

# EFFICIENT E-PAYMENT PROTOCOL USING HASH CHAIN

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## Abstract

*The **spreading** of information in the last decade has led to great development in e-commerce. For instance, e-trade and e-bank are two main Internet services that implement e-transaction from anyplace in the world. This helps merchant and bank **speed up** the financial transaction process and to give user **instant** services at any time. However, the cost of workers and communications falls down considerably while the cost of trusted authority and protecting information is increased. E-payment is now one of the most central research areas in e-commerce, mainly regarding online and offline payment scenarios. In this paper, we will discuss an important e-payment protocol namely pay-word scheme examine its advantages and **limitations**, which encourages the authors to develop **an improved** scheme that **keeps** all characteristics intact without concession of the security robustness of the protocol. The suggest protocol employs the idea of public key encryption scheme using the thought of hash chain. We will compare the proposed protocol with pay-word protocol and demonstrate that the proposed protocol offers more security and efficiency, which makes the protocol workable for real world services.*

**Keywords** e-payment protocol, public key cryptography, signature scheme, blind signature scheme, over-spending, e-commerce

## 1. INTRODUCTION

With the increasing impact of intangible merchandise in worldwide economies and their immediate delivery at small cost, traditional payment systems tend to be more costly than the modern methods. Online processing can be worth of value smaller than the smallest value of money in the manual world. However, there are two methods of running e-payment systems.

**Online payment:** in which vendor checks the payment send by purchaser with a bank before serving the purchaser.

**Offline payment:** in which over spending must be detected, and consequently, no online link to the bank is needed.

The e-payment schemes [1] can be sub-divided into two groups according to the online assumptions.

- Payments by transaction method: in which single payment does not need previous arrangements between purchaser and vendor.
- Payments by account method: in which purchaser and vendor should have system account with bank and certain type of agreement between both before carrying out the real payment transaction.

The payment by transaction can further be divided into two subgroups.

- The credit card payment transaction: is tailored for large charge payment of some hundreds or even thousands of dollars. In contrast, net money transaction is usually low value payment with difficult transaction cost and online features, similar to the thought of the e-payment transaction. The drawback of the credit card payment transaction is the fee of transactions, particularly from the perspective of the vendor that have to pay some invoices to the clearing house according to the

contract agreement with them. This certainly will have straight impact on the cost policy and the interest between the possible users.

- The e-payment by small value transactions on service: This is acquiring certain interest from the area of research. A number of important services of e-payment are e-publishing and multimedia service. In these services, due to the small transaction amount, the merchant acquires relatively shopping mall revenue from every transaction.

As a result, expensive calculations such as digital signature should be limited in order to reduce the investments in software applications. In the recent years, e-payments [2, 3, 4, 5] offering a relatively key improvement in the online revenue malls. The foundation of e-payments is to take benefit of the high level of viewers by present content for a low price. Other alternative of this thought is to rating fractions of cents for equally fractional contents sums. The main features in e-payment protocol are less charges of payment amount and high occurrence of transactions on the e-commerce system.

## 2. E-PAYMENT PROTOCOL REQUIRMENTS

The e-payment protocol encompasses three participants **which are as follows**:

**User**: The user (customer) purchases e-currency from the bank employing actual money by e-payment. The user can then utilize e-currency to carry out e-payment to buy goods.

**Merchant**: The merchant is the data storage which provides user with both services and information.

**Bank**: The bank is the trusted authority. It mediates between user and merchant in order to ease the duties they carry out. In general, the bank acts like a broker offers the e-coins for the e-payments.

While using e-currency, a shared set of characteristics for an e-payment protocol is:

- Anonymity: e-cash must not supply any user with information; it means that it must be anonymous e-currency transaction.
- Divisibility: e-cash can be sub-divided since the notes have a basic piece.
- Transference: e-cash can be transferred to a trusted authority by providing the suitable amount of currency.
- Over spending detection: e-cash must be used for only once.

The e-payments are stored and then converted to digital type. This will cause new difficulties during the developing secure e-payment protocol. The payment is simply be duplicated against the conventional physical paying methods. As the digital payment is characterized as simple sequences of bits, nothing in them stops them copying. When a security of the payment protocol is reliant on the method the payments are hidden from unknown. Every individual that can have access to payments maybe utilize them numerous times. We notice that getting anonymous cash transaction is an essential issue, and at the same time giving efficiency is another matter. In this paper, we study a merchant pay-word protocol [6]; that gives anonymity characteristic using the idea of blind signature scheme and hash chain. We then proposed a blind signature scheme that will be used in the protocol for reaching better efficiency without concession its security characteristics. Therefore, before discussion the rest of this paper, we will list the notation used **as follows**.

$U$  : User

$M$  : Merchant

$B$  : Bank

$p, q, x$  : **Prime numbers**

$n$  : **Public modulus (product of  $p * q$ )**

$ID_E$  : Identity of entity  $E$ , such that  $E \in \{U, M, B\}$

$A_E$  : Address of entity  $E$

$m$  : Message

$\oplus$  : **XOR Addition operation exclusive or**

$PK_E$  : Public key of entity  $E$

$SK_E$  : Private Key of entity  $E$   
 $K$  : Secret key of bank  $B$   
 $P$  : A generator point on elliptic curve  
 $r_E$  : Arbitrary number selected by entity  $E$   
 $C_U$  : User certificate  
 $CE_U$  : User certificate expiry information  
 $I_U$  : User certificate serial number credit card information  
 $OI$  : Order information (category, amount, etc)  
 $EI_R$  : Expiry information for redemption  
 $h$  : Secure hash function  
 $\parallel$  : Concatenation

### 3. RELATED WORKS

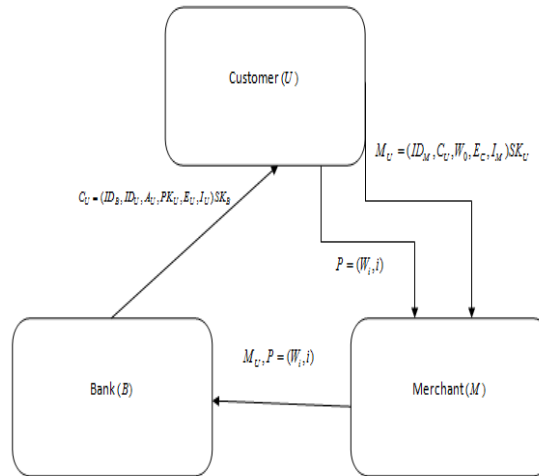
In 1988 Chaum, Fiat and Naor proposed their protocol entitled untraceable electronic cash [7] which is relied on a single use token method. The user creates blinded e-bank currency note and passes it to the bank to be signed using bank public key. The bank signs the currency note, subtracts the value from the user account, and returns the signed currency note back to the user. The user removes the blind thing and utilizes it to buy goods from the super market. The super market checks the authenticity of the bank currency note using the bank public key and passes it to the bank where they are verified contrary to a list of currency note already used. The amount is deposited into the supermarket account, the deposit approved, and the supermarket in turn emits the merchandise. In 1995, Glassman, Manasse, Abadi, Gauthier and Sobalvarro present their protocol entitled "The Millicent protocol for inexpensive electronic commerce"[8] which is a decentralized e-payment protocol, and it allow payments as low as 1/10 of a cent. It employs a type of e-coins. It is introduced to make the cost of committing a fraud, more than the cost of the real transaction. It utilizes asymmetric encryption techniques for all information transactions. Millicent is a lightweight and secure scheme for e-commerce through the internet. It is developed to support to buy goods charging less than a cent. It is relied on decentralized validation of e-currency at the seller server without any further communication, costly encryption, or off-line processing. Also, in 1997, Rivest suggested his protocol entitled "Electronic lottery tickets as e-payments" [9]. In this protocol there is a possibility to reduce the number of messages engaged with every transaction. Also, the lottery ticket scheme is relied on the assumption that financial agents are risk-neutral and will be satisfied with fair wagers. In 1998, Foo and Boyd proposed another protocol called "A payment scheme using vouchers" [10]. The e-vouchers can be moveable but the direct exchange between purchasers and vendors is impossible. As a result, a financial agent is needed and this will raise the transactions charges of exchange. However, during the last decade several new e-payment protocols [11, 12, 13] have been suggested. In this section, we will discuss pay-word protocol which is an efficient and flexible protocol [6].

### 4. THE PAY-WORD PROTOCOL

In 2001, Rivest and Shamir [6] introduced the "Pay-word and MicroMint: Two simple e-payment protocols", which is a credit-typed protocol. The protocol employs RSA public key cryptography [14] and the idea of hash chain [15]. In the pay-word protocol, if a registered user  $U$  requests the merchant  $M$  for a service, he should generate a pay-word chain that works as cash made due to a merchant  $M$ . The merchant  $M$  then must check if the user  $U$  is authorized and the pay-word (cash of the pay-word protocol) chain is created by the user  $U$ .

Afterward, the merchant  $M$  gathers user pay-word and redeems the payment from the bank  $B$ . The pay-word protocol decreases the number of on-line connections between bank  $B$  and merchant  $M$ , since the merchant  $M$  does not need to pay for each buy. The pay-word chain creation with size  $n$  and can be stated as  $x_i = h(x_i + 1)$ , such that  $i = n-1, n-2, \dots, 0$ . If creating the pay-word, the user  $U$  chooses an arbitrary number  $x_n$ , named a seed, and then  $x_n$  is hashed iteratively in reverse order until the root of the chain  $x_0$  is created. Throughout shopping, the user  $U$  in order from  $x_1$  to  $x_n$  releases pay-word, and the merchant  $M$  checks it simply by hash process.

Pay-word is a merchant  $M$  certain payment protocol, namely the pay-word chain is spent only to a specific merchant  $M$ . If a user  $U$  contacts a new merchant  $M$  for ordering service, besides making a new chain, the user  $U$  should pass a commitment to merchant  $M$ . The commitment includes the identity of the merchant  $M$ , the certificate published by the bank  $B$ , the root of an unused chain, the present date and other information. To implement continuous transactions, the user  $U$  pays pay-word within the chain which belongs to the merchant  $M$ . Following a suitable time, the merchant  $M$  will contact with the bank  $B$  to order redemption. For every chain, the merchant  $M$  passes the newest pay-word he received and the user  $U$  commitment to the bank  $B$ ; so, hashing from newest pay-word to the root of the chain can validate the rightness of transactions. When the validating is correct, the bank  $B$  debits user  $U$  account with the used size of the chain and credits merchant  $M$  account with the same amount. We show the transaction operation of the pay-word protocol in Figure 1.



**Figure 1: Transaction operation of the pay-word protocol**

Remarks: pay-word is developed as a credit-based scheme. It takes benefit of hash chain to ensure time efficiency, and reaches non-denial for every payment belonging to the same chain by just one signature. After receiving a certificate, a user is authorized to transact with a merchant in a specified amount without the online communication to bank, which reduces the communication and the risk of the bank becoming a bottleneck, provides the user more flexibility. However, the scheme suffers from the following limitation. First, the pay-word is a merchant specific payment scheme; so users have to preserve set of specific information of chains corresponding to distinct merchants. Second the user has to carry out hash chain processes as many as the number of merchants every time he needs to perform business with. Third the user has to keep all the different pay-words of every merchant and the last index used for the transactions. Fourth the user could make payments exceeding his authorized credit limit.

## 5. THE PROPOSED PROTOCOL

We will suggest an efficient protocol in this section, which gives more efficiency than its present version of the pay-word scheme; we describe a bit more on this protocol in order to make a simple comparison between both. Thus, gauging the efficiency and security of the protocol will be described in section 6. However, the protocol is divided into four schemes, registration scheme, blind scheme, transaction scheme, and redemption scheme. Also, in this section, we will introduce a blind scheme using the RSA-typed blind signature [16]. We will show this improvement makes the pay-word protocol more efficient and keeping all other characteristics consistent.

### Blind Scheme

The user passes a withdrawal order to the bank prior to his order for any service from merchant. The steps of the scheme are as follows:

Step 1: Bank

- 1.1. Select secretly and randomly two large prime  $p$  and  $q$
- 1.2. Calculate modulus  $n_B = p * q$
- 1.3. Compute  $\theta(n) = (p - 1)(q - 1)$
- 1.4. Choose exponent key  $e$  where  $1 < e < \theta(n)$  and  $\gcd(e, \theta(n)) = 1$
- 1.5 Calculate private key  $w$  where  $e * w \equiv 1 \pmod{\theta(n)}$
- 1.6 Determine the public key  $(e, n_B)$  and private key  $(w, \theta(n), p, q)$

Step 2: User

- 2.1. Select arbitrary numbers  $r$  and  $u$
- 2.2. Calculate  $a = r^e * h(x_0)(u^2 + 1) \pmod{\theta(n)}$
- 2.3. Pass  $(b, a)$  to the bank

Note that information  $b$  can indicate the expiry date; the value of cash (higher limit) that the user can employ that is the funds of every hash currency.

Step 3: Bank

- 3.1. Select an arbitrary number  $x_1 < \theta(n)$
- 3.2. Pass  $x_1$  to the user

Step 4: User

- 4.1. Choose an arbitrary value  $r_1$
- 4.2. Calculate  $b_2 = r * r_1$
- 4.3. Pass  $\beta = (b_2)^e * (u - x_1) \pmod{\theta(n)}$  to the bank

Step 5: Bank

- 5.1. Calculate  $\beta^{-1} \pmod{\theta(n)}$
- 5.2. Compute  $t_1 = h(b)^w * (a(x_1^2 + 1) * \beta^{-2})^{2*w} \pmod{\theta(n)}$
- 5.3. Pass  $(\beta^{-1}, t_1)$  to the user

Step 6: User

- 6.1  $c_1 = (u * x_1 + 1) * \beta^{-1} * (b_2)^e = (u * x_1 + 1)(u - x_1)^{-1} \pmod{\theta(n)}$
- 6.2. Calculate  $s_1 = t_1 * r^2 * (r_1)^4 \pmod{\theta(n)}$

The parameter  $(b, c_1, s_1)$  is the signature on message  $x_0$ . Anybody can check this signature by verifying if  $s_1^e \equiv h(b)h(x_0)^2 * (c_1^2 + 1)^2 \pmod{\theta(n)}$

## 6. DISCUSSIONS

### 6.1. Security

The proposed protocol withstands the following threats:

### Forgery Detection

The user  $U$  gets the bank  $B$  signature on  $x_0$  prior to any transaction. The blind signature is relied on RSA scheme, which is extensively employed a secure signature scheme. Also, in order to process an accurate redemption, the merchant  $M$  should have information of the payment transaction. It is almost unfeasible for any entity to forge the user  $U$  payment without knowing the private key  $K_{UM}$  and  $K_{UM}$ .

Thus, the opponent cannot forge signature. But to successfully achieve the verification of the formula:  $s_1^e \equiv h(b) * h(x_0)^2 * (c_1^2 + 1)^2 \mod \theta(n)$ . An opponent has to calculate  $s_1$  where  $s_1 \equiv h(b)^w * h(x_0)^{2*w} * (c_1^2 + 1)^{2*w} \mod \theta(n)$  provided the results of  $h(b)$ ,  $h(x_0)$  and  $c_1$ . However, it is computationally intractable to obtain the value of  $w$  without factoring  $\theta(n)$  that is hard to solving such problem. In contrast provided  $s_1$ ,  $h(b)$  and  $h(x_0)$  it is intractable to calculate  $c_1$  where  $c_1^2 \equiv (s_1^e * h(b)^{-1} * h(x_0)^{-2})^{1/2} - 1 \mod \theta(n)$  without factoring  $\theta(n)$ . Provided  $b$  and  $c_1$ , the opponent is unable to obtain  $s_2$  where  $s_2 \equiv s_1 * h(x_0)^{-2*w} * h(x_0')^{2*w} \mod \theta(n)$  without given  $w$ . Without factoring  $\theta(n)$ , it is hard to obtain  $c_2$  where  $(c_2)^2 \equiv (s_1^e * h(b)^{-1} * h(x_0')^{-2})^{1/2} - 1 \mod \theta(n)$ . It is also hard to derive message  $x_0'$  with  $x_0' \equiv x_0 \mod \theta(n)$  where  $h(x_0) \equiv h(x_0') \mod \theta(n)$ . Thus, the opponent is unable to forge the signature.

### Over Spending Prevention

The proposed protocol adopts the same transaction scheme of the pay-word [6]. The user  $U$  sends  $(f_{UM}, (b, c_1, s_1), x_0, (x_j, z), c_d, OI, Expire)K_{UM}$  to Merchant  $M$  prior to taking service from Merchant  $M$ . The payment source  $f_{UM}$  is identical to  $h(x_j \oplus (c_d \parallel K_{UM}))$ . However, note that the  $c_d, K_{UM}$  will be different in each purchase. As a result, the bank  $B$  would be able to identify over spent payment when the user  $U$  spends twice the payment.

### Connectivity Unallowable

For any provided valid signature  $(b, c_1, s_1)$  no one except the requester can connect the signature to its preceding signing order. This means that the signer is incapable to get the connection between the signature and its equivalent signing process order.

### Multiple Payments

In the transaction scheme, the user  $U$  sends an order to the bank  $B$  to obtain  $K_{UM}$  and generates the payment transaction  $R_{UM} = h(x_j \oplus (c_d \parallel K_{UM}))$  such that  $x_j$  is the first unused payment in the sequence. As a result, each time if the user  $U$  makes a purchase  $R_{UM}$  is not the same that enables the user  $U$  to make payments with multiple merchants.

### 6.2. Efficiency

In the e-payment protocol, the profit acquired by a merchant is little in every transaction. It is unwise to check the transaction employing a complicated technique that leads the average cost of the protocol more than the profit. On the other hand, large calculation in e-payment is not wise. In order to gauge efficiency of the proposed protocol, we compare the enhanced blind scheme with the pay-word scheme [6]. The time complexity of the remaining scheme stays the same in both protocols. We employ the following notation to gauge the efficiency of the schemes.

$T_h$ : Calculation time for hash function operation

$T_a$ : Calculation time for point addition in elliptic curve or modular multiplication

$T_m$ : Calculation time for point multiplication in elliptic curve or modular exponentiation

$T_e$ : Calculation time for asymmetric key encryption

**Table 1: Time complexity in blinding scheme**

Protocol Name	Blinding Scheme
The pay-word Protocol	$5*T_h + 9*T_a + 5*T_m + 3*T_e$
Proposed Protocol	$3*T_h + 7*T_a + 3*T_m + 1*T_e$

Actually, the modular exponentiation is a costly operation in comparisons with addition or hash function operations. As a result it is simple to observe from table 1 that the proposed protocol is efficient than the pay-word protocol. Furthermore, when any entity chooses small public key  $e$ , for example 3, then the proposed protocol becomes more efficient. This makes public key operations quicker while the secret key operations remaining unchanged. In this case, when an entity uses the short public key attack, he cannot succeed with this try since every signature is being randomized by certain random numbers. So, the proposed protocol decreases expensive exponential operation and has better time efficiency.

## 7. CONCLUSION

In this paper, we described the characteristics of e-payment protocol and evaluate one of the most important e-payment protocols that relied on a hash chain. The hash chain typed scheme gives anonymity security characteristic besides to other security features of e-payment protocol. The use of the blind signature scheme and one-way hash function makes the protocol more efficient and it guarantees the payment untraceable. Though, we notice that the blind scheme of the protocol takes significantly more computing time and we present an alternate blind scheme using the RSA signature scheme that gives more efficiency than the existing protocol. While the enhanced protocol needs large key length, around 1024-bit, in comparison with 160-bit key with elliptic curve encryption scheme, but we think that time complexity and rapidity are two significant issues than storage cost, and in this situation, the proposed protocol will give major benefit to small value payments. The research work accomplished in this paper has vast future prospects and can be extended towards a substantial protocol using hash function so that the modular exponentiation and costly operation can be shunned and also similar security depth can be reached

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