

MAT281E – Extra Final Exam – Part 1, Spring 2020, Duration: 30 Minutes

Instructions:

- Do NOT communicate with other people, including your friends, classmates, and family members!
- This is an open-book exam. Give your answers in English.
- Write the question number, your Name and İTÜ ID on the top of each page and **sign all pages**.
- Scan or take photo of your answers and upload them on Ninova within a **zip** file **before the deadline!**
- You will have 15 minutes to upload your answers on Ninova. **Accepted file formats** are *.pdf, *.jpeg, or *.png!

Q1) (20 pts) True/False. For each of the following statement please circle T (True) or F (False).

- T or F? The projection of a vector \mathbf{v} to a subspace W is neither inside W nor W^\perp .
- T or F? $T(x) = \pi^3 x$ is a linear transformation from \mathbb{R} to \mathbb{R} .
- T or F? If Q is an orthogonal matrix then $(Q^T x) \cdot (Q^T y) = x \cdot y$.
- T or F? Let A be $m \times n$ matrix, the $\text{rank}(A) = \text{rank}(A^T)$.
- T or F? Every system with two equations in three unknowns has infinitely many solutions.

Q2) (30 pts) Let $A = \begin{bmatrix} -3 & 6 & -1 & 1 & -7 \\ 1 & -2 & 2 & 3 & -1 \\ 2 & -4 & 5 & 8 & -4 \end{bmatrix}$ matrix.

- Find a basis for the null space of A .
- Find a basis for the column space of A .
- Determine the $\text{rank}(A)$?

Name:_____ İTÜ ID:_____ Signature:_____.

Use matrix $A = \begin{bmatrix} 1 & 3 \\ 1 & -1 \end{bmatrix}$ to solve following problems.

Q3) (25 pts) Find bases for the eigenspaces of A by explicitly showing eigenvalues and eigenvectors.

Q4) (25 pts)

a) (15 pts) What are geometric and algebraic multiplicities of A ? Explain why?

b) (10 pts) Does matrix A diagonalizable? Prove your answer!