

# Parallel Acceleration of EpicFlow with Red/Black Successive Over Relaxation Using GPUs with CUDA

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## Abstract

We propose a strategy to improve the computational speed of state-of-the-art optical flow estimation methods, targeted at large displacements with significant occlusions, by exploiting the substantial computational potential of Graphics Processing Units (GPUs) under the CUDA environment. The optical flow estimation method involves an energy minimization phase which we solve using an efficient and parallel numerical approximation scheme, Successive Over Relaxation with Red-Black ordering (Red-Black SOR). In addition, we show that choosing optimal memory allocation and access patterns are critical in maximizing the computational and memory throughput for the estimation. The primary contribution of this project extends EpicFlow[1], the state-of-the-art in optical flow estimation, by replacing the serial optimization procedure with a parallel optimization algorithm deployed on the GPU in the CUDA environment. Optimizations are focused on data parallelism and threads deployment tuning; the management of which is critical to efficient GPU implementations. The proposed energy minimization variation, along with efficient GPU memory access patterns, performs on par with the state of the art on the Middlebury dataset. Experimental results are shown on NVIDIA GTX 750M and compared against the performance of an Intel Core i7 CPU. The speed-up factor for our set of GPU optimizations reaches 2.5x for successive over relaxation computation time and 2x for the overall execution time for energy minimization as compared to the CPU.

## 1 Introduction

Programmable GPUs provide a competitive alternative to traditional CPUs by delivering high performance computing with extremely high floating point performance for scientific applications [2]. As a result, there has been plenty of research interest in exploiting GPU horsepower for problems in diverse fields, especially for applications that involve numerical computing techniques [3]. Multidimensional arrays are used as primary data structures in many numerical computing techniques, which provides an opportunity to take advantage of Single Instruction Multiple Data (SIMD) parallelism. It is quite challenging to optimize such techniques for the GPU since most numerical computing techniques are iterative in nature. One such problem of interest in computer vision is the estimation of optical flow.

Optical flow is a classic computer vision problem where the primary goal is to track moving objects, surfaces and edges in a sequence of image frames by way of computing the displacement of pixels between every pair of frames in the sequence. To achieve this goal, we assume that the gray values of corresponding pixels are the same in both image frames of the pair. Optical flow is important to providing visual systems the ability to discern possibilities for action within an environment [4]. In addition, optical flow stimulus is important for the perception of movement by an observer in the environment; perception of the shape, distance and movement of objects in the environment; and for locomotive control [5]. As a result, it is used as a fundamental framework for applications such as image and surface reconstruction; object tracking and detection; and robot navigation.

There have been an abundance of optical flow estimation techniques, but it remains challenging to deal with occlusions, motion discontinuities and large displacements.<sup>1</sup>

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<sup>1</sup> [github.com/jazzthejackrabbit/epic-flow-cuda](https://github.com/jazzthejackrabbit/epic-flow-cuda)

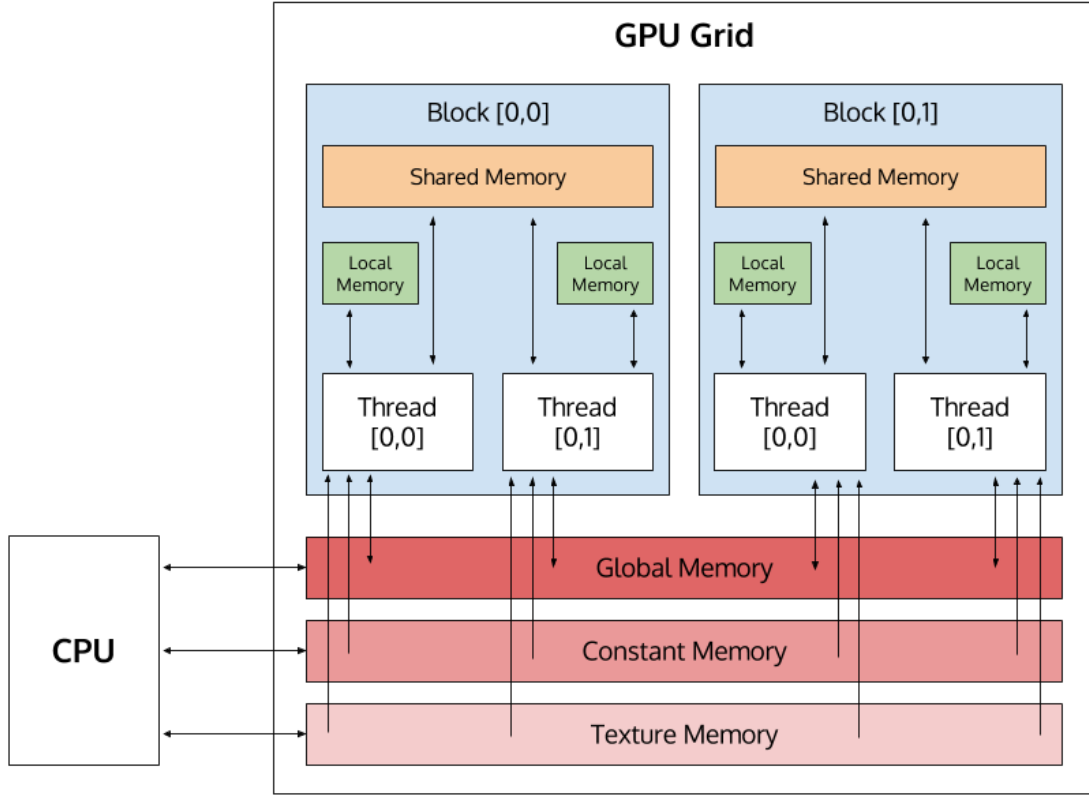


Figure 1: GPU Architecture and Structure of Communication

Our work extends [1] by accelerating the successive over relaxation method of solving the energy minimization; an inherently sequential method in its original form. Successive over relaxation is an iterative method that in the application of optical flow creates a bottleneck in terms of computational time. Due to its iterative nature, the energy minimization takes more than 50% of the computational time. Therefore, in the same spirit as [6], we use a multi colored ordering technique for the successive over relaxation method to decrease the computational time for optical flow estimation. In addition, as optimizing algorithms on the GPU within the CUDA environment can be challenging, we explore the use of different memory access patterns and memory types. It is very important to follow optimal access patterns to get maximum memory bandwidth; especially given how costly accesses to device memory are, thus making it a non-trivial task. The performance is commonly limited by the bandwidth, since majority of the operation consists of data-accesses.

The rest of the paper is organised as follows: **Section 2** describes the GPU programming model and architecture. **Section 3** details the EpicFlow algorithm and explores the parallel variation on energy minimization. **Section 4** describes the implementational details and experiments for different memory techniques used to improve speed of computation. **Section 5** presents results and performance benchmarks of the GPU experiments. **Section 6** provides concluding remarks.

## 2 Graphical Processing Unit

Graphical Processing Units (GPU), have evolved into highly parallel, multithreaded, multi-core co-processors. They offer a substantial amount of computational horsepower by featuring thousands of Arithmetic Logic Units (ALU), hundreds of processors and tens of thousands of concurrent threads per application. GPUs provide more hardware for computation which are potentially more power efficient but offer a more restrictive programming model and as a result implementations of algorithms on the GPU can be challenging.

### 2.1 CUDA Programming Model and Architecture

NVIDIA's Compute Unified Device Architecture (CUDA), is a general purpose programming model for GPUs. It is a heterogeneous model in which both the CPU and the GPU are used.

In CUDA, the host refers to the CPU and its memory, while the device refers to the GPU and its memory. A typical parallel GPU based program involves allocating memory on the device, moving data from the host memory into the allocated device memory, launching and executing computational units (kernels) in parallel by GPU threads and then copying data back into the host from the device. CUDA executes a kernel as a grid of thread-blocks. This allows the computational work to be divided among the available compute resources. Threads in a block share access to a fast memory store independent to each thread-block called shared memory. GPUs feature streaming multiprocessors (SM) which in turn comprise of many simple processors. Multiple thread blocks are assigned to a single SM and all threads in a thread block typically run in lock-step to solve a smaller subproblem. During execution there is a finer grouping of threads into warps. Multiprocessors on the GPU execute instructions for each warp in SIMD (Single Instruction Multiple Data) fashion. **Figure 1** shows the architecture and structure of communication between the CPU, GPU and the different memory types available on the GPU.

## 3 Optical Flow Estimation

### 3.1 Edge Preserving Interpolation of Correspondences

Edge Preserving Interpolation of Correspondences (EpicFlow) [1] is a novel approach for optical flow estimation, targeted at large displacements with significant occlusions. It consists of a novel scheme to interpolate a sparse set of matches obtained from [7] into a dense correspondence field based on an edge-aware geodesic distance instead of Euclidean distance. The distance between matches used in the interpolation is computed based on a cost map derived from [8] which respects motion boundaries. In this way, the distance between pixels belonging to the same region is low and ensures a proper edge-respecting interpolation. The interpolation process initiates the optical flow estimation.

### 3.2 Variational Energy Minimization

The dense matches obtained from the interpolation are then used in a variational energy minimization framework. The energy functional is defined as the sum of a data term and a smoothness term. The data term is based on the classical color-constancy and gradient constancy assumption with a normalization factor [9]. The flow gradient norm is penalized with a local smoothness weight for the smoothness term. The output from the sparse-to-dense interpolation is used to initialize the solution of the flow estimate for the energy minimization. The flow updates are then computed by solving linear systems using the successive over relaxation method.

#### 3.2.1 Successive Over Relaxation (SOR)

The successive over relaxation (SOR) iterative method [10] is an important solver for linear systems. It is widely used to solve linear systems or partial differential equations discretized by a finite difference method. It is inherently sequential in its original form. There have been many parallel versions of the SOR method that have been proposed to take advantage of the tremendously fast computational resources available. To distribute the computational load, the domain needs to be suitably decomposed. One of the widely used parallel versions is the multi-color SOR method which uses the multi-color ordering technique.

#### 3.2.2 Red Black Successive Over Relaxation (RB-SOR)

The image domain is split into a checkerboard pattern of 'red' and 'black' pixels, which are then processed in a color-wise manner. An element at position  $(i, j)$  is colored red if  $(i + j)$  is even, black if it is odd. The red-black ordering is illustrated in **Figure 2.1**. The computation of the flow increments takes place in two phases.

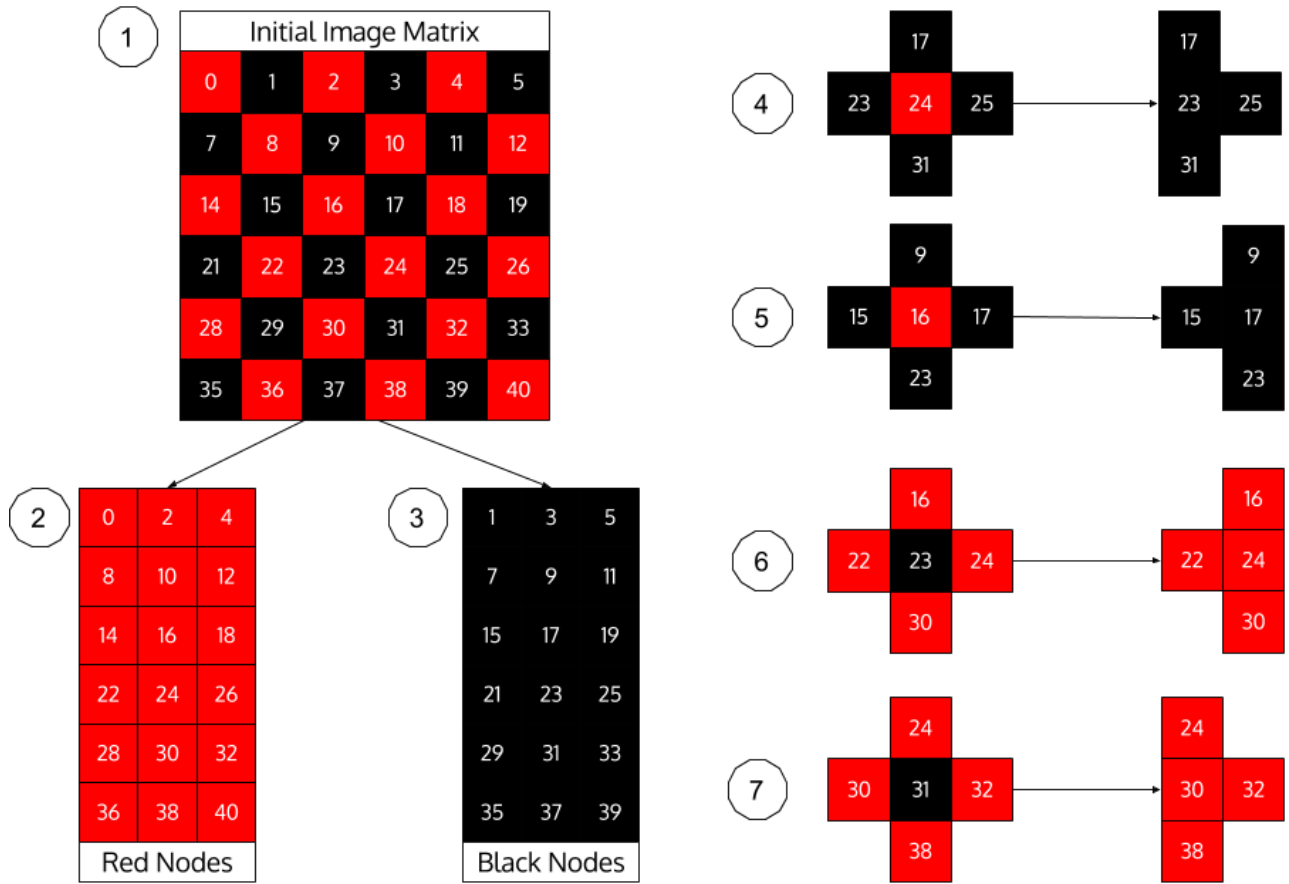


Figure 2: (1) Red black ordering of initial image matrix. (2) Matrix of red nodes. (3) Matrix of black nodes. (4-5) Black neighborhood around red nodes (6-7) Red neighborhood around black nodes.

In the first phase all the red nodes are computed as the flow-update value at each red node only depends on the neighborhood of black nodes (**Figure 2.4, 2.5**), which are completely available for all the red nodes. As a result, all the flow increments at red nodes can be partitioned into a number of independent tasks dependent only on their local neighborhood of black nodes and computed in parallel without any dependence on other red nodes. Similarly, in the second phase, the black nodes can be partitioned into independent tasks and computed in parallel as the flow-update values at these nodes only depend on the new values of the local neighborhood of red nodes which are completely available after the first phase (**Figure 2.6, 2.7**).

## 4 Implementations and Experiments

In this section, we look into various implementation strategies to speed up the process of optical flow estimation. The red-black ordering variation of the successive over relaxation method provides inherent parallelism, but it is challenging to optimize the energy minimization of the optical flow estimation for the GPU in the CUDA environment. There are many factors that could potentially affect the eventual speed-up that can be obtained; including coalesced access to memory, usage of faster memory types available on the GPU, data reordering for efficient access, usage of efficient memory allocation strategies and tuning the configuration of thread blocks deployed on the streaming multiprocessors. Adhering to these access patterns is a requirement for any performant kernel on the GPU. A more comprehensive and detailed description is provided in the CUDA programming guide [11]

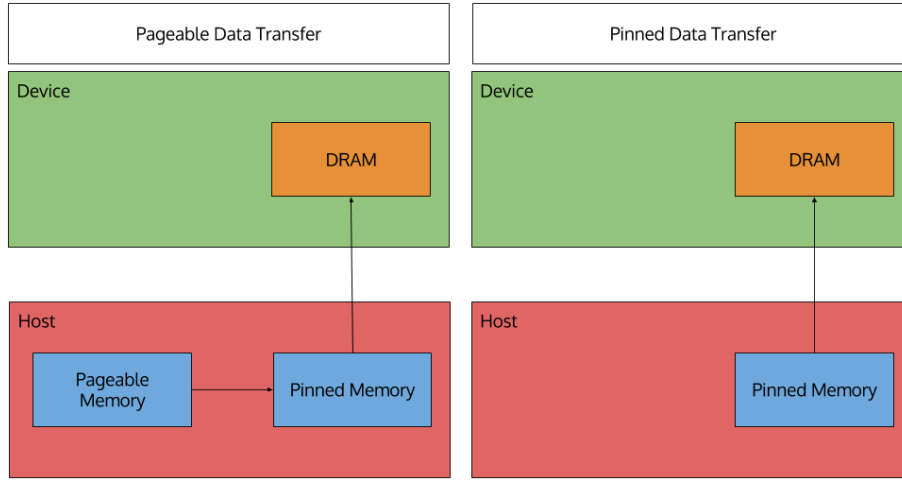


Figure 3: Pinned v/s Paged Memory Allocation

## 4.1 Global Memory

Using only the global memory provides a simple approach to parallelize the energy minimization. We first copy image data from the CPU (host) memory into the GPU (device) memory. We then define a separate GPU kernel for each of the two colors in the red-black ordering, where each kernel computes the flow update for the successive iteration for nodes of a single color. The kernel for the red nodes is executed first, followed by the kernel for the black nodes. The entire process is done five times to compute the non-linear weights that appear when applying the Euler Lagrange equations and the red-black kernels are executed thirty times to solve the linear systems to obtain the flow updates.

### 4.1.1 Comparison of Pinned and Paged Memory

By default, allocated memory on the host (CPU) is pageable. The device (GPU) cannot access this data from the pageable host memory. As a result, when a data transfer between the CPU and GPU is requested, the CUDA driver first creates a temporary page-locked host array, also known as “pinned” memory. The data is then transferred from the pageable memory to the pinned memory before it is transferred to the device memory (**Figure 3**).

Pinned memory is essentially used as a staging area for data transfers between the device to the host. An optimization strategy to improve the data transfer efficiency is to avoid the cost of the transfer between pageable and pinned host arrays by directly allocating our host arrays in pinned memory. We do so by using the CUDA specific API for allocating pinned host memory using `cudaMallocHost()` or `cudaHostAlloc()`, and deallocate it with `cudaFreeHost()`. However, over-allocating pinned memory can reduce overall system performance because it reduces the amount of physical memory available to the operating system and other programs. **Table 1** shows a comparison between the two allocation strategies.

Although using pinned host memory directly instead of pageable host memory improves access efficiency and decreases the computational time for the variational energy minimization, we can achieve a greater improvement by using better memory access strategies and faster types of memory.

### 4.1.2 Texture Memory

The successive over relaxation method accesses neighbors of a pixel, in a stencil pattern. As a result, such an access pattern doesn’t take advantage of the efficiencies provided by the GPU for coalesced memory access (explained in the next subsection). Texture memory provides an efficient access pattern for the global memory as it features an intermediate memory cache which is optimized for two dimensional locality. A memory segment allocated on the global memory has to be bound to the texture memory using `cudaBindTexture()` (costless operation) and can then be accessed using efficient read functions such as `tex1D()`, `tex2D()` or `tex3D()`. Texture memory was originally created to fetch textures applied to polygons in graphics. The texture memory space resides in device memory and is cached in texture cache, so a texture fetch costs one memory read from device memory only on a cache miss, otherwise it just costs one read from texture cache. Since texture cache is optimised for 2D spatial locality, threads of the same warp that read texture addresses that are close together in 2D will achieve best performance.

Using the texture memory access pattern, we can expect the read access to be much faster than that with global memory not bounded to a texture. Texture memory is a read-only memory and thus provides a speed bump only with respect to read access. All the writes are still performed to the global memory and thus are not at maximum efficiency.

## 4.2 Coalesced memory access

Every time a GPU thread accesses memory, it accesses a larger chunk of memory in one memory transaction. If other threads do the same, then similarly large chunks are accessed for each thread. However, if the other threads access memory contiguously, a new memory transaction is not required for every thread access as a larger chunk of memory is already retrieved by the previous memory transactions. As a result, maximizing coalesced access to memory will speed up the memory reads by the threads as separate memory transactions will not be required and thus, will allow the GPU program to complete faster. However, in the case of optical flow estimation, coalescing the access to memory is not as straightforward.

### 4.2.1 Memory Reorganization

In each iteration of the energy minimization, the black and red nodes are accessed first, and then the red nodes are written back, followed by accessing the red and black nodes and writing back the black nodes. This requires a strided pattern of reads and since such a pattern is not contiguous, it decreases the maximum amount of useable memory locations that can be retrieved with each memory transaction. As a result, there are more memory transactions involved. In order to avoid such sparse element accesses and to improve the coalescing, we explore the idea of reordering the elements of the image by grouping elements of the same color into a single matrix [6].

We divide the image matrix into two independent single-colored matrices, where one of them comprises only of red colored elements, and the other of only black colored elements (**Figure 2.2, 2.3**). This reordering is done parallelly in the GPU by copying the elements in the original red-black image matrix at position  $(i, j)$  to position  $(i/2, j)$  in the independent single-colored matrices appropriately, depending on the color of the element. Reordering in such a way allows warp threads to function at maximum efficiency and increases coalesced access to memory. Nonetheless, the reordering procedure could potentially take a significant amount of time if the size of the image matrices are large, but since the operation is done parallelly, it is scalable and fast. The red black SOR procedure involves access to black colored neighbor nodes of a red node and similarly red colored neighbor nodes of a black node. Due to the reordering, the neighbor elements of a node is in a different matrix and thus access to this neighborhood is more complex (**Figure 2.4 - 2.7**). The neighbors of a red node are three vertical nodes plus one on the left or right, depending on the row number in the reordered matrix of black nodes and vice versa for the neighbors of a black node.

## 4.3 Alternate Indexing

In CUDA, the deployed threads and blocks have indices that can be used to index elements in memory, from the CUDA kernels. These indices are linear and as a result, using the same linear indexing scheme to access alternating red elements in the first kernel and black elements in the second kernel would result in half the threads in each kernel diverging and hence, ceasing to do any useful computation. Minimizing thread divergence is important to maximize computational throughput on the GPU. As a result, we introduce an efficient alternate indexing scheme which computes the correct index of red elements and black elements within their respective kernels.

$$i_{ra} = 2i + (2(i_t/w) \bmod 2)$$

$$i_{ba} = (2i + 1) - (2(i_t/w) \bmod 2)$$

$i_{ra}$  is the alternate index for the red nodes in the matrix of red elements,  $i_{ba}$  is the alternate index for the black nodes in the matrix of black elements,  $i_t$  is the linear thread index,  $w$  is the width of the image. Using this indexing scheme, we minimize the divergence of threads and hence increase the computational efficiency.



Figure 4: Optical flow estimates from GPU and CPU implementations, and original ground truth optical flow.

## 5 Performance Results and Benchmarks

We use the NVIDIA GTX 750M GPU for all our experiments and compare the performance of the optical flow estimation against that of an Intel Core i7 CPU. To show that our GPU implementation provides an improvement over the CPU version of EpicFlow, we first show that the average endpoint error in optical flow estimation is similar in both CPU and GPU based estimations (in the average case). Then a comparison is made for computational performance between the CPU implementation and the GPU implementations. We then see how tuning the configuration of threads in a block affects computation time.

### 5.1 Optical Flow Estimation

**Figure 4** shows the optical flow visualized from the output of the GPU implementation, the CPU implementation and the ground truth flow for a sample sequence (Rubber Whale) in the Middlebury dataset [12]. **Table 1** shows the average endpoint error for the optical flow estimation using the CPU implementations and the GPU implementations. For both implementations, we use the locally affine interpolation from [1] for a sparse set of matches from [7].

Implementation	Average Endpoint Error
CPU	0.3806
GPU - Global Memory	0.3806
GPU - Texture Memory	0.3806
GPU - Memory Reorganization	0.3806

Table 1: Average End Point Errors of Optical Flow Estimation

All the GPU implementations have almost the same average endpoint error as the CPU implementations. As a result, the GPU implementation provides accurate optical flow estimation based on EpicFlow and thus can be used as a viable alternative to the CPU implementation. The following subsections show the improvement of the GPU over the CPU in terms of computational speed.

### 5.2 Computation and Execution Time

The first optimization for global memory access was to allocate data directly on the pinned memory, instead of pageable host memory. **Table 2** shows that allocating and accessing pinned memory is faster than that of pageable host memory, although it provides only a small speedup.

Type of Memory Allocation	Threads in Block	Execution Time
Paged Memory	16 x 8	1.1097
Pinned Memory	16 x 8	0.9652

Table 2: Execution Time for Pinned v/s Paged Memory Allocation

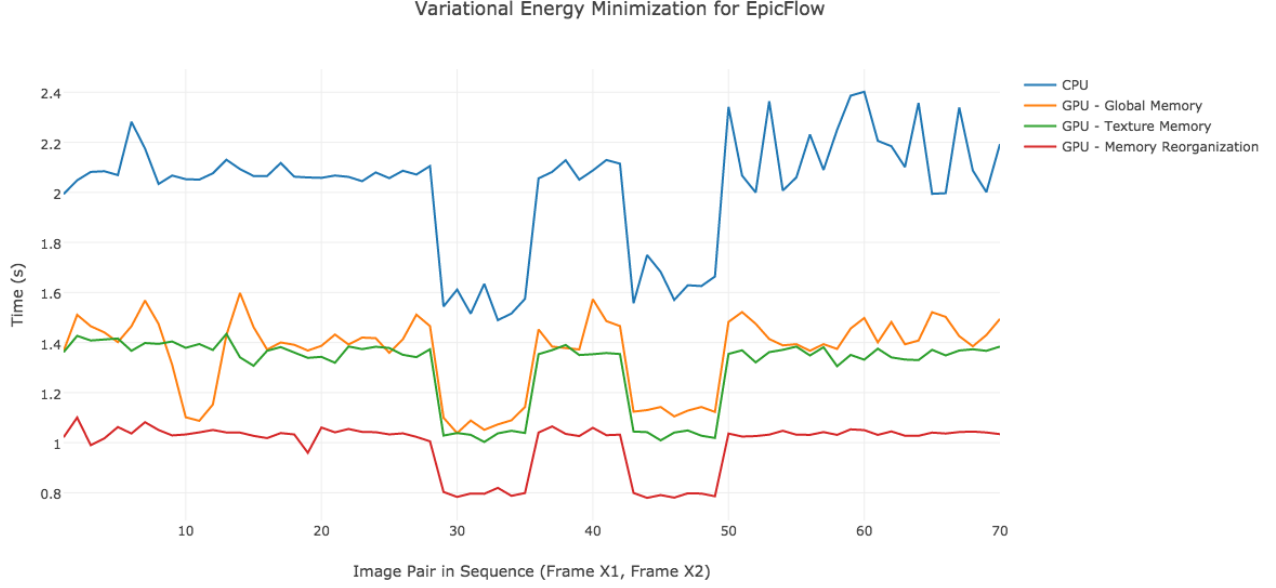


Figure 5: Execution Time for GPU and CPU implementations.

**Figure 4** shows the execution time for every pair of image in different sequences in the Middlebury dataset. **Table 3** shows the total execution time for the entire energy minimization process and computation time for the SOR method (RB-SOR for GPU), averaged for the images in the Middlebury dataset. As expected, all the GPU implementations perform faster than the CPU implementation. Specifically, the reordering of elements of the same color into two separate matrices performs (on average) 2x faster than the CPU benchmark for total execution time and 2.55x faster in terms of computation time. This indicates that memory coalescing is critical in improving the speed of execution and computation. Global memory with no other optimization is the slowest among the GPU implementations. Although it is 1.48x and 1.8x faster in terms of execution time and computation time, respectively, direct global memory access seems to be the bottleneck. Texture memory access pattern provides caching of local neighborhood access and provides a 1.54x and 1.82x improvement in execution and computation time respectively, over the CPU implementation. However, it surprisingly doesn't provide a huge improvement over direct global memory access. This is most likely because we use a one-dimensional texture. We believe that replacing one dimensional textures with two dimensional textures would improve caching of neighborhood elements and as a result improve the speed of computation.

Implementation	Execution Time (s) - Energy Minimization	Computation Time (ms) - SOR
CPU	2.0129	867.80
GPU - Global Memory	1.3565	480.33
GPU - Texture Memory	1.2995	475.15
GPU - Memory Reorganization	0.98854	340.68

Table 3: Execution Time for CPU and GPU implementations

The speed gain achieved in the computation time is higher than that of execution time primarily because the execution time takes into consideration the entire process of estimating the flow from the interpolation of dense matches and the computation time only considers the time taken by the SOR method/ Red-black SOR method. Clearly, the raw computational power of the GPU performs better than the serial CPU implementation of SOR (as evident from the computation time), but since the GPU implementation involves allocating memory on the GPU, transferring data between CPU memory and GPU memory, computing flow updates and writing them back to the CPU memory, creates a bottleneck in terms of read-write memory bandwidth. **Table 4** shows an example of profiling results obtained by running the parallel implementation of SOR on the GPU. 58.16% of the execution time is taken up by the memory copy operation to transfer data between the CPU memory and GPU memory. As a result, the maximum optimization for this application is limited by the maximum memory bandwidth.



Time	Time	Calls	Avg	Min	Max	Operation
47.79	542.36ms	45	12.052ms	12.007ms	12.110ms	CUDA memcpy HtoD
20.92	237.43ms	150	1.5829ms	1.5103ms	2.1174ms	red_sor kernel
20.91	237.26ms	150	1.5817ms	1.5084ms	2.1159ms	black_sor kernel
10.37	117.72ms	10	11.772ms	11.752ms	11.801ms	CUDA memcpy DtoH

Table 4: GPU Implementation Profiling

Furthermore, the alternate indexing scheme used to address memory locations is important while considering the speed of the computation. As we see from Table 4, using a conditional branch within the kernels to choose between the red and black elements is slower than using the alternate indexing scheme that allows access to only red or only black elements within a specific kernel. Table Y shows a comparison of the time profiles of the two indexing schemes. The alternate indexing provides an average of 1.14x speedup in execution time as compared to the conditional indexing.

Type of Indexing	Name	Time
Conditional Indexing	black_sor_reordered	146.34ms
Conditional Indexing	red_sor_reordered	142.61ms
Alternate Indexing	black_sor_reordered	128.20ms
Alternate Indexing	red_sor_reordered	129.05ms

Table 5: Kernel Execution time for indexing schemes

### 5.3 Thread Configuration

**Table 6** shows the execution times for different configurations of the best performing (memory reorganized) GPU implementation. It performs best with a 16x8 threads in a block configuration, with an execution time of 965.2 ms. The 8x4 configuration is the slowest as there are only a total of 32 threads in a block and many blocks are created during the computation. Since blocks are not guaranteed to be assigned to the same streaming multiprocessor, and thus, cannot be guaranteed to be executed at the exact same time as the others, some of the thread blocks are blocked until some of the others finish. As a result, this slows down the speed of execution.

Thread Block Size	16x8	32x8	16x16	32x4	8x16	32x16	16x32	8x32	64x2
Execution Time (s)	0.9652	0.9656	0.9659	0.9669	0.9695	0.9696	0.9706	0.9717	0.9723

Thread Block Size	64x4	64x16	64x8	8x8	32x32	16x4	32x2	16x2	8x4
Execution Time (s)	0.9745	0.9751	0.9766	0.9771	0.9885	1.0104	1.0142	1.1076	1.1344

Table 6: Thread block configuration

## 6 Conclusions

This paper explores GPU based optimizations in optical flow estimation (using EpicFlow). Since the successive over relaxation method used in the variational energy framework creates a bottleneck in performance due to its inherently serial, iterative nature, we improve the computational efficiency by offloading the heavy minimization computation to the GPU. To do so, we employ a variation on the SOR method by using a red-black color ordering to the elements in the image matrix and convert it into a two-phase parallel problem that can exploit the high computational performance of GPUs. We explore common GPU optimization strategies such as - caching non-coalesced local neighborhood of elements by using texture memory; improving memory coalescing by reorganizing data; combining texture caching and memory coalescing; using faster memory storage types such as memory registers, local thread memory and shared memory common to threads of a block; and by tuning the configuration of the deployed threads and blocks. Experimental results show a success for our techniques on NVIDIA GTX 750M, achieving good scalability and good performance versus an Intel Core i7 CPU. The speed-up factor for our set of GPU optimizations reaches a maximum of 2x for the execution times as compared to the CPU. Since this implementation is memory bandwidth limited, it prevents us from further implementation based optimizations. As a result, we can expect greater scalability moving towards a more sophisticated GPU architecture. The GPU used for experimentation is a mobile GPU that provides good computational power for small applications, but using the same strategies on more powerful GPUs with greater memory bandwidths, we can expect to see greater improvements.

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