CS101-Quiz9-Review

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Key Points

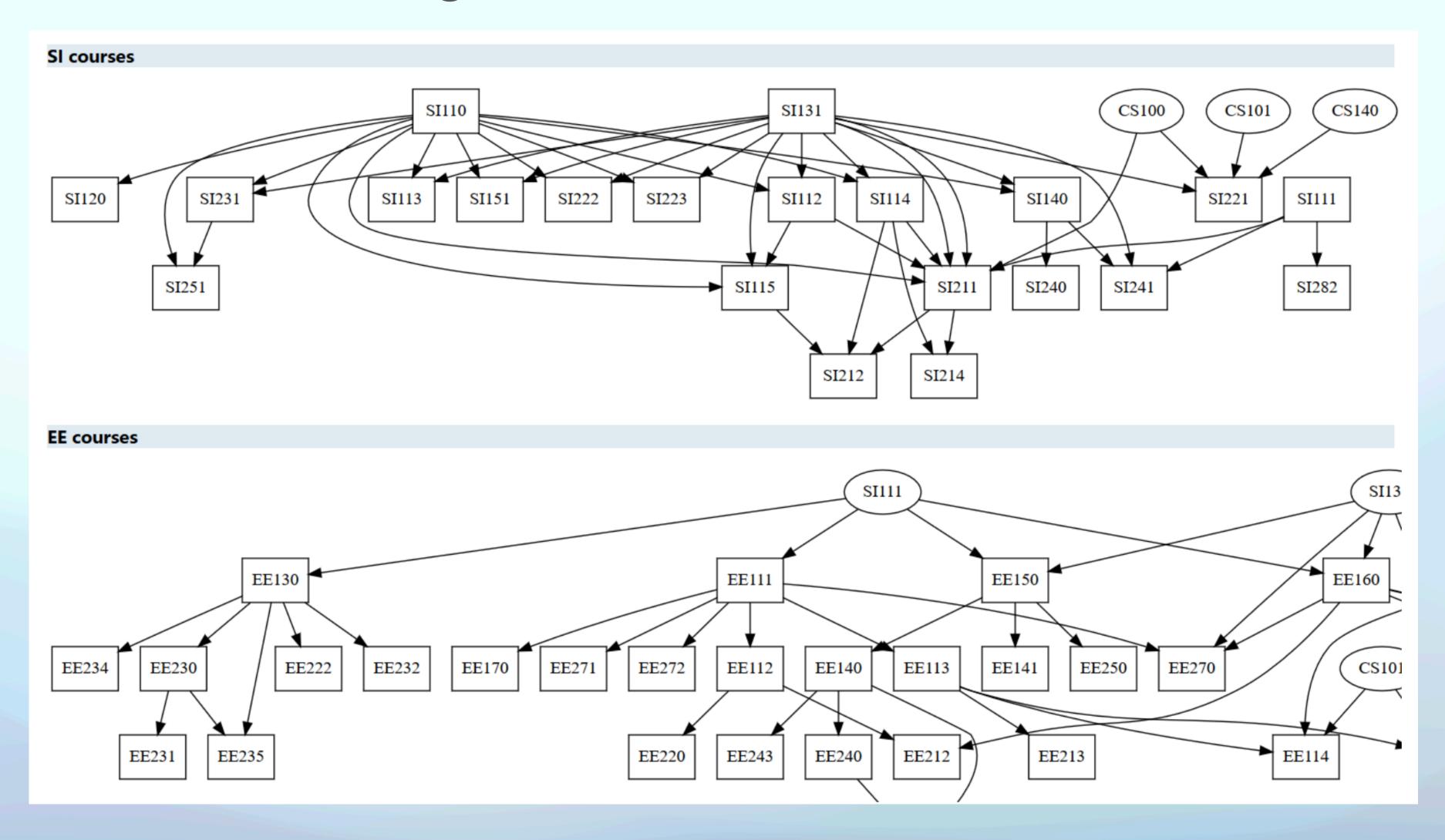
- 1. Topological Sort
- 2. Greedy Algorithms

- 1. An algorithm for ordering the vertices of a directed acyclic graph (DAG) in a linear ordering.
- 2. Time complexity: O(V + E)
- 3. Space complexity: O(V)

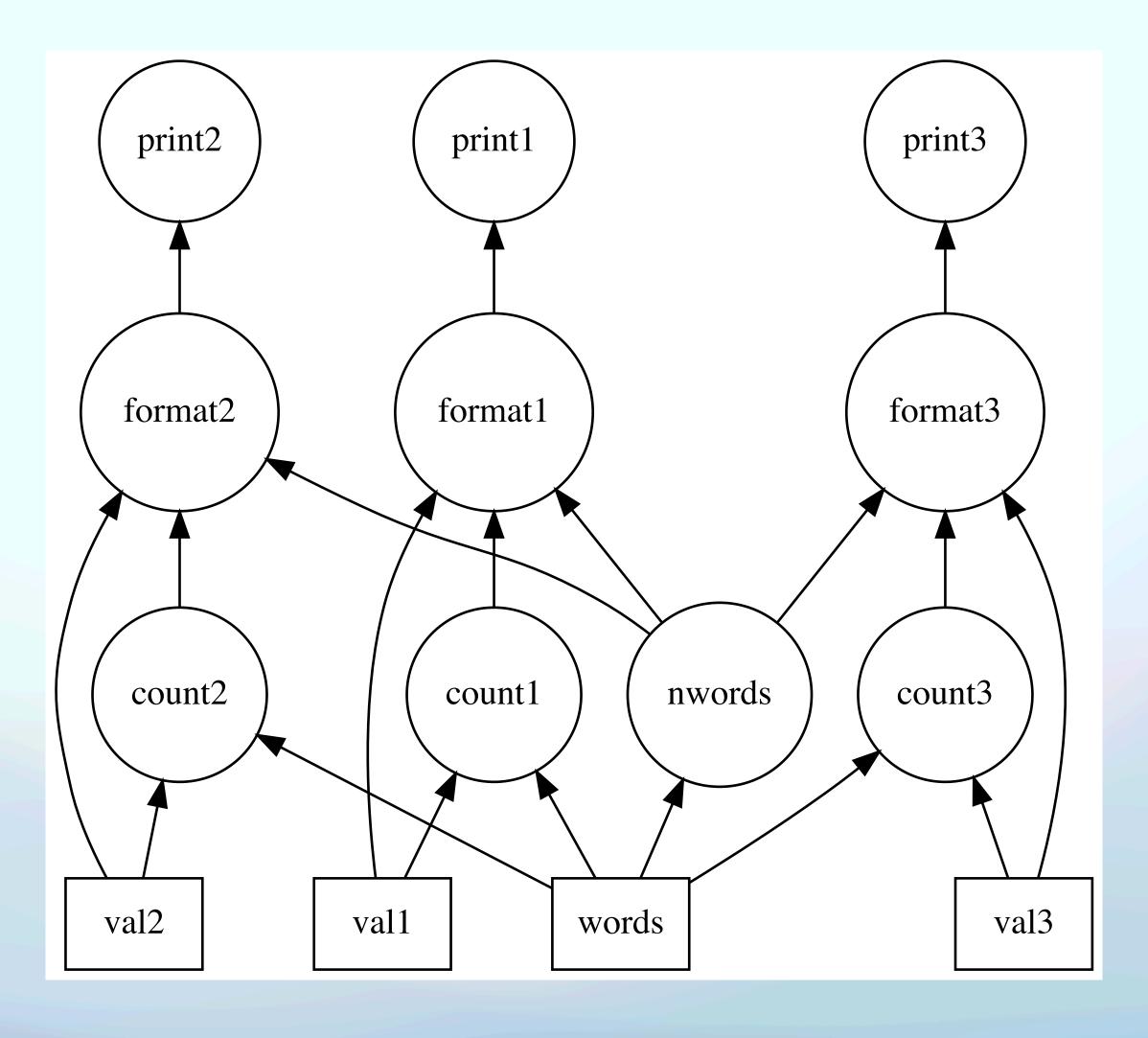
Basic Theorems and Lemmas

- 1. A graph is a DAG if and only if it has a topological sorting
- 2. A DAG always has at least one vertex with in-degree zero.
- 3. Any sub-graph of a DAG is a DAG.

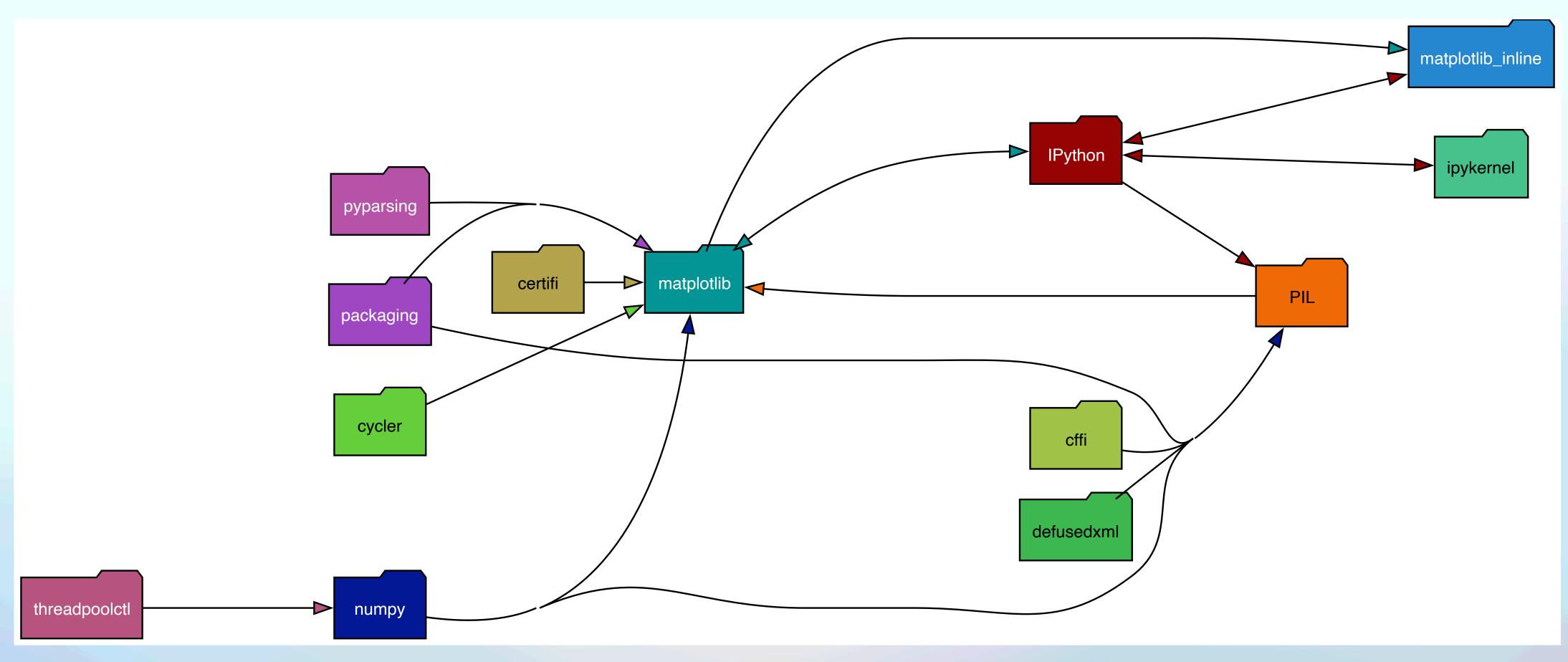
Curriculum scheduling



Task graph — Python Dask



Task graph — Dependency



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Key Points

1. Topological Sort

2. Greedy Algorithms

Array Section

```
1 def ArraySection(A):
 s = A[1]
 g = 1
for i = [2, ..., n]:
s = s + A[i]
if s > M:
     s = A[i]
     g = g + 1
return g
```

4 2 4 5 1 2

- 1. When all optimal solutions have the same size and differ only in their cost.
- 2. Justify with how you will replace some parts of the optimal solution.

- 1. Define subproblem and compare
- 2. Exchange
- 3. Iterate

- 1. Sub-problem g(i) means minimizing the number of sections for $\langle a_1, \dots, a_i \rangle$, and then maximizing the start indices of all the sections.
- 2. Exchange
- 3. Iterate

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- 1. Sub-problem g(i) means minimizing the number of sections for $\langle a_1, \dots, a_i \rangle$, and then maximizing the start indices of all the sections.
- 2. Assume the start index of sections is $\langle s_1, \dots, s_k \rangle$. Assume we can make s_t smaller.
 - Prove the new solution is not better than our solution (see (e.) in the answer book).
- 3. Iterate

Array Section — exchange argument

- 1. Sub-problem g(i) means minimizing the number of sections for $\langle a_1, \dots, a_i \rangle$, and then maximizing the start indices of all the sections.
- 2. Assume the start index of sections is $\langle s_1, \dots, s_k \rangle$. Assume we can make s_t smaller.
 - Prove the new solution is not better than our solution (see (e.) in the answer book).

3. 显然成立

Array Section — exchange argument — Take-home message

- 1. The **exchange method** assumes that the "size" of the solution is the same for both greedy and optimal solutions.
- 2. Exchange is then used to show that it is optimal.
- 3. Mathematical induction is often used to show how this consistency holds as the problem size increases.