
BLG 322E - COMPUTER ARCHITECTURE

Quiz 1

Q-1 SOLUTION:

a)

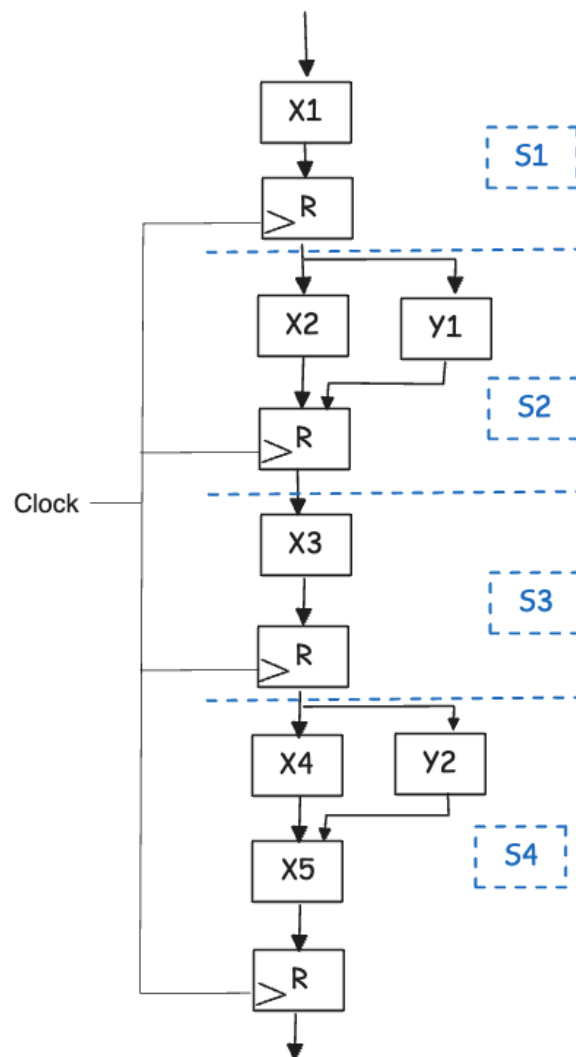


Fig. 1: Pipeline with 4 stages.

We want the highest possible speedup (i.e. the smallest pipeline “cycle”) while using the minimum number of registers (each register adds a 5 ns overhead).

- **Stage 1:** X1
 - Logic = 20 ns.
 - With register: 20+5=25 ns.
- **Stage 2:** X2 // Y1
 - Logic = max(15,25)=25 ns.

- With register: $25+5=30$ ns.
- **Stage 3: X3**
 - Logic = 20 ns.
 - With register: $20+5=25$ ns.
- **Stage 4: Must do (X4 // Y2) and then X5.**
 - $X4 // Y2 = \max(20,10)=20$, but X5(5 ns) must wait for both to finish.
 - So serially in one stage: $20 + 5 = 25$ ns of logic.
 - With register: $25+5=30$ ns.

Hence the four stages have lengths of 25, 30, 25, 30 ns.

- The pipeline “cycle time” is the longest = 30 ns.

b) All clock cycles are synced to t_p , so the total execution time is

$$T_1 = k \cdot t_p = 4 \cdot 30 = 120 \text{ ns.}$$

c) Non-Pipelined Time;

1. **X1:** 20 ns
2. **X2 // Y1:** $\max(15,25)=25$ ns
3. **X3:** 20 ns
4. **X4 // Y2:** $\max(20,10)=20$ ns
5. **X5:** 5 ns

Hence one complete task takes

$$t_n = 20 + 25 + 20 + 20 + 5 = 90 \text{ ns.}$$

Infinite-Stream Speedup;

- **Non-Pipelined:** 90 ns per task.
- **Pipelined:** once “filled,” it completes one task every 30 ns.

Thus, for an infinite number of tasks,

$$\text{Speedup} = 90 / 30 = 3.$$

Q-2 SOLUTION:

a) The total clock cycles = (number of A x CPI_A) + (number of B s CPI_B) + (number of C x CPI_C).

For S1:

$$\text{Cycles } S1 = 3 \times 1 + 2 \times 2 + 1 \times 5 = 3 + 4 + 4 = 11 \text{ cycles.}$$

For S2:

Cycles S2 = $2 \times 1 + 3 \times 2 + 2 \times 4 = 2 + 6 + 8 = 16$ cycles.

Hence, S1 is faster overall, even though S2 uses only one more instruction. The reason is that S2 has more B and C instructions, which have higher CPI values, driving up its total cycle count.

b) The effective CPI = (total clock cycles) / (total instruction count).

S1:

Effective $CPI_{S1} = 11 \text{ cycles} / 6 \text{ instructions} \approx 1.83$.

S2:

Effective $CPI_{S2} = 16 \text{ cycles} / 7 \text{ instructions} \approx 2.29$.

Thus S1 not only finishes in fewer cycles but also has the lower effective CPI (≈ 1.83 vs. ≈ 2.29).