

Tasks require solving 3D Poisson problems and 3D eigensystem problems.

For some problems - notably those in which the potential applied at the gates is constant, or only depends on one coordinate, e.g.

\$\(\frac{8}{A,\delta}(\frac{1}{4},\delta) = \text{constant} \text{ or } \text{gangle}(\frac{1}{4},\delta) = \text{gangle}(\frac{1}{4}) \text{ one can reduce the dimensionality of the tasks to 2D or 1D computational work.

With some boundary conditions one can erecte solutions of the 3D problem by combining analytical solutions with 1D or 2D computational work.

Why? Plug in formally, keter out dp/2) B, (y) x(2) to varify eigen functions.

Assume periodic with domain site l. $\frac{1}{2} \frac{1}{1} \frac{1}{1$ 2 + + + = (2 (2) 2 (2)) (Roly Boly) (rr 1 x rr 1x) = only a function of Pe is only a function of 2, e.g. pe = pe(2). Computation of Pe(2)? Compute eigenvolves and eigenvectors of $\left[-\frac{t}{2}\frac{d}{dt}\left(\frac{1}{m_{r}(t)}\frac{d}{dt}\right) + \phi(t)\right]\alpha_{r}(t) = \lambda_{p}\alpha_{p}(t)$ pm/s, r(x)s unit L'novm In the limit as the periodic domain size / as then one gets. $\beta_{e}(z) = 2 \stackrel{?}{\nearrow} (z) \stackrel{?$ "density of states"

- or infinite > ID Senruedinger Poissur.
- (0) Determine of (2) so that

(1) Determine \$ (7), pe(2) so that

$$\frac{1}{47} \times (7) \stackrel{?}{=} \stackrel{?}{=} - \stackrel{?}{=} (7) \stackrel{?}{\neq} (7) = 0 \qquad \stackrel{?}{\neq} (7) = 0$$

$$-\frac{1}{2}\frac{d}{dz}\frac{d}{m(2)}\frac{d}{dz}\frac{d(2)}{r} = \lambda_{p}d(2) \qquad \chi(2_{A}) = \chi(2_{B}) = 0$$

I weight factor due to energy contributions of transverse

er gan functions.

ID tasks for the solution of a SD problem.

The dimension reduction is not obtained by averagina over the transverse direction - it's obtained by using an analytic solution in the transverse directions.

Similarly if 9 A, 9B only vary in one of the transverse divertions them one only needs to compute the electrostatics and eigensystems for 2D problems.

= 2D Schroedwar - Poisson

30? You typically focus on computational efficiency.