

The measurement of the Hubble Constant: beyond the cosmic ladder

Z0962251

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A precisely determined Hubble's constant H_0 would have an overarching effect on any feature of cosmological theory: the age or critical density of the Universe, or with the formation of cosmic structure. Producing a conclusive value for H_0 is difficult as absolute distances on the cosmic scale are difficult to measure. Inhomogeneous gravitational acceleration generates motion which does not follow the simple expansion as described by Hubble's Law $v = H_0 d$. An uncertainty arises due to the discrepancy between the methods to connect local distances to the smooth large-scale Hubble flow (Fukugita et al. 1993).

Several approaches for cosmic distance measurement should therefore be used to reduce systematic errors. These measurements can form the “rungs” of a *cosmic distance ladder*, where large extragalactic distances (> 1000 Mpc) are informed and calibrated by techniques which have smaller ranges (Carroll and Ostlie 2007). Astronomers may employ a variety of methods in tandem, therefore the ladder could instead be expressed as several pathways (Figure 1).

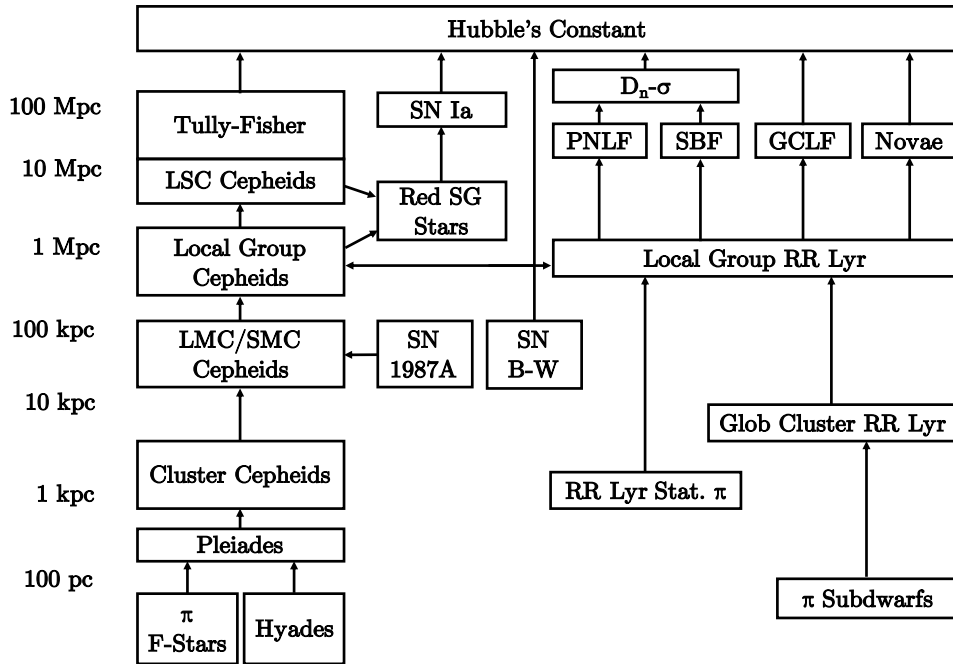


Figure 1: Adapted from Jacoby et al. (1992), this diagram illustrates the various approaches to calculate H_0 , each technique is roughly placed at the approximate range it operates at. One can see that there is not one strict “cosmic ladder”, rather multiple pathways. For reference, the acronyms used are: B-W - Baade-Wessenlink; GCLF - Globular-Cluster Luminosity Function; LSC - Local Super Cluster; PNLF - Planetary Nebula Luminosity Function; SBF - Surface-Brightness Fluctuations; SG - Super Giant; SN - Supernovae; π - parallax.

The Hubble Space Telescope (HST) H_0 Key Project was an effort in the early 2000s to determine H_0 by calculating distances to Cepheid variables in local galaxies (≤ 20

Mpc) then applying them as a calibration to 5 secondary independent distance indicators. Described by Freedman et al. (2001), four of the methods (Type Ia supernovae, Tully-Fisher relation, surface-brightness fluctuations, and Type II supernovae) were able to produce $70 \leq H_0 \leq 72 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and the remaining technique (fundamental plane for elliptical galaxies) $H_0 \approx 82 \text{ km s}^{-1} \text{ Mpc}^{-1}$. Over the next decade, the methodology would be refined and the sample of Cepheids and Type Ia supernovae improved (better observations and other data types) $H_0 = 73.48 \pm 1.66 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Riess et al. 2018, 2011, 2016). These results set a standard benchmark for H_0 , they were found by taking steps along the cosmic ladder and whilst they have high accuracy, it would be beneficial to directly calculate H_0 at large distances without the need for Cepheid-based calibration.

One alternative is measuring Cosmic Microwave Background (CMB) anisotropies. Through analysing all-sky temperature and polarisation maps, Λ CDM cosmology models can be fitted which constrain cosmological parameters. Surveys of the CMB have included those performed by the spacecraft COBE, WMAP, and more recently, Planck. The results of the latter include $H_0 = 67.5 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Planck Collaboration et al. 2018), this is of particular importance as it is discrepant when compared to the most recent HST-based result (Riess et al. 2018). Investigations of potential systematics in either methods have concluded that some arise due to the modelling of the Cepheids (Follin and Knox 2018) and residual systematics from certain spectra used in the Planck likelihood calculation (Spergel et al. 2015). However the tension between the H_0 values still exists, therefore it would be beneficial to explore other methods for calculating the constant, especially those which are able to function immediately at large cosmic distances.

Still considering the CMB, the Sunyaev-Zel'dovich effect (SZE) leads to a change in the apparent brightness of the CMB towards a cluster of galaxies or for any reservoir of hot plasma (Birkinshaw 1999, Carlstrom et al. 2002). Combined with X-ray emission from intracluster gas, the SZE can be used as a tracer for cosmological parameters. Birkinshaw (1999) describes the technique to be a comparison of the angular size of a galaxy cluster with a measure of the line-of-sight size of the cluster. With spectra data at hand, the emission of gas in a galaxy cluster can be described by the X-ray surface brightness, and the gas absorption by the measurement of the thermal SZE (an intensity change). The surface brightness and intensity change can be re-expressed in terms of physical constants and angular structure factors, this then leads to a single expression for calculating the angular diameter distance,

$$d_A = \left(\frac{N_{SZ}^2}{N_X} \right) \frac{\Lambda_{e0}}{4\pi(1+z)^3 [I_0 \Psi_0 \sigma_T]^2}. \quad (1)$$

The full derivation and definitions for Equation 1 can be found in Holzappel et al. (1997).

Employing this equation with values for cluster redshifts z and the deceleration parameter q_0 , H_0 can be obtained in a direct and alternate way which is independent of the chain of distance estimators. The South Pole Telescope Sunyaev-Zel'dovich (SPT-SZ) survey was a programme which made use of the SZE to detect galaxy clusters (Chang et al. 2009). Multiple analyses have been performed to constrain cosmological parameters using the resulting SPT-SZ datasets, the majority of which tested variations of the Λ CDM model (de Haan et al. 2016, Hou et al. 2014). Hou et al. (2014) examined models

which were constrained single or double parameters, for example constraining neutrino mass. They combined external data sets (WMAP7, BAOs and previous calibrations for H_0) with their SPT-SZ data and they were able to achieve $H_0 = 68.3 \pm 1.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$ which agrees with HST and Planck results, therefore showing the validity of the method.

The CMB can therefore be utilised in a variety of ways for the calculation of H_0 . In a similar vein, the effects of the gravity can be explored and employed as a method for measuring Hubble’s constant without the need for the cosmic ladder. The manifestation of which is in the form of gravitational lensing and gravitational waves.

Optical observations of the night sky may sometimes reveal multiple arcs of light surrounding a central object, this effect is more commonly known as *gravitational lensing*. It occurs when light travelling towards us from a distant bright object, for example a quasar, is curved by the space-time of a much massive object, say a galaxy cluster or hypothetical MACHOs, in the foreground which acts as a lens and produces the arcs of light (Carroll and Ostlie 2007). If the initial source, such as an active galactic nucleus or a supernovae, varies in luminosity then this variability can be viewed from the aberrations albeit with a time delay as a result of the different light paths (Suyu 2017). This time delay can be related to the distribution of the lens mass and the “time-delay distance” $D_{\Delta t}$, where the latter is multiplicative combination of three angular diameter distances: observer-source distance D_s , observer-lens distance D_d , and lens-source distance D_{ds} (Shajib et al. 2018, Suyu 2017). The application to cosmology arises as $D_{\Delta t}$ is inversely proportional to H_0 plus weakly dependent on other cosmological constants.

Koopmans et al. (2003) presents mass models which have been developed to determine a value for Hubble’s constant. They aimed to reduce known systematics such as the radial mass profile, dust extinction, etc. Three particular mass models (SIE, SPLE1, SPLE2) were tested which were based solely on the gravitational lensing constraints so no stellar dynamics were considered. This resulted in H_0 ranging from 71–74 $\text{km s}^{-1} \text{ Mpc}^{-1}$ and a best lensing-only value of $H_0 = 74^{+10}_{-11} \text{ km s}^{-1} \text{ Mpc}^{-1}$. It is clear then that whilst the uncertainties are large, the general value for H_0 agrees with the Cepheid result and with additional constraints it would become more precise. Courbin et al. (2011) demonstrate that parameters such as the baryonic fraction in the Einstein radius and the velocity dispersion of the lensing galaxy can be found by combining spatially deconvolved HST F160W images with VLT spectroscopic data.

Gravitational lensing is therefore a highly viable method in the measurement of H_0 . However it has the limitation of requiring long-periods of photometric observations on objects of interest to produce the time delays. A more suitable strategy would be to utilise gravitational waves where observatories have been purposely built for their detection. Waves originating from the decaying orbit of an ultra-compact, binary neutron star system would be the most likely to be registered by Earth based detectors (Schutz 1986).

LIGO Scientific Collaboration et al. (2017) describes the approach they used to calculate H_0 for object GW170817 detected by the Advanced Laser Interferometer Gravitational-wave Observatory (LIGO) (LIGO Scientific Collaboration et al. 2015) and the Virgo detector (Acernese et al. 2015). The gravitational wave data is used to infer the distance d to the source through the constraining of a posterior probability in a Bayesian framework model. An initial posterior distribution for the observed data

x_{GW} can be converted into a posterior on the inclination angle $\cos i$ and $H_0 = v_H/d$, where v_H is the Hubble flow velocity. $\cos i$ is of importance as it was found that the distance measurement is strongly correlated with the inclination of the binary orbital plane. Additionally, to obtain v_H for the source, the host galaxy’s measured recessional velocities can be corrected for local peculiar motions. This method is used as it does not require the Hubble flow velocities of any local calibrating galaxies which have been estimated using the distance ladder.

Applying the approximate $v_H = 3017 \pm 166 \text{ km s}^{-1}$ into the Bayesian model produces a maximum a posteriori value of $H_0 = 70.0^{+12.0}_{-8.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$.

Method	$H_0 \text{ (km s}^{-1} \text{ Mpc}^{-1})$
HST Key Project and Cepheid Variables	73.48 ± 1.66
Planck observations of the CMB	
SPT-SZ Sunyaev-Zel’dovich Effect	
Gravitational lenses mass modelling	
Gravitational waves with LIGO and Virgo	

Table I: Summarised results from the various methods to calculate Hubble’s Constant.

In conclusion, this discussion has explored a variety of methods which can be employed to measure and calculate Hubble’s constant H_0 without the need to climb the cosmic ladder. From Cosmic Microwave Background based methods to those employing the effects of gravity, one can successfully calculate and measure H_0 without the “traditional” standard candle techniques. These promising alternatives still require research, but no doubt as more observations are made, the accuracy and precision of H_0 will surely improve.

References

- Acernese, F., Agathos, M., Agatsuma, K., Aisa, D., Allemandou, N., Allocca, A., Amarni, J., Astone, P., Balestri, G., Ballardini, G., Barone, F., Baronick, J. P., Barsuglia, M., Basti, A., Basti, F., Bauer, T. S. et al. (2015), ‘Advanced Virgo: a second-generation interferometric gravitational wave detector’, *Classical and Quantum Gravity* **32**, 024001.
- Birkinshaw, M. (1999), ‘The Sunyaev-Zel’dovich effect’, *Physics Reports* **310**, 97–195.
- Carlstrom, J. E., Holder, G. P. and Reese, E. D. (2002), ‘Cosmology with the Sunyaev-Zel’dovich Effect’, *Annual Review of Astronomy and Astrophysics* **40**, 643–680.
- Carroll, B. W. and Ostlie, D. A. (2007), *An Introduction to Modern Astrophysics*, 2nd edn, Pearson.
- Chang, C. L., Ade, P. A. R., Aird, K. A., Benson, B. A., Bleem, L. E., Carlstrom, J. E., Cho, H.-M., de Haan, T., Crawford, T. M., Crites, A. T., Dobbs, M. A., Everett, W., Halverson, N. W., Holder, G. P., Holzzapfel, W. L. et al. (2009), SPT-SZ: a Sunyaev-Zel’dovich survey for galaxy clusters, in B. Young, B. Cabrera and A. Miller, eds, ‘American Institute of Physics Conference Series’, Vol. 1185 of *American Institute of Physics Conference Series*, pp. 475–477.
- Courbin, F., Chantry, V., Revaz, Y., Sluse, D., Faure, C., Tewes, M., Eulaers, E., Koleva, M., Asfandiyarov, I., Dye, S., Magain, P., van Winckel, H., Coles, J., Saha, P., Ibrahimov, M. and Meylan, G. (2011), ‘COSMOGRAIL: the COSmological MONitoring of GRAVItational Lenses. IX. Time delays, lens dynamics and baryonic fraction in HE 0435-1223’, *Astronomy and Astrophysics* **536**, A53.
- de Haan, T., Benson, B. A., Bleem, L. E., Allen, S. W., Applegate, D. E., Ashby, M. L. N., Bautz, M., Bayliss, M., Bocquet, S., Brodwin, M., Carlstrom, J. E., Chang, C. L., Chiu, I., Cho, H.-M., Clocchiatti, A., Crawford, T. M. et al. (2016), ‘Cosmological Constraints from Galaxy Clusters in the 2500 Square-degree SPT-SZ Survey’, *Astrophys. J.* **832**, 95.
- Follin, B. and Knox, L. (2018), ‘Insensitivity of the distance ladder Hubble constant determination to Cepheid calibration modelling choices’, *MNRAS* **477**, 4534–4542.
- Freedman, W. L., Madore, B. F., Gibson, B. K., Ferrarese, L., Kelson, D. D., Sakai, S., Mould, J. R., Kennicutt, Robert C., J., Ford, H. C., Graham, J. A., Huchra, J. P., Hughes, S. M. G., Illingworth, G. D., Macri, L. M. and Stetson, P. B. (2001), ‘Final Results from the Hubble Space Telescope Key Project to Measure the Hubble Constant’, *The Astrophysical Journal* **553**, 47–72.
- Fukugita, M., Hogan, C. J. and E., P. P. J. (1993), ‘The cosmic distance scale and the Hubble constant’, *Nature* **366**.
- Holzzapfel, W. L., Arnaud, M., Ade, P. A. R., Church, S. E., Fischer, M. L., Mauskopf, P. D., Rephaeli, Y., Wilbanks, T. M. and Lange, A. E. (1997), ‘Measurement of the Hubble Constant from X-Ray and 2.1 Millimeter Observations of Abell 2163’, *Astrophys. J.* **480**, 449–465.
- Hou, Z., Reichardt, C. L., Story, K. T., Follin, B., Keisler, R., Aird, K. A., Benson, B. A., Bleem, L. E., Carlstrom, J. E., Chang, C. L., Cho, H.-M., Crawford, T. M., Crites, A. T., de Haan, T., de Putter, R. et al. (2014), ‘Constraints on Cosmology from the Cosmic Microwave Background Power Spectrum of the 2500 deg² SPT-SZ Survey’, *Astrophys. J.* **782**, 74.
- Jacoby, G. H., Branch, D., Ciardullo, R., Davies, R. L., Harris, W. E., Pierce, M. J., Pritchet, C. J., Tonry, J. L. and Welch, D. L. (1992), ‘A critical review of selected techniques for measuring extragalactic distances’, *Astronomical Society of the Pacific* **104**, 599–662.
- Koopmans, L. V. E., Treu, T., Fassnacht, C. D., Blandford, R. D. and Surpi, G. (2003), ‘The Hubble Constant from the Gravitational Lens B1608+656’, *Astrophys. J.* **599**, 70–85.
- LIGO Scientific Collaboration, Aasi, J., Abbott, B. P., Abbott, R., Abbott, T., Abernathy, M. R., Ackley, K., Adams, C., Adams, T., Addesso, P. and et al. (2015), ‘Advanced LIGO’,

- Classical and Quantum Gravity **32**(7), 074001.
- LIGO Scientific Collaboration, Virgo Collaboration, 1M2H Collaboration, Dark Energy Camera GW-EM Collaboration, DES Collaboration, DLT40 Collaboration, Las Cumbres Observatory Collaboration, VINROUGE Collaboration, Master Collaboration et al. (2017), ‘A gravitational-wave standard siren measurement of the Hubble constant’, Nature (London) **551**, 85–88.
- Planck Collaboration et al. (2018), ‘Planck 2018 results. VI. Cosmological parameters’, arXiv e-prints p. arXiv:1807.06209.
- Riess, A. G., Casertano, S., Yuan, W., Macri, L., Anderson, J., MacKenty, J. W., Bowers, J. B., Clubb, K. I., Filippenko, A. V., Jones, D. O. and Tucker, B. E. (2018), ‘New Parallaxes of Galactic Cepheids from Spatially Scanning the Hubble Space Telescope: Implications for the Hubble Constant’, Astrophys. J. **855**, 136.
- Riess, A. G., Macri, L., Casertano, S., Lampeitl, H., Ferguson, H. C., Filippenko, A. V., Jha, S. W., Li, W. and Chornock, R. (2011), ‘A 3% Solution: Determination of the Hubble Constant with the Hubble Space Telescope and Wide Field Camera 3’, Astrophys. J. **730**, 119.
- Riess, A. G., Macri, L. M., Hoffmann, S. L., Scolnic, D., Casertano, S., Filippenko, A. V., Tucker, B. E., Reid, M. J., Jones, D. O., Silverman, J. M., Chornock, R., Challis, P., Yuan, W., Brown, P. J. and Foley, R. J. (2016), ‘A 2.4% Determination of the Local Value of the Hubble Constant’, Astrophys. J. **826**, 56.
- Schutz, B. F. (1986), ‘Determining the hubble constant from gravitational wave observations’, Nature **323**, 310.
- Shajib, A. J., Treu, T. and Agnello, A. (2018), ‘Improving time-delay cosmography with spatially resolved kinematics’, MNRAS **473**, 210–226.
- Spergel, D. N., Flauger, R. and Hložek, R. (2015), ‘Planck data reconsidered’, Phys. Rev. D **91**, 023518.
- Suyu, S. H. (2017), ‘Progress toward an accurate Hubble Constant’, Proceedings of the International Astronomical Union **13**(S336), 80–85.