu_{t-1}} + \mathbf{u_t}$$

$$G_t = \begin{bmatrix} 1 & 0 & -\sin \mu_{t-1,\theta} v_t \Delta t \\ 0 & 1 & \cos \mu_{t-1,\theta} v_t \Delta_t \\ 0 & 0 & 1 \end{bmatrix}$$
(5)

where G_t is the Jacobian of \mathbf{g} and $\mu_{t-1,\theta}$ is the orientation of the robot in the last time step.

3.2.2 Measurement Model

Assuming a range-bearing measurement setting, the measurement model for the sensor is given by (6).

$$\mathbf{h}(\mathbf{x}_{t}, M, j) = \begin{bmatrix}
\sqrt{(M_{j,x} - x_{t,x})^{2} + (M_{j,y} - x_{t,y})^{2}} \\
atan2(M_{j,y} - x_{t,y}, M_{j,x} - x_{t,x}) - x_{t,\theta}
\end{bmatrix}
\mathbf{z}_{t,j} = \mathbf{h}(\mathbf{x}_{t}, M, j) + \delta_{t}
\hat{\mathbf{z}}_{t,j} = \mathbf{h}(\bar{\boldsymbol{\mu}}_{t}, M, j)
H(\bar{\boldsymbol{\mu}}_{t}, M, j) = \begin{bmatrix}
\frac{\bar{\mu}_{t,x} - M_{j,x}}{\hat{z}_{1,j}} & \frac{\bar{\mu}_{t,y} - M_{j,y}}{\hat{z}_{1,j}} & 0 \\
-\frac{\bar{\mu}_{t,y} - M_{j,y}}{(\hat{z}_{1,j})^{2}} & \frac{\bar{\mu}_{t,x} - M_{j,x}}{(\hat{z}_{1,j})^{2}} & -1
\end{bmatrix}$$
(6)

where j is the index of the landmark being matched to the measurement observation, \mathbf{h} is the observation function, the first component of $\hat{\mathbf{z}}_{t,j}$ is $\hat{z}_{1,j}$, which is also the distance between the feature j and the state $\bar{\boldsymbol{\mu}}_t$; H is the Jacobian of h corresponding to any observation evaluated at $\bar{\boldsymbol{\mu}}_t$; $\bar{\mu}_{t,x}$ refers to the x component of $\bar{\boldsymbol{\mu}}_t$.

Please keep in mind that indecies i and j have no great fixed meaning and in your implementation what seemed natural might not be the same as here or in other solutions. Don't get fixated on the letters but rather on the function.

3.2.3 Data Association

One of the most challenging problems in estimation such as EKF localization is the data association. If we know which landmark is being observed in each observation, then we have a known associations problem. In most of the situations, we usually do not know this information and thus, need to somehow associate each observation with a landmark(or classify it as an outlier). One of the most popular and simple approaches to the data association problem is the Maximum Likelihood data association.

我們不知道測到的landmark是哪一個,所以不能確定在哪,只能用maximum likelihood 的方法找出最有可能的landmark然後再去預測

3.2.4 Maximum Likelihood Data Association

In the maximum likelihood data association approach, observations are associated with landmarks separately. For each observation one computes the likelihood of making the observation while observing each landmark from the best estimate of the state before the update $\operatorname{process}(\bar{\mu}_t)$. Then, each observation is associated with the landmark which leads to the maximum likelihood. Alg 2 shows the detailed steps of associating \hat{c}_t^i with the i^{th} observation³.

Algorithm 2 Maximum Likelihood Data Association Algorithm for the i^{th} observation

Notice that ML data association requires that you normalize the Gaussian pdf.

• Question 6: In the maximum likelihood data association, we assumed that the measurements are independent of each other. Is this a valid assumption? Explain why.

³You need to keep in mind that there may be more than one measurement at time t (here we use i to denote them). $z_{t,j}$ refers to the j^{th} feature being associated with any of the measurements at the time t. When the inovation is computed the actual i^{th} measurement needs to be used. Also ν_t^{i,\hat{c}_t^i} represents the innovation of the i^{th} observation/measurement associated with \hat{c}_t^i in time t.

3.2.5 Outlier Detection

Sometimes, due to various reasons like unforeseen dynamics in system (e.g. an un-modeled moving object), sensor failure and unreasonable noise, we get measurements which are not reliable. We refer to these measurements as outliers. To detect outliers, one can define a threshold on the likelihood of the measurement (ψ_t^i) and label the measurement as an outlier if the threshold exceeds the maximum likelihood. Alternatively, it is possible to define a threshold on the Mahalanobis distance between the measurement (z_t^i) and the most likely association which is given by:

$$D_M = (\bar{\boldsymbol{\nu}}_t^i)^T (\bar{S}_{t,i})^{-1} (\bar{\boldsymbol{\nu}}_t^i) \tag{7}$$

The upside of this method is the fact that D_M follows the inverse chi square (X_n^{-2}) cumulative distribution with n degree of freedom and therefore, one can define a threshold for this method based on a probability. As (in our case with two measurement components) ν has two degrees of freedom, the threshold (λ_M) is given by

$$\lambda_M = X_2^{-2}(\delta_M) \tag{8}$$

• Question 7: What are the bounds for δ_M in (8)? How does the choice of δ_M affect the outlier rejection process? What value do you suggest for λ_M when we have reliable measurements all arising from features in our map, that is all our measurements come from features on our map? What about a scenario with unreliable measurements with many arising from so called clutter or spurious measurements?

3.2.6 Update

Having computed the associations and rejected the outliers, the update process can be done easily. The most simple type of update namely sequential update, performs one update for each observation z_t^i in the t^{th} time step(Alg 3).

Algorithm 3 sequential update Algorithm for the i^{th} observation

```
for all Observations i in z_t do ... {Compute the i^{th} association using \bar{\mu}_t} K_{t,i} = \bar{\Sigma}_t (\bar{H}_{t,i})^T (\bar{S}_{t,i})^{-1} \bar{\mu}_t = \bar{\mu}_t + K_{t,i}\bar{\nu}_t^i \bar{\Sigma}_t = (I - K_{t,i}\bar{H}_{t,i})\bar{\Sigma}_t end for \mu_t = \bar{\mu}_t \Sigma_t = \bar{\Sigma}_t
```

• Question 8: Can you think of some down-sides of the sequential update approach(Alg 3)? Hint: How does the first [noisy] measurements affect the intermediate results?

3.2.7 Batch Update

An alternative to the sequential update is the batch update algorithm. The batch update algorithm associates all observations with landmarks simultaneously and performs one update for all the observations in each time step. The sequential update can cause problems if you get outliers into the system and you perform data association for every new measurement processed. After an update with an outlier the estimate might be thrown off and the uncertainty incorrectly reduced (this is called inconsistency, ie that the uncertainty does not capture the true situation) which means that the other measurements may be incorrectly discarded as outliers. The order in which the measurements are processed is therefore important in the sequential update as in the sequential update, the association of the i^{th} measurement is computed using the estimates that are updated using the $i-1^{th}$ measurement. The batch update is less sensitive to outliers as more measurements processed at the same time adds some robustness. The downside of the batch update is instead the computational cost. Alg 4 shows the complete EKF localization problem with the batch update.

Algorithm 4 EKF Localization with Batch update for the i^{th} time step

```
\begin{array}{lll} \hat{\mathbf{z}}_{t,j} & = & \mathbf{h}(\bar{\boldsymbol{\mu}}_t, M, j) \\ H_{t,j} & = & H(\bar{\boldsymbol{\mu}}_t, M, j, \hat{\mathbf{z}}_{t,j}) \\ S_{t,j} & = & H_{t,j} \bar{\Sigma}_t (H_{t,j})^T + Q \\ \boldsymbol{\nu}_t^{i,j} & = & \mathbf{z_{t,i}} - \hat{\mathbf{z}_{t,j}} \\ D_t^{i,j} & = & (\boldsymbol{\nu}_t^{i,j})^T (S_{t,j})^{-1} \boldsymbol{\nu}_t^{i,j} \\ \psi_t^{i,j} & = & \det(2\pi S_{t,j})^{-\frac{1}{2}} exp[-\frac{1}{2}D_t^{i,j}] \\ \mathbf{end \ for} \\ \hat{c}_t^i & = & \arg\max \ \psi_t^{i,j} \\ \hat{o}_t^i & = & D^{i,c_t^i} \geq \lambda_M \\ \bar{\boldsymbol{\nu}}_t^i & = & \boldsymbol{\nu}_t^{i,c_t^i} \\ \bar{H}_{t,i} & = & H_{t,\hat{c}_t^i} \\ \mathbf{end \ for} \\ \{ \text{For inlier indices } 1, \dots, n \} \\ \bar{\boldsymbol{\nu}}_t & = & \left[ & (\bar{\boldsymbol{\nu}}_t^1)^T \ (\bar{\boldsymbol{\nu}}_t^2)^T \ \dots \ (\bar{\boldsymbol{\nu}}_t^n)^T \ \right]^T \\ \bar{H}_t & = & \left[ & (\bar{H}_{t,1})^T \ (\bar{\boldsymbol{\nu}}_{t,2})^T \ \dots \ (\bar{H}_{t,n})^T \ \right]^T \\ \bar{Q}_t & = & \begin{bmatrix} Q & 0 & 0 & 0 \\ 0 & Q & 0 & 0 \\ 0 & 0 & \dots & 0 \\ 0 & 0 & 0 & Q \end{bmatrix}_{(2n \times 2n)} \\ K_t & = & \bar{\Sigma}_t (\bar{H}_t)^T (\bar{H}_t \bar{\Sigma}_t (\bar{H}_t)^T + \bar{Q}_t)^{-1} \\ \boldsymbol{\mu}_t & = & \bar{\boldsymbol{\mu}}_t + K_t \bar{\boldsymbol{\nu}}_t \\ \Sigma_t & = & (I - K_t \bar{H}_t) \bar{\Sigma}_t \\ \end{array}
```

for all Observations i in z_t do for all Landmarks j in M do

- Question 9: How can you modify Alg 4 to avoid redundant re-computations?
- Question 10: What are the dimensions of $\bar{\nu}_t$ and \bar{H}_t in Alg 4? What were the corresponding dimensions in the sequential update algorithm? What does this tell you?

3.2.8 Instructions

Download el2320_lab1.zip. Start with the **runlocalization_track.m** which is the entrance function to your lab. This function reads two files determined by simoutfile and mapfile input arguments which contain information about sensor readings and the map of the environment respectively, runs a loop for all the sensor readings and calls the ekf_localize.m to perform one iteration of EKF localization on the readings and plots the estimation(red)/ground truth(green) and odometry(blue) information. The verbose parameter determines the verbose level(0= no visual output and bigger values correspond to more visual information). Read the code and get some idea about what is going on.

The **ekf_localize.m** is responsible to perform the EKF localization(surprise!). You do not need to change any parts of this file but you need to know what it is doing. You can use the USE_KNOWN_ASSOCIATIONS parameter for debugging purposes and USE_BATCH_UPDATE to determine if the filter should work in the batch mode or in the sequential mode.

The most common error in implementing these is to not realize that an angle error (innovation) of 2π is an error of 0. One should explicitly make sure that all angles (even intermeadiate results are) are between $-\pi$ and π . This is done by adding or subtracting 2π . (Technically this is not always important but it is easier to have an allways rule that true to reason if it matters.) May we suggest using this line of code to put an angle a in the range:

```
a = mod(a + pi, 2*pi)-pi;
```

Another common error H(:,k)... instead of H(:,:,k)=... or similar. Matlab has its rules and they take some getting used to.

You need to complete the following functions:

- 1. calculate_odometry.m: Use (4)
- 2. **predict.m**: Use Alg 1 and (5)
- 3. observation_model.m: Use (6)
- 4. jacobian_observation_model.m: Use (6)
- 5. associate.m: Use Alg 2
- 6. **update.m**: Use Alg 3
- 7. batch_associate.m: Use Alg 4
- 8. batch_update.m: Use Alg 4

9. init.m: Parameter setting/tuning. Depends on the problem at hand. See section 3.3.

The total number of lines of code you need to write to complete all mentioned functions is approximately 80 lines. When you are writing the codes, you can use the dimension of the input/outputs of functions (mentioned in each file in the heading comments) for debugging purposes. You can also use the matlab's help command to see the comments: e.g. "help predict".

Implement the functions in the order above and after each function is writen test it with the provided test functions found in 'test_cases_lab1_v0.2.zip'. These should be downloaded and unzipped. Then in matlab do

• path(path,'../test_cases_lab1_v0.2')

for example if you have to do

 \bullet ls ../test_cases_lab1_v0.2

to see the test files. This then allows you to call the test functions from the directory where your newly written functions are located. For example, after coding **calculate_odometry.m** call:

• test_case_calculate_odometry()

This will return 1 if there is no problem otherwise you must debug this function. The function test_cases_lab1() tests all the fuctions in turn and can be run as a final check.

3.3 Data sets

Fig 1 depicts the ground-truth and odometry information related to the data sets in this lab. An example command to run your code on the map map_o3.txt and sensor readings so_o3_ie.txt is:

```
runlocalization_track('so_o3_ie.txt', 'map_o3.txt', 1, 1, 1, 2);
```

The trajectory plot is color coded by red= estimated, green=true, and blue= odometry. Often the red is mostly covered by the green and thus not very visible.

Below you are asked tor run certain data sets under certain conditions. You need to document these runs in your report. You should save the plots (as .jpg or .png or best as part of the pdf but NOT .figs please) and the information that the program printed out. The printout should also be included in the report to the extent that they confirm that everything described and asked for worked.

1. map_o3.txt + so_o3_ie.txt: In this data set, the laser scanner has an accuracy of (1 cm,1 degree), the odometry information has an un-modeled noise of approximately 1 cm and 1 degree per time step. Decide about

reasonable noise models for process and observation noises and set your model in init.m. If you have done everything correctly, the resulting mean absolute error of your estimations should be less than 0.01 on all dimensions

- 2. map_pent_big_10.txt + so_pb_10_outlier.txt: In this data set, there are certain outliers that need to be detected(and rejected). The measurements have undergone a white Gaussian with the standard deviation of 0.2(m,rad). You can see how this noise affects the measurements by setting the verbose flag of runlocalization_track to 3. Try to find a reasonable value for process noise covariance matrix. If your outlier detection works correctly, the resulting mean absolute error of your estimations should be less than 0.06 on all dimensions.
- 3. map_pent_big_40.txt + so_pb_40_no.txt: This data set does not include any odometry information and therefore, we should compensate for it by considering a big standard deviation for the process noise. Model the measurement noise with a standard deviation of 0.1(m,rad), the process noise with a standard deviation of 1(m,m,rad) and set δ_M to 1 to disable the outlier detection. Run your algorithm on the data set using 1) the sequential update algorithm, 2) the batch update algorithm. If you have done everything right, you should be able to see a sensible difference between the results of the two algorithms with mean absolute error of the batch update algorithm being less than 0.1 on all dimensions.

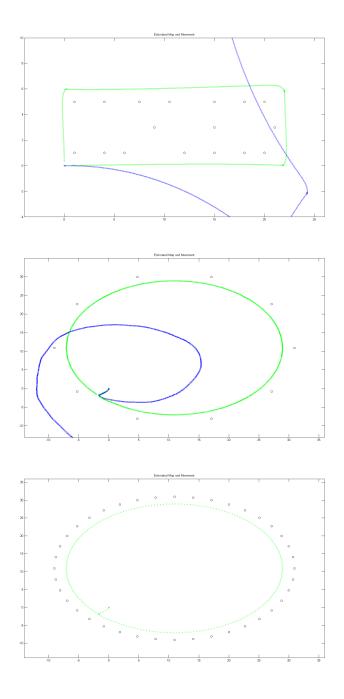


Figure 1: The data sets, top: so_o3_ie, middle: so_pb_10_outlier, bottom: so_pb_40_no