### Causality and directed acyclic graphs

# Get to know and have some intuition about

- Causality in philosophy (of science)
- Conditional independence relations
- Causal discovery algorithms
- Confounds and back doors



David Hume (1711-1776)



Aristotle (384 - 322 BC)



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Example: a person has eyes to see



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- Evolution: we have eyes to find and hunt for food



Form follows from the goal of the object

Aristotle (384 - 322 BC)

- Example: a person has eyes to see
- Evolution: we have eyes to find and hunt for food
- But: how do you know the goal and what is its purpose



René Descartes (1596 – 1650)



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Naturalism: Explanation of phenomena in terms of physical objects



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Naturalism: Explanation of phenomena in terms of physical objects

- Example: the dials of a clock rotate by cogwheels and springs
- Divide mechanism into parts
- Not of mental processes like memory



Carl Hempel (1905 - 1977)

Logical positivists



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Logical positivists

Deductive-nomological model



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#### Logical positivists

Deductive-nomological model

- $C_1, \ldots, C_k$  (circumstances)
- $L_1, \ldots, L_n$  (laws)
- ⊢ E (explanandum)



Logical positivists

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Necessarily true if C and L are true.



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Deductive-nomological model

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Carl Hempel (1905 – 1977)

- Necessarily true if C and L are true.
- The basis for all sciences are laws and logical deductions.

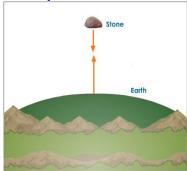


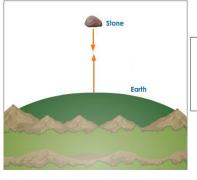
Isaac Newton (1643 - 1727)

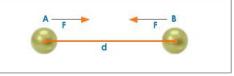


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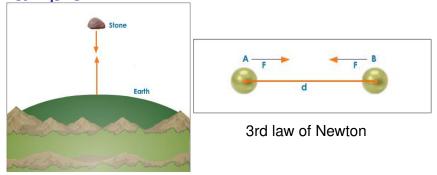
You can fall back on the laws of Newton



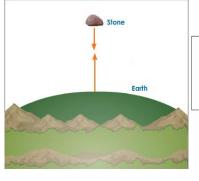


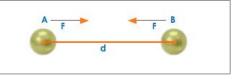


3rd law of Newton



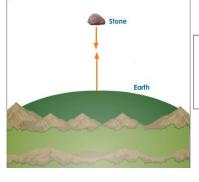
 $\bullet$  C: we are in the gravitational pull of the earth

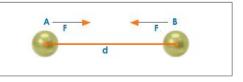




3rd law of Newton

- C: we are in the gravitational pull of the earth
- L: 2nd and 3rd laws of Newton

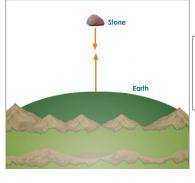


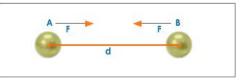


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$$F = ma$$
 and  $F = \frac{gm_1m_2}{d^2}$ 





3rd law of Newton

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 and  $F = \frac{gm_1m_2}{d^2}$ 

+ the rock falls to the earth

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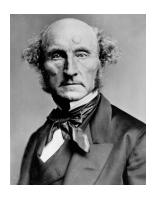
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- But it is a causal relation? That could be, but what is causality....
- This is what we need to figure out. It is the key to providing an explanation.

#### Causal relation and laws

#### John Stuart Mill's conditions

- A always co-occurs with B
- A occurs before B
- There is no alternative explanation for the co-occurrence of A and B

But this was unsatisfactory because A does not always occur with B; no universality.



John Stuart Mill (1806-1973)

### Probabilities enter the stage

 Probability is essential to replace 'universal laws'
 Example

```
P(\text{catch fish} \mid \text{fishing rod}) \ge
P(\text{catch fish} \mid \text{no fishing rod})
```

 Conditional independence relations are the key to causal relations Example

```
P({
m shark \ bite \ | \ ice \ cream}) \geq
P({
m shark \ bite \ | \ no \ ice \ cream})
P({
m shark \ bite \ | \ ice \ cream, \ hot \ weather}) =
P({
m shark \ bite \ | \ hot \ weather})
```



Hans Reichenbach (1891-1953)

#### Probabilities enter the stage

 Conditional independence relations are the key to causal relations Example

> P(shark bite | ice cream, hot weather)= P(shark bite | hot weather)

 'Screening off': search for nonredundent and sufficient 'variables' that define the relation (statistically relevant)



Wesley Salmon (1925-2001)

#### Probabilities enter the stage

- Spirtes and Glymour: Use screening off principle to identify unique relations from data
- Pearl: Semantics for difference between 'see' and 'do' Example



Judea Pearl (1936-)



 $P(\text{catch fish} \mid \text{rod}) \neq P(\text{catch fish} \mid \text{do(rod)})_{i}^{l}$ 

Peter Spirtes (1956-)

Causality definition:



 $E(\text{catch fish}) \neq E(\text{catch fish} \mid \text{do(rod)})$ 

Clark Glyfflour (1942-)