

$$\frac{\partial E}{\partial w_2} = \frac{\partial \sum (T_i - z_i)^2}{\partial w_2}$$

$$= 2(T - z) \frac{\partial z}{\partial w_2}$$

$$= 2(T - z) \frac{\partial \left(\sigma \left(w_2^T y + b_2\right)\right)}{\partial w_2}$$

$$= 2(T - z)\sigma' \left(w_2^T y + b_2\right) x$$

$$\frac{\partial E}{\partial b_2} = \frac{\partial \sum (T_i - z_i)^2}{\partial b_2}$$

$$= 2(T - z)\frac{\partial z}{\partial b_2}$$

$$= 2(T - z)\frac{\partial \left(\sigma\left(w_2^T y + b_2\right)\right)}{\partial w_2}$$

$$= 2(T - z)\sigma'\left(w_2^T y + b_2\right)$$

$$\frac{\partial E}{\partial w_1} = \frac{\partial \sum (T_i - z_i)^2}{\partial w_1}$$

$$= 2(T - z) \frac{\partial z}{\partial w_1}$$

$$= 2(T - z) \frac{\partial \left(\sigma \left(w_2^T y + b_2\right)\right)}{\partial w_1}$$

$$= 2(T - z)\sigma' \left(w_2^T y + b_2\right) w_2 \frac{\partial y}{\partial w_1}$$

$$= 2(T - z)\sigma' \left(w_2^T y + b_2\right) w_2 \frac{\partial \left(\sigma \left(w_1^T x + b_1\right)\right)}{\partial w_1}$$

$$= 2(T - z)\sigma' \left(w_2^T y + b_2\right) w_2 \sigma' \left(w_1^T x + b_1\right) x$$

$$\begin{split} \frac{\partial E}{\partial b_1} &= \frac{\partial \sum \left(T_i - z_i\right)^2}{\partial b_1} \\ &= 2(T - z) \frac{\partial z}{\partial b_1} \\ &= 2(T - z) \frac{\partial \left(\sigma\left(w_2^T y + b_2\right)\right)}{\partial b_1} \\ &= 2(T - z) \sigma'\left(w_2^T y + b_2\right) w_2 \frac{\partial y}{\partial b_1} \\ &= 2(T - z) \sigma'\left(w_2^T y + b_2\right) w_2 \frac{\partial \left(\sigma\left(w_1^T x + b_1\right)\right)}{\partial b_1} \\ &= 2(T - z) \sigma'\left(w_2^T y + b_2\right) w_2 \sigma'\left(w_1^T x + b_1\right) \end{split}$$