

CS101-Quiz9-Review

Key Points

- 1. Dijkstra's algorithm
- 2. Bellman-Ford algorithm
- 3. A* Search Algorithm

- 1. Solves single-source shortest path problem.
- 2. Choose the vertex "nearest" to the source each time.
- 3. Does not work for graphs with negative weight edges.
- 4. Time complexity of Dijkstra's algorithm is $O\left((V+E)\log V\right)$

Algorithm analysis

- 1. We need to initialize the distance array and the binary heap with all **vertices**.
- 2. Each **edge** is processed once when relaxing the distances.
- 3. **Binary heap** is used to find the vertex with the minimum distance.

Algorithm analysis — Time

- 1. Inserting all the vertices into the binary heap: $O\left(V\log V\right)$
- 2. Every edge visit could update distances in binary heap: $O\left(E\log V\right)$
- 3. Total time complexity: $O\left((V+E)\log V\right)$

Algorithm analysis — Better **time** complexity with fib heap

- 1. Inserting all the vertices into the fib heap: $O\left(V\log V\right)$
- 2. Every edge visit could update distances in fib heap: O(E)
- 3. Total time complexity: $O(V \log V + E)$

但fib确实难写,而且因为常数巨大,所以我们也不会让你写。

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Bellman-Ford algorithm

- 1. Solves single-source shortest path problem.
- 2. Update cost of all vertices in each iteration.
- 3. Work for graphs with negative weight edges.
- 4. Time complexity is O(VE)

Bellman-Ford algorithm

Algorithm analysis — Time

- 1. In each iteration, the algorithm goes through all the edges in the graph: $O\left(E\right)$
- 2. Relaxation process is run for O(V) times.
- 3. Total time complexity: O(VE)

Comparison

	Dijkstra's	Bellman-Ford
Time complexity	$O\left((V+E)\log V\right)$ $O\left(V\log V+E\right)$	O (VE)
Negative weights	×	✓
Negative cycle	×	Detect

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A* Search Algorithm

- 1. Heuristic-based Pathfinding algorithm
- 2. Admissible and consistent
- 3. We don't care the time complexity

A* Search Algorithm

Admissible and consistent

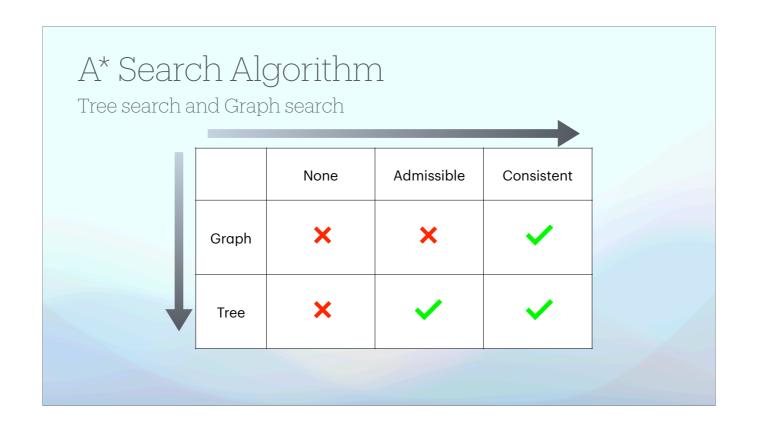
- 1. Admissible: never overestimates.
- 2. Consistent: triangle inequality.
- 3. Consistency implies admissibility (See post <u>@173</u>)

两边之和大于第三边

A* Search Algorithm

Tree search and Graph search

- 1. Tree search is the algorithm that **believes** it is running on a tree, so it will not check whether a vertex is visited
- 2. By using tree search:
 - 2.1. You could fall into an infinite loop
 - 2.2. "Scores" or "Costs" of vertices can be updated multiple times
- 3. By using graph search:
 - 3.1. Your algorithm will terminate
 - 3.2. Avoid visiting the same vertices a second time



Tree的搜索比Graph"充分";

Consistent的结论比Admissible强;

总之要想optimal,要么搜的多,要么猜的准。

红色的叉只是不保证optimal,不代表一定很差。