Optional practice problems

Stat 151A, Fall 2017

October 19, 2017

- 1. For the following statements determine whether they are true of false. In each case provide a reason behind your choice.
 - (a) AIC tends to favor model selection of models with larger number of parameters.
 - (b) Say the true model is

$$y_i = x_i^T \beta + z_i^T \delta + e_i, \quad i = 1, \dots, n.$$

Then if we use only the x variables, we get an unbiased estimator of β .

- (c) The studentized residuals have variance equal to one.
- (d) Cook distance can only detect outliers on x.
- (e) Any high leverage point is also an influential point.
- $2. \ \, \text{The following problems from the book: } 11.1,\,11.3,\,12.2,\,12.3,\,12.4,\,12.5.$
- 3. Recall that the delta method tells us that

$$Var(h(y)) \approx h'(Ey)^2 Var(y).$$

Prove that $sin^{-1}(\sqrt{Y})$ is approximately variance stabilizing when $Y_i = X_i/m_i$ is a proportion distributed as binomial with X_i successes and m_i trials.

$$\frac{d}{dz}sin^{-1}(z) = \frac{1}{\sqrt{1-z^2}}$$
$$\int sin^{-1}(z)dz = zsin^{-1}(z) + \sqrt{1-z^2} + C$$

- 4. Let h_i be the leverage point for an observation i.
 - (a) Show that $\sum h_i = tr(H) = p + 1$. Hint: Recall that tr(ABC) = tr(BCA) = tr(CAB) when the dimension of the matrices are such that all of those operations are well defined.
 - (b) What implications does this have for interpreting large leverage values?