

Toward Understanding the Different Influences of Grain Boundaries on Ion Transport in Sulfide and Oxide Solid Electrolytes

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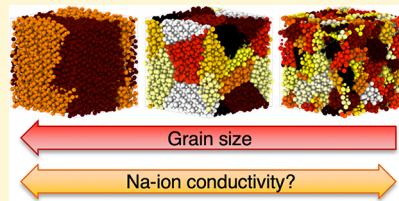
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S Supporting Information

ABSTRACT: Solid electrolytes provide a route to the development of all-solid-state batteries that can potentially surpass the safety and performance of conventional liquid electrolyte-based devices. Sulfide solid electrolytes have received particular attention as a result of their high ionic conductivities. One of the main reasons for such high ionic conductivity is the apparently reduced grain boundary resistance of sulfide solid electrolytes compared to their oxide counterparts, but this is not fully established. Using two model electrolyte systems, Na_3PS_4 and Na_3PO_4 , we apply a novel microscale simulation approach to analyze ionic transport in polycrystalline materials with various grain volumes. For Na_3PO_4 , high grain boundary resistance is found, with the Na-ion conductivity decreasing with decreasing grain volume. For Na_3PS_4 , the overall influence of grain boundaries (GBs) is significantly reduced compared to the oxide. Detailed analysis reveals a minimal change in the local structures and Na-ion conduction mechanism between bulk and polycrystalline Na_3PS_4 , whereas the change is far more substantial for Na_3PO_4 , with evidence of overcoordination of Na ions at the GBs. Our microscale approach helps to explain the fundamentally different influences of GBs on ion transport in phosphate and thiophosphate solid electrolytes.



Research into solid electrolytes for high-performance all-solid-state batteries has seen a dramatic rise in recent years.^{1–9} By replacing the flammable liquid electrolytes currently employed in commercial Li- and Na-ion batteries with solid electrolytes, the safety of the devices can be significantly enhanced,¹⁰ as well as providing an avenue to potentially improve their energy and power densities. A multitude of structural classes, including garnet, NASICON, LISICON, thio-LISICON, and perovskite structures, have been considered as solid electrolyte materials.^{6,11–17} Amongst these families of materials, Li- and Na-ion conducting thiophosphates, including $\text{Li}_{10}\text{MP}_2\text{S}_{12}$ ($\text{M} = \text{Ge}, \text{Si}$ or Sn), Li_3PS_4 , Na_3PS_4 , and $\text{Na}_{11}\text{Sn}_2\text{PS}_{12}$,^{6,18–24} have received significant interest because of their intrinsic soft mechanical nature and fast-ion conduction.^{3,25}

In oxide-based solid electrolytes, grain boundaries (GBs) are generally considered to inhibit ion migration and therefore represent a substantial hurdle for fast-ion conduction.^{14,16} For sulfide-based solid electrolytes, the influence of GBs on the overall ion transport is not as clear, with conflicting reports of GBs that either hinder ionic conduction^{20,26,27} or have no significant effect on ionic conduction.^{20,21,28,29} In any case, it is frequently observed that oxides show larger GB resistance than sulfides.^{30–32}

GBs are also important microstructural features that are linked to dendrite formation and penetration,^{33–35} and defect segregation.³⁶ Furthermore, there is growing interest in glass-

ceramic ion conductors, where the roles of nanocrystallite and GB effects are not clear.^{37,38} Although many reports discuss the influence of GB resistance on ionic conductivity, its origins and mechanisms are not entirely understood, particularly at the atomic scale.

Na_3PS_4 has recently experienced a resurgence in interest,^{21,39–47} primarily as a result of the work of Hayashi et al.,^{26,48} who synthesized a stable glass–ceramic cubic phase at room temperature with an unprecedented Na-ion conductivity of $2 \times 10^{-4} \text{ S cm}^{-1}$. Krauskopf et al.²¹ report that the influence of GBs appears to be small in these mechanically soft materials. Small GB resistances have also been reported for other well-known sulfide solid electrolytes, such as the argyrodite $\text{Li}_6\text{PS}_5\text{Br}$ ⁴⁹ and $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$.^{20,29,50} Conversely, earlier studies have speculated that the Na-ion conductivity of Na_3PS_4 is influenced by GBs.^{26,27} Although Na_3PO_4 has been studied for over 4 decades as a solid electrolyte,^{51–53} its GB resistance has not been fully characterized.

In this study, we elucidate the role of GBs in the transport of ions in solid electrolytes by proposing a novel microscale strategy based on large-scale molecular dynamics (MD) simulations. We apply this method to analyze two well-

Received: May 7, 2019

Revised: June 26, 2019

Published: June 26, 2019

known polycrystalline model systems, Na_3PS_4 and Na_3PO_4 , with various grain volumes, in order to elucidate the different contributions of GB resistance in sulfide and oxide solid electrolytes. Our findings show high GB resistance for Na_3PO_4 , but for Na_3PS_4 , the relationship between ion transport and grain volume is less significant. Structural and mechanistic results reveal pronounced differences between the local environments of the ions at the GBs of Na_3PO_4 , whereas for Na_3PS_4 , these differences are minimized. This novel microscale approach illustrates the fundamentally different influences of GBs on ion transport at the atomic scale in sulfide and oxide solid electrolytes.

■ RESULTS AND DISCUSSION

Structures and Na-Ion Conductivity of Bulk Na_3PS_4 and Na_3PO_4 . Two crystal polymorphs are known for Na_3PS_4 : a tetragonal phase with space group $P4_2_{1}c$ and lattice parameters of $a = 6.952 \text{ \AA}$ and $c = 7.076 \text{ \AA}$ ⁵⁴ and a cubic phase with space group $I\bar{4}3m$ and a lattice parameter of $a = 6.989 \text{ \AA}$.²¹ These polymorphs are very similar, with minor differences in the orientation of the PS_4 tetrahedra and the corresponding positions of the Na ions. Furthermore, they also exhibit similar Na-ion conductivities,^{21,39} although earlier studies have reported higher conductivities for the cubic phase.^{26,27} Similarly, a tetragonal phase with space group $P4_2_{1}c$ and lattice parameters of $a = 10.811 \text{ \AA}$ and $c = 6.818 \text{ \AA}$,⁵⁵ and a cubic phase with space group $Fm\bar{3}m$ and a lattice parameter of $a = 7.544 \text{ \AA}$ ⁵⁵ also exist for Na_3PO_4 . The tetragonal–cubic transition for Na_3PO_4 results in a sudden increase in Na-ion conductivity.⁵⁵

In this work, we focus on the cubic polymorphs as the crystallographic similarities between cubic Na_3PS_4 and Na_3PO_4 allow us to examine key GB effects. The calculated lattice parameters for cubic Na_3PS_4 and Na_3PO_4 are 6.992 and 7.524 \AA , respectively, in excellent agreement with experimental data.^{20,55} The agreement between the experimental and calculated bond distances is also excellent, as shown in the Supporting Information (Table S2).

Figure 1 shows the Arrhenius plots for the calculated Na-ion conductivity for bulk Na_3PS_4 and Na_3PO_4 . Mean squared

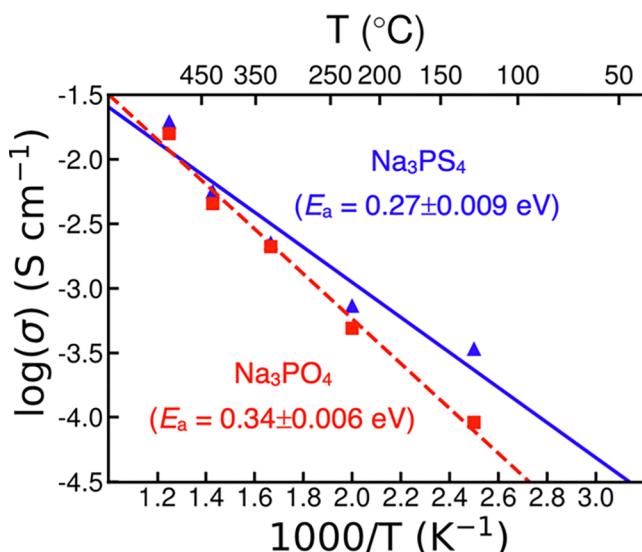


Figure 1. Na-ion conductivities (σ) and activation energies (E_a) for bulk Na_3PS_4 and Na_3PO_4 .

displacement (MSD) plots for Na-ion diffusion in bulk Na_3PS_4 and Na_3PO_4 are given in Figure S1. We find that the Na-ion conductivity is higher in the sulfide than the oxide, with calculated bulk conductivities at 400 K of 3.42×10^{-4} and $9.18 \times 10^{-5} \text{ S cm}^{-1}$ for Na_3PS_4 and Na_3PO_4 , respectively.

Our conductivity values are in good agreement with the impedance measurements of Krauskopf et al.²¹ for tetragonal Na_3PS_4 obtained from a high-temperature solid-state synthetic route ($\sim 8 \times 10^{-5} \text{ S cm}^{-1}$ at 333 K) and Yu et al.²⁷ for cubic and tetragonal Na_3PS_4 ($\sim 1 \times 10^{-4}$ and $\sim 1 \times 10^{-5} \text{ S cm}^{-1}$ at 300 K, respectively). The calculated activation energy of 0.27 eV for Na_3PS_4 agrees well with the value of 0.28 eV derived from impedance measurements.²⁶

A conductivity of $2.1 \times 10^{-3} \text{ S cm}^{-1}$ was found for Na_3PO_4 at 600 K. This is in agreement with the value of $\sim 1 \times 10^{-3} \text{ S cm}^{-1}$ obtained from impedance values at the same temperature.^{52,56} Our calculated activation energy of 0.34 eV is slightly lower than the experimental value of 0.42 eV.^{52,56}

Na-Ion Conductivity of Polycrystalline Na_3PS_4 and Na_3PO_4 . To assess the impact of GBs on the Na-ion conductivity of the model Na_3PS_4 and Na_3PO_4 systems, we investigated polycrystalline systems with different grain volumes, as illustrated in Figure 2. The grain volumes are

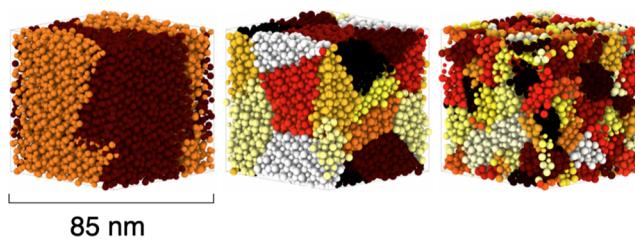


Figure 2. Polycrystals of Na_3PS_4 containing (a) 2, (b) 10, and (c) 100 grains (equivalent to grain volumes of 108, 21.6, and 2.16 nm^3 , respectively). Each color represents a unique grain.

calculated by simply dividing the total volume of the polycrystal by the number of grains. Figure 3a,b shows the Arrhenius plots for the calculated Na-ion conductivity for bulk and polycrystalline Na_3PS_4 and Na_3PO_4 , respectively. Example MSD plots for Na-ion diffusion in polycrystalline Na_3PS_4 and Na_3PO_4 are given in Figure S2.

The Arrhenius plots for Na_3PS_4 in Figure 3a reveal two important findings. First, the conductivities for the polycrystalline systems are higher than for bulk Na_3PS_4 . The highest conductivities are found for polycrystals with the smallest grain volume of 2.16 nm^3 , with values of 6.15×10^{-4} and $3.38 \times 10^{-2} \text{ S cm}^{-1}$ at 400 and 800 K, respectively, compared to the bulk conductivities of 3.42×10^{-4} and $1.97 \times 10^{-2} \text{ S cm}^{-1}$ at 400 and 800 K, respectively. Furthermore, when the conductivities of the polycrystals of Na_3PS_4 are extrapolated to room temperature, they are very similar to the bulk conductivity. These results suggest that GB resistance in Na_3PS_4 is indeed small, as proposed in recent impedance experiments of this mechanically soft material.²¹

Second, the calculated activation energies are all similar for the polycrystals of Na_3PS_4 (0.28–0.30 eV) compared to the bulk value of 0.27 eV, which suggests that the overall influence of GBs on Na-ion transport in this material is minimal.

In contrast, Figure 3b shows a reduction in conductivity and a small increase in activation energy for all the Na_3PO_4 polycrystalline systems compared to the bulk. The lowest

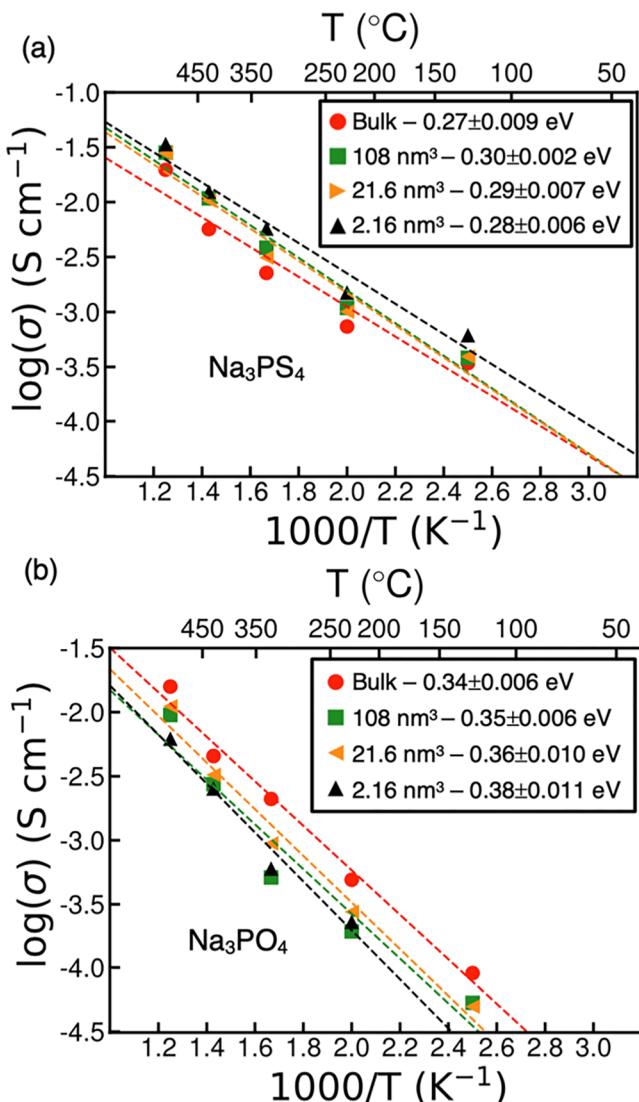


Figure 3. Na-ion conductivities (σ) and activation energies (E_a) for bulk and polycrystalline (for three different grain volumes of 108, 21.6, and 2.16 nm^3) (a) Na_3PS_4 and (b) Na_3PO_4 . Conductivity data for all five grain volumes are given in Figure S3.

conductivities are obtained for the systems with the smallest grain volume, reaching 2.24×10^{-5} and $6.20 \times 10^{-3} \text{ S cm}^{-1}$ at 400 and 800 K, respectively. These values are significantly lower than the bulk conductivities of 9.19×10^{-5} and $1.58 \times 10^{-2} \text{ S cm}^{-1}$ at 400 and 800 K, respectively. Furthermore, there is a relationship between the activation energy and the grain volume, with a rising trend in activation energy from bulk Na_3PO_4 to the Na_3PO_4 polycrystal with the smallest grain volume of 2.16 nm^3 . Hence, the results from Figure 3b provide evidence of GB resistance in Na_3PO_4 . Although we are not aware of any experimental characterization of GB resistance specifically in Na_3PO_4 , significant GB resistance for the majority of oxide-based Li- and Na-ion fast conductors is well documented.^{5,16,30,57–59}

We have previously demonstrated the important role of GB resistance in the fast-ion conductor, Li_3OCl , which allowed us to provide accurate estimates of ionic conductivities and activation barriers in agreement with experimental data.¹⁶ This earlier work¹⁶ and other studies¹² have also shown that it is

important to bear in mind that ionic diffusion at GBs can be different in different structural phases of solid electrolytes.

Figure 4 shows the activation energies for bulk and polycrystalline Na_3PS_4 and Na_3PO_4 as a function of grain

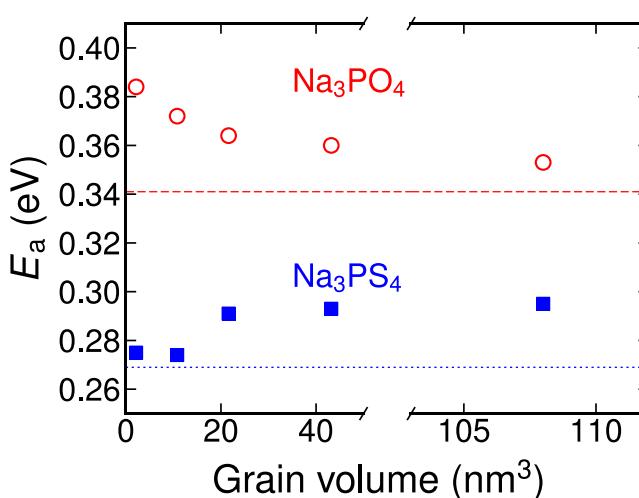


Figure 4. Activation energies (E_a) for bulk (dashed lines) and polycrystalline Na_3PS_4 (squares) and Na_3PO_4 (circles) as a function of grain volume.

volume. The activation energies decrease for Na_3PO_4 , but increase for Na_3PS_4 , as the grain volume becomes larger. These findings highlight the opposing influences of GBs on Na-ion transport in sulfide and oxide solid electrolytes.

In order to confirm the trends between conductivity, activation energy, and grain volume discussed above, we also carried out a number of simulations with much larger $125 \times 125 \times 125 \text{ \AA}^3$ cells containing 80 000–120 000 ions, thereby increasing the grain volumes by almost an order of magnitude. Arrhenius plots for the conductivities obtained from these calculations with grain volumes of 976.56, 195.31, and 19.53 nm^3 (equivalent to 2, 10, and 100 grains, respectively) at 400, 600, and 800 K are given in Figure S4. From these results, it is clear that the same trends are observed as in Figures 3 and 4, namely, decreasing conductivity and increasing activation energy with decreasing grain volume for the oxide and increasing conductivity with decreasing grain volume for the sulfide.

In summary, our results show two distinct and opposing behaviors for the effect of GBs on Na-ion conduction in two model sulfide and oxide solid electrolytes.

Local Structural Insights into GB Effects. The analysis of ion transport presented here shows the distinctly different influences of GBs on ion conduction in Na_3PS_4 and Na_3PO_4 ; however, the underlying reasons for these differences are not fully understood. To probe the local structural factors, we analyze the radial distribution functions (RDFs) for Na–Na, Na–P, and Na–S/O in the bulk materials and the polycrystals with the largest (108 nm^3) and smallest (2.16 nm^3) grain volumes. The RDFs for both Na_3PS_4 and Na_3PO_4 at 400 K are displayed in Figure 5.

First considering Na_3PS_4 , the bulk and polycrystal systems show a sharp primary peak at $\sim 3.3 \text{ \AA}$ in their Na–Na RDFs. For the polycrystals, these peaks are higher, marginally broadened, and their distance reduced by $\sim 0.1 \text{ \AA}$, compared to the bulk. These features suggest that the GBs in Na_3PS_4 allow the Na ions to be closer to each other. It is noteworthy

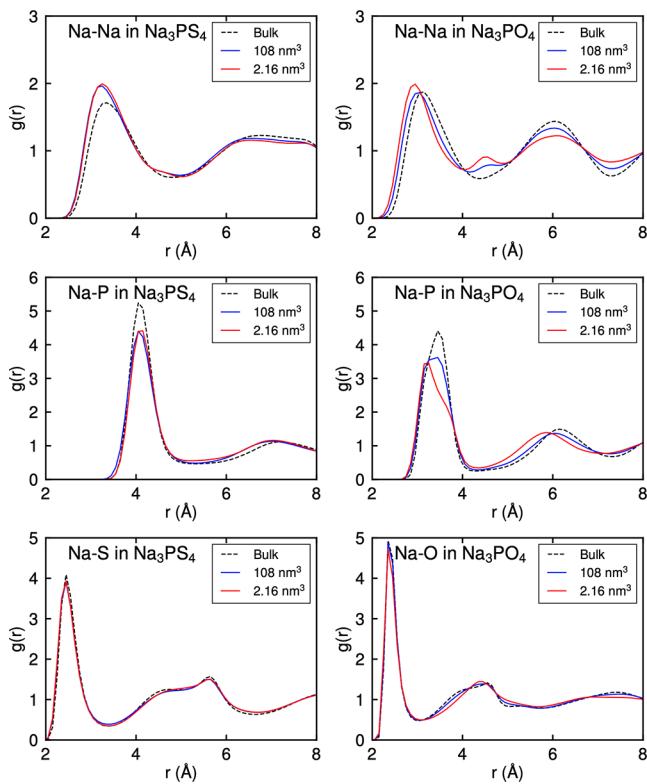


Figure 5. Na–Na, Na–P, and Na–S/O RDFs for bulk and polycrystalline (grain volumes of 108 and 2.16 nm^3) Na_3PS_4 (left) and Na_3PO_4 (right) at 400 K.

that the Na–Na RDFs for the Na_3PS_4 polycrystals with the largest and smallest grain volumes are almost identical, suggesting that the difference between the conductivities of these polycrystals is not a primary result of the Na distributions. This is in agreement with the ab initio MD results of de Clerk and Wagemaker.³⁹ The Na–P RDFs for the bulk and polycrystals of Na_3PS_4 show comparable behavior. The Na–S RDFs for Na_3PS_4 are almost identical for each system, with similar trends to those previously observed for RDFs of successful Na-ion hopping.³⁹

Overall, the RDFs for bulk and polycrystalline Na_3PS_4 are strikingly congruent, which strongly suggests that there is no substantial change in the conduction mechanism as a result of the GBs. This is further corroborated by the fact that the RDFs of the polycrystals are almost indistinguishable. These results again advocate that it is the point defect concentrations and compositional changes that are responsible for the small changes in Na-ion transport characteristics in Na_3PS_4 and not the GBs themselves.

We now turn our attention to Na_3PO_4 . The bulk RDFs are in excellent agreement with previous MD studies.⁵³ In contrast to Na_3PS_4 , the Na–Na RDFs for bulk and polycrystalline Na_3PO_4 show very different behavior. The Na–Na distances of the primary peaks are 3.15 Å for the bulk and 3.05 and 2.95 Å for the polycrystals with grain volumes of 108 and 2.16 nm^3 , respectively.

For the Na–P RDFs in Na_3PO_4 , the main peaks at 3.5 Å undergo substantial changes when moving from the bulk system to the polycrystals. The peaks become smaller and increasingly asymmetrical, particularly for the polycrystal with the smallest grain volume of 2.16 nm^3 where a second peak on the right shoulder of the first peak becomes visible. Similar

peak deformation has been observed for Na–P RDFs in Na_3PS_4 , where de Clerk and Wagemaker³⁹ associated the formation of two peaks at $\sim 3\text{--}5 \text{ \AA}$ with unsuccessful Na-ion migration, as it results in a contraction of the free volume around the Na ions. Given that such behavior is indicative of unsuccessful hops, these results help to explain the reduced Na-ion conductivity that we observed as a function of grain volume for Na_3PO_4 .

As with the Na–S RDFs for Na_3PS_4 , the Na–O RDFs for Na_3PO_4 are all similar. Our structural analysis shows that the distributions of Na–S and Na–O distances are not crucial factors in determining the changes in conductivity when comparing bulk and polycrystalline systems.

Analysis of the integrated RDFs provides useful information on the local coordination of a species. The integration of the Na–Na, Na–P, and Na–S/Na–O RDFs for bulk and polycrystalline Na_3PS_4 and Na_3PO_4 at 400 K are given in Figure 6.

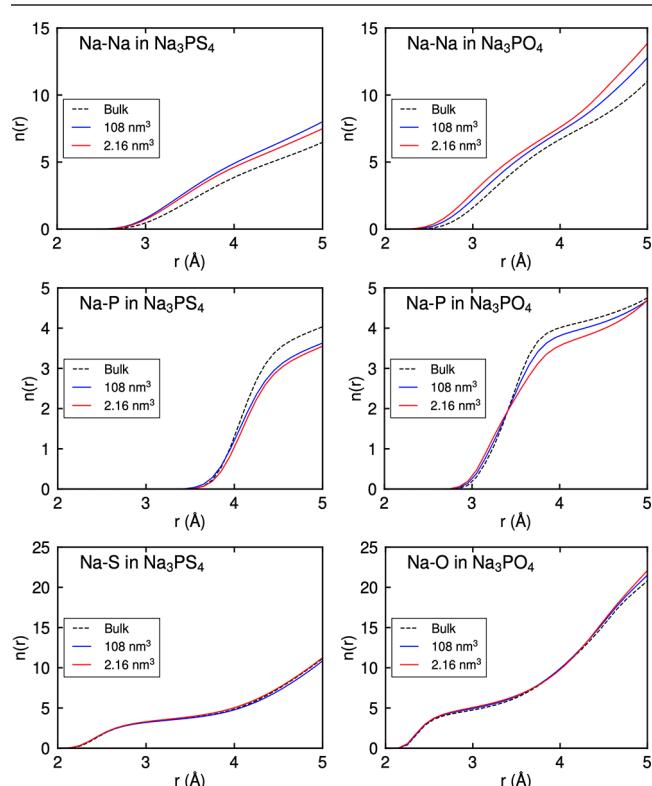


Figure 6. Integration of Na–Na, Na–P, and Na–S/O RDFs for bulk and polycrystalline (grain volumes of 108 and 2.16 nm^3) Na_3PS_4 (left) and Na_3PO_4 (right) at 400 K.

The main feature revealed from the data in Figure 6 is the difference in the coordination of Na ions to neighboring Na ions between the polycrystals of Na_3PS_4 and Na_3PO_4 . For Na_3PS_4 , the coordination number of Na ions to other Na ions is highest in the polycrystal with the largest grain volume of 108 nm^3 , whereas for Na_3PO_4 , the polycrystal with the smallest grain volume of 2.16 nm^3 has the highest coordination number. This fundamental difference indicates that Na ions effectively become under-coordinated with decreasing grain volume in Na_3PS_4 , thereby providing potential for higher Na-ion diffusion in these polycrystals.

In contrast, the opposite is true for Na_3PO_4 , where the Na ions become over-coordinated with decreasing grain volume.

These two opposing effects may help to explain the difference between the GB behavior of sulfide and oxide solid electrolytes.

In summary, this local structural analysis has clearly shown different behavior for the Na_3PS_4 and Na_3PO_4 electrolytes. For the sulfide, the differences between the RDFs of the bulk and polycrystalline systems are small, suggesting that the structural changes induced by the GBs do not have a dramatic effect on Na-ion transport. Conversely, for the oxide, the differences are much more pronounced. The GBs have a significant impact on the short- and long-range atomic distributions, suggesting a fundamental change in the Na-ion conduction mechanism of Na_3PO_4 . These results help to explain the reasons for the impact of GBs on conductivity in sulfides being weaker than in oxides.

Na-Ion Conduction Mechanisms. To clarify the underlying atomistic conduction mechanisms in these two materials and how the GBs affect these mechanisms, we produce density plots of the accumulated Na-ion trajectories over the simulated timescale, which are a powerful means of visualizing the migration pathways and all the positions in the lattice that are traversed.

Figure 7 shows the Na-ion diffusion density plots for selected regions of bulk Na_3PS_4 and Na_3PO_4 at 400 K. As

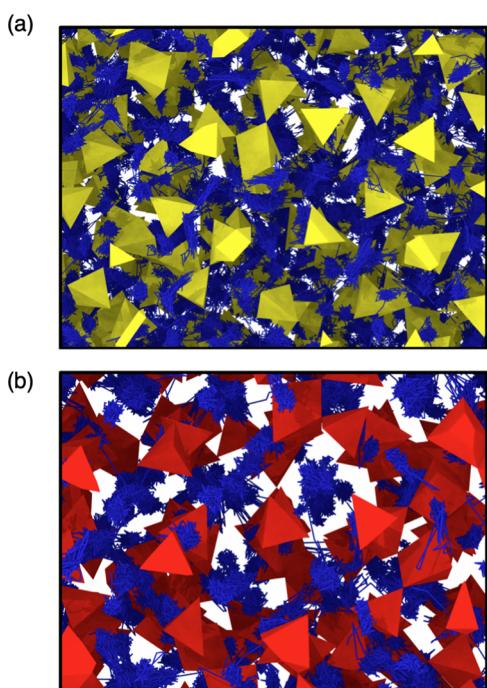


Figure 7. Diffusion density plots of Na ions (blue lines) overlaid on PS_4 (yellow) and PO_4 (red) tetrahedra in bulk (a) Na_3PS_4 and (b) Na_3PO_4 , respectively, at 400 K.

expected, significant long-range three-dimensional Na-ion diffusion is observed in both systems. A greater density of Na-ion diffusion pathways is observed for Na_3PS_4 compared to Na_3PO_4 , in agreement with the faster Na-ion diffusion of the sulfide system. Both materials exhibit the same vacancy diffusion mechanism, where the Na ions vibrate around their own sites before migration to a nearby vacant site. Vacancy migration has been proposed previously for both Na_3PS_4 ^{39,44,60} and Na_3PO_4 .^{51,53,55}

It has been proposed that Na-ion diffusion in Na_3PO_4 can occur through the coupling of Na ions with the reorientation of their neighboring phosphate anions, that is, the so-called “paddle-wheel” effect.⁶¹ In agreement with earlier MD studies,^{39,53,62} we find no strong evidence of this effect for either Na_3PO_4 or Na_3PS_4 . As shown by the images in Figure S5, we do not observe any significant rotation of the PS_4 and PO_4 tetrahedra. Furthermore, correlated motions have been excluded for Na_3PO_4 on the basis of high-resolution neutron backscattering studies.⁶³

We now turn our attention to Na-ion diffusion in the polycrystals. Figures 8 and 9 show the diffusion density plots of

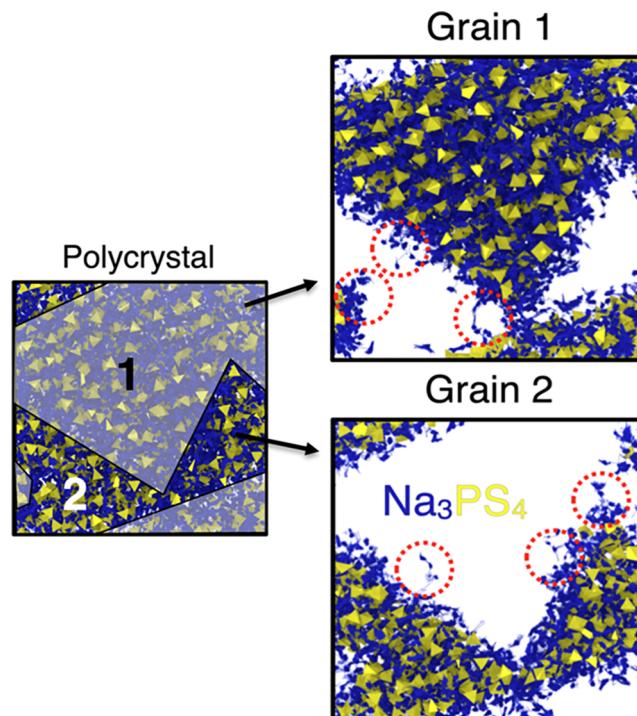


Figure 8. Diffusion density plots of Na ions overlaid on PS_4 tetrahedra in Na_3PS_4 polycrystals with two grains at 400 K. Red circles highlight areas of significant intergranular diffusion.

Na ions in Na_3PS_4 and Na_3PO_4 polycrystals, respectively, with a grain volume of 108 nm^3 (two grains) at 400 K. Both grains (labeled 1 and 2) of the polycrystals are shown in separate images in order to better visualize Na-ion diffusion at the GBs. Significant areas of intergranular diffusion (diffusion between different grains) are highlighted for Na_3PS_4 . Figure 8 shows a higher level of Na-ion diffusion at the GBs for Na_3PS_4 compared to Na_3PO_4 (Figure 9), as can be observed by the dense blue areas located at the edges of the grains of Na_3PS_4 .

In Na_3PO_4 , the majority of Na-ion diffusion takes place within the grains, with very few Na ions hopping across the GBs from one grain to another. In contrast, intergranular diffusion is far more prevalent in Na_3PS_4 , as highlighted by the red circles in Figure 8. These results strongly suggest that GBs in Na_3PS_4 do not restrict ion transport to the same extent as those in Na_3PO_4 . Such findings are in complete agreement with our conductivity and structural analysis.

On this basis, it can be proposed that the undercoordination of conducting ions at the GBs of mechanically soft sulfides can be beneficial for conductivity, whereas for oxides, the overcoordination is detrimental to ion transport.

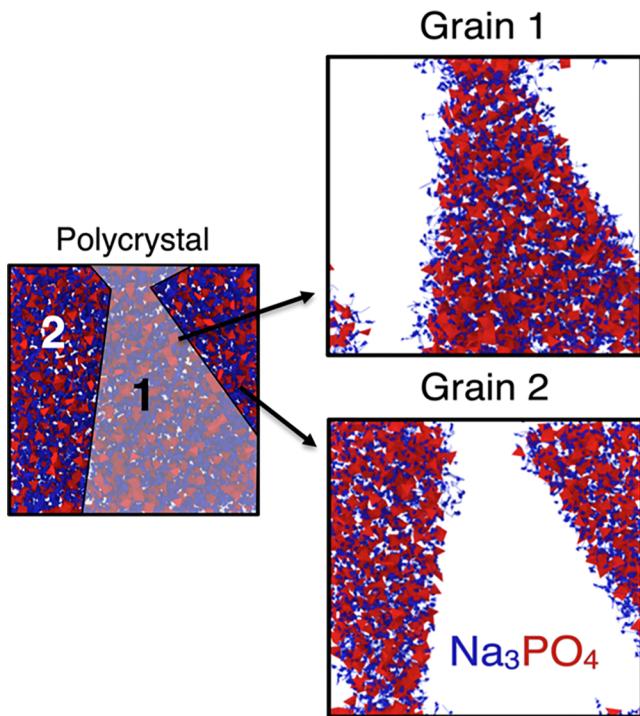


Figure 9. Diffusion density plots of Na ions overlaid on PO_4 tetrahedra in Na_3PO_4 polycrystals with two grains at 400 K.

These results help to explain the opposing effects of GBs in solid electrolytes reported in the literature.^{16,21,30,57}

CONCLUSIONS

Grain boundary resistance is one of the key challenges that must be overcome for the successful utilization of all-solid-state batteries. It is generally accepted that grain boundary resistance is higher in oxides than sulfides; however, the underlying reasons for this are not fully understood. In this work, we have used a novel microscale simulation approach to identify and explain the fundamentally different influences of GBs on ion transport in two model solid electrolytes, Na_3PS_4 and Na_3PO_4 , with the following key results:

- High grain boundary resistance is found for Na_3PO_4 , in which the Na-ion conductivity decreases with decreasing grain volume.
- In contrast, the results for Na-ion transport in polycrystalline Na_3PS_4 suggest very small or insignificant grain boundary resistance, in agreement with recent experimental findings. Indeed, visualization of the Na-ion conduction pathways shows significant intergranular conduction in Na_3PS_4 .
- The local structures in bulk and polycrystalline Na_3PS_4 are very similar, which suggests that the structural changes induced by the GBs do not have a dramatic effect on Na-ion transport. In contrast, the local structure of Na_3PO_4 exhibits distinct changes, including over-coordination around Na ions at the GBs, indicative of a fundamental change in the ion conduction mechanism.

Our results help to clarify the opposing behavior of GBs in phosphate-and thiophosphate-based solid electrolytes and their impact on ion conduction. Given the importance of interfaces in all-solid-state batteries, we propose that the computational

microscale approach used in this work can be widely applied to other Na- and Li-ion solid electrolyte materials.

METHODS

The MD simulations are based on established techniques and have been widely used to determine the ion transport properties in a wide variety of Li- and Na-ion battery materials.^{16,62,64–68} A new potential model was developed for cubic Na_3PS_4 (Table S1) using the empirical derivation procedure of the General Utility Lattice Program (GULP).⁶⁹ For Na_3PO_4 , we used the proven potential model of Tilocca et al.⁷⁰ (Table S2) that was developed for MD calculations of phosphosilicate glasses, augmented here with an Na–Na interatomic potential from Harding.⁷¹ Formal valence charges for all ions and a potential cut-off of 12 Å were used. A full description of the potential models is available in the Supporting Information (Tables S1–S4).

The MD calculations were performed using the large-scale atomic/molecular massively parallel simulator (LAMMPS).⁷² Long MD runs of 10 ns were completed using a time step of 1 fs and supercells of 9000–13 000 ions for both the bulk (single crystal) and polycrystal systems. Larger polycrystals of 80 000–120 000 ions were also tested in order to verify the trends determined for the smaller polycrystalline cells. Simulations were carried out for a temperature range of 400–800 K at intervals of 100 K using the NVT ensemble with a Nose–Hoover thermostat,⁷³ with initial equilibration performed using the NPT ensemble for \sim 2 ns. We note that our calculations were carried out at elevated temperatures to improve computational efficiency.

Disorder was introduced to the bulk systems to promote long-range diffusion using Na vacancies (compensated by S or O vacancies) that were randomly distributed throughout the supercells at a concentration of 10%. A lower Na vacancy concentration of 3% was also tested (see Figure S6), with only a minor reduction in Na-ion conductivity below 800 K and a minor increase in activation energy observed compared to the 10% Na vacancy bulk systems. Such disorder was not introduced into the polycrystals as point defects were already present as a result of the GBs. The average stoichiometries of the polycrystals are given in Table S5. Self-diffusion data for Na were obtained from an MSD analysis according to

$$\langle r_i^2(t) \rangle = 6D_{\text{Na}}t \quad (1)$$

where $\langle r_i^2(t) \rangle$ is the MSD, D_{Na} is the diffusion coefficient for Na, and t is time. The diffusion data were then converted to conductivities (σ) using the Nernst–Einstein relationship

$$\frac{\sigma}{D_{\text{Na}}} = H_{\text{R}} \frac{nq^2}{kT}$$

(2) where n is the number of Na ions per unit volume, q is the electron charge, k is the Boltzmann constant, T is the temperature, and H_{R} is the Haven ratio, which is set to 1 in our calculations.

The polycrystal models used in this study were constructed using Voronoi tessellations, as employed in the Atomsk program,⁷⁴ in which nodes are introduced at given positions inside the simulation box that are then linked with their neighboring nodes. The normals to these links are then found and these define the contours of the randomly orientated grains, that is, the GBs in this study. Unit cells are then placed at the nodes and are expanded in three dimensions. The final polycrystal is then obtained after the unit cells have been expanded and cut into the respective grains. The unit cell structures and example polycrystals for cubic Na_3PS_4 and Na_3PO_4 are given in Figure 10. Further details regarding the setup of the polycrystals for the MD simulations are given in the Supporting Information.

Cubic polycrystals with dimensions of $60 \times 60 \times 60 \text{ \AA}^3$ were used. Polycrystals with 2, 5, 10, 20, and 100 grains (equivalent to grain volumes of 108, 43.2, 21.6, 10.8, and 2.16 nm^3 , respectively) were used to investigate the effects of GBs on Na-ion transport in these systems. Example polycrystals with 2, 10, and 100 grains for Na_3PS_4 are illustrated in Figure 2. MD simulations were carried out on three different random polycrystals for each grain volume and the data were

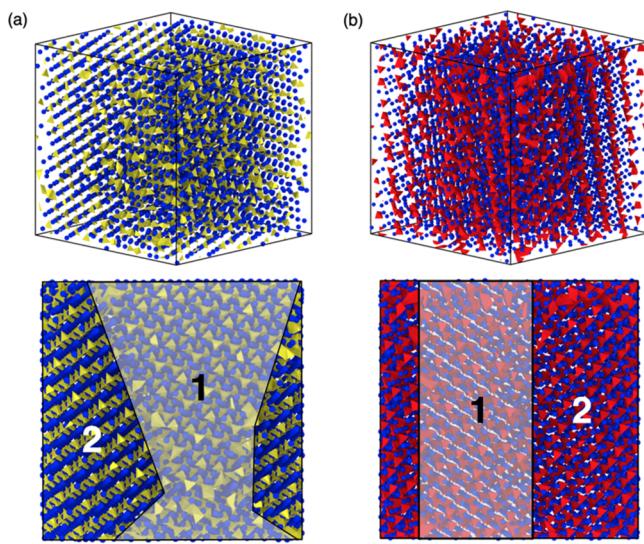


Figure 10. Example polycrystals containing two grains (grain volume of 108 nm^3) for (a) Na_3PS_4 and (b) Na_3PO_4 . The top images show the three-dimensional polycrystals, whereas the bottom images indicate the approximate positions of the two grains. Na ions and PS_4 and PO_4 tetrahedra are given in blue, yellow, and red, respectively.

averaged. The variance in conductivity between the random three polycrystals for each grain volume was minimal, as detailed in Tables S6 and S7, which show the activation energy of each polycrystal for Na_3PS_4 and Na_3PO_4 , respectively.

■ ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: [10.1021/acs.chemmater.9b01794](https://doi.org/10.1021/acs.chemmater.9b01794).

Potential model for Na_3PS_4 ; potential model for Na_3PO_4 ; MD simulation procedure for polycrystals; activation energies; Na-ion diffusion and conductivity; PS_4 and PO_4 orientations; and influence of Na vacancy concentration ([PDF](#))

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Notes

The authors declare no competing financial interest.

■ ACKNOWLEDGMENTS

The authors gratefully acknowledge the EPSRC Programme Grant “Enabling next generation lithium batteries” (EP/M009521/1) and the MCC/Archer consortium (EP/L000202/1).

■ REFERENCES

- Bachman, J. C.; Muy, S.; Grimaud, A.; Chang, H.-H.; Pour, N.; Lux, S. F.; Paschos, O.; Maglia, F.; Lupart, S.; Lamp, P.; et al. Inorganic Solid-State Electrolytes for Lithium Batteries: Mechanisms and Properties Governing Ion Conduction. *Chem. Rev.* **2016**, *116*, 140–162.
- Tikekar, M. D.; Choudhury, S.; Tu, Z.; Archer, L. A. Design Principles for Electrolytes and Interfaces for Stable Lithium-Metal Batteries. *Nat. Energy* **2016**, *1*, 16114.
- Janek, J.; Zeier, W. G. A Solid Future for Battery Development. *Nat. Energy* **2016**, *1*, 16141.
- Manthiram, A.; Yu, X.; Wang, S. Lithium Battery Chemistries Enabled by Solid-State Electrolytes. *Nat. Rev. Mater.* **2017**, *2*, 16103.
- Kim, J.-J.; Yoon, K.; Park, I.; Kang, K. Progress in the Development of Sodium-Ion Solid Electrolytes. *Small Methods* **2017**, *1*, 1700219.
- Kamaya, N.; Homma, K.; Yamakawa, Y.; Hirayama, M.; Kanno, R.; Yonemura, M.; Kamiyama, T.; Kato, Y.; Hama, S.; Kawamoto, K.; et al. A Lithium Superionic Conductor. *Nat. Mater.* **2011**, *10*, 682–686.
- Wang, Y.; Richards, W. D.; Ong, S. P.; Miara, L. J.; Kim, J. C.; Mo, Y.; Ceder, G. Design Principles for Solid-State Lithium Superionic Conductors. *Nat. Mater.* **2015**, *14*, 1026–1031.
- Gao, Z.; Huabin, S.; Lin, F.; Fangliang, Y.; Yi, Z.; Wei, L.; Yunhui, H. Promises, Challenges, and Recent Progress of Inorganic Solid-State Electrolytes for All-Solid-State Lithium Batteries. *Adv. Mater.* **2018**, *30*, 1705702.
- Zhao, C.; Lilu, L.; Xinguo, Q.; Yaxiang, L.; Feixiang, W.; Junmei, Z.; Yan, Y.; Yong-Sheng, H.; Liquan, C. Solid-State Sodium Batteries. *Adv. Energy Mater.* **2018**, *8*, 1703012.
- Inoue, T.; Mukai, K. Are All-Solid-State Lithium-Ion Batteries Really Safe?—Verification by Differential Scanning Calorimetry with an All-Inclusive Microcell. *ACS Appl. Mater. Interfaces* **2017**, *9*, 1507–1515.
- Goodenough, J. B.; Hong, H. Y.-P.; Kafalas, J. A. Fast Na^+ -Ion Transport in Skeleton Structures. *Mater. Res. Bull.* **1976**, *11*, 203–220.
- Bruce, P. G.; West, A. R. The A-C Conductivity of Polycrystalline LISICON, $\text{Li}_{2+2x}\text{Zn}_{1-x}\text{GeO}_4$, and a Model for Intergranular Constriction Resistances. *J. Electrochem. Soc.* **1983**, *130*, 662–669.
- Kanno, R.; Hata, T.; Kawamoto, Y.; Irie, M. Synthesis of a New Lithium Ionic Conductor, Thio-LISICON–Lithium Germanium Sulfide System. *Solid State Ionics* **2000**, *130*, 97–104.
- Murugan, R.; Thangadurai, V.; Weppner, W. Fast Lithium Ion Conduction in Garnet-Type $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$. *Angew. Chem., Int. Ed.* **2007**, *46*, 7778–7781.
- Dawson, J. A.; Attari, T. S.; Chen, H.; Emge, S. P.; Johnston, K. E.; Islam, M. S. Elucidating Lithium-Ion and Proton Dynamics in Anti-Perovskite Solid Electrolytes. *Energy Environ. Sci.* **2018**, *11*, 2993–3002.
- Dawson, J. A.; Canepa, P.; Famprakis, T.; Masquelier, C.; Islam, M. S. Atomic-Scale Influence of Grain Boundaries on Li-Ion Conduction in Solid Electrolytes for All-Solid-State Batteries. *J. Am. Chem. Soc.* **2018**, *140*, 362–368.
- Canepa, P.; Dawson, J. A.; Sai Gautam, G.; Statham, J. M.; Parker, S. C.; Islam, M. S. Particle Morphology and Lithium Segregation to Surfaces of the $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ Solid Electrolyte. *Chem. Mater.* **2018**, *30*, 3019–3027.
- Yu, C.; Ganapathy, S.; de Klerk, N. J. J.; Roslon, I.; van Eck, E. R. H.; Kentgens, A. P. M.; Wagelmaker, M. Unravelling Li-Ion Transport from Picoseconds to Seconds: Bulk versus Interfaces in an Argyrodite $\text{Li}_6\text{PS}_5\text{Cl}-\text{Li}_2\text{S}$ All-Solid-State Li-Ion Battery. *J. Am. Chem. Soc.* **2016**, *138*, 11192–11201.
- Kato, Y.; Hori, S.; Saito, T.; Suzuki, K.; Hirayama, M.; Mitsui, A.; Yonemura, M.; Iba, H.; Kanno, R. High-Power All-Solid-State Batteries Using Sulfide Superionic Conductors. *Nat. Energy* **2016**, *1*, 16030.

- (20) Kuhn, A.; Duppel, V.; Lotsch, B. V. Tetragonal $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$ and Li_xGePS_8 – Exploring the Li Ion Dynamics in LGPS Li Electrolytes. *Energy Environ. Sci.* **2013**, *6*, 3548–3552.
- (21) Krauskopf, T.; Culver, S. P.; Zeier, W. G. Local Tetragonal Structure of the Cubic Superionic Conductor Na_3PS_4 . *Inorg. Chem.* **2018**, *57*, 4739–4744.
- (22) Lepley, N. D.; Holzwarth, N. A. W.; Du, Y. A. Structures, Li^+ Mobilities, and Interfacial Properties of Solid Electrolytes Li_3PS_4 and Li_3PO_4 from First Principles. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2013**, *88*, 104103.
- (23) Zhang, Z.; Ramos, E.; Lalère, F.; Assoud, A.; Kaup, K.; Hartman, P.; Nazar, L. F. $\text{Na}_{11}\text{Sn}_2\text{PS}_{12}$: A New Solid State Sodium Superionic Conductor. *Energy Environ. Sci.* **2018**, *11*, 87–93.
- (24) Kudu, Ö. U.; Famprakis, T.; Fleutot, B.; Braida, M.-D.; Le Mercier, T.; Islam, M. S.; Masquelier, C. A Review of Structural Properties and Synthesis Methods of Solid Electrolyte Materials in the $\text{Li}_2\text{S}-\text{P}_2\text{S}_5$ Binary System. *J. Power Sources* **2018**, *407*, 31–43.
- (25) Hayashi, A.; Sakuda, A.; Tatsumisago, M. Development of Sulfide Solid Electrolytes and Interface Formation Processes for Bulk-Type All-Solid-State Li and Na Batteries. *Front. Energy Res.* **2016**, *4*, 25.
- (26) Hayashi, A.; Noi, K.; Sakuda, A.; Tatsumisago, M. Superionic Glass-Ceramic Electrolytes for Room-Temperature Rechargeable Sodium Batteries. *Nat. Commun.* **2012**, *3*, 856.
- (27) Yu, C.; Ganapathy, S.; de Klerk, N. J. J.; van Eck, E. R. H.; Wagemaker, M. Na-Ion Dynamics in Tetragonal and Cubic Na_3PS_4 , a Na-Ion Conductor for Solid State Na-Ion Batteries. *J. Mater. Chem. A* **2016**, *4*, 15095–15105.
- (28) Duchardt, M.; Ruschewitz, U.; Adams, S.; Dehnen, S.; Roling, B. Vacancy-Controlled Na^+ Superion Conduction in $\text{Na}_{11}\text{Sn}_2\text{PS}_{12}$. *Angew. Chem., Int. Ed.* **2017**, *57*, 1351–1355.
- (29) Bron, P.; Dehnen, S.; Roling, B. $\text{Li}_{10}\text{Si}_{0.3}\text{Sn}_{0.7}\text{P}_2\text{S}_{12}$ – A Low-Cost and Low-Grain-Boundary-Resistance Lithium Superionic Conductor. *J. Power Sources* **2016**, *329*, 530–535.
- (30) Hori, S.; Suzuki, K.; Hirayama, M.; Kato, Y.; Kanno, R. Lithium Superionic Conductor $\text{Li}_{9.42}\text{Si}_{1.02}\text{P}_{2.1}\text{S}_{9.96}\text{O}_{2.04}$ with $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$ -Type Structure in the $\text{Li}_2\text{S}-\text{P}_2\text{S}_5-\text{SiO}_2$ Pseudoternary System: Synthesis, Electrochemical Properties, and Structure–Composition Relationships. *Front. Energy Res.* **2016**, *4*, 38.
- (31) Sakuda, A.; Hayashi, A.; Tatsumisago, M. Sulfide Solid Electrolyte with Favorable Mechanical Property for All-Solid-State Lithium Battery. *Sci. Rep.* **2013**, *3*, 2261.
- (32) Tatsumisago, M.; Nagao, M.; Hayashi, A. Recent Development of Sulfide Solid Electrolytes and Interfacial Modification for All-Solid-State Rechargeable Lithium Batteries. *J. Australas. Ceram. Soc.* **2013**, *1*, 17–25.
- (33) Raj, R.; Wolfenstine, J. Current Limit Diagrams for Dendrite Formation in Solid-State Electrolytes for Li-Ion Batteries. *J. Power Sources* **2017**, *343*, 119–126.
- (34) Shen, F.; Dixit, M. B.; Xiao, X.; Hatzell, K. B. Effect of Pore Connectivity on Li Dendrite Propagation within LLZO Electrolytes Observed with Synchrotron X-Ray Tomography. *ACS Energy Lett.* **2018**, *3*, 1056–1061.
- (35) Porz, L.; Swamy, T.; Sheldon, B. W.; Rettenwander, D.; Frömling, T.; Thaman, H. L.; Berends, S.; Uecker, R.; Carter, W. C.; Chiang, Y.-M. Mechanism of Lithium Metal Penetration through Inorganic Solid Electrolytes. *Adv. Energy Mater.* **2017**, *7*, 1701003.
- (36) Stegmaier, S.; Voss, J.; Reuter, K.; Luntz, A. C. Li^+ Defects in a Solid-State Li Ion Battery: Theoretical Insights with a Li_3OCl Electrolyte. *Chem. Mater.* **2017**, *29*, 4330–4340.
- (37) Liu, Z.; Fu, W.; Payzant, E. A.; Yu, X.; Wu, Z.; Dudney, N. J.; Kiggans, J.; Hong, K.; Rondinone, A. J.; Liang, C. Anomalous High Ionic Conductivity of Nanoporous $\beta\text{-Li}_3\text{PS}_4$. *J. Am. Chem. Soc.* **2013**, *135*, 975–978.
- (38) Tsukasaki, H.; Mori, S.; Morimoto, M. A.; Hayashi, A.; Tatsumisago, M. Direct Observation of a Non-Crystalline State of $\text{Li}_2\text{S}-\text{P}_2\text{S}_5$ Solid Electrolytes. *Sci. Rep.* **2017**, *7*, 4142.
- (39) de Klerk, N. J. J.; Wagemaker, M. Diffusion Mechanism of the Sodium-Ion Solid Electrolyte Na_3PS_4 and Potential Improvements of Halogen Doping. *Chem. Mater.* **2016**, *28*, 3122–3130.
- (40) Krauskopf, T.; Pompe, C.; Kraft, M.; Zeier, W. G. Influence of Lattice Dynamics on Na^+ -Transport in the Solid Electrolyte $\text{Na}_3\text{PS}_{4-x}\text{Se}_x$. *Chem. Mater.* **2017**, *29*, 8859–8869.
- (41) Nishimura, S.-i.; Tanibata, N.; Hayashi, A.; Tatsumisago, M.; Yamada, A. The Crystal Structure and Sodium Disorder of High-Temperature Polymorph $\beta\text{-Na}_3\text{PS}_4$. *J. Mater. Chem. A* **2017**, *5*, 25025–25030.
- (42) Chu, I.-H.; Kompella, C. S.; Nguyen, H.; Zhu, Z.; Hy, S.; Deng, Z.; Meng, Y. S.; Ong, S. P.; Jung, Y. S. Room-Temperature All-Solid-State Rechargeable Sodium-Ion Batteries with a Cl-Doped Na_3PS_4 Superionic Conductor. *Sci. Rep.* **2016**, *6*, 33733.
- (43) Tanibata, N.; Noi, K.; Hayashi, A.; Tatsumisago, M. Preparation and Characterization of Highly Sodium Ion Conducting $\text{Na}_3\text{PS}_4-\text{Na}_4\text{SiS}_4$ Solid Electrolytes. *RSC Adv.* **2014**, *4*, 17120–17123.
- (44) Moon, C. K.; Lee, H.-J.; Park, K. H.; Kwak, H.; Heo, J. W.; Choi, K.; Yang, H.; Kim, M.-S.; Hong, S.-T.; Lee, J. H.; et al. Vacancy-Driven Na^+ Superionic Conduction in New Ca-Doped Na_3PS_4 for All-Solid-State Na-Ion Batteries. *ACS Energy Lett.* **2018**, *3*, 2504–2512.
- (45) Zhu, Z.; Chu, I.-H.; Deng, Z.; Ong, S. P. Role of Na^+ Interstitials and Dopants in Enhancing the Na^+ Conductivity of the Cubic Na_3PS_4 Superionic Conductor. *Chem. Mater.* **2015**, *27*, 8318–8325.
- (46) Krauskopf, T.; Muy, S.; Culver, S. P.; Ohno, S.; Delaire, O.; Shao-Horn, Y.; Zeier, W. G. Comparing the Descriptors for Investigating the Influence of Lattice Dynamics on Ionic Transport Using the Superionic Conductor $\text{Na}_3\text{PS}_{4-x}\text{Se}_x$. *J. Am. Chem. Soc.* **2018**, *140*, 14464–14473.
- (47) Famprakis, T.; Dawson, J. A.; Fauth, F.; Suard, E.; Fleutot, B.; Courty, M.; Chotard, J.-N.; Islam, S.; Masquelier, C. A New Phase of the Na^+ Ion Conductor Na_3PS_4 . **2019**, ChemRxiv, https://chemrxiv.org/articles/A_New_Phase_of_the_Na_Ion_Conductor_Na3PS4/8003717/1?file=14906957 (accessed May 15, 2019).
- (48) Hayashi, A.; Noi, K.; Tanibata, N.; Nagao, M.; Tatsumisago, M. High Sodium Ion Conductivity of Glass–Ceramic Electrolytes with Cubic Na_3PS_4 . *J. Power Sources* **2014**, *258*, 420–423.
- (49) Yu, C.; Ganapathy, S.; van Eck, E. R. H.; van Eijck, L.; Basak, S.; Liu, Y.; Zhang, L.; Zandbergen, H. W.; Wagemaker, M. Revealing the Relation between the Structure, Li-Ion Conductivity and Solid-State Battery Performance of the Argyrodite $\text{Li}_6\text{PS}_5\text{Br}$ Solid Electrolyte. *J. Mater. Chem. A* **2017**, *5*, 21178–21188.
- (50) Sun, Y.; Suzuki, K.; Hori, S.; Hirayama, M.; Kanno, R. Superionic Conductors: $\text{Li}_{10+\delta}[\text{Sn}_y\text{Si}_{1-y}]_{1+\delta}\text{P}_{2-\delta}\text{S}_{12}$ with a $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$ -Type Structure in the $\text{Li}_3\text{PS}_4-\text{Li}_4\text{SnS}_4-\text{Li}_4\text{SiS}_4$ Quasi-Ternary System. *Chem. Mater.* **2017**, *28*–*30*, 5858–5864.
- (51) Hooper, A.; McGeehin, P.; Harrison, K. T.; Tofield, B. C. Ionic Conductivity of Pure and Doped Na_3PO_4 . *J. Solid State Chem.* **1978**, *24*, 265–275.
- (52) Hruschka, H.; Lissel, E.; Jansen, M. Na-Ion Conduction in the Solid Solutions of $\text{Na}_3\text{PO}_4/\text{Na}_2\text{SO}_4$ and $\text{Na}_3\text{AlF}_6/\text{Na}_2\text{SO}_4$. *Solid State Ionics* **1988**, *28*–*30*, 159–162.
- (53) Yin, W.-G.; Liu, J.; Duan, C.-G.; Mei, W. N.; Smith, R. W.; Hardy, J. R. Superionicity in Na_3PO_4 : A Molecular Dynamics Simulation. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2004**, *70*, 64302.
- (54) Jansen, M.; Henseler, U. Synthesis, Structure Determination, and Ionic Conductivity of Sodium Tetrathiophosphate. *J. Solid State Chem.* **1992**, *99*, 110–119.
- (55) Harrison, R. J.; Putnis, A.; Kockelmann, W. Phase Transition Behaviour and Equilibrium Phase Relations in the Fast-Ion Conductor System $\text{Na}_3\text{PO}_4-\text{Na}_2\text{SO}_4$. *Phys. Chem. Chem. Phys.* **2002**, *4*, 3252–3259.
- (56) Pompetzki, M.; Dinnebier, R. E.; Jansen, M. Sodium Dithiophosphate(V): Crystal Structure, Sodium Ionic Conductivity and Dismutation. *Solid State Sci.* **2003**, *5*, 1439–1444.

- (57) Yu, S.; Siegel, D. J. Grain Boundary Contributions to Li-Ion Transport in the Solid Electrolyte $\text{Li-La}_3\text{Zr}_2\text{O}_{12}$ (LLZO). *Chem. Mater.* **2017**, *29*, 9639–9647.
- (58) Ma, C.; Chen, K.; Liang, C.; Nan, C.-W.; Ishikawa, R.; More, K.; Chi, M. Atomic-Scale Origin of the Large Grain-Boundary Resistance in Perovskite Li-Ion-Conducting Solid Electrolytes. *Energy Environ. Sci.* **2014**, *7*, 1638–1642.
- (59) Park, H.; Jung, K.; Nezafati, M.; Kim, C.-S.; Kang, B. Sodium Ion Diffusion in Nasicon ($\text{Na}_3\text{Zr}_2\text{Si}_2\text{PO}_{12}$) Solid Electrolytes: Effects of Excess Sodium. *ACS Appl. Mater. Interfaces* **2016**, *8*, 27814–27824.
- (60) Huang, H.; Wu, H.-H.; Wang, X.; Lalère, B.; Zhang, T.-Y. Enhancing Sodium Ionic Conductivity in Tetragonal- Na_3PS_4 by Halogen Doping: A First Principles Investigation. *Phys. Chem. Chem. Phys.* **2018**, *20*, 20525–20533.
- (61) Wilmer, D.; Funke, K.; Witschas, M.; Banhatti, R. D.; Jansen, M.; Korus, G.; Fitter, J.; Lechner, R. E. Anion Reorientation in an Ion Conducting Plastic Crystal – Coherent Quasielastic Neutron Scattering from Sodium Ortho-Phosphate. *Phys. B* **1999**, *266*, 60–68.
- (62) Deng, Y.; Eames, C.; Chotard, J.-N.; Lalère, F.; Seznec, V.; Emge, S.; Pecher, O.; Grey, C. P.; Masquelier, C.; Islam, M. S. Structural and Mechanistic Insights into Fast Lithium-Ion Conduction in $\text{Li}_4\text{SiO}_4-\text{Li}_3\text{PO}_4$ Solid Electrolytes. *J. Am. Chem. Soc.* **2015**, *137*, 9136–9145.
- (63) Heijmans, P.; Kärger, J. *Diffusion in Condensed Matter: Methods, Materials, Models*; Springer Berlin Heidelberg: Berlin, Heidelberg, 2005.
- (64) Islam, M. S.; Fisher, C. A. J. Lithium and Sodium Battery Cathode Materials: Computational Insights into Voltage, Diffusion and Nanostructural Properties. *Chem. Soc. Rev.* **2014**, *43*, 185–204.
- (65) Muralidharan, A.; Chaudhari, M. I.; Pratt, L. R.; Rempe, S. B. Molecular Dynamics of Lithium Ion Transport in a Model Solid Electrolyte Interphase. *Sci. Rep.* **2018**, *8*, 10736.
- (66) de Klerk, N. J. J.; van der Maas, E.; Wagemaker, M. Analysis of Diffusion in Solid-State Electrolytes through MD Simulations, Improvement of the Li-Ion Conductivity in $\beta\text{-Li}_3\text{PS}_4$ as an Example. *ACS Appl. Energy Mater.* **2018**, *1*, 3230–3242.
- (67) Dawson, J. A.; Chen, H.; Islam, M. S. Composition Screening of Lithium- and Sodium-Rich Anti-Perovskites for Fast-Conducting Solid Electrolytes. *J. Phys. Chem. C* **2018**, *122*, 23978–23984.
- (68) Aparicio, P. A.; Dawson, J. A.; Islam, M. S.; de Leeuw, N. H. Computational Study of NaVOPO_4 Polymorphs as Cathode Materials for Na-Ion Batteries: Diffusion, Electronic Properties, and Cation-Doping Behavior. *J. Phys. Chem. C* **2018**, *122*, 25829–25836.
- (69) Gale, J. D.; Rohl, A. L. The General Utility Lattice Program (GULP). *Mol. Simul.* **2003**, *29*, 291–341.
- (70) Tilocca, A.; Cormack, A. N.; de Leeuw, N. H. The Structure of Bioactive Silicate Glasses: New Insight from Molecular Dynamics Simulations. *Chem. Mater.* **2007**, *19*, 95–103.
- (71) Harding, J. H. Database of Published Interatomic Potential Parameters. <http://www.ucl.ac.uk/klmc/Potentials/Library/diller.lib> (accessed Nov 12, 2018).
- (72) Plimpton, S. Fast Parallel Algorithms for Short-Range Molecular Dynamics. *J. Comput. Phys.* **1995**, *117*, 1–19.
- (73) Evans, D. J. The Nose–Hoover Thermostat. *J. Chem. Phys.* **1985**, *83*, 4069–4074.
- (74) Hirel, P. Atomsk: A Tool for Manipulating and Converting Atomic Data Files. *Comput. Phys. Commun.* **2015**, *197*, 212–219.