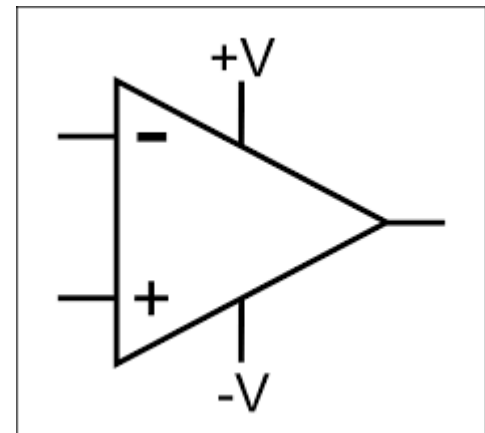
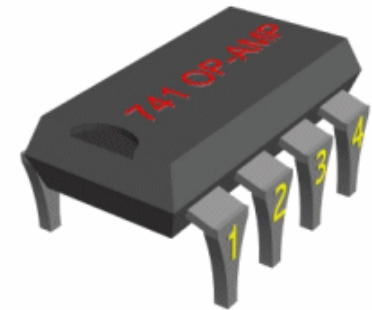
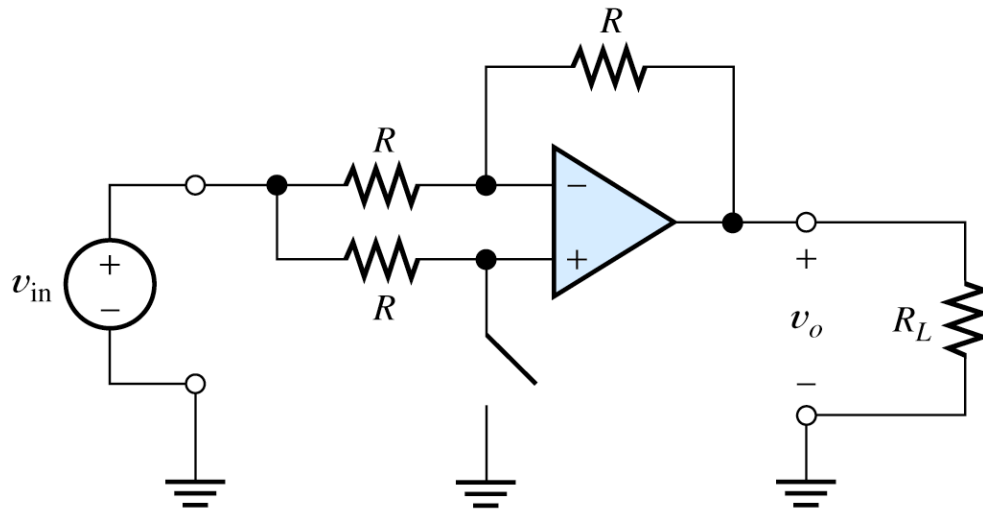
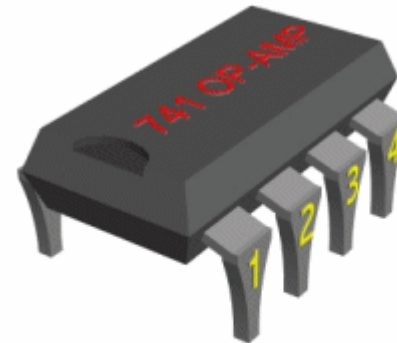
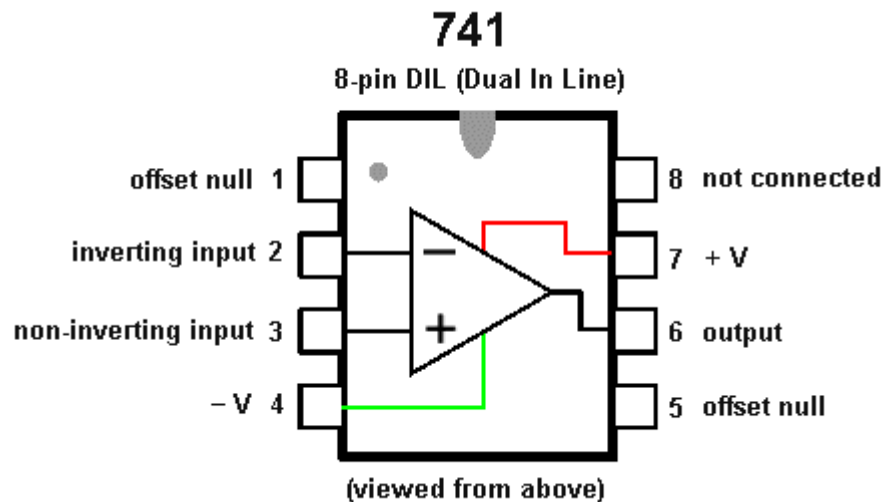


Operational Amplifiers



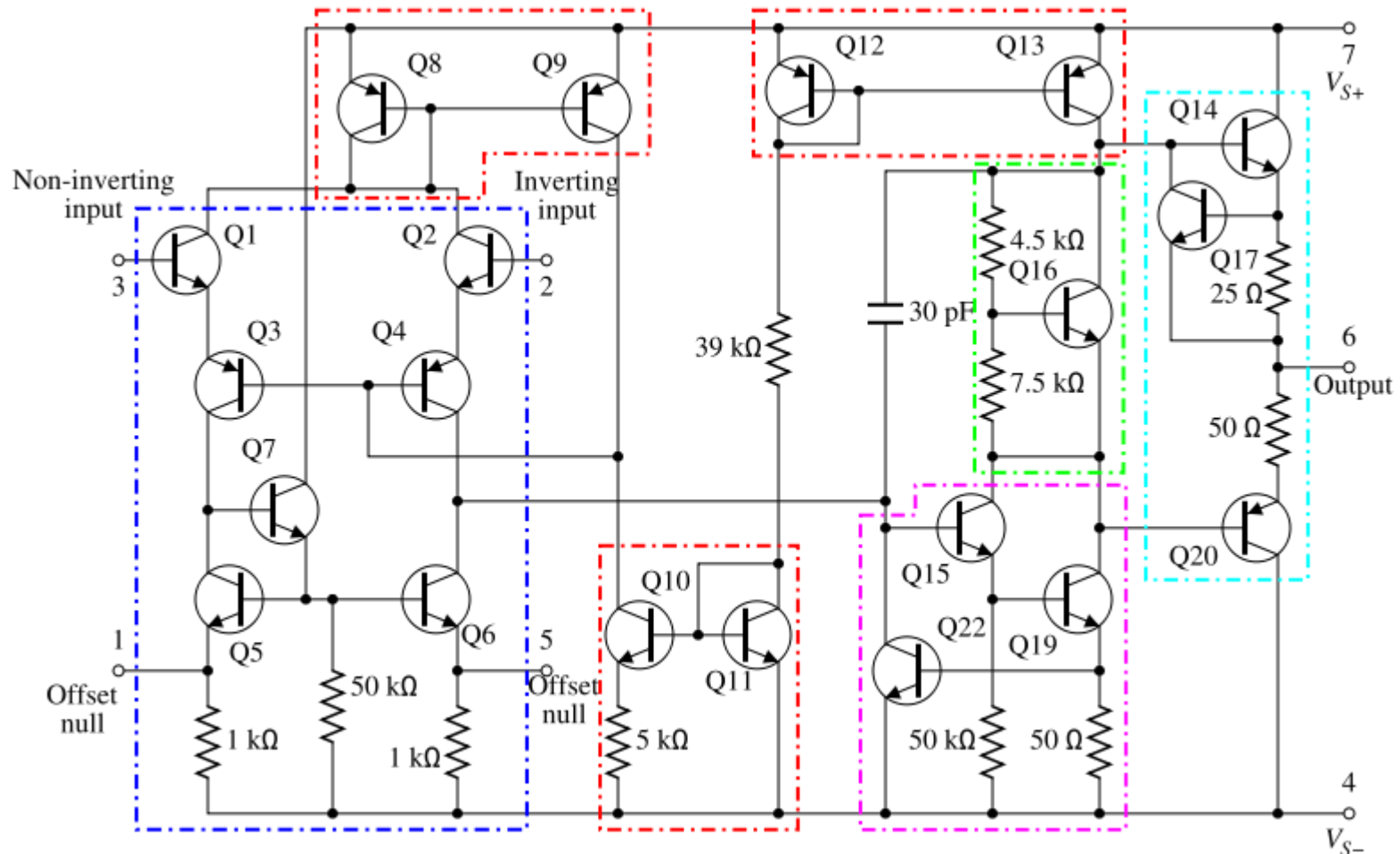
Operational amplifiers (op-amps)

741 Amplifier is the most popular amplifier it has $A_{vo}=100000$ (voltage gain without load)



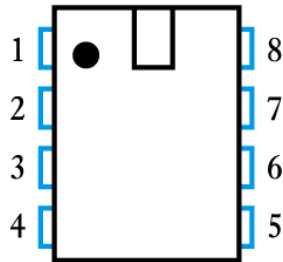
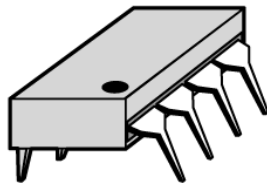
Operational amplifiers (op-amps)

741 Amplifier BJT transistor level schematic

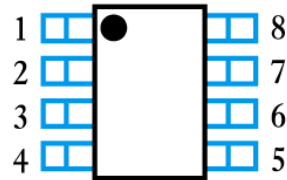
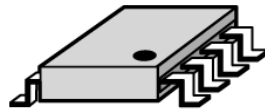


Operational amplifiers (op-amps) are among the most widely used integrated circuits (ICs) in electronics.

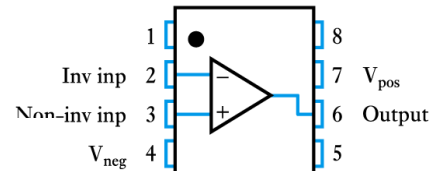
A single package will often contain several op-amps



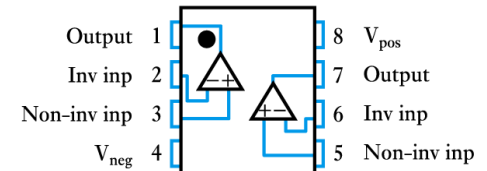
(a) A DIP package



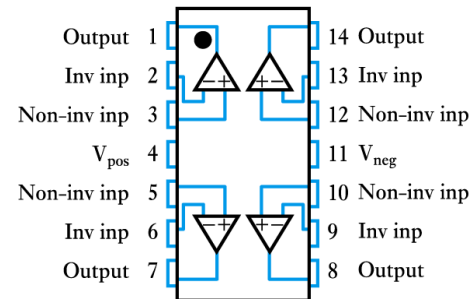
(b) An SMT package



(a) A single op-amp



(b) A dual op-amp

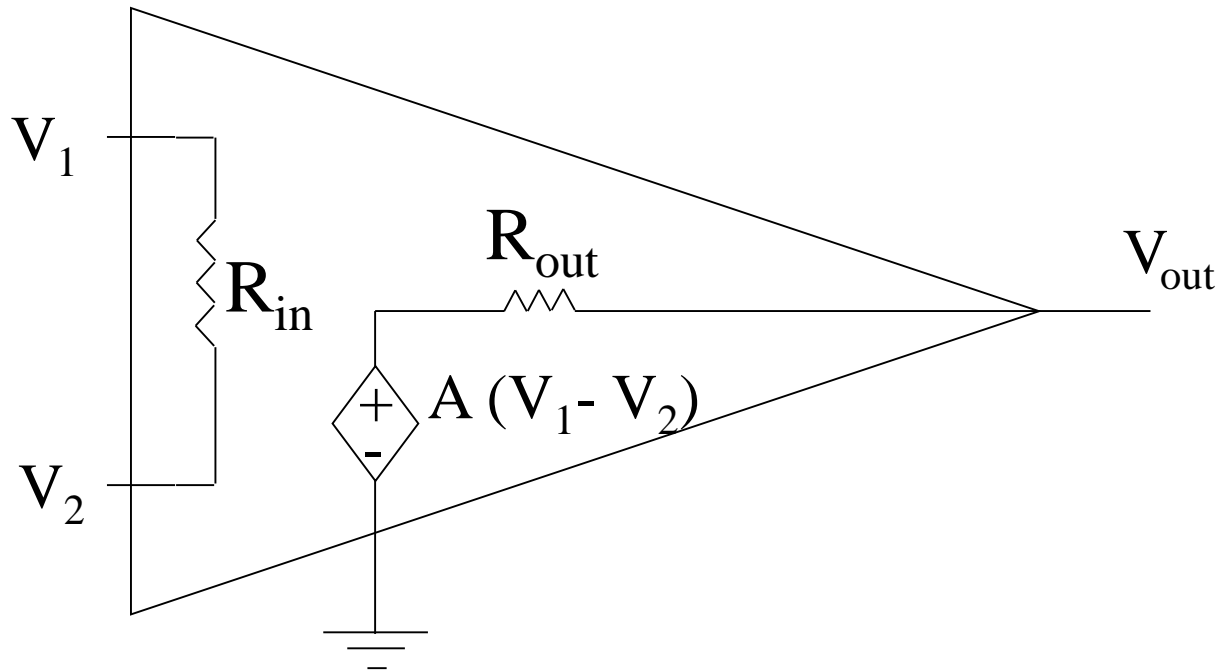


(c) A quad op-amp

Operational Amplifier Model

An operational amplifier circuit is designed so that

- 1) $V_{\text{out}} = A (V_1 - V_2)$ (A is a very large gain)
- 2) Input resistance (R_{in}) is very large
- 3) Output resistance (R_{out}) is very low

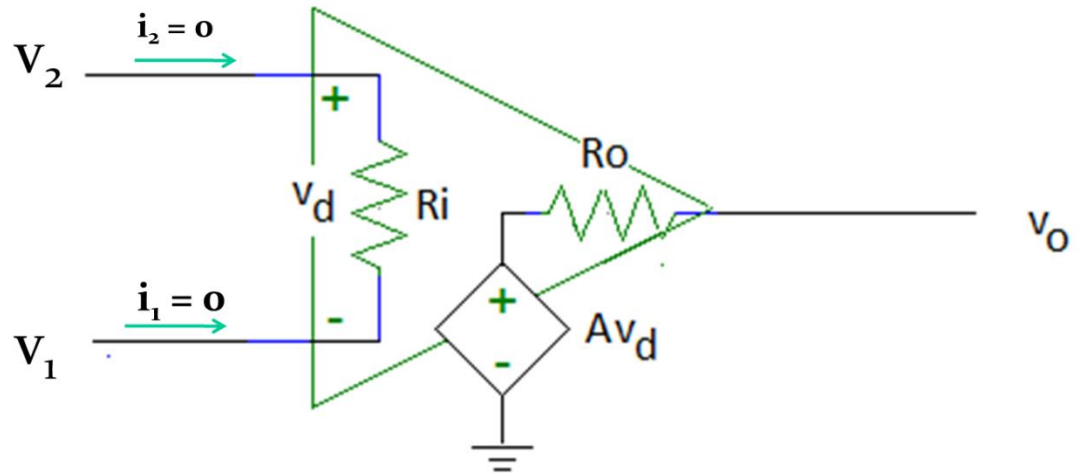


Typical Op Amp Parameters

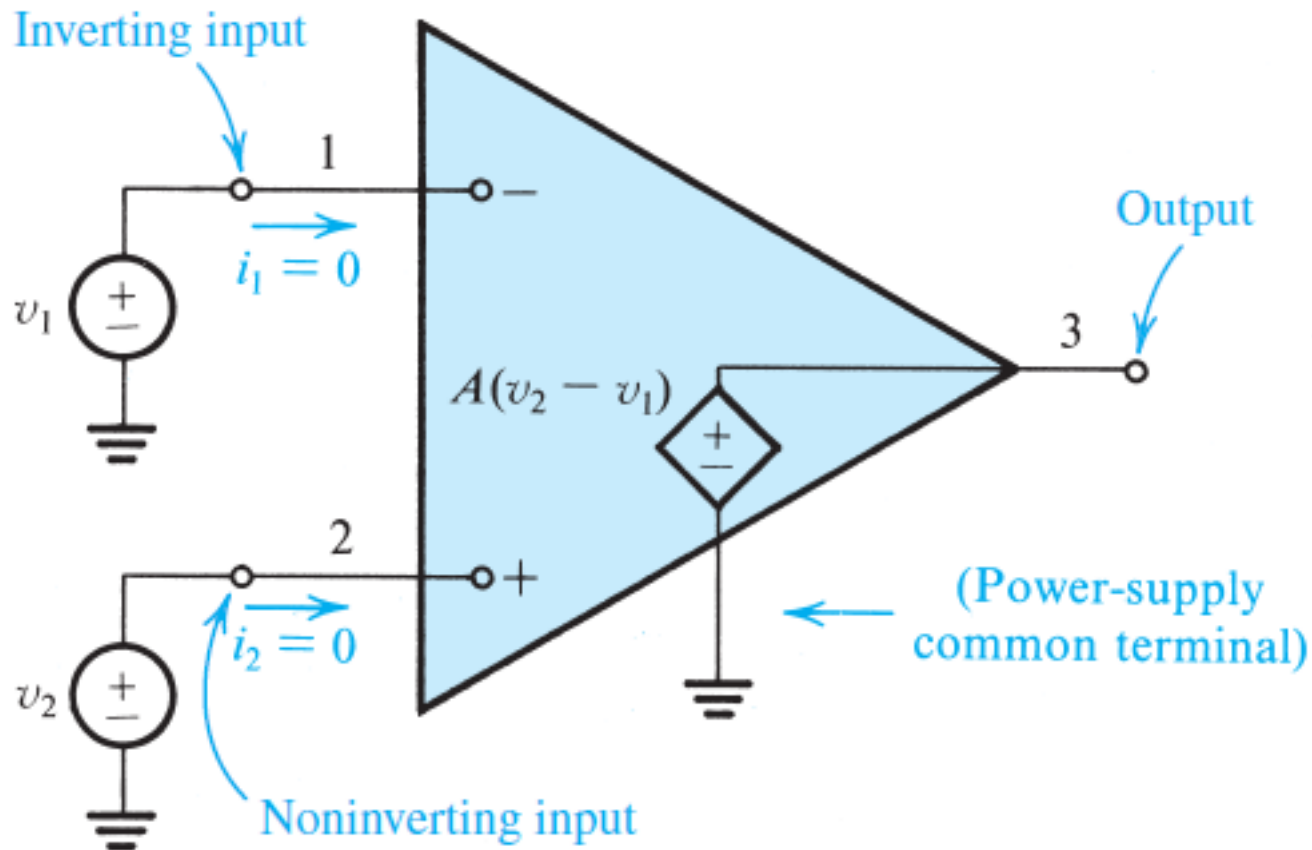
Parameter	Variable	Typical Ranges	Ideal Values
Open-Loop Voltage Gain	A	10^5 to 10^8	∞
Input Resistance	R_i	10^5 to $10^{13} \Omega$	$\infty \Omega$
Output Resistance	R_o	10 to 100 Ω	0 Ω
Supply Voltage	V_{cc}/V^+ $-V_{cc}/V^-$	5 to 30 V -30V to 0V	N/A N/A

An Ideal Operational Amplifier

- $R_i = \infty$
- Therefore, $i_1 = i_2 = 0A$
- $R_o = 0$



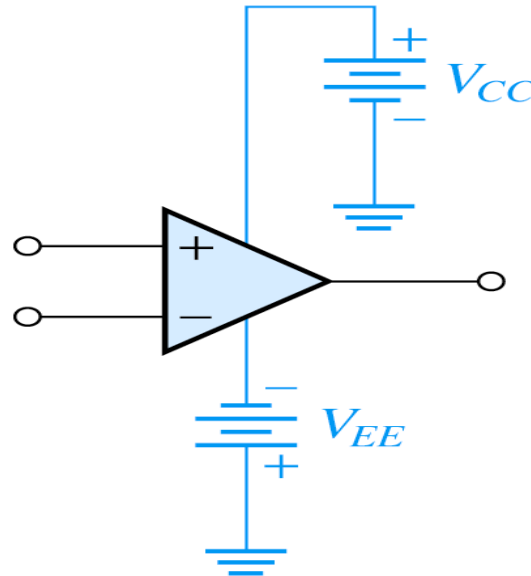
An Ideal Operational Amplifier



Equivalent circuit of the ideal op amp.

An Ideal Operational Amplifier

A real op-amp must have a DC supply voltage which is often not shown on the schematics.



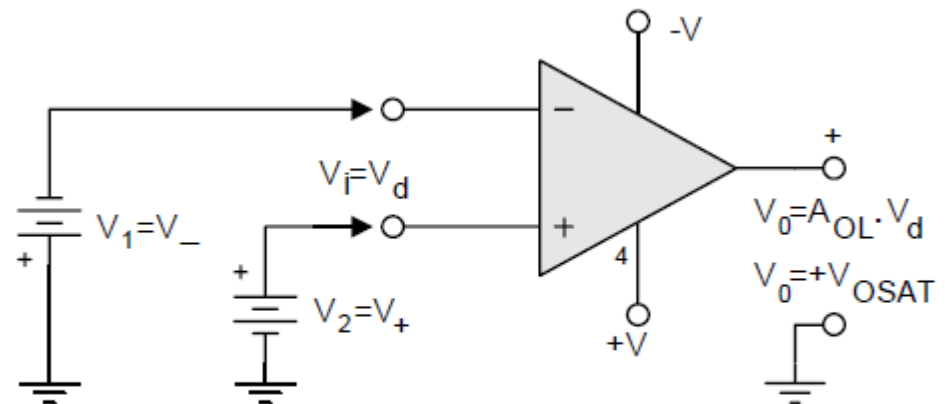
Op-amp symbol showing the dc power supplies, V_{CC} and V_{EE} .

Op-amps

Output voltage of an Op-amp can not be greater than DC supply voltage.

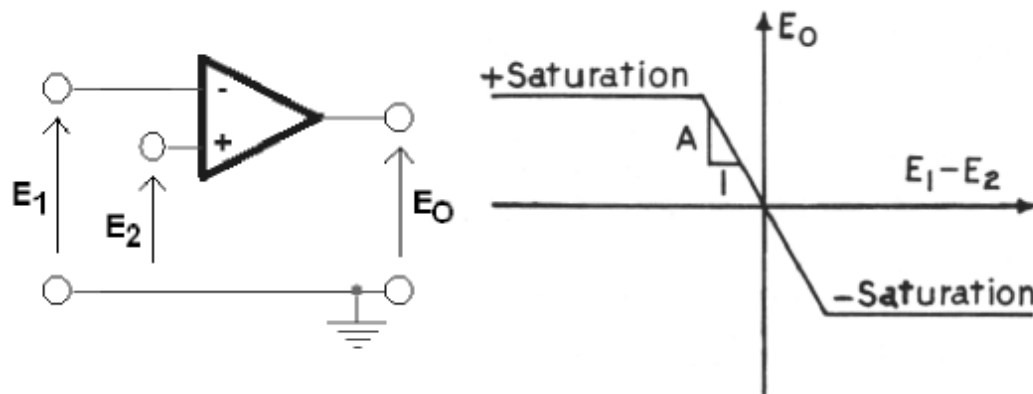
Maximum output voltage is usually slightly lower than the DC supply voltage and called as saturation voltage.

$$V_{out} = A_{OL} (V_2 - V_1)$$

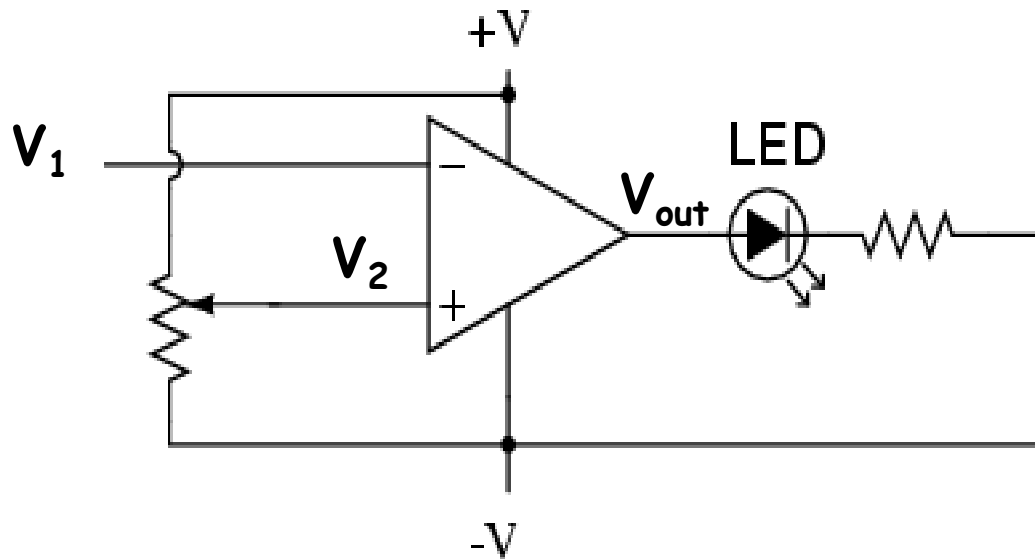


$$V_2 > V_1 \text{ ise } V_d = + \quad V_o = +V_{SAT} \text{ 'dir}$$

$$V_2 < V_1 \text{ ise } V_d = - \quad V_o = -V_{SAT} \text{ 'dir}$$

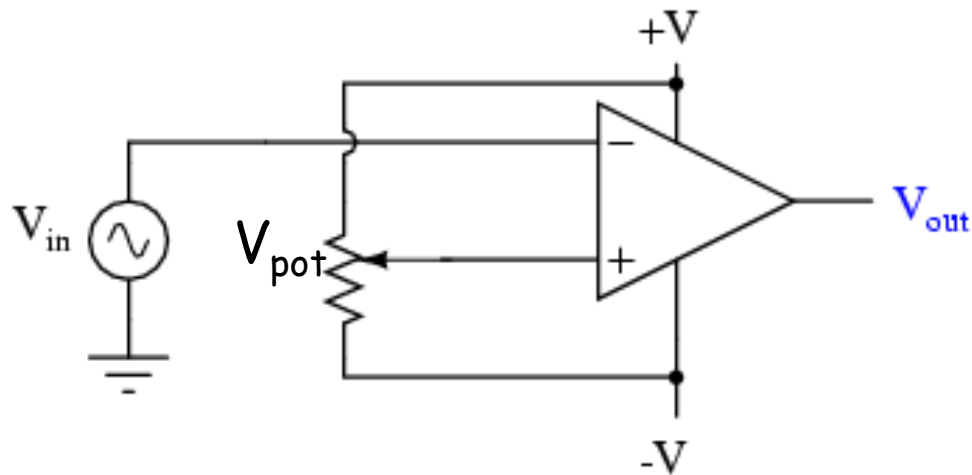


Comparator

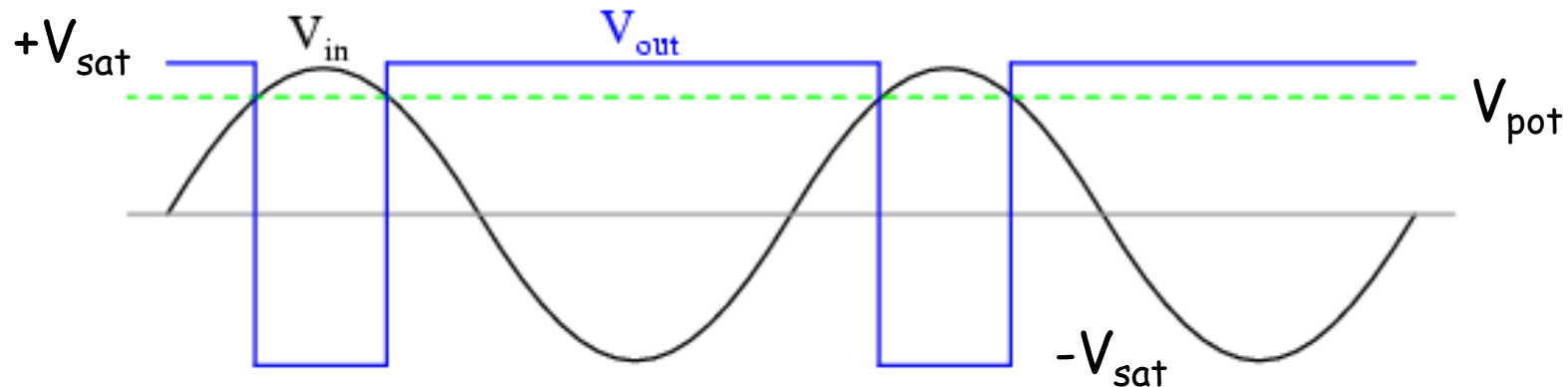


Applications: Low-voltage alarms, night light controller

Pulse Width Modulator



- Output changes when $V_{\text{in}} \approx V_{\text{pot}}$



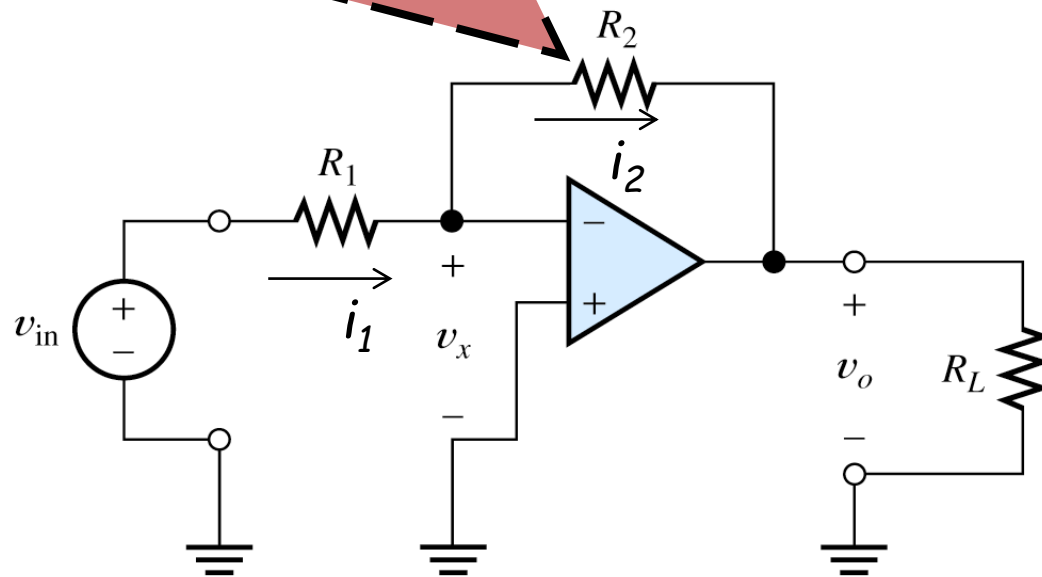
Application: Motor controllers

Negative feedback

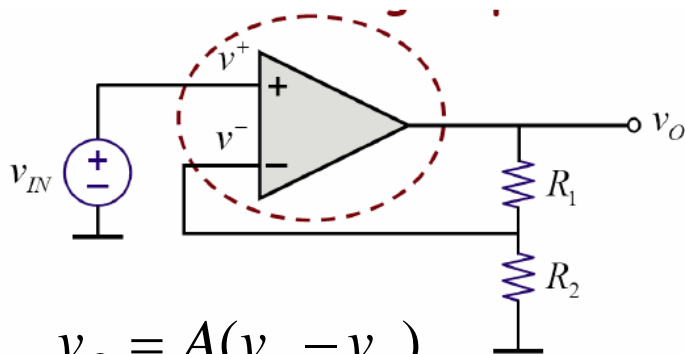
Op-amp are almost always used with a negative feedback:

- Part of the output signal is returned to the input.
- Feedback reduces the gain of op-amp.

Negative feedback forces the voltage at the inverting input terminal to be equal to the voltage at the noninverting input terminal.



When A is very large:



$$v_O = A(v_+ - v_-)$$

$$v_- = \frac{v_O R_2}{R_1 + R_2}$$

$$v_O = \frac{A v_{IN}}{1 + \frac{A R_2}{R_1 + R_2}}$$

$$v_O = \frac{A v_{IN}}{A \cdot \frac{R_2}{R_1 + R_2}}$$

$$v_O \approx v_{IN} \frac{R_1 + R_2}{R_2}$$

Take $A=10^6$, $R_1=9R$, $R_2=R$

$$v_O = \frac{10^6 v_{IN}}{1 + \frac{10^6 R}{9R + R}}$$

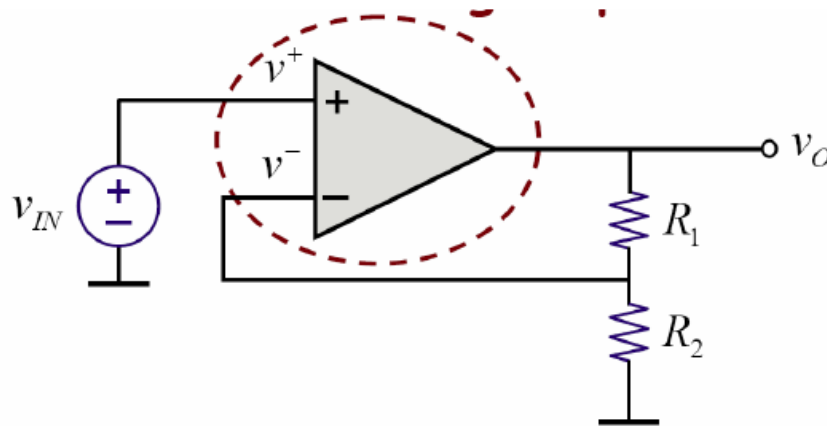
$$v_O = \frac{10^6 v_{IN}}{1 + 10^6 \cdot \frac{1}{10}}$$

$$v_O \approx v_{IN} \cdot 10$$

- Gain now determined only by resistance ratio
- Doesn't depend on A (or temperature, frequency, variations in fabrication).

Why use Negative feedback?:

- Makes properties predictable - independent of temperature, manufacturing differences or other properties of the opamp.
- Circuit properties only depend upon the external feedback network and so can be easily controlled.



More insight (Under negative feedback)

$$v_O \approx v_{IN} \frac{R_1 + R_2}{R_2}$$

$$v^+ - v^- = \frac{v_O}{A} = \left(\frac{R_1 + R_2}{R_2} \right) v_{IN} \rightarrow 0$$

$$v^+ \approx v^-$$

• We also know

$$\bullet i^+ \approx 0$$

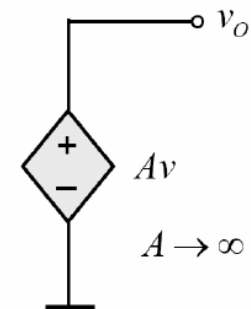
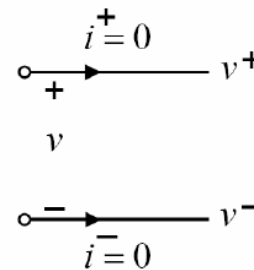
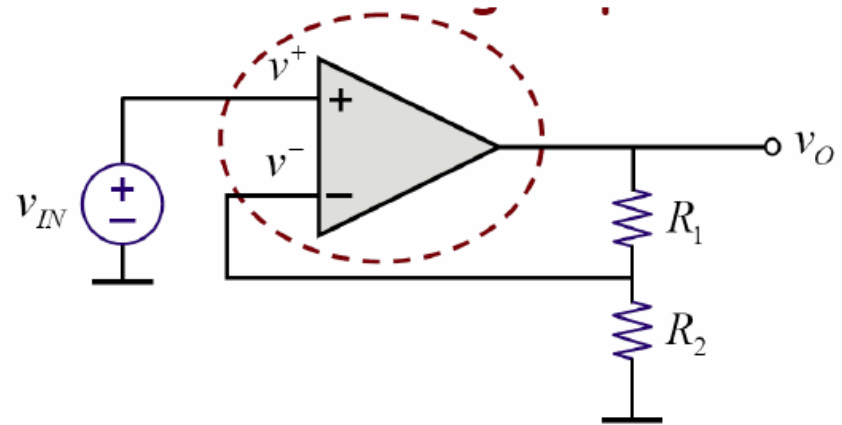
$$\bullet i^- \approx 0$$

• Helpful for analysis (under negative feedback)

• Two "Golden Rules«

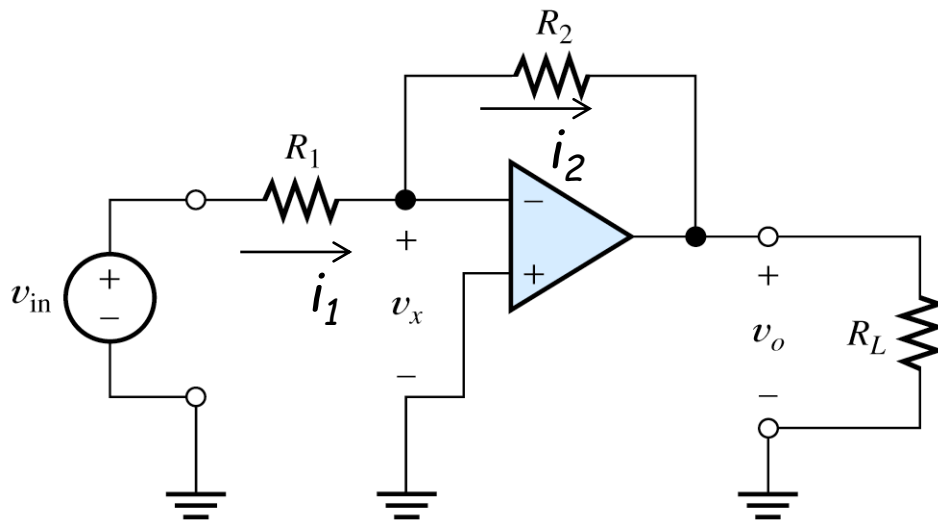
1) No current flows into the op-amp

2) $v^+ \approx v^-$



Inverting Amplifier

Since negative feedback forces the voltage at the inverting input terminal (v_-) to be equal to the voltage at the noninverting input terminal (v_+), v_x is equal to zero.



$$v_- = v_+ = 0V$$

$$i_1 = v_{in} / R_1$$

$$i_2 = i_1 \quad \text{and}$$

$$v_o = -i_2 R_2 = -v_{in} R_2 / R_1$$

So

$$A_v = v_o / v_{in} = -R_2 / R_1$$

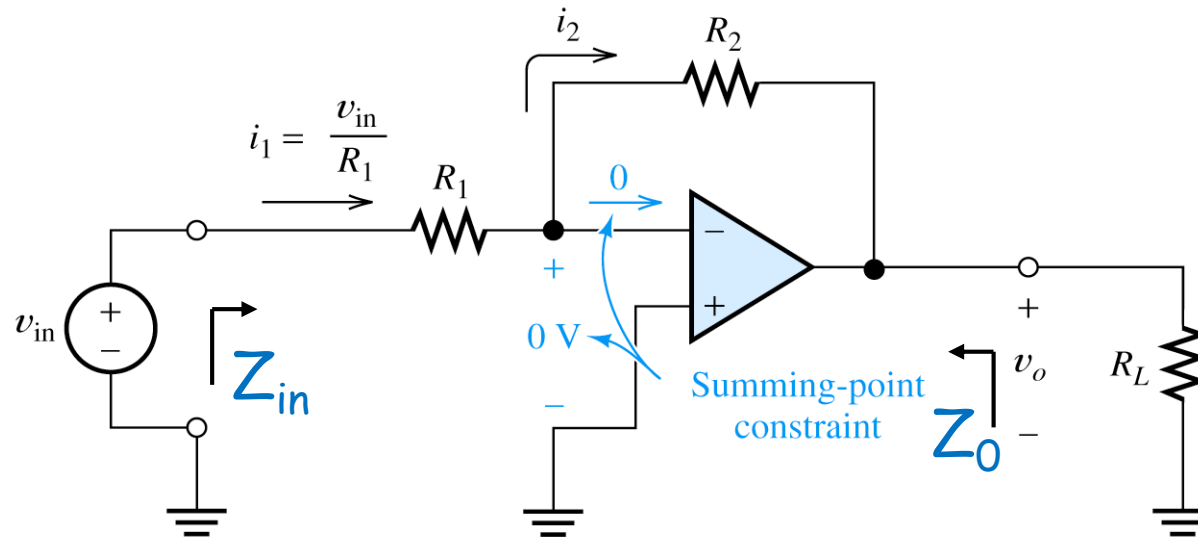
Inverting Amplifier

Since $v_o = -i_2 R_2 = -v_{in} R_2 / R_1$

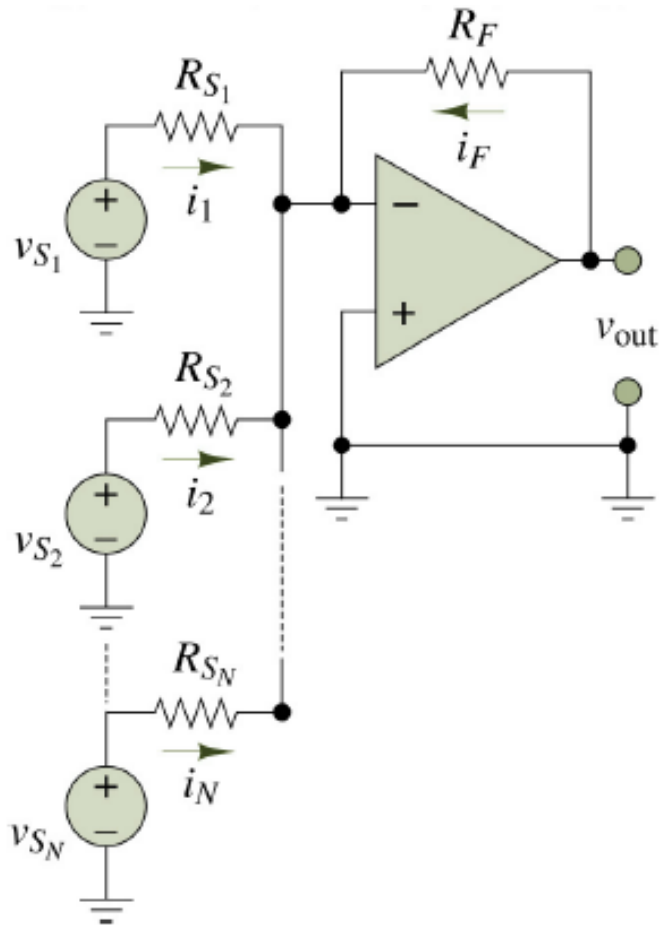
We see that the output voltage does not depend on the load resistance.

The output impedance of the inverting amplifier is zero.

The input impedance is: $Z_{in} = v_{in} / i_1 = R_1$



Summing Amplifier



The output voltage in summing amplifier is $v_{out} = i_f \cdot R_f$ since $v_- = v_+ = 0$

$$i_1 + i_2 + \dots + i_N = -i_F$$

$$\frac{v_{S1}}{R_{S1}} + \frac{v_{S2}}{R_{S2}} + \dots + \frac{v_{SN}}{R_{SN}} = -\frac{v_{out}}{R_F}$$

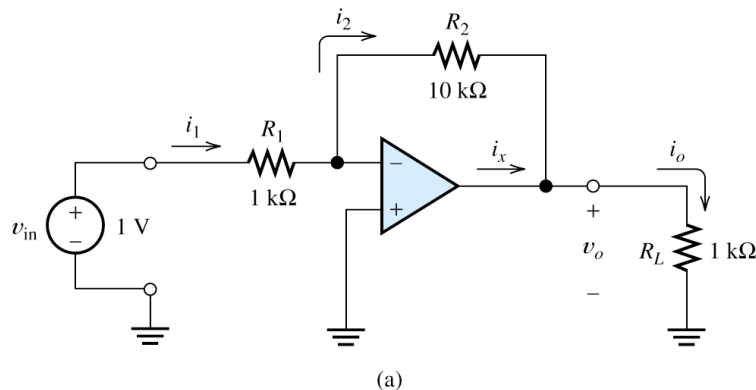
$$v_{out} = -\left(\frac{R_F}{R_{S1}} v_{S1} + \frac{R_F}{R_{S2}} v_{S2} + \dots + \frac{R_F}{R_{SN}} v_{SN} \right)$$

If $R_{S1} = R_{S2} = \dots = R_{SN} = R_S$

$$v_{out} = -\frac{R_F}{R_S} (v_{S1} + v_{S2} + \dots + v_{SN})$$

Exercise

Find the currents and voltages in these two circuits:



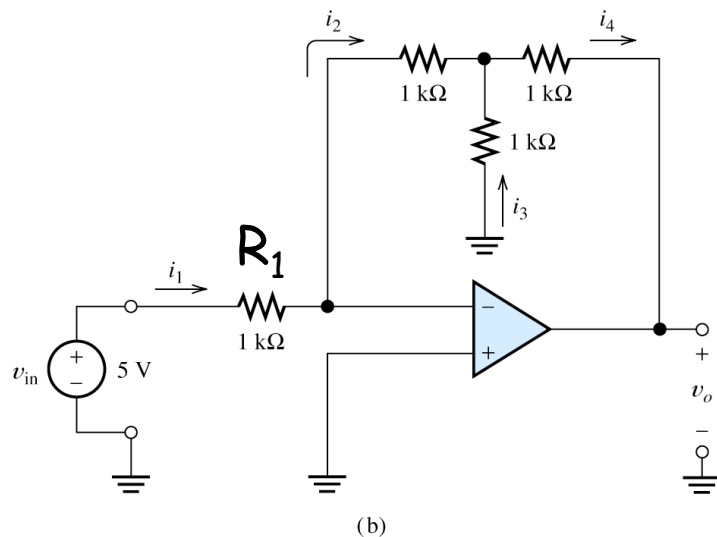
$$a) \quad i_1 = v_{in} / R_1 = 1V / 1k\Omega = 1mA$$

$$i_2 = i_1 = 1mA \text{ from KCL}$$

$$v_o = -i_2 * R_2 = -10V \text{ from KVL}$$

$$i_o = v_o / R_L = -10mA \text{ from Ohms law}$$

$$i_x = i_o - i_2 = -10mA - 1mA = -11mA$$



$$b) \quad i_1 = v_{in} / R_1 = 5mA$$

$$i_2 = i_1 = 5mA$$

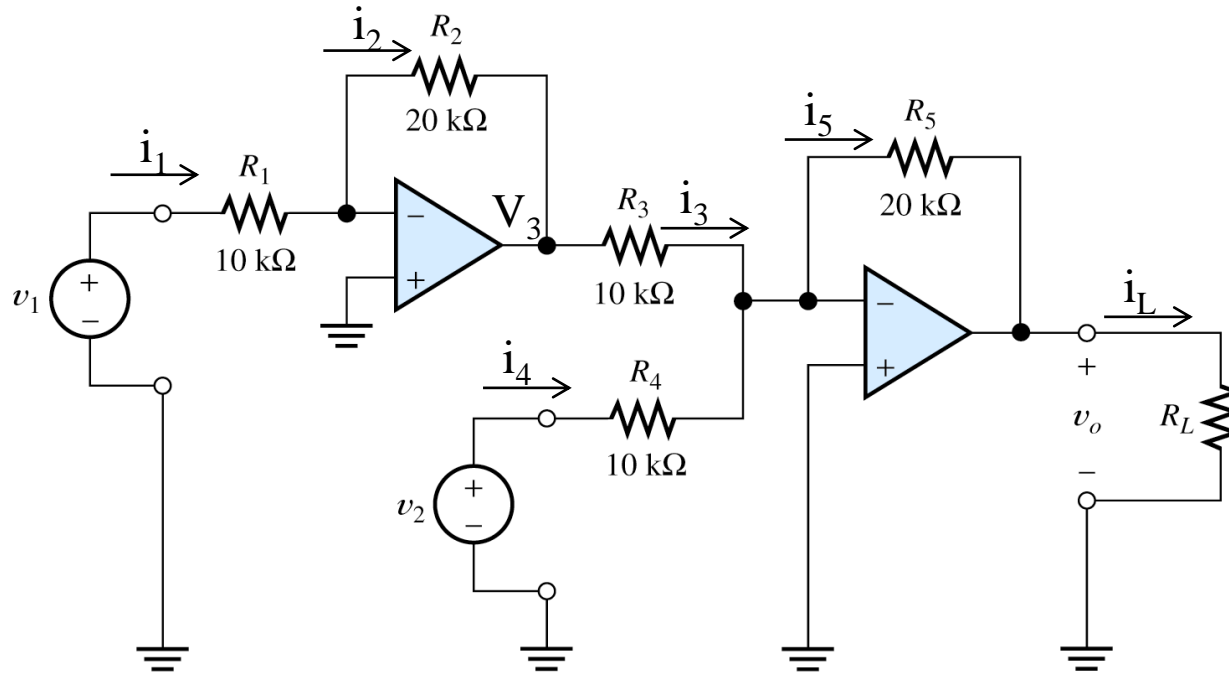
$$i_2 * 1k\Omega = i_3 * 1k\Omega \Rightarrow i_3 = 5mA$$

$$i_4 = i_2 + i_3 = 10mA$$

$$v_o = -i_2 * 1k\Omega - i_4 * 1k\Omega = -15V$$

Exercise

Find expression for the output voltage in the amplifier circuit:



$$i_1 = v_1 / R_1 = v_1 / 10\text{ k}\Omega$$

$$i_2 = i_1 = v_1 / 10\text{ mA}$$

$$v_3 = -i_2 \cdot R_2 = -v_1 / 10\text{ k}\Omega \cdot 20\text{ k}\Omega = -2v_1$$

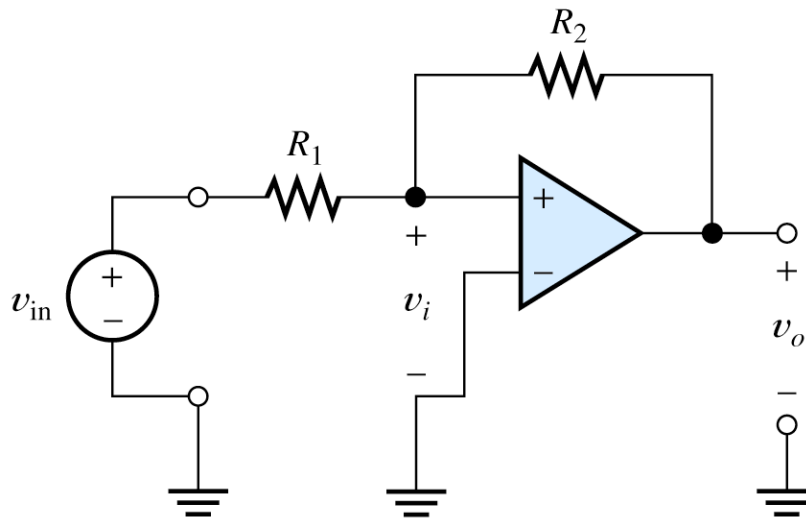
$$i_5 = i_3 + i_4 = v_3 / 10\text{ k}\Omega + v_2 / 10\text{ k}\Omega$$

$$v_o = -i_5 \cdot R_5 = -(v_3 / 10\text{ k}\Omega + v_2 / 10\text{ k}\Omega) \cdot 20\text{ k}\Omega = -2v_3 - 2v_2 = 4v_1 - 2v_2$$

Positive Feedback

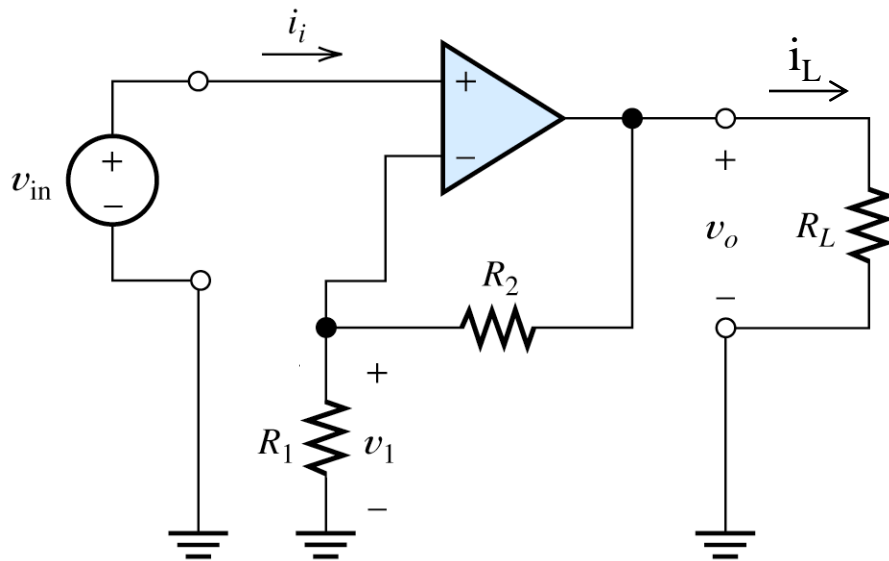
When we flip the polarization of the op-amp as shown on the figure we will get a positive feedback that **saturates** the amplifier output.

This is not a good idea.



Circuit with positive feedback.

Noninverting Amplifier



Noninverting amplifier.

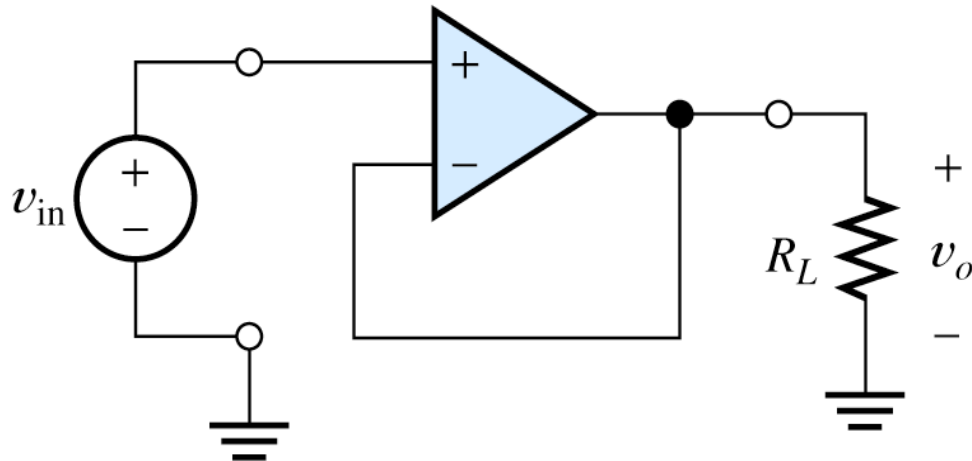
$$v_1 = v_{in}$$

$$v_{in}/R_1 + (v_{in} - v_o)/R_2 = 0$$

Thus the voltage gain of noninverting amplifier is:

$$A_v = v_o / v_{in} = 1 + R_2 / R_1$$

Voltage Follower



The voltage follower which has $A_v = 1$.

- What's the application of this circuit?

- **Buffer**

voltage gain = 1

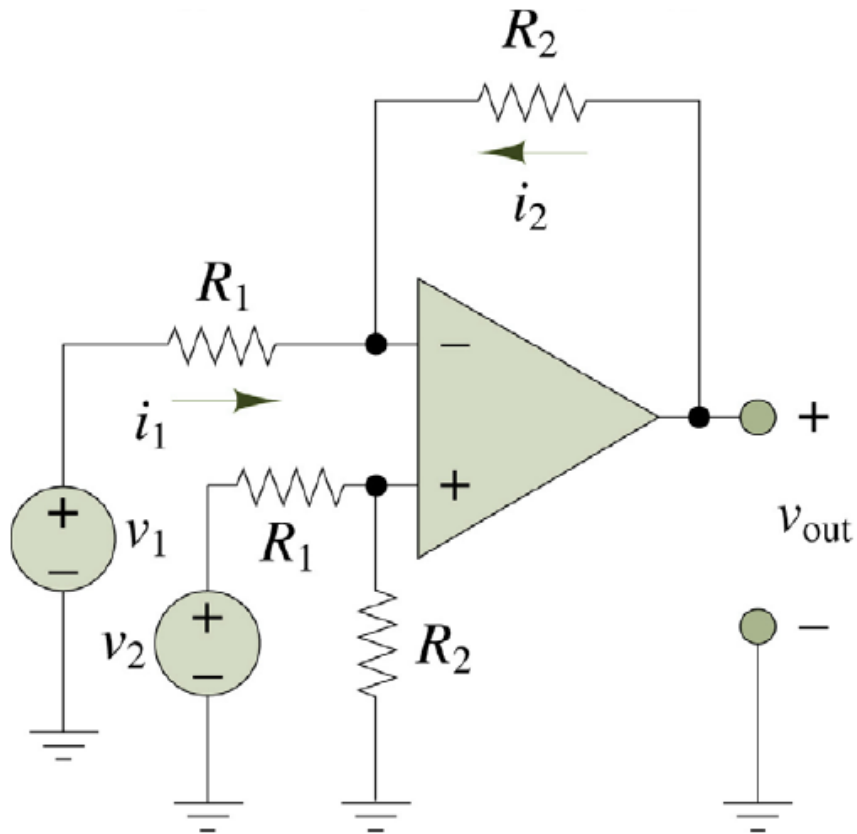
input impedance = ∞

output impedance = 0

Useful interface between different circuits:

Has minimum effect on previous and next circuit in signal chain

Differential Amplifier (subtractor)



$$i_1 + i_2 = 0$$

$$\frac{v_1 - v^-}{R_1} = - \frac{v_{out} - v^-}{R_2}$$

$$v^- = v^+$$

$$v^+ = \frac{R_2}{R_1 + R_2} v_2 = v^-$$

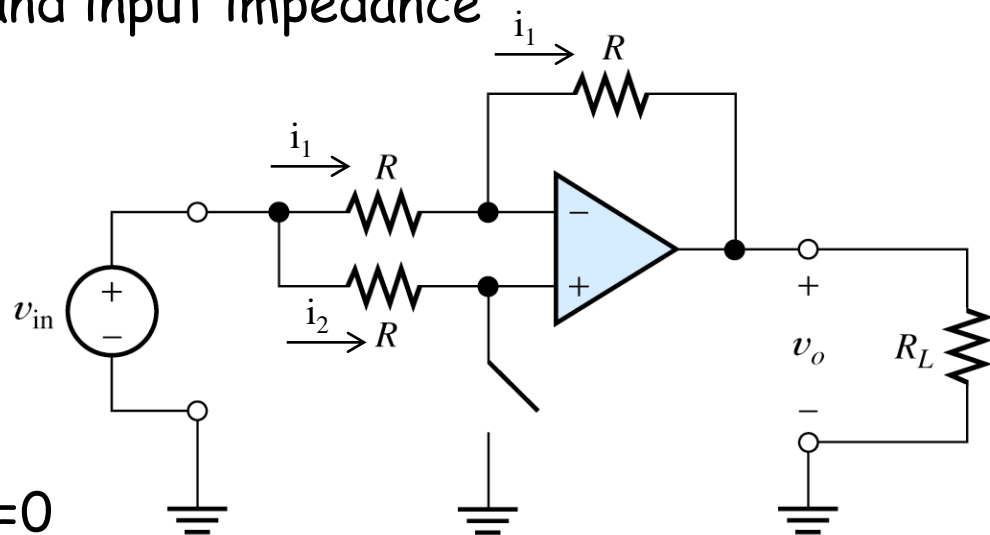
$$v_{out} = \frac{R_2}{R_1} (v_2 - v_1)$$

Exercise

Find voltage gain $A_v = v_o / v_{in}$ and input impedance

a. With the switch open

b. With the switch closed



a. With the switch open

$$i_2 = 0 \text{ and } i_1 R = i_2 R \Rightarrow i_1 = 0$$

$$\text{so } v_{in} = v_o \text{ and } A_v = v_o / v_{in} = 1$$

Input impedance:

$$Z_{in} = v_{in} / i_{in} = v_{in} / 0 = \infty$$

Exercise

Find voltage gain $A_v = v_o / v_{in}$ and input impedance

- With the switch open
- With the switch closed**

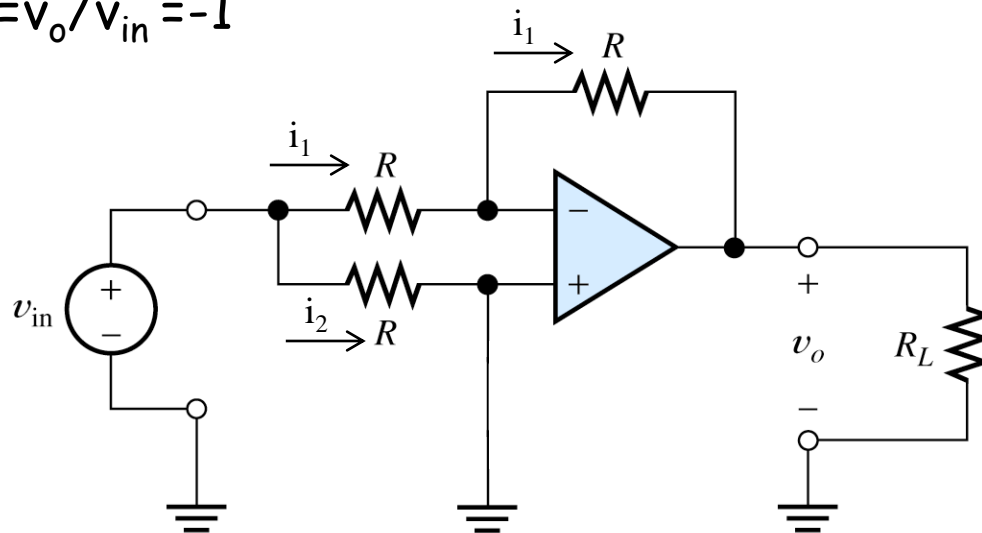
b. for closed switch: $i_2 = v_{in} / R$

and $i_1 * R = i_2 * R \Rightarrow i_1 = i_2$

$$v_{in} = i_1 * R + i_1 * R + v_o$$

so $v_{in} = v_{in} / R * R + v_{in} / R * R + v_o \Rightarrow -v_{in} = v_o$

and $A_v = v_o / v_{in} = -1$



Exercise

Find voltage gain $A_v = v_o / v_{in}$ and input impedance

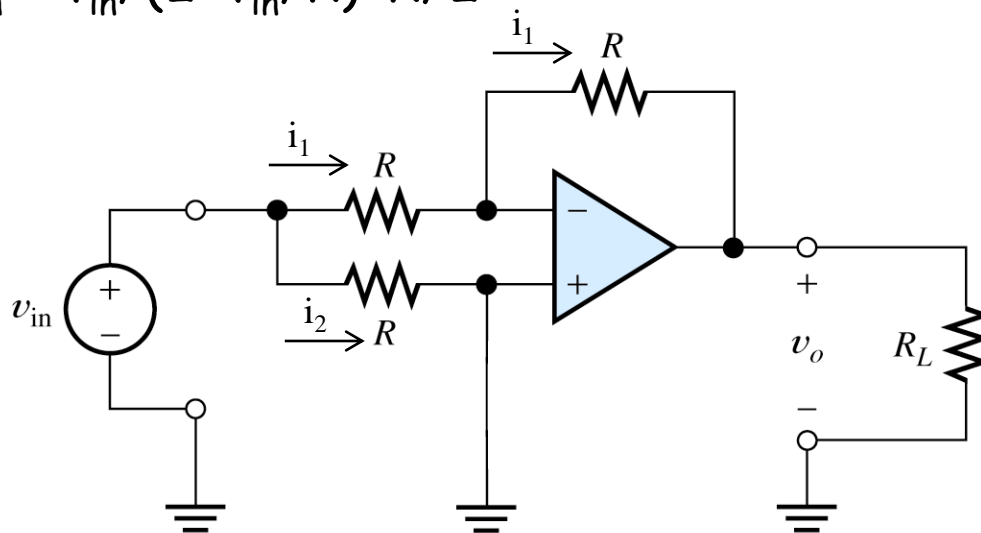
- With the switch open
- With the switch closed**

b. $i_2 = v_{in} / R$

Input impedance: $Z_{in} = v_{in} / i_{in}$
 $= v_{in} / (i_1 + i_2)$

and $i_1 = i_2 \Rightarrow$

$Z_{in} = v_{in} / i_{in} = v_{in} / (2 * v_{in} / R) = R / 2$



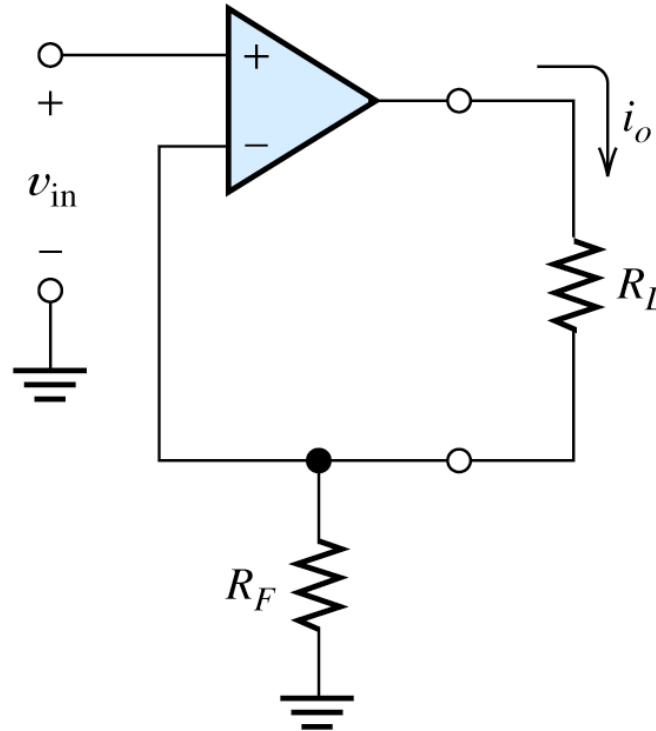
Voltage to Current Converter

Find the output current i_o as a function of v_{in}

$$v_{in} = i_o * R_f$$

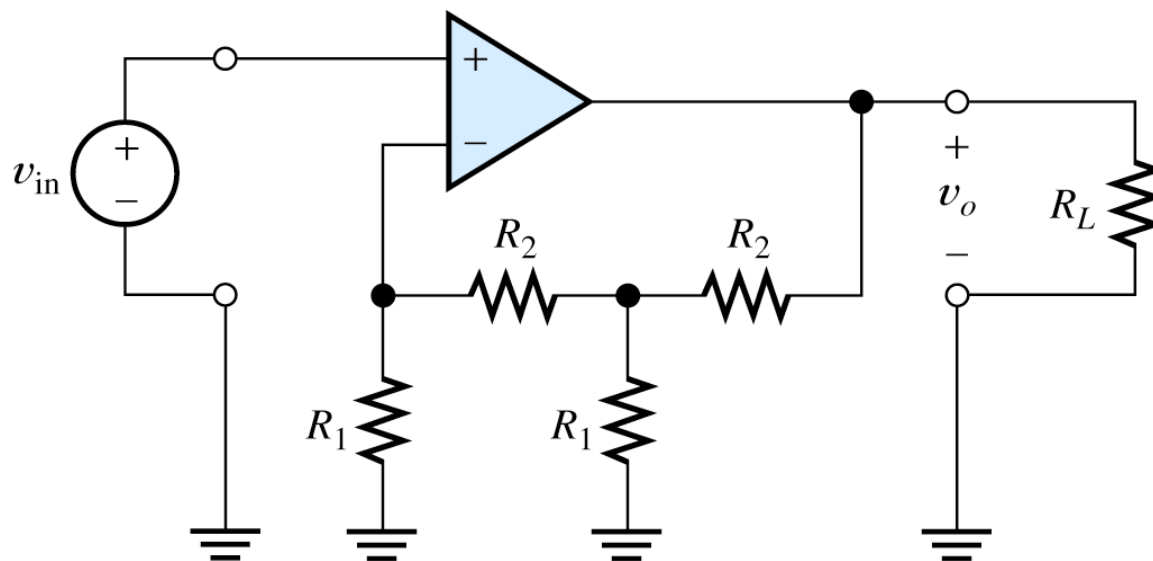
SO

$$i_o = v_{in} / R_f$$



Exercise

- a) Calculate the voltage gain v_o/v_{in} for $R_1=10\text{ k}\Omega$, $R_2=100\text{ k}\Omega$
- b) Find the input resistance



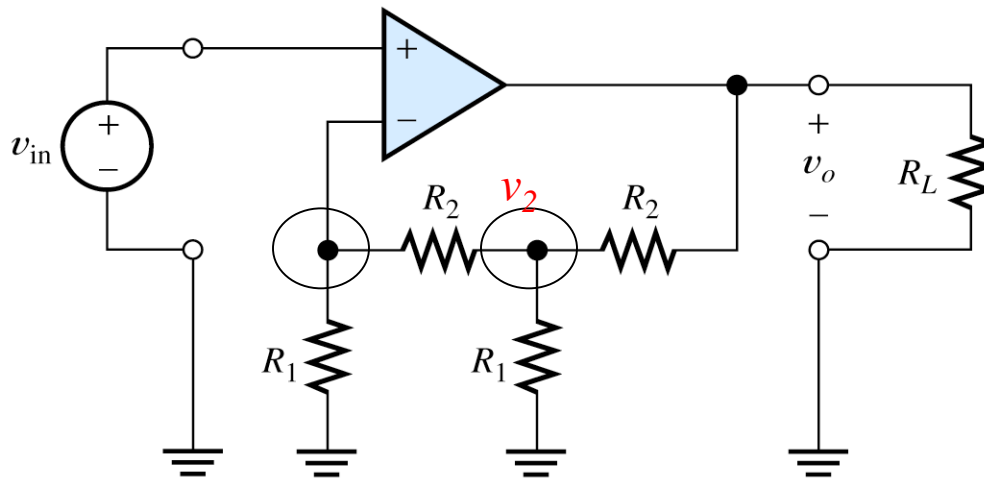
Exercise

- a) Calculate the voltage gain v_o/v_{in} for $R_1=10\text{k}\Omega$, $R_2 = 100\text{k}\Omega$
 b) Find the input resistance

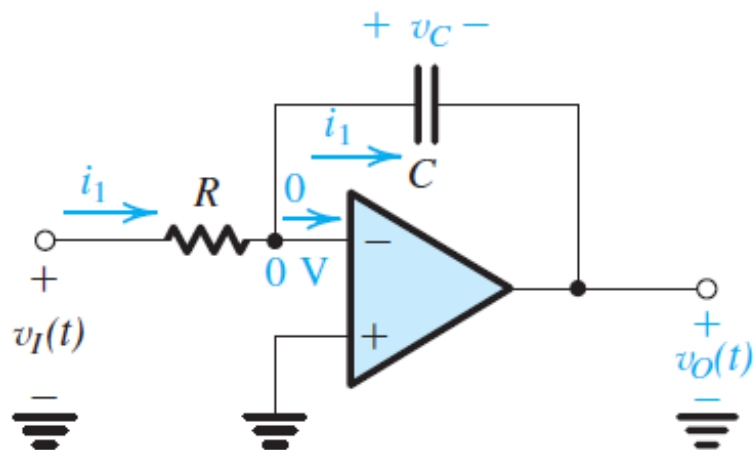
From KCL1: $v_{in}/R_1 + (v_{in}-v_2)/R_2=0 \Rightarrow v_2= v_{in} (1+ R_2 /R_1)=11v_{in}$

From KCL2: $(v_2-v_{in})/ R_2 +v_2/R_1+(v_2-v_o)/ R_2 =0 \Rightarrow$

$$v_o=(v_2-v_{in}) +v_2R_2/R_1+v_2 \Rightarrow v_o / v_{in} = 131$$



Op-amp integrator



$$i_1 = \frac{v_i - v_-}{R} = \frac{v_i}{R}$$

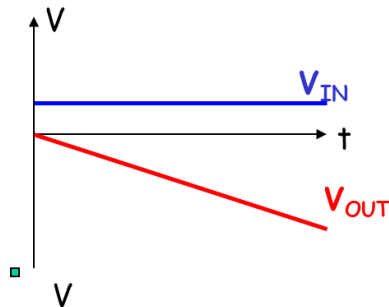
$$i_1 = i_C = C \frac{dv_C}{dt} = C \frac{dv_O}{dt}$$

Combining the 2 Eq.s
and integrating

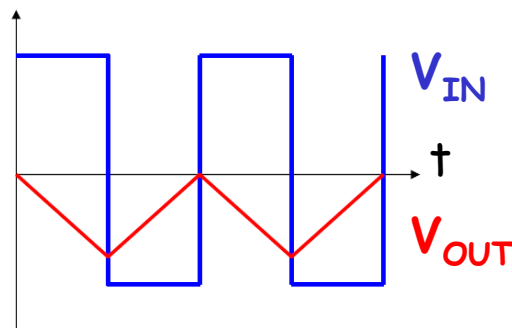
$$C \frac{dv_O}{dt} = \frac{v_i}{R}$$

$$V_{\text{out}} = \int_0^t -\frac{V_{\text{in}}}{RC} dt + V_{\text{initial}}$$

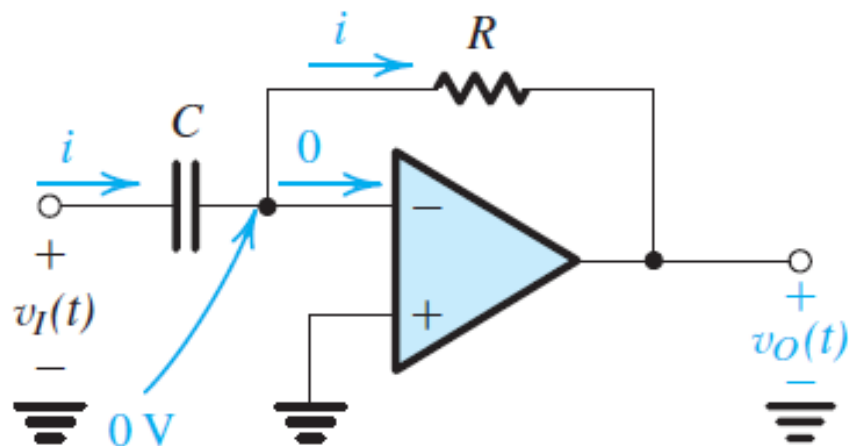
Integrator response to a
constant voltage:



What's the integrator
response to a square
wave?



Differentiating Op-Amp



$$i = i_C = C \frac{dv_C}{dt} = C \frac{dv_i}{dt}$$

$$i = \frac{v_- - v_o}{R} = -\frac{v_o}{R}$$

Combining the 2 Eq.s

$$C \frac{dv_i}{dt} = -\frac{v_o}{R}$$

$$v_o = -RC \frac{dv_i}{dt}$$

Op-Amp Imperfections in a Linear Mode

We consider the following op-amp imperfections:

Input and output impedances:

Ideal opamp $R_{in} = \infty$; $R_{out} = 0\Omega$

Real op-amp has $R_{in} = 1M\Omega - 10^{12}\Omega$;

$$R_{out} = 1\Omega - 100\Omega$$

Nonlinear Limitations

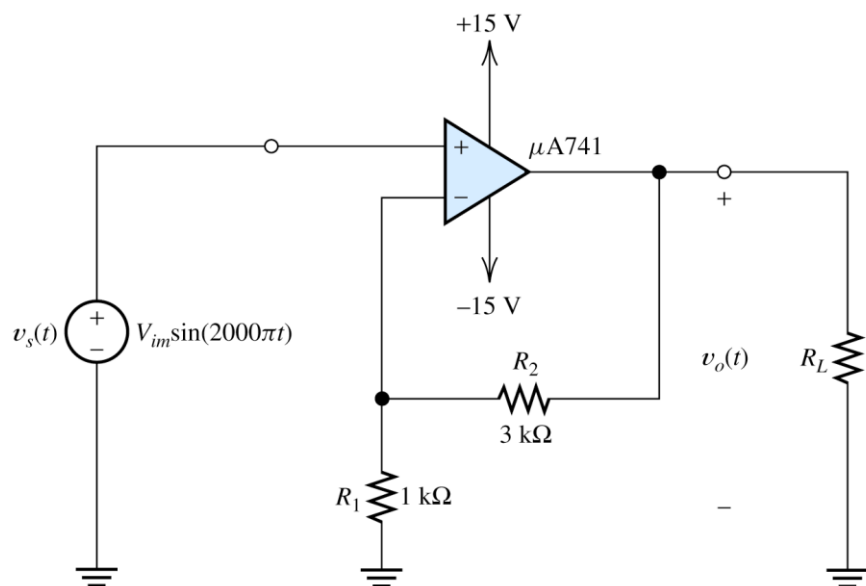
Nonlinear limitations:

Output voltage swing is limited and depend on power supply voltage for

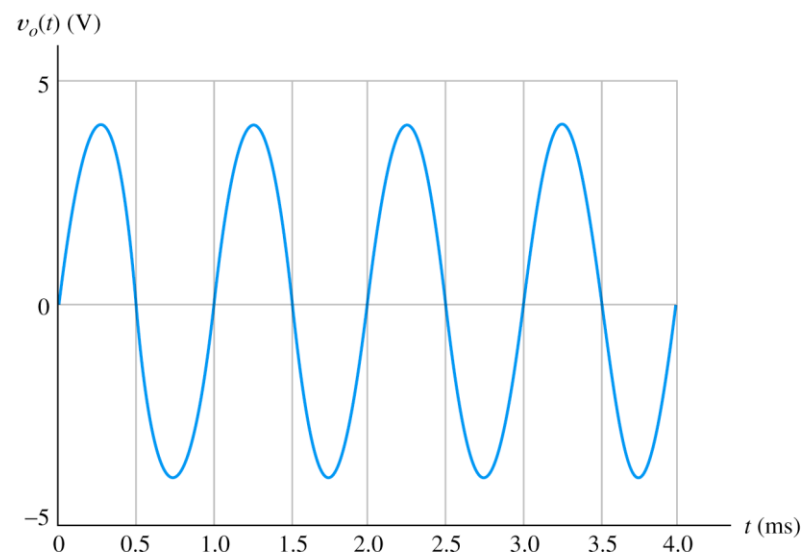
$$V_{DD} \in (-15V, +15V), \quad v_o(t) \in (-12V, +12V)$$

Maximum output current is limited

for $\mu A741$ amplifier $i_o(t) \in (-40mA, +40mA)$



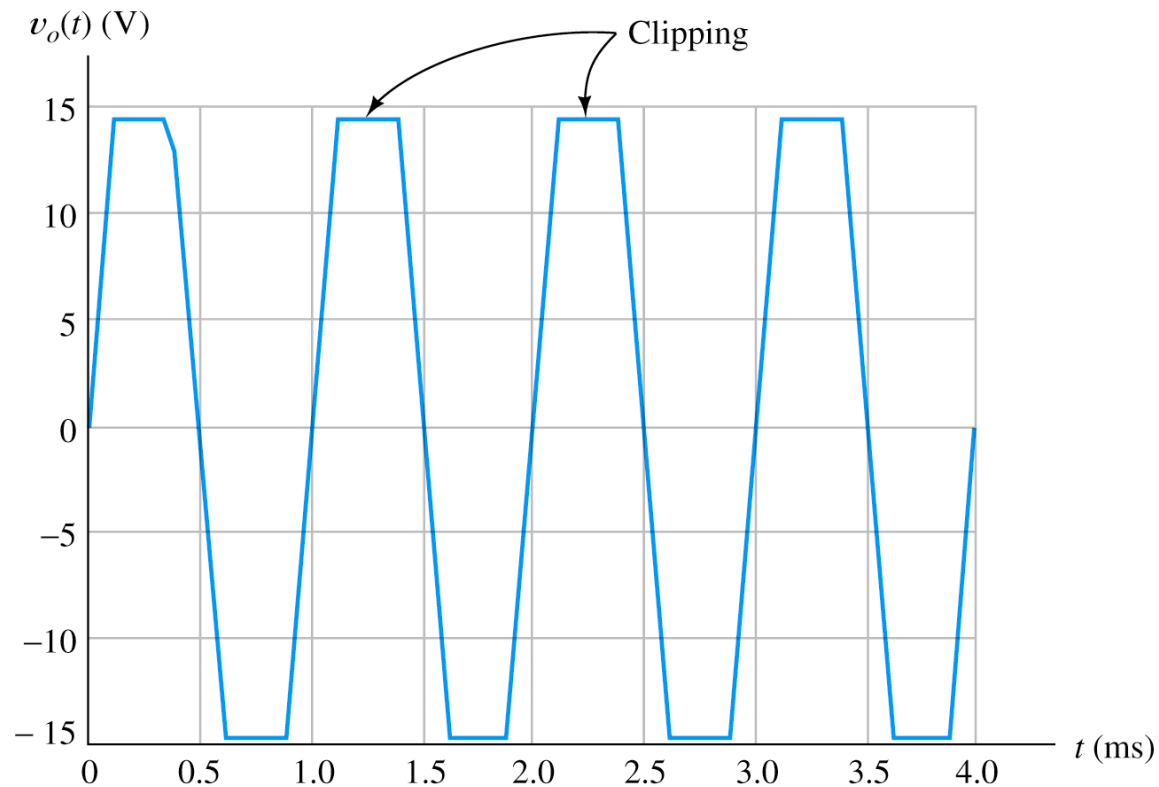
Noninverting amplifier used to demonstrate various nonlinear limitations of op amps.



Output of the circuit of Figure 14.23 for $R_L = 10 \text{ k}\Omega$ and $V_{im} = 1 \text{ V}$. None of the limitations are exceeded, and $v_o(t) = 4v_s(t)$.

Nonlinear Limitations

When voltage or current limits are exceeded, clipping of the output signal occurs causing large nonlinear distortions



Nonlinear Limitations

Another nonlinear limitation is **limited rate of change** of the **output signal** known as the **slew-rate limit SR**

$$\left| \frac{dv_o}{dt} \right| \leq SR$$

Using slew rate (SR), we can find maximum frequency known as full-power bandwidth.

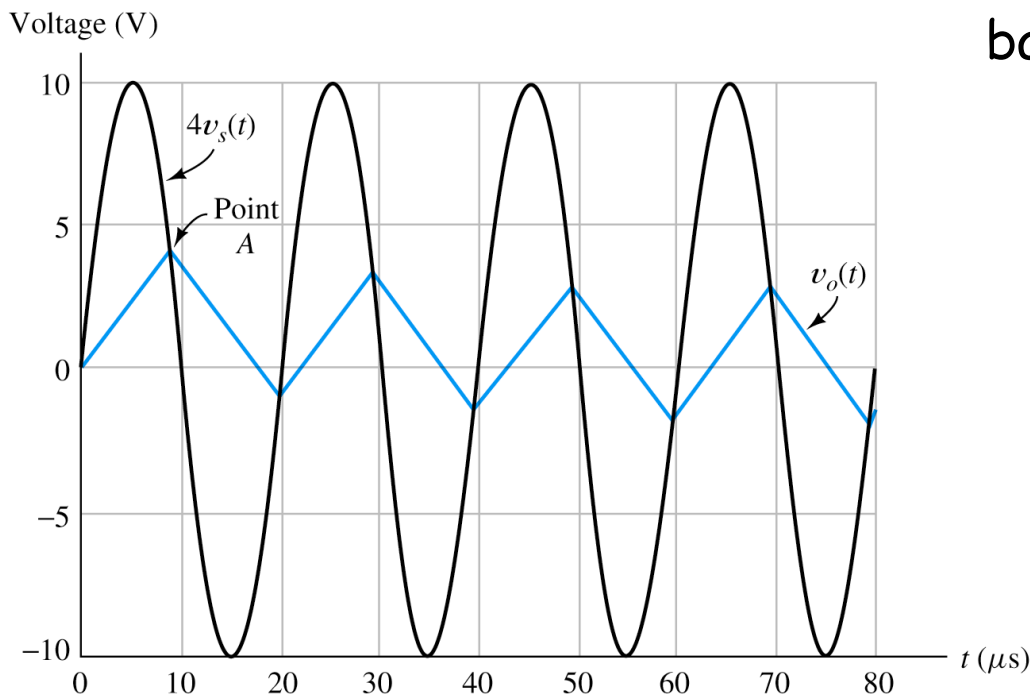
Assuming:

$$v_o(t) = V_{om} \sin(\omega t)$$

$$\frac{dv_o}{dt} = \omega V_{om} \cos(\omega t) \leq$$

$$\leq 2\pi f V_{om} \leq SR$$

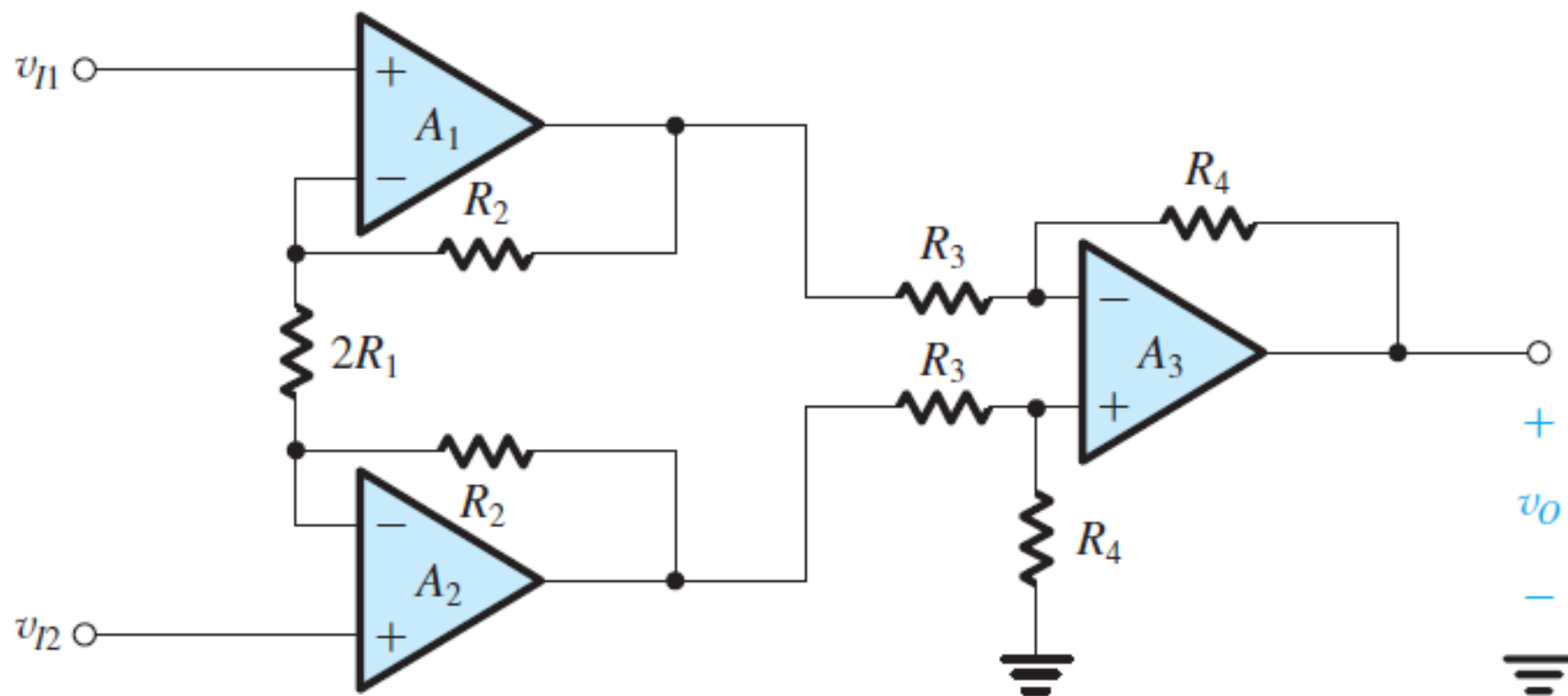
So the **full-power bandwidth**



maximum frequency

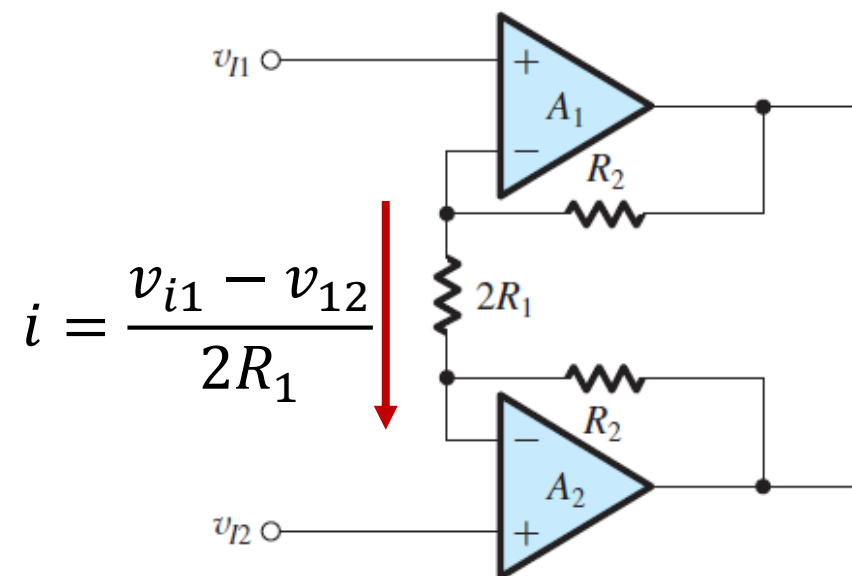
$$f_{FP} \leq \frac{SR}{2\pi V_{om}}$$

Instrumentation Amplifier



Instrumentation Amplifier -First Stage

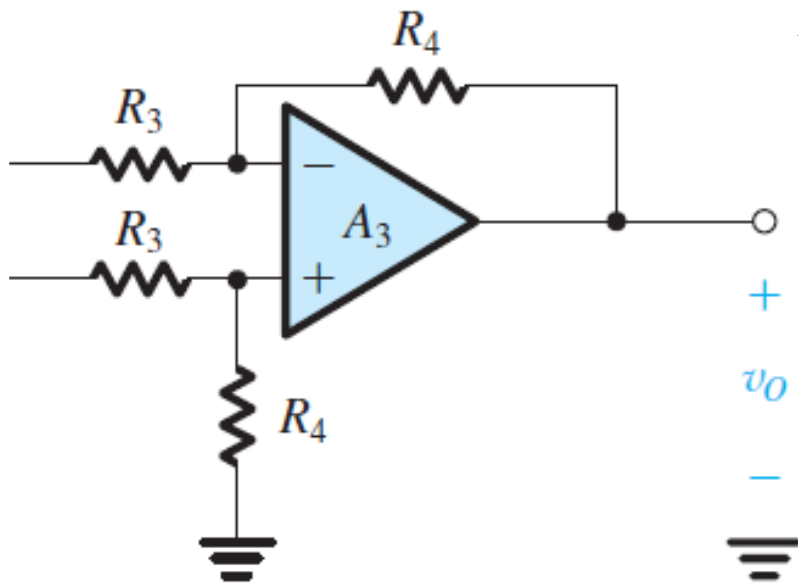
$$v_{o1} - v_{o2} = 2i(R_1 + R_2) = 2 \frac{v_{i1} - v_{i2}}{2R_1} (R_1 + R_2)$$



$$v_{o1} - v_{o2} = \frac{R_1 + R_2}{R_1} (v_{i1} - v_{i2})$$

$$A_d = \frac{v_{o1} - v_{o2}}{v_{i1} - v_{i2}} = \frac{R_1 + R_2}{R_1} = 1 + \frac{R_2}{R_1}$$

Instrumentation Amplifier - Second Stage

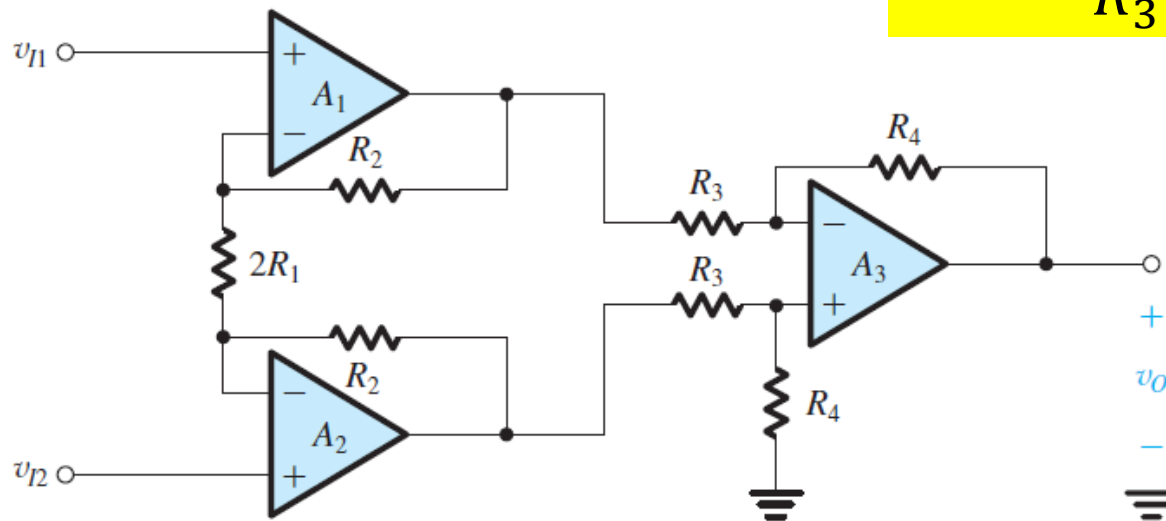


$$v_o = -\frac{R_4}{R_3} v_{o1} + \frac{R_4}{R_3 + R_4} \left[\frac{R_4}{R_3} + 1 \right] v_{o2}$$

$$v_o = -\frac{R_4}{R_3} [v_{o1} - v_{o2}]$$

Instrumentation Amplifier - Both Stages

$$v_o = -\frac{R_4}{R_3} \left(1 + \frac{R_2}{R_1} \right) [v_{i1} - v_{i2}]$$



$$v_{o1} - v_{o2} = \frac{R_1 + R_2}{R_1} (v_{i1} - v_{i2})$$

$$v_o = -\frac{R_4}{R_3} [v_{o1} - v_{o2}]$$