



Determining the radius of curvature of a planoconvex lens through measurements of the Newton's Rings interference pattern (possibly retitle)

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The half-life of Ba-137m and the Poisson and Gaussian probabilities for Am-241 can be calculated by collecting the activity and time period obtained from radioactive decay. Using a Geiger-Müller tube and software such as *CASSY Labs* and Excel it is possible to do so. The values obtained for half-life are $t_{1/2\text{-CSY}} = 2.73 \pm 0.03$ mins and $t_{1/2\text{-EXL}} = 2.92 \pm 0.07$ mins, which are consistent with literature. The experimental probability does not fit the theoretical probability distributions due to incomplete data set.

I. INTRODUCTION

In nature, light can behave in two states, through wave-like and through particle-like properties. It is possible to observe the wave-like behaviour when rays of light are reflected or transmitted from different surfaces of a thin film. They interfere with one another when outgoing rays overlap, creating interference patterns.

For two waves to cause a steady interference pattern, the waves must be coherent. The usage of a thin film allows for coherency as the two reflected waves are part of the same initial burst. We can achieve this thin film of air by having a convex surface of a lens in contact with a plane glass plate; a thin film of air is then formed between the two surfaces. Then by using a monochromatic light source we can create an interference pattern known as Newton's Rings - a pattern of concentric rings progressively getting further apart from each other. These were first observed by Robert Hooke in 1665 and then later by Sir Isaac Newton in 1775. [??]

By observing and measuring this phenomena it is possible to calculate the radius of curvature of a planoconvex lens.

We can derive a relationship between the radius of curvature, R , and other quantities. Initially, through using geometry, R can be shown to be related to the length of the lens divided by two (r), the greatest distance between lens and glass plate (d), and the spacing between the lens and the plate due to a non perfect contact (d_0),

$$R = \frac{r^2}{2(d + d_0)}. \quad (1)$$

Since interference is involved, $\Delta = m\lambda$ (constructive interference with light of wavelength λ), and $\Delta = 2d + \lambda$ (path difference due to reflections) can be used to find the square of the radius of a bright fringe with fringe number m ,

$$r_m^2 = \lambda R((m - 1) + 2d_0). \quad (2)$$

Generally to observe the fringes the image is magnified by a factor of M so we get,

$$\rho_m^2 = M^2 R \lambda (m - 1) + 2M^2 R d_0, \quad (3)$$

this can be used accordingly with data collected from experimentation.

II. METHOD

The light source used in this experiment was provided by a mercury lamp. That light was then passed through a set-up as shown in Fig. 1(a), this allowed for the interference pattern to be projected onto a screen along with a horizontal scale.

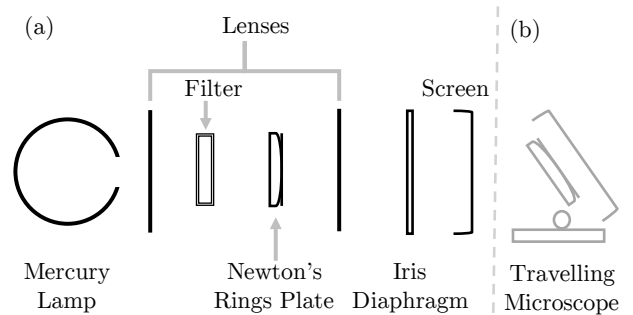


FIG. 1: (a) A schematic of the experimental set-up used to collect the initial set of data. Entire set-up was placed on an optical bench, allowing accurate positioning of the lenses. (b) Modified set-up used in subsequent investigations - Newton's Rings Plate is moved, the screen is adjusted, and a Travelling Microscope is added.

The two main filters used varied by colour, yellow and green, this created the monochromatic light needed to view the interference fringes. It is worth noting that during set-up the positions of the lenses and rings plate often had to be adjusted so that the pattern and the horizontal scale could be both focussed to the best that they both could be. An iris diaphragm was added to the setup so that there could be the greatest contrast between the light and dark fringes. Once this was done an initial measurement of the magnification was performed by comparing the distance of one of the projected tick-marks on the scale to the actual given value.

Two sets of data were taken for each filter. In both cases the positions of the centre of the bright fringes along a horizontal axis were marked on a piece of paper attached to the screen. This was done for the 10 innermost bright fringes. The diameter was then measured and a radius value was obtained. A least squares fitting was applied to the fringe radius squared along with $(m - 1)\lambda$, where m is the ring number and λ is the wavelength of light used.



III. RESULTS

The measured fringe radius squared, ρ_m^2 , and $(m - 1)\lambda$ (with m as fringe number and λ as wavelength of light), is shown in Fig. 1. Through using a least squares fitting and equation (3) a value obtained for the radius of curvature, R_{IE} , turns out to be $15 \pm 3\text{m}$.

In Table 1 we can see other values calculated for the radius of curvature from subsequent investigations using different methods but the same calculations. For example using a Travelling Microscope instead of direct screen measurements (see Fig. 1(b)) to measure fringe radius, and also repeating data collection.

Shown also in the table are values for d_0 .

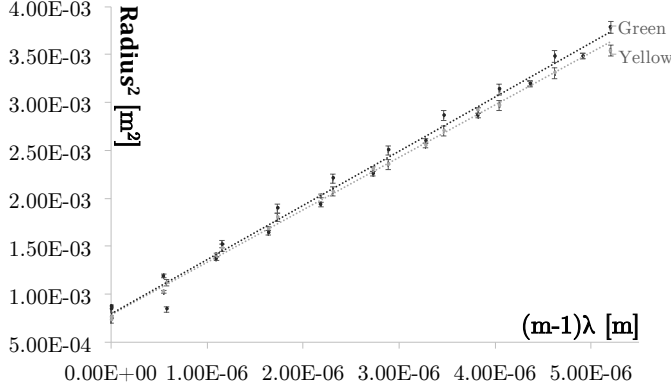


FIG. 2: The fringe radius squared plotted as a function of $(m - 1)$ multiplied by wavelength. Horizontal error bars are too small to be seen.

Experiment	Radius of Curvature, R [m]	$d_0 [\times 10^{-7}, \text{m}]$
IE	15 ± 3	7 ± 2
TM	24 ± 2	4.6 ± 0.9
RP	18 ± 5	8 ± 3

TABLE I: Values for radius of curvature of the planoconvex lens, and values for d_0 . IE denotes the 'Initial Experiment', TM for 'Travelling Microscope', and RP for 'Repeated'.

IV. DISCUSSION

In analysing our data we find that there are no official manufacturer's value for the radius of curvature of the lens. We must compare the initial data and data collected in subsequent weeks of investigation in order to be able to draw some form of conclusion on what the radius of curvature should be.

Looking at our initial measurements we see that the data generally follows a linear relationship showing agreement with equation (3), the plotted trendlines shown in Fig. 2. pass through the majority of the error bars, however there are a number of points which do not. This could be due to the fact that during data collection distinguishing where the centre of the bright fringe lay was difficult to do, coupled with the rings not being able to be fully focussed, this inevitably would lead to distances being incorrectly measured.

However when using this data we do find a value for the radius of curvature, R_{IE} , which at first does not seem

reasonable. But, if we compare this value with the one calculated using data collected with a Travelling Microscope (R_{TM}) then we see that both are similar. We would now be more inclined to accept the initial value, even if it is larger and the values themselves do not overlap in each other's uncertainties. Although we do need to consider that it was again difficult to collect data, the bright and dark fringes blur into one another allowing for mistakes to be made, plus random errors may have arisen due to varying eyesight. The latter could be reduced if one person took the results and kept using the same eye.

When the initial experiment was repeated we get a value which does agree with R_{IE} (the values lie in each others uncertainties), and also with R_{TM} . Although the uncertainty does appear to have increased, this is because a different magnification was used, $\times 4$ instead of $\times 6$.

There are a range of possible reasons for the differing values of R , some of them related to experimental issues. For example, one reason could be due to different filters being used in the investigations, even though what appeared to be the same colour each time could potentially be different. This leading to different wavelengths of monochromatic light being used which would cause the calculated value for the radius of curvature to change accordingly. We can see this by manipulating equation (3), if λ increases then R decreases as a result.

Additionally, the spacing between the lens and the glass plate should be taken into account. If the thickness of the air gap (film) between lens and plate increases then the wavelength of the light in the film increases, and as shown above the radius of curvature will decrease.

From Table 1 we see that for IE and RP, the values of d_0 are fairly similar, on the other hand for TM the value is far smaller. However, this could be a product of the way we took measurements when using the TM. Using the set-up as shown in Fig. 1(b), the geometric path difference of the interfering light waves could have been decreasing after being reflected at an angle from the screen thus resulting in a decrease of the value for d_{0-TM} .

There are other ways in which the radius of curvature of a lens can be measured using Newton's Rings, one is to use a digital camera and directly image the interference pattern produced - then digital software could be used to measure the fringe radius to a higher precision, avoiding any unnecessary random errors. On the other hand we could coat the convex lens and the glass plate with high reflecting transparent silverings, this would allow the rings to appear sharper to circumnavigate the issue of focussing the rings, moreover high precision could be attained here as well [2].

V. CONCLUSIONS

In conclusion, through measurements of Newton's Rings it has been possible to determine a value for the radius of curvature of a planoconvex lens, $R_{IE} = 15 \pm 3$. A value which at first could be doubted, however after additional investigation it has been possible to compare this value with other ones and verify it is valid. However through using a different experimental set-up it could be

possible to reduce certain sources of uncertainties, and to remove some of the experimental issues experienced.

[1] Hugh D. Young and Roger A. Freedman. *University Physics with Modern Physics, 13th Edition*. Pearson Education Limited, Harlow, Essex, 2015.

[2] S. Tolansky. *New Interference Phenomena with Newton's Rings*. Nature, Vol. 153, 1944, p. 314.



Appendix



The uncertainty calculated for the radius of curvature R was found by propagating other uncertainties related to quantities found in equation (3). The majority of them are based off formulae found in *Measurements and their Uncertainties* [I. G. Hughes and T. P. A. Hase, *Measurements and their Uncertainties*, Oxford University Press, Oxford, United Kingdom, 2010].

Firstly for the square of the magnified radius of a bright fringe, ρ_m^2 , the error is,

$$\alpha_{r^2} = \alpha_r |2 \times r| \quad (4)$$

where r is the value for the magnified radius of a bright fringe, and α_r is the uncertainty on that. This arises due to a 30 cm ruler being used to measure the diameter, so the highest precision achievable would have been limited at half a division, therefore $\alpha_r=0.5$ cm.

The uncertainty on the magnification squared, M^2 , is found by,

$$\alpha_{M^2} = M^2 \left| 2 \times \frac{\alpha_M}{M} \right| \quad (5)$$

with α_M as the error on the magnification. For the combined term $(m-1)\lambda = n$, the uncertainty on this was found by using a least squares fitting function in the software Microsoft® Excel.

To calculate the error on the radius of curvature R , the following equation is thus used,

$$\alpha_R = R \times \sqrt{\left(\frac{\alpha_n}{n}\right)^2 + \left(\frac{\alpha_{M^2}}{M^2}\right)^2} \quad (6)$$

The uncertainty on d_0 is found by further propagating the uncertainties found above, the resulting equation is,

$$\alpha_{d_0} = d_0 \times \sqrt{\left(\frac{\alpha_c}{c}\right)^2 + \left(\frac{\alpha_{M^2}}{M^2}\right)^2 + \left(\frac{\alpha_R}{R}\right)^2} \quad (7)$$

where c is the intercept of the least squares fitting, and α_c is it's respective uncertainty.

