Homework 1 - Berkeley STAT 157

Handout 1/22/2017, due 1/29/2017 by 4pm in Git by committing to your repository. Please ensure that you add the TA Git account to your repository.

- 1. Write all code in the notebook.
- 2. Write all text in the notebook. You can use MathJax to insert math or generic Markdown to insert figures (it's unlikely you'll need the latter).
- 3. Execute the notebook and save the results.
- 4. To be safe, print the notebook as PDF and add it to the repository, too. Your repository should contain two files: homework1.ipynb and homework1.pdf.

The TA will return the corrected and annotated homework back to you via Git (please give rythei access to your repository).

```
In [2]: from mxnet import ndarray as nd
import time
import numpy as np
```

1. Speedtest for vectorization

Your goal is to measure the speed of linear algebra operations for different levels of vectorization. You need to use wait_to_read() on the output to ensure that the result is computed completely, since NDArray uses asynchronous computation. Please see

http://beta.mxnet.io/api/ndarray/ autogen/mxnet.ndarray.NDArray.wait to read.html (http://beta.mxnet.io/api/ndarray/ autogen/mxnet.ndarray.NDArray.wait to read.html) for details.

- 1. Construct two matrices A and B with Gaussian random entries of size 4096×4096 .
- 2. Compute C = AB using matrix-matrix operations and report the time.
- 3. Compute C = AB, treating A as a matrix but computing the result for each column of B one at a time. Report the time.
- 4. Compute C = AB, treating A and B as collections of vectors. Report the time.
- 5. Bonus question what changes if you execute this on a GPU?

```
In [5]: # 1. Construct two matrices A and B with Gaussian random entries of size
          4096×4096.
        A = nd.random.normal(0, 1, shape=(4096, 4096))
        B = nd.random.normal(0, 1, shape=(4096, 4096))
        print("A is ", A)
        print("B is ", B)
        # 2. Compute C=AB using matrix-matrix operations and report the time.
        tic = time.time()
        C = nd.dot(A,B)
        C.wait to read()
        print("C is ", C)
        print("Q2 takes", time.time()- tic)
        # 3. Compute C=AB, treating A as a matrix but computing the result for e
        ach column of B one at a time. Report the time.
        tic = time.time()
        C=nd.empty((4096,4096))
        for i in range(4096):
            C[:,i] = nd.dot(A,B[:,i])
        C.wait to read()
        print("C is ", C)
        print("Q3 takes", time.time() - tic)
        # 4. Compute C=AB, treating A and B as collections of vectors. Report th
        e time.
        tic = time.time()
        C=nd.zeros((4096,4096))
        for i in range(4096):
            a = A[:,i].reshape(4096,1)
            b = B[i,:].reshape(1,4096)
            C += nd.dot(a,b)
        C.wait to read()
        print("C is ", C)
        print("Q4 takes", time.time() - tic)
```

```
A is
 [[ \ 0.04010138 \ -0.82130146 \ \ 0.02005161 \ \dots \ \ 0.80797803 \ \ 0.0349124 
 -0.9425538 ]
             0.35110465 -2.7191465 ... 0.2302415
 [ 0.4579651
                                                     0.2839324
 -0.54985106]
             0.30501708 0.80644757 ... -1.6631485
 [-1.1534044]
                                                     0.69836503
   0.6364544 ]
 \begin{bmatrix} 0.5691745 & -1.0284108 & -0.515387 & \dots & 0.40762436 & 1.068956 \end{bmatrix}
 -0.01077725]
 [0.34715003 - 0.70612836 - 0.7524027 \dots -0.4507234]
                                                     1.2779481
  0.852945 ]
 [ 0.24677981 - 0.17408593 \ 1.8073856 \ \dots \ 0.7218124 \ -0.4130202 
  -0.07617839]]
<NDArray 4096x4096 @cpu(0)>
B is
[1.2563426e+00 2.0983241e+00 -6.1626399e-01 ... 7.1981925e-01
 -1.5064095e-01 -1.6847348e+00]
 [-5.9105557e-01 -7.4600556e-04 3.9198685e-01 ... -2.2434056e+00
   2.0302789e+00 6.1633265e-011
 [-6.1852258e-01 \ 2.1420236e-01 \ -5.6821045e-02 \ \dots \ 4.1352261e-02
 -1.0406296e+00 1.0598879e+00]
 . . .
 [ 2.7899129e+00 1.4155358e-01 1.0943099e+00 ... 5.1718676e-01
 -1.2406477e+00 -8.1241745e-01]
 [-1.1760486e+00 \quad 2.6735411e+00 \quad -2.4220882e-01 \quad \dots \quad -3.0564606e-01]
   1.5179449e+00 2.4704537e+00]
 [-1.3527721e+00 \quad 7.0983845e-01 \quad -2.0442135e+00 \quad \dots \quad -1.5420042e+00
 -1.7140442e-01 4.6152738e-03]]
<NDArray 4096x4096 @cpu(0)>
C is
-35.496662
 -109.732544 ]
               23.37611 -56.675674 ... 24.243011 49.816593
 [ 30.453777
   15.3279705]
 -4.885561
                                                       -10.728184
   76.08944 ]
 [-151.3319]
             107.07407 -125.48469
                                             56.779675
                                                        129.2976
 -109.78065 ]
               -22.664043 -7.4296336 ... 121.454994
 [ -45.615746
                                                        -58.20906
  -95.325264 ]
 [-82.03247]
               -5.521243
                            30.89802
                                       ... -11.5960655 -122.28372
    1.2381835]]
<NDArray 4096x4096 @cpu(0)>
Q2 takes 1.3674461841583252
C is
... 112.58604 -35.496643
 -109.732544 ]
 [ 30.453712
                23.376108
                           -56.67568
                                             24.242981
                                                         49.81656
   15.32799 ]
 [ -24.976753 -35.07466
                           -30.914482 ...
                                             -4.8855286 -10.728184
    76.08942
 [-151.33191]
               107.074066 -125.484665 ...
                                             56.779675
                                                        129.29756
 -109.78069 1
               -22.664051 -7.4296474 ... 121.45499
 [-45.615738]
                                                        -58.209015
```

```
-95.32531
 [-82.03244]
                -5.521265
                            30.89798
                                           -11.596052 -122.28375
    1.2382298]]
<NDArray 4096x4096 @cpu(0)>
Q3 takes 23.638182163238525
C is
112.58585
                                                       -35.4967
 -109.73244
                           -56.675602
                                            24.242912
 [ 30.453823
                23.376108
                                                        49.816586
   15.327974 ]
                           -30.914282 ...
 [ -24.976778
               -35.074673
                                            -4.885559
                                                       -10.728128
   76.08936
 [-151.3321]
               107.074196 -125.484535 ...
                                            56.77968
                                                       129.2975
 -109.780495 ]
                            -7.4296207 ... 121.45502
 [ -45.615623
               -22.664017
                                                        -58.209126
   -95.32538 ]
 [ -82.03248
                -5.521231
                            30.89808
                                      ... -11.596074 -122.283905
    1.2382019]]
<NDArray 4096x4096 @cpu(0)>
Q4 takes 179.12236976623535
```

1. Bonus question - what changes if you execute this on a GPU?

C is [[-13.2856455 -28.294075 -120.39991 ... 112.58585 -35.4967 -109.73244] [$30.453823 \ 23.376108 \ -56.675602 \ ... 24.242912 \ 49.816586 \ 15.327974$] [-24.976778 -35.074673 -30.914282 ... -4.885559 -10.728128 \ 76.08936] ... [-151.3321 \ 107.074196 -125.484535 ... \ 56.77968 \ 129.2975 -109.780495] [-45.615623 -22.664017 -7.4296207 ... \ 121.45502 -58.209126 -95.32538] [-82.03248 -5.521231 \ 30.89808 ... -11.596074 -122.283905 \ 1.2382019]] \ Q5 \ takes \ 1.7138192653656006

2. Semidefinite Matrices

Assume that $A \in \mathbb{R}^{m \times n}$ is an arbitrary matrix and that $D \in \mathbb{R}^{n \times n}$ is a diagonal matrix with nonnegative entries.

- 1. Prove that $B = ADA^{T}$ is a positive semidefinite matrix.
- 2. When would it be useful to work with B and when is it better to use A and D?
- 1. Let x be an arbitrary non-zero vector. $x^TBx = x^TADA^Tx = (A^Tx)^TDA^Tx = b^TDb = \sum_{i=1}^n \lambda_i b_i^2 >= 0$. so B is a PSD
- 2. B is diagnolizable. Assume the eigenvalues are postive, then we can get a basis of orthonormal eigenvectors, many calculations become easier using orthonormal eigenbasis. When calculating the power of B, it's easy to use ADA^T

3. MXNet on GPUs

- 1. Install GPU drivers (if needed)
- 2. Install MXNet on a GPU instance
- 3. Display !nvidia-smi
- 4. Create a 2 × 2 matrix on the GPU and print it. See http://d2l.ai/chapter_deep-learning-computation/use-gpu.html) for details.

ubuntu@ip-172-31-37-85:~\$ nvidia-smi Sun Jan 27 08:13:31 2019 +
+ NVIDIA-SMI 410.79 Driver Version: 410.79 CUDA Version: 10.0 + NVIDIA-SMI 410.79 Driver Version: 410.79 CUDA Version: 10.0 ++ GPU Name Persistence-M Bus-Id Disp.A Volatile Uncorr. ECC Fan
Temp Perf Pwr:Usage/Cap Memory-Usage GPU-Util Compute M.
=======++===================
+ Processes: GPU Memory GPU PID Type Process name Usage
running processes found ++ [[0. 1.] [2. 3.]]

4. NDArray and NumPy

Your goal is to measure the speed penalty between MXNet Gluon and Python when converting data between both. We are going to do this as follows:

- 1. Create two Gaussian random matrices A, B of size 4096×4096 in NDArray.
- 2. Compute a vector $\mathbf{c} \in \mathbb{R}^{4096}$ where $c_i = ||AB_i||^2$ where \mathbf{c} is a **NumPy** vector.

To see the difference in speed due to Python perform the following two experiments and measure the time:

- 1. Compute $\|AB_{i\cdot}\|^2$ one at a time and assign its outcome to \mathbf{c}_i directly.
- 2. Use an intermediate storage vector \mathbf{d} in NDArray for assignments and copy to NumPy at the end.

```
In [4]: A = nd.random.normal(shape=(4096,4096))
        B = nd.random.normal(shape=(4096,4096))
        # 1. Compute MABiM2 one at a time and assign its outcome to ci directly.
        c = np.zeros((4096,1))
        start = time.time()
        for i in range(4096):
            c[i] = nd.norm(nd.dot(A, B[:,i])).asscalar()
        end = time.time()
        print("Method 1 takes ", end - start)
        # 2. Use an intermediate storage d in NDArray for assignments and copy t
        o NumPy at the end.
        d = nd.zeros((4096,1))
        start = time.time()
        for i in range(4096):
            d[i] = nd.norm(nd.dot(A, B[:,i])).asscalar()
        c = d.asnumpy()
        end = time.time()
        print("Method 2 takes ", end - start)
```

Method 1 takes 25.370314121246338 Method 2 takes 23.677567958831787

5. Memory efficient computation

We want to compute $C \leftarrow A \cdot B + C$, where A, B and C are all matrices. Implement this in the most memory efficient manner. Pay attention to the following two things:

- 1. Do not allocate new memory for the new value of C.
- 2. Do not allocate new memory for intermediate results if possible.

```
In [4]: C = nd.zeros((4096,4096))
        #tic = time.time()
        C = nd.elemwise_add(nd.dot(A,B),C)
        #print(time.time()-tic)
        #tic = time.time()
        nd.elemwise_add(nd.dot(A,B),C,out=C)
        #print(time.time()-tic)
Out[4]: [[-6.43394279e+00 -1.37317566e+02 -8.94156723e+01 ... 6.33354111e+01
           7.78073883e+01 8.15101318e+01]
         [-1.49630295e+02 1.58471893e+02
                                           6.12498245e+01 ... -5.57203674e+00
           1.27422363e+02 -9.79201736e+01]
         [-1.26177185e+02 -1.60241714e+02 5.05774918e+01 ... 3.18762283e+01
          -1.06060280e+02 2.81837463e-01]
         [ 1.89660625e+01 -1.08990974e+01 1.35774994e+02 ... 1.20331802e+02
          -3.09089050e+01 1.33221344e+02]
         [ 9.73447418e+01 2.68981476e+01 -1.48852234e+02 ... -2.40328922e+01
          -1.02886139e+02 1.24706306e+02]
         [-1.58903694e+00 -2.09539986e+01 -3.99479187e+02 ... -3.73300819e+01
           7.10207214e+01 1.08717667e+02]]
        <NDArray 4096x4096 @cpu(0)>
```

6. Broadcast Operations

In order to perform polynomial fitting we want to compute a design matrix A with

$$A_{ij} = x_i^j$$

Our goal is to implement this **without a single for loop** entirely using vectorization and broadcast. Here $1 \le j \le 20$ and $x = \{-10, -9.9, \dots 10\}$. Implement code that generates such a matrix.

```
In [8]: j=nd.arange(1,21)
    x=nd.arange(-10,11).reshape(21,1)
    nd.broadcast_power(x,j)
    #x**j
```

```
Out[8]: [[-1.00000000e+01
                           1.00000000e+02 -1.0000000e+03
                                                            1.00000000e+04
          -1.0000000e+05
                            1.00000000e+06 -1.0000000e+07
                                                            1.0000000e+08
                           1.00000000e+10 -9.99999980e+10
          -1.0000000e+09
                                                            9.9999996e+11
          -9.99999983e+12
                           1.00000000e+14 -9.99999987e+14
                                                            1.00000003e+16
                           9.99999984e+17 -9.99999998e+18
          -9.99999984e+16
                                                            1.00000002e+20]
                           8.10000000e+01 -7.29000000e+02
                                                            6.56100000e+03
         [-9.0000000e+00
                           5.31441000e+05 -4.78296900e+06
          -5.90490000e+04
                                                            4.30467200e+07
          -3.87420480e+08
                           3.48678451e+09 -3.13810596e+10
                                                            2.82429522e+11
          -2.54186593e+12
                           2.28767931e+13 -2.05891136e+14
                                                            1.85302015e+15
                           1.50094642e+17 -1.35085174e+18
          -1.66771819e+16
                                                            1.21576651e+19]
                           6.40000000e+01 -5.12000000e+02
         [-8.0000000e+00
                                                            4.09600000e+03
          -3.27680000e+04
                           2.62144000e+05 -2.09715200e+06
                                                            1.67772160e+07
                           1.07374182e+09 -8.58993459e+09
          -1.34217728e+08
                                                            6.87194767e+10
          -5.49755814e+11
                            4.39804651e+12 -3.51843721e+13
                                                            2.81474977e+14
                           1.80143985e+16 -1.44115188e+17
          -2.25179981e+15
                                                            1.15292150e+18]
                           4.90000000e+01 -3.43000000e+02
         [-7.0000000e+00
                                                            2.40100000e+03
                           1.17649000e+05 -8.23543000e+05
          -1.68070000e+04
                                                            5.76480100e+06
          -4.03536080e+07
                           2.82475264e+08 -1.97732672e+09
                                                            1.38412872e+10
          -9.68890122e+10
                           6.78223086e+11 -4.74756153e+12
                                                            3.32329302e+13
          -2.32630511e+14
                            1.62841363e+15 -1.13988947e+16
                                                            7.97922632e+161
         [-6.0000000e+00
                           3.60000000e+01 -2.16000000e+02
                                                            1.29600000e+03
                           4.66560000e+04 -2.79936000e+05
          -7.77600000e+03
                                                            1.67961600e+06
                           6.04661760e+07 -3.62797056e+08
          -1.00776960e+07
                                                            2.17678234e+09
                           7.83641641e+10 -4.70184985e+11
          -1.30606940e+10
                                                            2.82110984e+12
                            1.01559954e+14 -6.09359759e+14
          -1.69266591e+13
                                                            3.65615856e+15]
         [-5.0000000e+00
                           2.50000000e+01 -1.25000000e+02
                                                            6.25000000e+02
          -3.12500000e+03
                           1.56250000e+04 -7.81250000e+04
                                                            3.90625000e+05
                           9.76562500e+06 -4.88281240e+07
          -1.95312500e+06
                                                            2.44140624e+08
          -1.22070310e+09
                           6.10351565e+09 -3.05175777e+10
                                                            1.52587895e+11
          -7.62939441e+11
                           3.81469721e+12 -1.90734863e+13
                                                            9.53674336e+13]
                           1.60000000e+01 -6.40000000e+01
         [-4.00000000e+00
                                                            2.56000000e+02
          -1.02400000e+03
                           4.09600000e+03 -1.63840000e+04
                                                            6.55360000e+04
                           1.04857600e+06 -4.19430400e+06
          -2.62144000e+05
                                                            1.67772160e+07
          -6.71088640e+07
                           2.68435456e+08 -1.07374182e+09
                                                            4.29496730e+09
                           6.87194767e+10 -2.74877907e+11
          -1.71798692e+10
                                                            1.09951163e+12]
                           9.00000000e+00 -2.7000000e+01
         [-3.0000000e+00
                                                            8.10000000e+01
          -2.43000000e+02
                           7.29000000e+02 -2.18700000e+03
                                                            6.56100000e+03
                           5.90490000e+04 -1.77147000e+05
          -1.96830000e+04
                                                            5.31441000e+05
                           4.78296900e+06 -1.43489070e+07
          -1.59432300e+06
                                                            4.30467200e+07
          -1.29140160e+08
                           3.87420480e+08 -1.16226150e+09
                                                            3.48678451e+091
                           4.00000000e+00 -8.00000000e+00
         [-2.0000000e+00
                                                            1.6000000e+01
          -3.20000000e+01
                           6.4000000e+01 -1.28000000e+02
                                                            2.56000000e+02
          -5.12000000e+02
                           1.02400000e+03 -2.04800000e+03
                                                            4.09600000e+03
          -8.19200000e+03
                            1.63840000e+04 -3.27680000e+04
                                                            6.55360000e+04
                           2.62144000e+05 -5.24288000e+05
          -1.31072000e+05
                                                            1.04857600e+061
         [-1.0000000e+00
                           1.00000000e+00 -1.0000000e+00
                                                            1.0000000e+00
                           1.00000000e+00 -1.0000000e+00
          -1.00000000e+00
                                                            1.0000000e+00
                           1.00000000e+00 -1.0000000e+00
          -1.00000000e+00
                                                            1.0000000e+00
                            1.00000000e+00 -1.0000000e+00
          -1.0000000e+00
                                                            1.0000000e+00
          -1.00000000e+00
                            1.00000000e+00 -1.0000000e+00
                                                            1.0000000e+001
         [ 0.0000000e+00
                           0.00000000e+00
                                            0.00000000e+00
                                                            0.0000000e+00
           0.0000000e+00
                                            0.0000000e+00
                           0.00000000e+00
                                                            0.0000000e+00
           0.0000000e+00
                           0.00000000e+00
                                            0.0000000e+00
                                                            0.0000000e+00
           0.0000000e+00
                           0.00000000e+00
                                            0.0000000e+00
                                                            0.0000000e+00
           0.0000000e+00
                           0.0000000e+00
                                            0.0000000e+00
                                                            0.00000000e+001
         [ 1.0000000e+00
                            1.0000000e+00
                                            1.0000000e+00
                                                            1.0000000e+00
                           1.00000000e+00
                                            1.0000000e+00
                                                            1.0000000e+00
           1.0000000e+00
```

```
1.0000000e+00
                                    1.0000000e+00
                                                     1.0000000e+00
                   1.00000000e+00
   1.0000000e+00
                   1.00000000e+00
                                    1.0000000e+00
                                                     1.0000000e+00
   1.0000000e+00
                   1.0000000e+00
                                    1.0000000e+00
                                                     1.0000000e+00]
 [ 2.0000000e+00
                   4.00000000e+00
                                    8.0000000e+00
                                                     1.60000000e+01
   3.20000000e+01
                   6.4000000e+01
                                    1.28000000e+02
                                                     2.56000000e+02
   5.12000000e+02
                   1.02400000e+03
                                    2.04800000e+03
                                                     4.09600000e+03
   8.19200000e+03
                   1.63840000e+04
                                    3.27680000e+04
                                                     6.55360000e+04
   1.31072000e+05
                   2.62144000e+05
                                    5.24288000e+05
                                                     1.04857600e+061
 [ 3.0000000e+00
                   9.0000000e+00
                                    2.70000000e+01
                                                     8.10000000e+01
   2.43000000e+02
                   7.29000000e+02
                                    2.18700000e+03
                                                     6.56100000e+03
   1.96830000e+04
                   5.90490000e+04
                                    1.77147000e+05
                                                     5.31441000e+05
   1.59432300e+06
                   4.78296900e+06
                                    1.43489070e+07
                                                     4.30467200e+07
   1.29140160e+08
                   3.87420480e+08
                                    1.16226150e+09
                                                     3.48678451e+09]
 [ 4.0000000e+00
                   1.60000000e+01
                                    6.4000000e+01
                                                     2.56000000e+02
   1.02400000e+03
                   4.09600000e+03
                                    1.63840000e+04
                                                     6.55360000e+04
   2.62144000e+05
                   1.04857600e+06
                                    4.19430400e+06
                                                     1.67772160e+07
   6.71088640e+07
                   2.68435456e+08
                                    1.07374182e+09
                                                     4.29496730e+09
   1.71798692e+10
                   6.87194767e+10
                                    2.74877907e+11
                                                     1.09951163e+12]
 [ 5.0000000e+00
                   2.50000000e+01
                                    1.25000000e+02
                                                     6.25000000e+02
   3.12500000e+03
                   1.56250000e+04
                                    7.81250000e+04
                                                     3.90625000e+05
   1.95312500e+06
                   9.76562500e+06
                                    4.88281240e+07
                                                     2.44140624e+08
                                                     1.52587895e+11
   1.22070310e+09
                   6.10351565e+09
                                    3.05175777e+10
   7.62939441e+11
                   3.81469721e+12
                                    1.90734863e+13
                                                     9.53674336e+131
 [ 6.0000000e+00
                   3.60000000e+01
                                    2.16000000e+02
                                                     1.29600000e+03
   7.77600000e+03
                   4.66560000e+04
                                    2.79936000e+05
                                                     1.67961600e+06
   1.00776960e+07
                   6.04661760e+07
                                    3.62797056e+08
                                                     2.17678234e+09
                   7.83641641e+10
   1.30606940e+10
                                    4.70184985e+11
                                                     2.82110984e+12
   1.69266591e+13
                   1.01559954e+14
                                    6.09359759e+14
                                                     3.65615856e+15]
 [ 7.0000000e+00
                   4.90000000e+01
                                    3.43000000e+02
                                                     2.40100000e+03
   1.68070000e+04
                   1.17649000e+05
                                    8.23543000e+05
                                                     5.76480100e+06
                                                     1.38412872e+10
   4.03536080e+07
                   2.82475264e+08
                                    1.97732672e+09
   9.68890122e+10
                   6.78223086e+11
                                    4.74756153e+12
                                                     3.32329302e+13
   2.32630511e+14
                   1.62841363e+15
                                    1.13988947e+16
                                                     7.97922632e+161
 [ 8.0000000e+00
                   6.4000000e+01
                                    5.12000000e+02
                                                     4.09600000e+03
   3.27680000e+04
                   2.62144000e+05
                                    2.09715200e+06
                                                     1.67772160e+07
   1.34217728e+08
                   1.07374182e+09
                                    8.58993459e+09
                                                     6.87194767e+10
   5.49755814e+11
                   4.39804651e+12
                                    3.51843721e+13
                                                     2.81474977e+14
   2.25179981e+15
                   1.80143985e+16
                                    1.44115188e+17
                                                     1.15292150e+18]
 [ 9.0000000e+00
                   8.10000000e+01
                                    7.29000000e+02
                                                     6.56100000e+03
   5.90490000e+04
                   5.31441000e+05
                                    4.78296900e+06
                                                     4.30467200e+07
                   3.48678451e+09
   3.87420480e+08
                                    3.13810596e+10
                                                     2.82429522e+11
   2.54186593e+12
                   2.28767931e+13
                                    2.05891136e+14
                                                     1.85302015e+15
                   1.50094642e+17
   1.66771819e+16
                                    1.35085174e+18
                                                     1.21576651e+191
 [ 1.0000000e+01
                   1.00000000e+02
                                    1.00000000e+03
                                                     1.0000000e+04
   1.00000000e+05
                   1.00000000e+06
                                    1.00000000e+07
                                                     1.00000000e+08
                                                     9.99999996e+11
   1.0000000e+09
                   1.0000000e+10
                                    9.99999980e+10
   9.99999983e+12
                   1.00000000e+14
                                    9.99999987e+14
                                                     1.00000003e+16
   9.99999984e+16
                   9.99999984e+17
                                    9.9999998e+18
                                                     1.00000002e+20]]
<NDArray 21x20 @cpu(0)>
```

In []: