

Assignment 1

Problem 1 : Design Combinational Circuit

Simplify the following functions using Karnaugh Maps, draw the circuit.

1. $F(W, X, Y, Z) = \sum m(0, 2, 3, 8, 9, 10, 11, 12, 13, 14, 15)$

		YZ			
		00	01	11	10
WX	00	1	0	1	1
	01	0	0	0	0
	11	1	1	1	1
	10	1	1	1	1

$$\Rightarrow F = W + X'Z' + X'Y$$

2. $F(W, X, Y, Z) = \sum m(3, 9, 11, 12, 13, 14, 15) + \sum d(1, 4, 6)$

		YZ			
		00	01	11	10
WX	00	0	X	1	0
	01	X	0	0	X
	11	1	1	1	1
	10	0	1	1	0

$\Rightarrow F = WX + X'Z$

3. $F(A, B, C, D) = AC'D' + A'C + ABC + AB'C + A'C'D'$

$$\begin{aligned}
 F &= AC'D' + A'C + ABC + AB'C + A'C'D' \\
 &= A(C' + D') + A'C + ABC + AB'C + A'C'D' \\
 &= A(C' + D') + A'C + ABC + AB'C + A' + C' + D' \\
 &= A(C' + D') + ABC + AB'C + A' + C' + D' \\
 &= C' + D' + ABC + AB'C + A' + C' + D' \\
 &= C' + D' + ABC + AB'C + A' + D' \\
 &= C' + D' + ABC + AB'C + A' \\
 &= C' + D' + AC(B + B') + A' \\
 &= C' + D' + AC1 + A' \\
 &= C' + D' + AC + A' \\
 &= C' + D' + A + A' \\
 &= C' + D' + 1 \\
 &= 1
 \end{aligned}$$

4. $F(A, B, C, D) = A'B'C'D + CD + AC'D$

$$\begin{aligned}
 F &= A'B'C'D + CD + AC'D \\
 &= (A' + B' + C')D + CD + AC'D \\
 &= (A' + B' + C')D + D(C + AC') \\
 &= DA' + DB' + DC' + D(A + C) \\
 &= DA' + DB' + DC' + DA + DC \\
 &= D(A + A') + DB' + DC' + DC \\
 &= D1 + DB' + DC' + DC \\
 &= D + DB' + DC' + DC \\
 &= D + DC' + DC \\
 &= D + DC \\
 &= D
 \end{aligned}$$

Promblem 2 : Design Sequential Circuit

Current State (S)	Next State (S')		Output (Z)
	X=0	X=1	
A	F	B	0
B	A	F	1
C	A	D	1
D	F	E	0
E	D	B	1
F	D	E	0

For the given state table, design the circuit for FSM using JK Flip-Flop.