

# CPT205 Computer Graphics Revision

Lecture 13 2022-23

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# **Topics covered**

Lecture	Topics
01	Introduction / Hardware and software
02	Mathematics for computer graphics
03	Graphics primitives
04	Geometric transformations
05	Viewing and projection
06	Parametric curves and surfaces
07	3D modelling
08	Hierarchical modelling
09	Lighting and materials
10	Texture mapping
11	Clipping
12	Hidden-surface removal

### **Graphics hardware and software**

#### Graphics Hardware

- Input (light, sound and vision), processing (GPU) and output devices (Data glovers, Google glass, etc.)
- Frame buffers
- Pixels and screen resolution

#### Graphics Software

- Techniques (low-level, e.g. algorithms and procedures)
- Programming library / API (OpenGL, JOGL, etc.)
- Not our focus: high level interactive systems (Maya, Studio Max, AutoCAD, etc.)

### Mathematics for computer graphics

- Computer representation of objects
- Cartesian co-ordinate system
- Points, lines and angles
- Trigonometry
- Vectors, unit vectors and vector calculations
  - Magnitude and direction
  - Form of  $\mathbf{v} = \mathbf{v}_{x}\mathbf{i} + \mathbf{v}_{y}\mathbf{j} + \mathbf{v}_{z}\mathbf{k}$
  - Dot product  $(V1 \bullet V2 = x1*x2 + y1*y2$ and  $V1 \bullet V2 = |V1| |V2| \cos(\alpha)$ , so  $\cos(\alpha) = ?$
  - Cross product  $(V1 \times V2 = |V1| |V2| \sin(\alpha)n$ , thus  $|V1 \times V2| = |V1| |V2| \sin(\alpha)$ )
- Matrices and matrix calculations
  - Dimensions (rows x columns)
  - Square, symmetric, identity and inverse matrices (if  $\mathbf{A} \times \mathbf{B} = \mathbf{B} \times \mathbf{A} = \mathbf{I}$ , then  $\mathbf{A} = \mathbf{B}^{-1}$  and  $\mathbf{B} = \mathbf{A}^{-1}$ )
  - Multiplication: condition and resultant matrix  $(\mathbf{M_1}(\mathbf{r_1}, \mathbf{c_1}) \times \mathbf{M_2}(\mathbf{r_2}, \mathbf{c_2}) = \mathbf{M_3}(\mathbf{r_1}, \mathbf{c_2})$  where  $\mathbf{c_1} = \mathbf{r_2}$

#### **Geometric primitives**

- > Transformation pipeline
- Primitives: points, lines and polygons
- > Algorithms
  - DDA (Digital Differential Analyser) for line generation
  - The Bresenham line algorithm
  - Use of symmetry to reduce computation for circle generation (computation of only one octant)
- Polygons and triangles
  - Polygon as an ordered set of vertices
  - Graphics hardware is optimised for processing points and flat polygons
  - Complex objects are decomposed into triangles as they are always flat
  - Polygon fill

# Transformation pipeline and geometric transformations

- ➤ The transformation pipeline (Modelling-Viewing-Projection-Normalisation-Device)
- > Types of transformation
  - Translation
  - Rotation (about origin in 2D and an axis in 3D)
  - Scaling
  - Reflection (about an axis in 2D and a plane in 3D)
  - Shearing
- > Homogeneous co-ordinate transformation matrices (4x4 in 3D)
  - For single transformations
  - Composite matrices (e.g. T·R·S)
- Proper OpenGL functions
  glMatrixMode(), glLoadIdentity(), glTranslate(), glRotate(),
  glScale(), glPushMatrix(), glPopMatrix(),

### Viewing and projection

- Types of projection
  - Planar geometric projection
  - Parallel orthogonal
  - Perspective
  - Advantages and disadvantages
- Orthogonal projection
- Frustum / Perspective projection
- Parameters for 3D viewing and projection
  - Camera position, look-at point, view-up vector for x<sub>view</sub>-axis
  - Viewing volume, near and far clipping planes
  - Viewing plane / clipping window
- Proper OpenGL functions
  glMatrixMode(), glFrustum()/gluPerspective(), gluLookAt(),
  glOrtho(), gluOrtho2D() ...

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#### Parametric curves and surfaces

- Why parametric (explicit) representation?
- Parametric curves

• In 2D: 
$$x = x(t)$$
,  $y = y(t)$ ,  $(0 \le t \le 1)$ 

• In 3D: 
$$x = x(t)$$
,  $y = y(t)$ ,  $z = z(t)$ ,  $(0 \le t \le 1)$ 

- 2D Line:  $x = x_1 + t(x_2 x_1),$  $y = y_1 + t(y_2 - y_1), (0 \le t \le 1)$
- 2D Circle:  $x = r \cos(360t)$ ,  $y = r \sin(360t)$ ,  $(0 \le t \le 1)$

- Cubic curves and splines
  - Control points
  - Interpolation curves and design curves
  - Local control: tension and bias

 $x(t) = a_0 + a_1t + a_2t^2 + a_3t^3$ ,  $(0 \le t \le 1)$  $y(t) = b_0 + b_1t + b_2t^2 + b_3t^3$ 

- Parametric surfaces
  - Revolved, extruded and swept surfaces
  - Tensor product surfaces
    - Interpolation surfaces and design surfaces
    - Controls

## 3D modelling

- ➤ Basic techniques: wireframes, surface models and solids; their advantages and disadvantages
- Constructive Solid Geometry (CSG)
  - CSG tree
  - Non-uniqueness
- Boundary Representation (B-Rep)
  - Boundary elements (geometry: points, curves and surfaces)
  - Relationships between boundary elements (topology / connectivity: vertices, edges and faces)
  - Types of B-Rep models: manifold and non-manifold (vertex connecting at least 3 edges and edge connecting exactly 2 faces)
  - Validity of B-Rep models and Euler's law (V E + F R + 2H = 2S)
  - Implementation of B-Rep models with OO techniques (e.g. C++)

## Hierarchical modelling

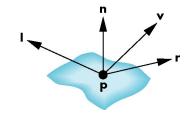
- Important concepts
  - Local and world co-ordinate frames of reference
  - Object transformations
- > Linear modelling
  - Symbols (primitives): box, cone, cylinder, sphere, torus, etc.
  - Instance and copy / array (linear and radial)
  - Flat structure and no information of relationships between the parts
- Hierarchical modelling
  - Hierarchical trees and articulated models
  - Child inherits transformations from its parent (M = M<sub>parent</sub> · M<sub>local</sub>)
  - While traversing the tree, **glPushMatrix()** is called when going <u>down</u> a level, and **glPopMatrix()** when going <u>up</u>
  - Examples: car, robot, humanoid figure, solar system and train track

## **Lighting and materials**

- Lighting sources and properties
  - Infinite distant and positional
  - Position, colour, direction, shape and reflectivity
- Light and material effects: ambient, diffuse and specular
- > Attenuation for positional light sources
  - Idea situation: inversely proportional to the square of distance
  - Flexible implementation to include constant, linear and quadratic terms:  $f(d) = \frac{1}{k_c + k_d d + k_d d^2}$
- Lighting model and shading
  - Phong model: 3 components, 4 vectors, 9 intensity and 9 absorption factors

$$I = k_d I_d I \cdot n + k_s I_s (\mathbf{v} \cdot \mathbf{r})^a + k_a I_a$$

- Polygon shading: constant (flat) and interpolative (smooth),
   Gouraud shading
- Material properties of objects being illuminated
- Combined effects: multiple lights, and light and materials



#### **Texture mapping**

- Concepts and types of texture mapping
  - Texture mapping, environment mapping and bump mapping
  - Takes place at the end of the rendering pipeline
- > Types of texture
  - 1D, 2D and 3D
  - Defined by an image file or a procedure
- Co-ordinate systems for texture mapping
- Secondary mapping
- Control
  - Modes: decal, modulating and blending
  - Filtering: magnification and minification, and nearest or linear interpolation
  - Wrapping: repeating and clamping
  - Multiple levels of detail: mipmapping
- OpenGL functions
  glTexImage2D(target,level,components,w,h,border,format,type,texels)

## Clipping

#### Concepts

- Clipping window vs viewport
- Clipping primitives: points, lines, polygons, curves and text

#### > Line clipping algorithms

- Brute Force Simultaneous Equations: slope-intercept formula does not handle vertical lines
- Brute Force Similar Triangles: use of similar triangles to work out co-ordinate of intersect points with clipping window edges – very expensive!
- Cohen-Sutherland
  - Outcodes for 9 regions of clipping plane
  - Logic OR and AND of outcodes for the two end points of the line
    - Trivial accept and trivial reject of a line
    - Calculate intersections when necessary
- Liang-Barsky (parametric lines): value range of parameters for the 4 intersections determine if lines are to be accepted / rejected
- Polygon clipping: bounding box used for trivial accept/reject

#### **Hidden-surface removal**

- Concepts: clipping vs hidden-surface removal
- Object-space and image-space approaches
- > Algorithms
  - Back-face culling
    - If  $\mathbf{v} \cdot \mathbf{n} \ge 0$  (viewing direction and face normal), polygon is visible
    - Limitations: single and convex object
  - Painter's algorithm: depth sort, overlap test in x and y directions, hard cases, ...
  - Binary Spatial Partition (BSP) tree
    - Structure and creation of BSP
    - Rendering of BSP
  - Z-buffer
    - A depth buffer is used in addition to frame buffer
    - For each pixel position, the polygon closest to the viewport is determined, and corresponding colour used
- OpenGL functions: glutInitDisplayMode(), glClear(),
  glClearDepth(), glDepthRange(); glDepthFunc(), glDepthMask(),
  glPolygonMode(), glEnable(GL\_DEPTH\_TEST), glEnable(GL\_FOG),
  glCullFace()

#### **About final exam**

- > Format of exam
  - > 5 Questions, each worth 20 marks
  - Question 1 has 10 short-answer questions
  - Questions 2-5 cover main topics of the module, and each has several sub-questions
- > Study of a past exam paper
- > Answer of general questions