# **HW05**

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#### Problem 1

```
test = read.csv("test.csv")
test$Pclass = as.factor(test$Pclass)
train = read.csv("train.csv")
train$Pclass = as.factor(train$Pclass)
summary(train$Age)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
## 0.42 20.12 28.00 29.70 38.00 80.00 177
```

We notice that Age has 177 missing values. So we have to fill in these missing values. We'd like to replace them with average Age. But we divided data into several groups. People with the "Miss." title are ususally young. So we replace their missing Age by the average Age of the people with "Miss." title. Etc.

```
#average age for "Miss."
agel = mean(train[grep("Miss",train$Name),]$Age,na.rm = TRUE)
#average age for "Mrs."
age2 = mean(train[grep("Mrs",train$Name),]$Age,na.rm=TRUE)
#average age for "Master."
age3 = mean(train[grep("Master",train$Name),]$Age,na.rm = TRUE)
#average age for "Mr."
age4 = mean(train[grep("Mr",train$Name),]$Age,na.rm = TRUE)

train$Age[grep("Miss",train$Name)]= age1
train$Age[grep("Mrs",train$Name)]= age2
train$Age[grep("Master",train$Name)]= age3
train$Age[grep("Mr",train$Name)]= age4
train$Age[grep("Dr",train$Name)] = age4
summary(train$Age)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 4.574 28.000 33.118 29.744 33.118 70.000
```

```
train$Title = "Other"
train$Title[grep("Miss",train$Name)]="Miss"
train$Title[grep("Mrs",train$Name)]="Mrs"
train$Title[grep("Master",train$Name)]="Master"
train$Title[grep("Mr",train$Name)]= "Mr"
```

```
#average age for "Miss."
age1 = mean(test[grep("Miss",test$Name),]$Age,na.rm = TRUE)
#average age for "Mrs."
age2 = mean(test[grep("Mrs",test$Name),]$Age,na.rm=TRUE)
#average age for "Master."
age3 = mean(test[grep("Master",test$Name),]$Age,na.rm = TRUE)
#average age for "Mr."
age4 = mean(test[grep("Mr",test$Name),]$Age,na.rm = TRUE)

test$Age[grep("Miss",test$Name)]= age1
test$Age[grep("Mrs",test$Name)]= age2
test$Age[grep("Master",test$Name)]= age3
test$Age[grep("Mr",test$Name)]= age4
test$Age[grep("Ms",test$Name)]= age4
test$Age[grep("Ms",test$Name)]= age1
summary(test$Age)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 7.406 33.747 33.747 30.306 33.747 53.000
```

```
test$Title = "Other"
test$Title[grep("Miss",test$Name)]="Miss"
test$Title[grep("Mrs",test$Name)]="Mrs"
test$Title[grep("Master",test$Name)]="Master"
test$Title[grep("Mr",test$Name)]= "Mr"

test$Title[grep("Mr",test$Name)]= "Mr"
```

```
formula = "Survived ~ Title + Pclass + Sex + Age + Fare + SibSp + Parch"
model = glm(formula, family = "binomial", data=train)
rs =summary(regsubsets(Survived ~ Title + Pclass + Sex + Age + Fare + SibSp + Parch+E
mbarked,data=train))
fit = predict(model,test,type = 'response')
sur = rep(2, 418)
for (i in 1:418) {
  if (fit[i] > 0.6){
    sur[i] = 1
  }else{
    sur[i] = 0
  }
}
test$Survived = sur
write.csv(test[c("PassengerId", "Survived")], file = "submmision.csv", row.names = FALSE
)
```

#### Adding a title feature gives a 0.79425 accuracy



### Problem 2

For logistic regression, we estimate  $\beta_i$  by maximize the log likelihood  $\ell(\beta)$  and its gradient is given by  $\nabla \ell(\beta) = X^T (Y - \hat{p})$  in order to maximize the log likelihood, we let  $\nabla \ell(\beta) = 0$   $X^T (Y - \hat{p}) = 0$ , this means  $Y - \hat{p}$  is orthogonal to the row of  $X^T$ , which is also the column of X

## **Problem 3**

```
se = 0.6864/0.313 = 2.193
              Coefficients:
                                Estimate Std.Error z value Pr(>|z|)
               (Intercept)
                                0.6864
                                            XXXXX
                                                      0.313
                                                              0.754146
                                                                            se=-0.905/-4.349=0.208
                                                              1.37e-05 ***
              log(distance)
                               -0.9050
                                            XXXXX
                                                     -4.349
              log(NoOfPools)
                                0.5027
                                            0.2004
                                                      2.509
                                                              0.012102 *
              meanmin
                                 1.1153
                                            0.3131
                                                      3.562
                                                              0.000369 ***
                               0 âĂŸ***âĂŹ 0.001 âĂŸ**âĂŹ 0.01 âĂŸ*âĂŹ 0.05 âĂŸ.âĂŹ 0.1 âĂŸ âĂŹ
              Signif. codes:
               (Dispersion parameter for binomial family taken to be 1)
ybar=79/212 mll.null = 212*ybar*log(ybar) + 212*(1-ybar)*log(1-ybar) = -139.99 null deviance = -2*mll.null = 279.98
              Null deviance: XXXXX on XXX degrees of freedom df=212-1=211
              Residual deviance: XXXXX on XXX degrees of freedom
                              214.18
              AIC: 222.18
                                            df=n-p-1=208
                                                            AIC = residual deviance plus 2*(p+1)
              Number of Fisher Scoring iterations: 5
                                                            p=3
              Also consider the following R code:
                                                            222.18-8=214.18
              X = model.matrix(frogs.glm)
              W = diag(frogs.glm$fitted.values*(1 - frogs.glm$fitted.values))
              solve(t(X) %*% W %*% X)
              which gave me the output
                                (Intercept) log(distance) log(NoOfPools)
                                                                               meanmin
                                4.8038479 -0.363947754
               (Intercept)
                                                            -0.255928180 -0.49698440
              log(distance)
                               -0.3639478
                                             0.043313307
                                                             0.008053415 0.01562971
              log(NoOfPools) XXXXXXXXX
                                             0.008053415
                                                             0.040141698 0.02678507
                               -0.4969844
                                             0.015629708
                                                             0.026785069 XXXXXXXX
                              -0.255928180, same as (1,3) entry
                                                                          0.3131^2 = 0.09803161
```

b. plug in data we get

$$p_i = \frac{e^{\beta_0 + X\beta}}{1 + e^{\beta_0 + X\beta}} = 0.7646$$

c. the null deviance won't get affected, because it has not involved any explanatory variables the residual deviance could increase or decrease, because it is related to AIC, which could increase or decrease when we add more parameters.

# **Problem 4**

a.

$$\nabla \mathcal{E}(\beta) = X^T (Y - \hat{p}) = 0$$

b)

$$\hat{p} = \frac{e^{\hat{\beta}_0 + X\hat{\beta}}}{1 + e^{\hat{\beta}_0 + X\hat{\beta}}}$$

c)

 $Y - \hat{p}$  is orthogonal to column of XX has 1 as its first column, so

$$\sum_{i=1}^{n} y_i - \hat{p_i} = 0$$

the number of  $y_i$  that are equal to 1

$$\sum_{i=1}^{n} y_i = \sum_{i=i}^{n} \hat{p_i}$$

d)

residual deviance = 
$$-2 * \sum_{i=1}^{n} [y_i \cdot log(\hat{p}_i) + (1 - y_i) \cdot log(1 - \hat{p}_i)]$$

#### Problem 5

```
Coefficients:
                                   Estimate Std. Error z value
                                                                   z=4.11947/0.36342=11.335
                 (Intercept)
                                   4.11947
                                               0.36342
                                                         XXXXXX
                 log(crl.tot)
                                   0.30228
                                               0.03693
                                                           8.185
                 log(dollar + s) 0.32586
                                               0.02365
                                                          13.777
                 log(bang + s)
                                   0.40984
                                               0.01597
                                                          25.661
                                                                  estimate=0.028*12.345=0.34566
                 log(money + s)
                                                          12.345
                                   XXXXXXX
                                               0.02800
                 log(n000 + s)
                                   0.18947
                                                           6.463
                                               0.02931
                                                          -5.177
                 log(make + s)
                                  -0.11418
                                               0.02206
                 Signif. codes: 0 âĂŸ***âĂŹ 0.001 âĂŸ**âĂŹ 0.01 âĂŸ*âĂŹ 0.05 âĂŸ.âĂŹ 0.1 âĂŸ âĂŹ
n = 4601
ybar=1813/4601
                 (Dispersion parameter for binomial family taken to be 1)
   =0.394
                mll.null = 4601*0.394*log(0.394) + 4601*(1-0.394)*log(1-0.394) = -3084.99
                 Null deviance: XXXXXX on XXXX degrees of freedom null deviance=-2*mll.null=6169.97
p=6
                                                                             df = n-1=4600
                 Residual deviance: 3245.1 on XXXX degrees of freedom
                 AIC: XXXXXX AIC = residual deviance + 2*(p+1)=3245.1+2*7=3259.1
                               df = n-p-1=4601-7=4594
                 Number of Fisher Scoring iterations: 6
```

b. plug in data we get

$$\beta_0 + X\beta = 4.11947 + 0.30228 * log(157) + 0.32586 * log(0.868 + 0.001) + 0.40984 * log(2.894 + 0.001) = 6.037771$$

$$p_i = \frac{e^{(\beta_0 + X\beta)}}{1 + e^{(\beta_0 + X\beta)}} = \frac{e^{(6.037771)}}{1 + e^{(6.037771)}} = 0.9976188$$

c. I would use M1, since AIC is smaller for M1 than M2. Perhaps the original data are skewed, so taking logarithms transformation is better.