## Lab 3: Panel Models

US Traffic Fatalities: 1980 - 2004

### Contents

## \$ s165

## \$ s170

1	U.S. traffic fatalities: 1980-2004	1
2	(30 points, total) Build and Describe the Data	4
3	(15 points) Preliminary Model	19
4	(15 points) Expanded Model	20
5	(15 points) State-Level Fixed Effects	22
6	(10 points) Consider a Random Effects Model	23
7	(10 points) Model Forecasts	24
8	(5 points) Evaluate Error	24
##	Warning: package 'plm' was built under R version 4.2.3	

### 1 U.S. traffic fatalities: 1980-2004

In this lab, we are asking you to answer the following **causal** question:

#### "Do changes in traffic laws affect traffic fatalities?"

To answer this question, please complete the tasks specified below using the data provided in data/driving.Rdata. This data includes 25 years of data that cover changes in various state drunk driving, seat belt, and speed limit laws.

Specifically, this data set contains data for the 48 continental U.S. states from 1980 through 2004. Various driving laws are indicated in the data set, such as the alcohol level at which drivers are considered legally intoxicated. There are also indicators for "per se" laws—where licenses can be revoked without a trial—and seat belt laws. A few economics and demographic variables are also included. The description of the each of the variables in the dataset is also provided in the dataset.

<dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.458, 1~

<dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0~

```
## $ s175
            ## $ slnone
            ## $ seatbelt
            <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 2, 2, 2, 2, 2, 2, ~
            <dbl> 18, 18, 18, 18, 18, 20, 21, 21, 21, 21, 21, 21, 21, 21, 2
## $ minage
## $ zerotol
            <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0~
## $ gdl
            <dbl> 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00
## $ bac10
            <dbl> 1.000, 1.000, 1.000, 1.000, 1.000, 1.000, 1.000, 1.000, 1~
            <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0~
## $ bac08
## $ perse
            <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0~
## $ totfat
            <int> 940, 933, 839, 930, 932, 882, 1080, 1111, 1024, 1029, 112~
## $ nghtfat
            <int> 422, 434, 376, 397, 421, 358, 500, 499, 423, 418, 466, 47~
            <int> 236, 248, 224, 223, 237, 224, 279, 300, 226, 247, 271, 27~
## $ wkndfat
## $ totfatpvm
            <dbl> 3.200, 3.350, 2.810, 3.000, 2.830, 2.510, 3.177, 2.970, 2~
            <dbl> 1.437, 1.558, 1.259, 1.281, 1.278, 1.019, 1.471, 1.334, 1~
## $ nghtfatpvm
## $ wkndfatpvm
            <dbl> 0.803, 0.890, 0.750, 0.719, 0.720, 0.637, 0.821, 0.802, 0~
## $ statepop
            <int> 3893888, 3918520, 3925218, 3934109, 3951834, 3972527, 399~
            <dbl> 24.14, 24.07, 21.37, 23.64, 23.58, 22.20, 27.08, 27.67, 2~
## $ totfatrte
## $ nghtfatrte
            <dbl> 10.84, 11.08, 9.58, 10.09, 10.65, 9.01, 12.53, 12.43, 10.~
## $ wkndfatrte
            <dbl> 6.060000, 6.330000, 5.710000, 5.670000, 6.000000, 5.64000~
            <dbl> 29.37500, 27.85200, 29.85765, 31.00000, 32.93286, 35.1394~
## $ vehicmiles
## $ unem
            <dbl> 8.8, 10.7, 14.4, 13.7, 11.1, 8.9, 9.8, 7.8, 7.2, 7.0, 6.9~
## $ perc14 24
            <dbl> 18.9, 18.7, 18.4, 18.0, 17.6, 17.3, 17.0, 16.6, 16.2, 15.~
            <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0~
## $ s170plus
            ## $ sbprim
## $ sbsecon
            <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, ...
## $ d80
            ## $ d81
            ## $ d82
            ## $ d83
            ## $ d84
            ## $ d85
            ## $ d86
            <int> 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, ~
## $ d87
            <int> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, ~
            <int> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, ~
## $ d88
## $ d89
            <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0,
## $ d90
            <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, ~
## $ d91
            <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, ~
## $ d92
            <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, ~
## $ d93
            <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, ~
## $ d94
            ## $ d95
## $ d96
            ## $ d97
            ## $ d98
            ## $ d99
            ## $ d00
            ## $ d01
            ## $ d02
            ## $ d03
            ## $ d04
            ## $ vehicmilespc <dbl> 7543.874, 7107.785, 7606.622, 7879.802, 8333.562, 8845.61~
desc
```

## variable label

```
## 1
                                                  1980 through 2004
              year
## 2
                               48 continental states, alphabetical
             state
## 3
              s155
                                                  speed limit == 55
## 4
              s165
                                                  speed limit == 65
## 5
              s170
                                                  speed limit == 70
## 6
              s175
                                                  speed limit == 75
## 7
            slnone
                                                     no speed limit
## 8
                        =0 if none, =1 if primary, =2 if secondary
          seatbelt
## 9
            minage
                                               minimum drinking age
## 10
                                                 zero tolerance law
           zerotol
                                     graduated drivers license law
## 11
               gdl
## 12
                                            blood alcohol limit .10
             bac10
## 13
             bac08
                                            blood alcohol limit .08
## 14
             perse administrative license revocation (per se law)
## 15
            totfat
                                           total traffic fatalities
## 16
           nghtfat
                                         total nighttime fatalities
## 17
           wkndfat
                                           total weekend fatalities
## 18
         totfatpvm
                            total fatalities per 100 million miles
## 19
        nghtfatpvm
                       nighttime fatalities per 100 million miles
## 20
        wkndfatpvm
                          weekend fatalities per 100 million miles
## 21
          statepop
                                                   state population
## 22
         totfatrte
                           total fatalities per 100,000 population
## 23
        nghtfatrte
                       nighttime fatalities per 100,000 population
## 24
        wkndfatrte
                          weekend accidents per 100,000 population
## 25
        vehicmiles
                                  vehicle miles traveled, billions
## 26
              unem
                                         unemployment rate, percent
## 27
         perc14_24
                             percent population aged 14 through 24
## 28
          sl70plus
                                               s170 + s175 + slnone
## 29
            sbprim
                                         =1 if primary seatbelt law
## 30
           sbsecon
                                      =1 if secondary seatbelt law
## 31
               d80
                                                 =1 if year == 1980
## 32
               d81
## 33
               d82
## 34
               d83
## 35
               d84
## 36
               d85
## 37
               d86
## 38
               d87
## 39
               d88
## 40
               d89
## 41
               d90
## 42
               d91
## 43
               d92
## 44
               d93
## 45
               d94
## 46
               d95
## 47
               d96
## 48
               d97
## 49
               d98
## 50
               d99
## 51
               d00
## 52
               d01
## 53
               d02
## 54
               d03
```

```
## 55 d04 =1 if year == 2004
## 56 vehicmilespc
```

### 2 (30 points, total) Build and Describe the Data

- 1. (5 points) Load the data and produce useful features. Specifically:
  - Produce a new variable, called speed\_limit that re-encodes the data that is in s155, s165, s170, s175, and slnone;
  - Produce a new variable, called year\_of\_observation that re-encodes the data that is in d80, d81, ..., d04. #TODO: Asked Vinod if this is stil necessary, since we didn't do this
  - Produce a new variable for each of the other variables that are one-hot encoded (i.e. bac\* variable series).
  - Rename these variables to sensible names that are legible to a reader of your analysis. For example, the dependent variable as provided is called, totfatrte. Pick something more sensible, like, total\_fatalities\_rate. There are few enough of these variables to change, that you should change them for all the variables in the data. (You will thank yourself later.)

```
df <- data %>%
  mutate(state = factor(state)) %>%
  rowwise() %>%
  # speed_limit
  mutate(
    speed_limit_70plus = factor(s170plus),
    speed_limit = parse_number(
      colnames(
        select(data, starts_with("sl"))
      )[which.max(c_across(starts_with("sl")))],
      na = "slnone"
   ),
  ) %>%
  select(-starts with("sl")) %>%
  mutate(year_of_observation = factor(year)) %>% # year_of_observation
  select(-starts_with("d")) %>%
  mutate(blood_alcohol_limit = parse_number(
    colnames(
      select(data, starts with("bac"))
   )[which.max(c_across(starts_with("bac")))]
  ) / 100) %>% # blood_alcohol_limit
  select(-starts_with("bac")) %>%
    seatbelt = factor(seatbelt), # 'seatbelt' categorizes primary or secondary
    speed_limit_70plus = ifelse(speed_limit == 55 | speed_limit == 65, 0, 1)
  select(-starts_with("sb"))
df <- df %>%
  dplyr::rename(
    "total fatalities rate" = "totfatrte",
    "minimum_drinking_age" = "minage",
    "zero_tolerance_law" = "zerotol",
    "graduated_drivers_license_law" = "gdl",
    "per_se_laws" = "perse",
    "total_traffic_fatalities" = "totfat",
```

```
"total_nighttime_fatalities" = "nghtfat",
    "total_weekend_fatalities" = "wkndfat",
    "total_fatalities_per_100_million_miles" = "totfatpvm",
    "nighttime_fatalities_per_100_million_miles" = "nghtfatpvm",
    "weekend fatalities per 100 million miles" = "wkndfatpvm",
    "nighttime_fatalities_rate" = "nghtfatrte",
    "weekend_fatalities_rate" = "wkndfatrte",
    "vehicle_miles" = "vehicmiles",
    "unemployment_rate" = "unem",
    "pct_population_14_to_24" = "perc14_24",
    "vehicle_miles_per_capita" = "vehicmilespc"
  ) %>%
  select(
   year_of_observation,
    state,
   year,
    # response variables
   total fatalities rate,
   nighttime_fatalities_rate,
   weekend_fatalities_rate,
   total_traffic_fatalities,
   total nighttime fatalities,
   total_weekend_fatalities,
   total_fatalities_per_100_million_miles,
   nighttime_fatalities_per_100_million_miles,
   weekend fatalities per 100 million miles,
    # potential explanatory variables
    seatbelt,
   zero_tolerance_law,
    graduated_drivers_license_law,
   per_se_laws,
   minimum_drinking_age,
   speed_limit_70plus,
   speed_limit,
   blood_alcohol_limit,
   vehicle_miles,
   vehicle_miles_per_capita,
    # econ and demographic variables
   statepop,
   unemployment_rate,
   pct_population_14_to_24, vehicle_miles
  ) # keep the similar variables together
df %>% glimpse()
## Rows: 1,200
## Columns: 25
## Rowwise:
## $ year_of_observation
                                                 <fct> 1980, 1981, 1982, 1983, 198~
## $ state
                                                 <fct> 1, 1, 1, 1, 1, 1, 1, 1, 1, ~
## $ year
                                                 <int> 1980, 1981, 1982, 1983, 198~
                                                 <dbl> 24.14, 24.07, 21.37, 23.64,~
## $ total fatalities rate
## $ nighttime_fatalities_rate
                                                 <dbl> 10.84, 11.08, 9.58, 10.09, ~
## $ weekend_fatalities_rate
                                                 <dbl> 6.060000, 6.330000, 5.71000~
```

```
## $ total traffic fatalities
                                                  <int> 940, 933, 839, 930, 932, 88~
## $ total_nighttime_fatalities
                                                  <int> 422, 434, 376, 397, 421, 35~
                                                  <int> 236, 248, 224, 223, 237, 22~
## $ total weekend fatalities
                                                   <dbl> 3.200, 3.350, 2.810, 3.000,~
## $ total_fatalities_per_100_million_miles
## $ nighttime_fatalities_per_100_million_miles <dbl> 1.437, 1.558, 1.259, 1.281,~
## $ weekend_fatalities_per_100_million_miles
                                                   <dbl> 0.803, 0.890, 0.750, 0.719,~
                                                  <fct> 0, 0, 0, 0, 0, 0, 0, 0, 0, ~
## $ seatbelt
## $ zero_tolerance_law
                                                  <dbl> 0.000, 0.000, 0.000, 0.000,~
## $ graduated_drivers_license_law
                                                  <dbl> 0.00, 0.00, 0.00, 0.00, 0.0~
## $ per_se_laws
                                                  <dbl> 0.000, 0.000, 0.000, 0.000,~
## $ minimum_drinking_age
                                                  <dbl> 18, 18, 18, 18, 18, 20, 21,~
## $ speed_limit_70plus
                                                  <dbl> 0, 0, 0, 0, 0, 0, 0, 0, 0, ~
## $ speed_limit
                                                  <dbl> 55, 55, 55, 55, 55, 55, 55,~
## $ blood_alcohol_limit
                                                  <dbl> 0.10, 0.10, 0.10, 0.10, 0.1~
## $ vehicle_miles
                                                  <dbl> 29.37500, 27.85200, 29.8576~
                                                  <dbl> 7543.874, 7107.785, 7606.62~
## $ vehicle_miles_per_capita
                                                  <int> 3893888, 3918520, 3925218, ~
## $ statepop
## $ unemployment rate
                                                  <dbl> 8.8, 10.7, 14.4, 13.7, 11.1~
                                                  <dbl> 18.9, 18.7, 18.4, 18.0, 17.~
## $ pct_population_14_to_24
     data %>% filter(sl65>0 & sl65<1) %>% select(sl55,sl65,sl70,sl75,slnone) %>% mutate(sum_sl
     = sum(sl55,sl65,sl70,sl75,slnone)), we are choosing the max when it's pct
     speed_limit_70plus column has values that are not 0 or 1, reclassify based on speed_limit column.
     Also classify the states with no speed limit as 1 for this variable.
df$zero tolerance law %>%
  table(useNA = "ifany") %>%
  as.data.frame()
##
                        . Freq
## 1
                           636
      0.0829999968409538
## 2
                             1
       0.166999995708466
## 3
## 4
                     0.25
                             6
## 5
       0.333000004291534
                             2
## 6
       0.416999995708466
                             3
## 7
                            17
## 8
       0.583000004291534
                             5
                             2
## 9
       0.666999995708466
## 10
                     0.75
                             1
                           525
                        1
df$graduated_drivers_license_law %>%
  table(useNA = "ifany") %>%
  as.data.frame()
##
                      . Freq
## 1
                      0
                         981
## 2 0.166999995708466
                           1
## 3
                   0.25
                           2
## 4
                    0.5
                          14
## 5 0.670000016689301
                   0.75
## 7 0.833000004291534
                           1
## 8
                         199
```

```
df$per_se_laws %>%
  table(useNA = "ifany") %>%
  as.data.frame()
##
                      . Freq
## 1
                      0
                         528
## 2 0.0829999968409538
                           1
## 3 0.166999995708466
                           1
## 4
                   0.25
                           4
## 5 0.333000004291534
                           2
                           2
## 6 0.416999995708466
                          16
## 7
                    0.5
## 8
                   0.75
                           1
## 9
                      1
                         645
df <- df %>%
  mutate(
    zero_tolerance_law = ifelse(
      zero_tolerance_law == 0 | zero_tolerance_law == 1, zero_tolerance_law, 1
    ),
    graduated_drivers_license_law = ifelse(
      graduated_drivers_license_law == 0 | graduated_drivers_license_law == 1,
      graduated_drivers_license_law,
      1
    ),
    per_se_laws = ifelse(
      per_se_laws == 0 | per_se_laws == 1, per_se_laws, 1
  )
```

We observed non-binary values in the following columns: zero\_tolerance\_law, graduated\_drivers\_license\_law, per\_se\_laws. But we expect them to be binary given the definition.

We decided to treat all non-zero values as 1 and make it a binary variable.

```
df$minimum_drinking_age %%
table(useNA = "ifany") %>%
as.data.frame()
```

```
##
                      . Freq
## 1
                          98
                     18
## 2
                           5
                   18.5
## 3 18.6000003814697
                           1
## 4
      18.7000007629395
## 5
                     19
                          58
## 6
                  19.5
                           5
## 7 19.7000007629395
## 8
      19.7999992370605
                           1
## 9
                     20
                          35
                  20.5
                           2
## 11 20.7000007629395
                           4
## 12
                     21
                         985
df <- df %>%
mutate(
```

```
minimum_drinking_age = round(minimum_drinking_age, 0)
)
```

We noticed that the minimum\_drinking\_age column has values that are not integers. We decided to round them to the nearest integer.

```
df %>%
  filter(is.na(speed_limit)) %>%
  select(state, year_of_observation, speed_limit, speed_limit_70plus)
## # A tibble: 9 x 4
## # Rowwise:
##
     state year_of_observation speed_limit speed_limit_70plus
##
     <fct> <fct>
                                       <dbl>
## 1 27
           1996
                                          NA
                                                              NΑ
## 2 27
           1997
                                          NA
                                                              NA
## 3 27
           1998
                                          NA
                                                              NA
## 4 27
           1999
                                          NA
                                                              NA
## 5 27
           2000
                                          NA
                                                              NA
## 6 27
           2001
                                          NΑ
                                                              NA
## 7 27
           2002
                                          NA
                                                              NA
## 8 27
           2003
                                          NA
                                                              NA
## 9 27
           2004
                                          NA
                                                              NA
# TODO: verifying with Vinod
df <- df %>%
  mutate(
    speed_limit = ifelse(
      is.na(speed_limit) & state == 27, ifelse(
        year >= 1996 \& year <= 1999, 85, 75
      ), speed_limit
    ),
    speed_limit_70plus = ifelse(
      is.na(speed_limit_70plus) & state == 27, 1, speed_limit_70plus
```

Looking at the data, we realized the *speed\_limit* is not set for State 27, between 1996 to 2004. Through some background research, this is reflecting the fact that "for three years after the 1995 repeal of the increased 65 mph limit, Montana had a non-numeric" reasonable and prudent" speed limit during the daytime on most rural roads". But it doesn't mean there was no speed limit.

We decided to set the *speed\_limit* to 85 for Montana between 1996 to 1999, given the legal case of State v. Rudy Stanko (1998), who got charged for speed of 85. Effective May 28, 1999, as a result of that decision, the Montana Legislature established a speed limit of 75 mph. So we set the *speed\_limit* to 75 for Montana between 2000 to 2004.

- 2. (5 points) Provide a description of the basic structure of the dataset. What is this data? How, where, and when is it collected? Is the data generated through a survey or some other method? Is the data that is presented a sample from the population, or is it a *census* that represents the entire population? Minimally, this should include:
  - How is the our dependent variable of interest total\_fatalities\_rate defined? This data set is a balanced longitudinal dataset and contains traffic fatalities data for the 48 continental U.S. states from 1980 through 2004. For each year of observation, the dataset contains state-level cross sectional measurements of fatality count and rate. This data is collected and distributed by Jeffrey M. Wooldridge through this link.

After our data processing work, the clean dataset has 25 columns/fields which include:

- Index variables: year\_of\_observation, state
- 9 fatality variables: There are three measurements fatality count, fatality count per 100M miles and fatality rate as defined as count per 100k population. These three measurements are provided for total, nighttime and weekend
- 10 law and vehicle variables: 8 traffic laws indicators (seatbelt, zero\_tolerance\_law, grad-uated\_drivers\_license\_law, per\_se\_laws, minimum\_drinking\_age, speed\_limit\_70plus, speed\_limit, blood\_alcohol\_limit) and 2 driving variables (vehicle\_miles, vehicle\_miles\_per\_capita)
- 3 Economics and demographic variables: statepop, unemployment rate, pct population 14 to 24

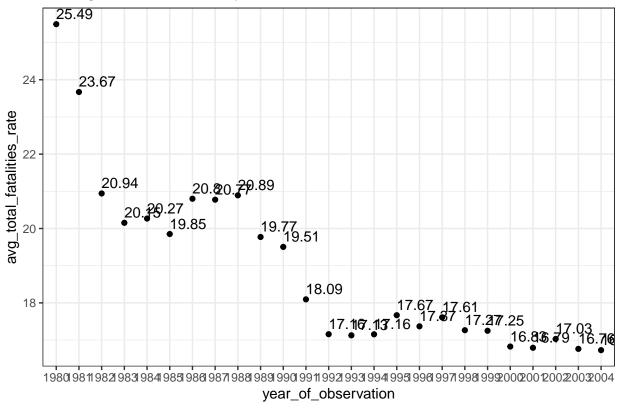
In this dataset, the total fatalities rate is defined as total fatalities per 100,000 population.

- 3. (20 points) Conduct a very thorough EDA, which should include both graphical and tabular techniques, on the dataset, including both the dependent variable total\_fatalities\_rate and the potential explanatory variables. Minimally, this should include:
- How is the our dependent variable of interest total\_fatalities\_rate defined?

  In this dataset, the total fatalities rate is defined as total fatalities per 100,000 population.
- What is the average of total\_fatalities\_rate in each of the years in the time period covered in this dataset?

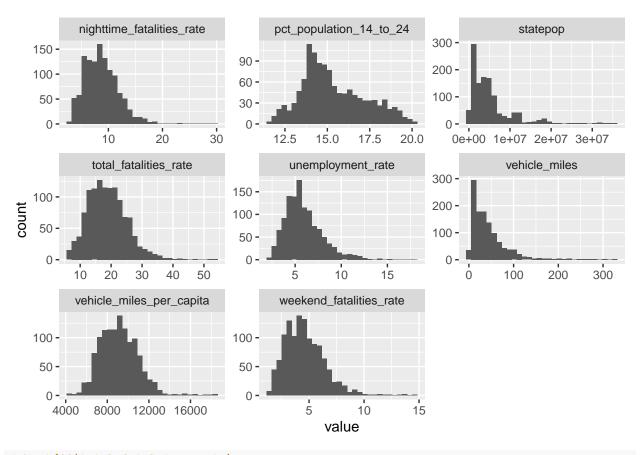
```
df avg <- df %>%
  group_by(year_of_observation) %>%
  summarise(avg_total_fatalities_rate = mean(total_fatalities_rate))
# average fatality by year
years <- unique(df$year_of_observation)</pre>
avg_df <- data.frame(</pre>
  year = years,
  avg_fatality = round(df_avg$avg_total_fatalities_rate, 2)
# plot fatality by year
df_avg %>%
  ggplot(aes(year_of_observation, avg_total_fatalities_rate,
    label = round(avg_total_fatalities_rate, 2)
  )) +
  geom_point() +
  geom_text(hjust = 0, vjust = -0.5) +
  theme bw() +
  labs(title = "Average Total Fatalities by Year")
```

## Average Total Fatalities by Year



```
df %>%
  select(
    total_fatalities_rate,
    nighttime_fatalities_rate,
    weekend_fatalities_rate,
    vehicle_miles,
    vehicle_miles_per_capita,
    statepop,
    unemployment_rate,
    pct_population_14_to_24
  ) %>%
  keep(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
  facet_wrap(~key, scales = "free") +
  geom_histogram()
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.

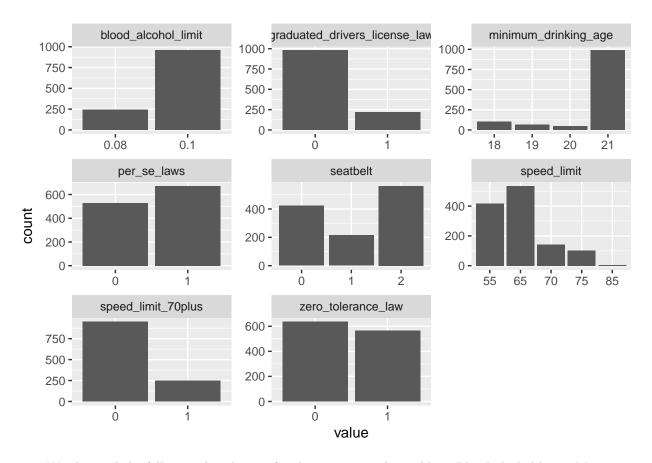


# hist(df\$total\_fatalities\_rate)
# hist(log(df\$total\_fatalities\_rate))

For the continuous variables, the distributions are right-skewed for most of these variables.

```
df %>%
    select(
        seatbelt,
        zero_tolerance_law,
        graduated_drivers_license_law,
        per_se_laws,
        minimum_drinking_age,
        speed_limit_70plus,
        speed_limit,
        blood_alcohol_limit
) %>%
    gather() %>%
    gather() %>%
    ggplot(aes(value)) +
    facet_wrap(~key, scales = "free") +
    geom_bar()
```

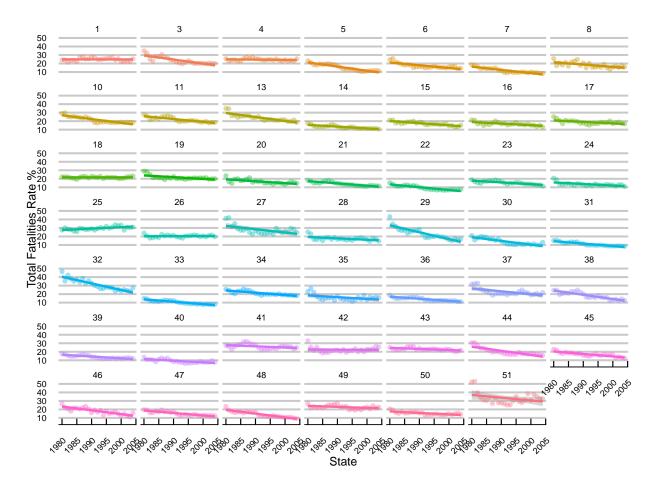
## Warning: attributes are not identical across measure variables; they will be ## dropped



We observed the following distribution for these categorical variables - Blood alcohol limit: Most states have the limit of 0.1. - Minimum drinking age: Most states have 21. - Graduated drivers license law, most states have 0 - Speed limit: Most states have less than 70 miles

```
# TODO: For Ken: why are there 51 plots, with 48 states?
df %>%
  ggplot(aes(year, total_fatalities_rate, color = state)) +
  geom_point(alpha = 0.4) +
  geom_smooth(method = "lm") +
  facet_wrap(~state) +
  theme_economist_white(gray_bg = FALSE) +
  theme(
   legend.position = "none",
   axis.text.x = element_text(angle = 45, hjust = 1, vjust = 1, size = 8),
   axis.text.y = element_text(size = 8),
   strip.text = element_text(size = 8)
  ) +
  scale_y_continuous() +
  xlab("State") +
  ylab("Total Fatalities Rate %")
```

## `geom\_smooth()` using formula = 'y ~ x'

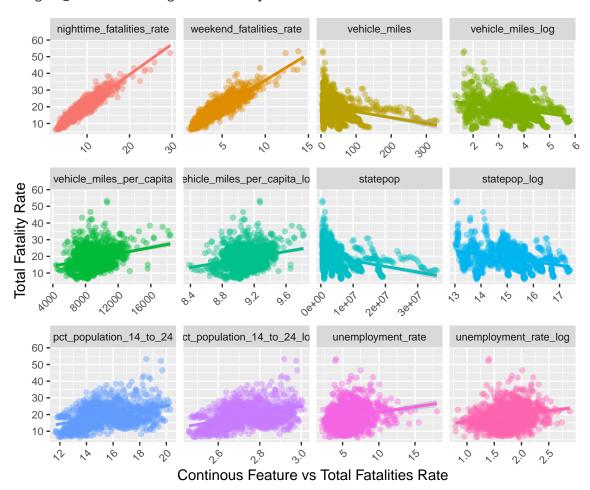


Most states have downward trends in total fatalities rate.

```
df %>%
  mutate(
    vehicle_miles_log = log(vehicle_miles),
    vehicle_miles_per_capita_log = log(vehicle_miles_per_capita),
    statepop_log = log(statepop),
    pct_population_14_to_24_log = log(pct_population_14_to_24),
    unemployment_rate_log = log(unemployment_rate)
  ) %>%
  select(
    total_fatalities_rate,
    nighttime_fatalities_rate,
    weekend_fatalities_rate,
    vehicle_miles,
    vehicle_miles_log,
    vehicle_miles_per_capita,
    vehicle_miles_per_capita_log,
    statepop,
    statepop_log,
    pct_population_14_to_24,
    pct_population_14_to_24_log,
    unemployment_rate,
    unemployment_rate_log
```

```
) %>%
melt(id.vars = c("total_fatalities_rate")) %>%
ggplot(aes(value, total_fatalities_rate, color = variable)) +
geom_point(alpha = 0.4) +
geom_smooth(method = "lm") +
facet_wrap(~variable, scales = "free_x") +
# theme_economist_white(gray_bg=F) +
theme(
  legend.position = "none",
  axis.text.x = element_text(angle = 45, hjust = 1, vjust = 1, size = 8),
  axis.text.y = element_text(size = 8),
  strip.text = element_text(size = 8)
) +
\# scale_y\_continuous(label=percent) +
xlab("Continous Feature vs Total Fatalities Rate") +
ylab("Total Fatality Rate")
```

## `geom\_smooth()` using formula = 'y ~ x'



We conducted log transformation on the following variables: vehicle\_miles, vehicle\_miles\_per\_capita, statepop, pct\_population\_14\_to\_24, unemployment\_rate. We visualized both the original and log transformed variables, and decided to use log transformation for our interpretation for vehicle\_miles, vechicle\_miles\_per\_capita, statepop and unemployment\_rate.

Total fatalities rate is positively correlated with unemployment\_rate and percentage of population aged 14 through 24.

Total fatalities rate is negatively correlated with vehicle miles and state population, but positively correlated with vehicle miles per capita.

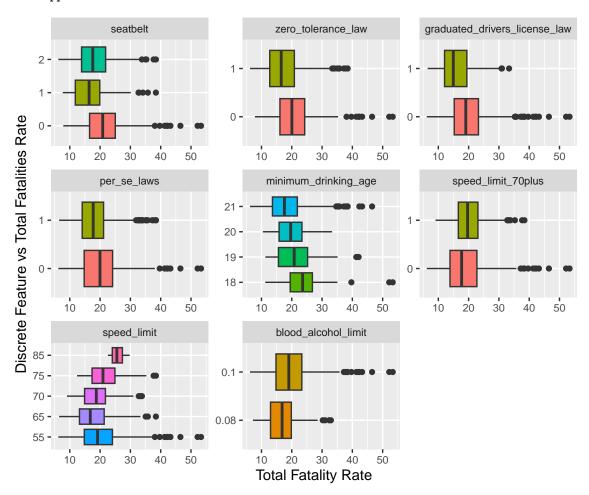
We interpret this as population and vehicle miles are both increasing with time, so is the other driving forces of fatalities rate (quality of the car, technology of the car, road conditions, etc.), so the relationship between total fatalities rate vs vehicle miles and state population is potentially spurious, and thus inconsistent with our background knowlege.

However, the relationship between total fatalities rate and vehicle miles per capita is positive, because as the density of the population increases, there is expected to be more severe traffic incidents that leads to higher fatalities rate. This is consistent with our background knowledge.

```
# TODO: talk about this?
df <- df %>%
  mutate(
   vehicle_miles_log = log(vehicle_miles),
   vehicle_miles_per_capita_log = log(vehicle_miles_per_capita),
   statepop_log = log(statepop),
   unemployment_rate_log = log(unemployment_rate)
  ) %>%
  select(
   -vehicle_miles,
   -vehicle_miles_per_capita,
   -statepop,
    -unemployment rate
  )
df %>%
  select(
   total fatalities rate,
   seatbelt,
   zero tolerance law,
    graduated_drivers_license_law,
   per_se_laws,
   minimum_drinking_age,
   speed_limit_70plus,
    speed_limit,
   blood_alcohol_limit
  ) %>%
  melt(id.vars = c("total_fatalities_rate")) %>%
  ggplot(aes(value, total_fatalities_rate)) +
  geom_boxplot(aes(fill = factor(value))) +
  coord flip() +
  facet_wrap(~variable, scales = "free") +
  theme(
    legend.position = "none",
   axis.text.x = element text(size = 8),
   axis.text.y = element text(size = 8),
   strip.text = element_text(size = 8)
 ) +
  xlab("Discrete Feature vs Total Fatalities Rate") +
  ylab("Total Fatality Rate")
```

## Warning: attributes are not identical across measure variables; they will be

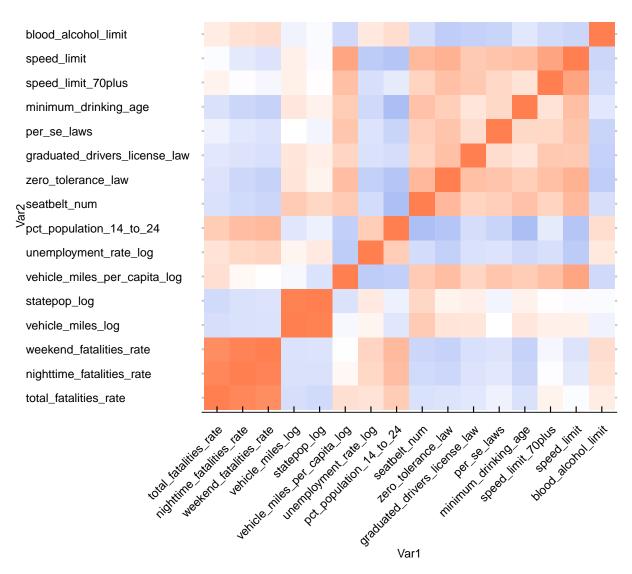
#### ## dropped



```
df %>%
  # TODO: does this even make sense to calculate corrolation on discrete variables? Don't we need to us
  mutate(seatbelt_num = as.numeric(seatbelt)) %>%
  select(
    total_fatalities_rate,
    nighttime_fatalities_rate,
    weekend_fatalities_rate,
    vehicle_miles_log,
    statepop_log,
    vehicle_miles_per_capita_log,
    unemployment_rate_log,
    pct_population_14_to_24,
    seatbelt_num,
    zero_tolerance_law,
    graduated_drivers_license_law,
    per_se_laws,
    minimum_drinking_age,
    speed_limit_70plus,
    speed_limit,
    blood_alcohol_limit
  ) %>%
```

```
cor() %>%
melt() %>%
ggplot(aes(Var1, Var2, fill = value)) +
geom_tile() +
theme_economist_white(gray_bg = FALSE) +
theme(
    legend.title = element_blank(),
    legend.text = element_text(size = 10),
    axis.text.x = element_text(angle = 45, hjust = 1, vjust = 1)
) +
scale_fill_gradient2(
    low = "cornflowerblue", high = "coral", mid = "white",
    midpoint = 0, limit = c(-1, 1)
)
```





The state population and vehicle miles are almost perfectly correlated. So to avoid the colinearity problem, we will only use vehicle\_miles\_per\_capita in our model, which is impacted both of them.

#### 2.0.1 Summary Of EDA

- 1. clean up the dataframe to keep only variables we care; #TODO: as a team, we can write some observations, and rationalize which are the variables we end up using in the next session.
- 2. transform some variables via log #TODO: later in the Expanded Model part: > A log transformation is applied to total\_fatalities\_rate and unemployment\_rate because the skewed distribution needs to be normalized.

As with every EDA this semester, the goal of this EDA is not to document your own process of discovery – save that for an exploration notebook – but instead it is to bring a reader that is new to the data to a

full understanding of the important features of your data as quickly as possible. In order to do this, your EDA should include a detailed, orderly narrative description of what you want your reader to know. Do not include any output – tables, plots, or statistics – that you do not intend to write about.

### 3 (15 points) Preliminary Model

## year\_of\_observation1992

## year\_of\_observation1993 -8.3669

Estimate a linear regression model of *totfatrte* on a set of dummy variables for the years 1981 through 2004 and interpret what you observe. In this section, you should address the following tasks:

- Why is fitting a linear model a sensible starting place? > Fitting a linear model helps identify significant explanatory variables and evaluate how strong the linear correlation is.
- What does this model explain, and what do you find in this model? > This model explains whether a given year has a linear relationship with total fatalities rate. Based on the model, there is strong evidence that all the years except 1981 are related to total fatalities rate at the significance level of 0.

This makes sense as we are using 1980 as the baseline year, so 1981 is the first year after 1980 and as a result, all the time-variant effects have not kicked in.

- Did driving become safer over this period? Please provide a detailed explanation. > In 1980, the average total fatalities rate was 24% and by 2004, the average total fatalities decreased down to 16%.
- What, if any, are the limitation of this model. In answering this, please consider at least:
  - Are the parameter estimates reliable, unbiased estimates of the truth? Or, are they biased due to the way that the data is structured?
  - Are the uncertainty estimate reliable, unbiased estimates of sampling based variability? Or, are they biased due to the way that the data is structured? > TODO: let's do this. > We can note on  $R^2$ .

```
mod.lm1 <- lm(total_fatalities_rate ~ year_of_observation, data = df)</pre>
summary(mod.lm1)
##
## Call:
## lm(formula = total_fatalities_rate ~ year_of_observation, data = df)
##
## Residuals:
##
        Min
                   1Q
                        Median
                                      3Q
                                              Max
##
   -12.9302
             -4.3468
                      -0.7305
                                 3.7488
                                          29.6498
##
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
                             25.4946
## (Intercept)
                                          0.8671
                                                  29.401 < 2e-16 ***
## year_of_observation1981
                             -1.8244
                                          1.2263
                                                  -1.488 0.137094
## year_of_observation1982
                             -4.5521
                                          1.2263
                                                  -3.712 0.000215 ***
## year of observation1983
                             -5.3417
                                          1.2263
                                                  -4.356 1.44e-05 ***
## year_of_observation1984
                             -5.2271
                                          1.2263
                                                  -4.263 2.18e-05 ***
## year of observation1985
                             -5.6431
                                          1.2263
                                                  -4.602 4.64e-06 ***
## year_of_observation1986
                             -4.6942
                                                  -3.828 0.000136 ***
                                          1.2263
                             -4.7198
## year_of_observation1987
                                          1.2263
                                                  -3.849 0.000125 ***
## year of observation1988
                             -4.6029
                                          1.2263
                                                  -3.754 0.000183 ***
## year of observation1989
                             -5.7223
                                          1.2263
                                                  -4.666 3.42e-06 ***
## year_of_observation1990
                             -5.9894
                                                  -4.884 1.18e-06 ***
                                          1.2263
                                                  -6.034 2.14e-09 ***
## year_of_observation1991
                             -7.3998
                                          1.2263
```

1.2263

-6.798 1.68e-11 \*\*\*

1.2263 -6.823 1.43e-11 \*\*\*

-8.3367

```
## year of observation1994
                           -8.3394
                                       1.2263 -6.800 1.66e-11 ***
                           -7.8260
                                       1.2263
## year_of_observation1995
                                              -6.382 2.51e-10 ***
## year of observation1996
                           -8.1252
                                       1.2263
                                               -6.626 5.25e-11 ***
## year_of_observation1997
                           -7.8840
                                       1.2263
                                               -6.429 1.86e-10 ***
## year_of_observation1998
                           -8.2292
                                       1.2263
                                               -6.711 3.01e-11 ***
## year of observation1999
                                       1.2263
                          -8.2442
                                              -6.723 2.77e-11 ***
## year of observation2000 -8.6690
                                       1.2263
                                              -7.069 2.67e-12 ***
## year_of_observation2001
                           -8.7019
                                       1.2263
                                               -7.096 2.21e-12 ***
## year_of_observation2002
                          -8.4650
                                       1.2263
                                               -6.903 8.32e-12 ***
## year_of_observation2003
                          -8.7310
                                       1.2263
                                              -7.120 1.88e-12 ***
## year_of_observation2004
                          -8.7656
                                       1.2263
                                              -7.148 1.54e-12 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.008 on 1175 degrees of freedom
## Multiple R-squared: 0.1276, Adjusted R-squared: 0.1098
## F-statistic: 7.164 on 24 and 1175 DF, p-value: < 2.2e-16
```

### 4 (15 points) Expanded Model

Expand the Preliminary Model by adding variables related to the following concepts:

- Blood alcohol levels
- Per se laws
- Primary seat belt laws (Note that if a law was enacted sometime within a year the fraction of the year is recorded in place of the zero-one indicator.)
- Secondary seat belt laws
- Speed limits faster than 70
- Graduated drivers licenses
- Percent of the population between 14 and 24 years old
- Unemployment rate
- Vehicle miles driven per capita.

If it is appropriate, include transformations of these variables. Please carefully explain carefully your rationale, which should be based on your EDA, behind any transformation you made. If no transformation is made, explain why transformation is not needed. > A log transformation is applied to total\_fatalities\_rate and unemployment\_rate because the skewed distribution needs to be normalized.

```
##
       factor(blood_alcohol_limit) + per_se_laws + seatbelt + speed_limit_70plus +
##
       graduated_drivers_license_law + pct_population_14_to_24 +
##
       unemployment_rate_log + vehicle_miles_per_capita_log, data = df)
##
## Residuals:
                      Median
       Min
                  1Q
                                   30
##
                                           Max
   -0.58465 -0.12657 -0.00148 0.14135
##
## Coefficients:
##
                                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                 -1.135e+01 4.023e-01 -28.208 < 2e-16 ***
                                                        -2.221
## year_of_observation1981
                                 -9.146e-02
                                             4.117e-02
                                                                 0.0265 *
                                 -2.949e-01
## year_of_observation1982
                                             4.203e-02
                                                        -7.016 3.87e-12 ***
## year_of_observation1983
                                 -3.516e-01
                                             4.263e-02 -8.247 4.32e-16 ***
## year_of_observation1984
                                 -3.056e-01 4.283e-02 -7.136 1.69e-12 ***
## year_of_observation1985
                                 -3.439e-01
                                             4.370e-02
                                                        -7.870 8.04e-15 ***
## year_of_observation1986
                                 -3.208e-01 4.563e-02 -7.029 3.54e-12 ***
## year_of_observation1987
                                 -3.570e-01 4.762e-02 -7.498 1.28e-13 ***
## year_of_observation1988
                                 -3.673e-01 5.025e-02 -7.309 4.99e-13 ***
## year_of_observation1989
                                 -4.525e-01 5.222e-02
                                                        -8.664
                                                                < 2e-16 ***
## year_of_observation1990
                                 -5.119e-01 5.344e-02 -9.579
                                                                < 2e-16 ***
                                 -6.277e-01 5.458e-02 -11.500
## year_of_observation1991
                                                                < 2e-16 ***
## year of observation1992
                                 -7.338e-01 5.562e-02 -13.193
                                                                < 2e-16 ***
## year_of_observation1993
                                 -7.251e-01 5.637e-02 -12.863
                                                                < 2e-16 ***
## year_of_observation1994
                                 -7.111e-01 5.755e-02 -12.356 < 2e-16 ***
## year_of_observation1995
                                 -6.887e-01 5.894e-02 -11.684 < 2e-16 ***
                                 -8.135e-01 6.108e-02 -13.319
                                                                < 2e-16 ***
## year_of_observation1996
## year_of_observation1997
                                 -8.217e-01 6.218e-02 -13.214 < 2e-16 ***
## year_of_observation1998
                                 -8.686e-01 6.331e-02 -13.720 < 2e-16 ***
## year_of_observation1999
                                 -8.664e-01 6.431e-02 -13.473 < 2e-16 ***
## year_of_observation2000
                                 -8.768e-01
                                             6.549e-02 -13.388
                                                                < 2e-16 ***
## year_of_observation2001
                                 -9.303e-01 6.591e-02 -14.114
                                                                < 2e-16 ***
## year_of_observation2002
                                 -9.744e-01 6.610e-02 -14.740
                                                                < 2e-16 ***
## year_of_observation2003
                                 -9.969e-01 6.642e-02 -15.009
                                                                < 2e-16 ***
## year_of_observation2004
                                 -9.795e-01
                                             6.792e-02 -14.421
                                                                < 2e-16 ***
## factor(blood_alcohol_limit)0.1 4.539e-02 1.835e-02
                                                         2.473
                                                                 0.0135 *
## per se laws
                                 -2.197e-02 1.437e-02
                                                        -1.529
                                                                 0.1264
## seatbelt2
                                                                 0.3656
                                  1.936e-02 2.139e-02
                                                         0.905
## seatbelt1
                                 -6.715e-04
                                             2.448e-02
                                                        -0.027
                                                                 0.9781
## speed_limit_70plus
                                  2.211e-01 2.160e-02
                                                        10.238
                                                                < 2e-16 ***
## graduated_drivers_license_law -3.434e-02 2.513e-02
                                                        -1.367
                                                                 0.1720
## pct_population_14_to_24
                                                                 0.0036 **
                                  1.780e-02 6.103e-03
                                                         2.917
## unemployment_rate_log
                                  2.673e-01 2.413e-02
                                                        11.078
                                                                < 2e-16 ***
## vehicle_miles_per_capita_log
                                  1.541e+00 4.436e-02 34.747
                                                                < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2013 on 1166 degrees of freedom
## Multiple R-squared: 0.668, Adjusted R-squared: 0.6586
## F-statistic: 71.1 on 33 and 1166 DF, p-value: < 2.2e-16
```

- How are the blood alcohol variables defined? Interpret the coefficients that you estimate for this concept. > #TODO: add the bac definition.
- Do per se laws have a negative effect on the fatality rate? > per se laws have a negative effect on the

fatality rate, but the variable yielded a p-value > 0.1 thus suggesting that there is weak evidence it is correlated with fatality rate.

• Does having a primary seat belt law? > primary seatbelt laws also has a negative effect on the fatality rate, but the variable yielded a p-value > 0.1 thus suggesting that there is weak evidence it is correlated with fatality rate.

### 5 (15 points) State-Level Fixed Effects

Re-estimate the **Expanded Model** using fixed effects at the state level.

- What do you estimate for coefficients on the blood alcohol variables? How do the coefficients on the blood alcohol variables change, if at all?
- What do you estimate for coefficients on per se laws? How do the coefficients on per se laws change, if at all?
- What do you estimate for coefficients on primary seat-belt laws? How do the coefficients on primary seatbelt laws change, if at all?

Which set of estimates do you think is more reliable? Why do you think this?

• What assumptions are needed in each of these models?

## year\_of\_observation1984
## year\_of\_observation1985

## year\_of\_observation1986

## year\_of\_observation1987

## year\_of\_observation1988

## year\_of\_observation1989

• Are these assumptions reasonable in the current context?

```
# estimate the fixed effects regression with plm()
mod.fe <- plm(</pre>
 log(total_fatalities_rate) ~ year_of_observation
   + factor(blood_alcohol_limit)
   + per_se_laws
   + seatbelt
   + speed_limit_70plus
   + graduated_drivers_license_law
   + pct_population_14_to_24
   + unemployment rate log
   + vehicle_miles_per_capita_log,
 data = df,
 index = c("state"),
 model = "within"
)
# print summary using robust standard errors
coeftest(mod.fe, vcov. = vcovHC, type = "HC1")
##
## t test of coefficients:
##
##
                              Estimate Std. Error t value Pr(>|t|)
## year of observation1981
                            ## year_of_observation1982
                            ## year_of_observation1983
```

-0.2124940 0.0213503 -9.9528 < 2.2e-16 \*\*\*

-0.2379207 0.0262729 -9.0557 < 2.2e-16 \*\*\*

```
## year of observation1990
                            ## year_of_observation1991
## year of observation1992
                            ## year_of_observation1993
                            ## year_of_observation1994
                            ## year of observation1995
                            ## year of observation1996
                            -0.5600408  0.0752837  -7.4391  2.014e-13 ***
                                     0.0770172 -7.5679 7.898e-14 ***
## year_of_observation1997
                            -0.5828591
## year_of_observation1998
                            -0.6356498  0.0772402  -8.2295  5.183e-16 ***
## year_of_observation1999
                            0.0792438 -8.6022 < 2.2e-16 ***
## year_of_observation2000
                            -0.6816718
## year_of_observation2001
                                     0.0831842 -7.8109 1.301e-14 ***
                            -0.6497400
## year_of_observation2002
                            -0.6105826
                                     0.0810339 -7.5349 1.005e-13 ***
## year_of_observation2003
                            -0.6127145
                                     0.0835637 -7.3323 4.329e-13 ***
## year_of_observation2004
                                     0.0875255 -7.4315 2.127e-13 ***
                            -0.6504450
## factor(blood_alcohol_limit)0.1
                            0.0048883
                                     0.0176342
                                              0.2772
                                                    0.781673
## per_se_laws
                            -0.0554823
                                     0.0163076 -3.4022
                                                     0.000692 ***
## seatbelt2
                            0.0046718
                                     0.0162378
                                              0.2877
                                                     0.773621
## seatbelt1
                                     0.0248524 -1.6658
                            -0.0413988
                                                     0.096035
## speed limit 70plus
                            0.0727041
                                     0.0222040
                                              3.2744
                                                     0.001091 **
## graduated_drivers_license_law -0.0311878
                                    0.0195683 -1.5938
                                                    0.111265
## pct_population_14_to_24
                                     0.0105815 1.8231 0.068556 .
                            0.0192910
                                     0.0235478 -8.2393 4.799e-16 ***
## unemployment_rate_log
                            -0.1940177
## vehicle miles per capita log
                            0.6678486   0.1374350   4.8594   1.345e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

### 6 (10 points) Consider a Random Effects Model

Instead of estimating a fixed effects model, should you have estimated a random effects model?

- Please state the assumptions of a random effects model, and evaluate whether these assumptions are met in the data.
  - Random Effect Model Assumptions: the idiosyncratic error uit should be uncorrelated with each explanatory variable across all time period the error uit are homoskedastic and serially uncorrelated across all time periood the unobservbed effect term at is independent of all explanatory variables in all the time periods in the model
- If the assumptions are, in fact, met in the data, then estimate a random effects model and interpret the coefficients of this model. Comment on how, if at all, the estimates from this model have changed compared to the fixed effects model.

```
# re.model <- plm(</pre>
    log(total_fatalities_rate) ~ year_of_observation
#
      + factor(blood_alcohol_limit)
#
      + per se laws
#
      + seatbelt
#
      + speed limit 70plus
#
      + graduated drivers license law
      + pct_population_14_to_24
#
      + log(unemployment_rate)
#
      + vehicle_miles_per_capita,
    data = df,
    index = c("state"),
```

```
# model = "random"
# )
# summary(re.model)
```

• If the assumptions are **not** met, then do not estimate the data. But, also comment on what the consequences would be if you were to *inappropriately* estimate a random effects model. Would your coefficient estimates be biased or not? Would your standard error estimates be biased or not? Or, would there be some other problem that might arise?

# 7 (10 points) Model Forecasts

The COVID-19 pandemic dramatically changed patterns of driving. Find data (and include this data in your analysis, here) that includes some measure of vehicle miles driven in the US. Your data should at least cover the period from January 2018 to as current as possible. With this data, produce the following statements:

- Comparing monthly miles driven in 2018 to the same months during the pandemic:
  - What month demonstrated the largest decrease in driving? How much, in percentage terms, lower was this driving?
  - What month demonstrated the largest increase in driving? How much, in percentage terms, higher was this driving?

We have collected the United States Motor Vehicle Miles Traveled Total (Millions) data from the US Department of Transformation. This data is available at here [https://www.fhwa.dot.gov/policyinformation/statistics/2021/vm202.cfm].

We have downloaded the data that is compiled by Bloomberg (under ticker: VMTDVCLE Index) and saved it in the file data/VMTDVCLE.csv.

Now, use these changes in driving to make forecasts from your models.

- Suppose that the number of miles driven per capita, increased by as much as the COVID boom. Using the FE estimates, what would the consequences be on the number of traffic fatalities? Please interpret the estimate.
- Suppose that the number of miles driven per capita, decreased by as much as the COVID bust. Using the FE estimates, what would the consequences be on the number of traffic fatalities? Please interpret the estimate.

# 8 (5 points) Evaluate Error

If there were serial correlation or heteroskedasticity in the idiosyncratic errors of the model, what would be the consequences on the estimators and their standard errors? Is there any serial correlation or heteroskedasticity?