

120. Triangle

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Given a triangle, find the minimum path sum from top to bottom. Each step you may move to adjacent numbers on the row below.

For example, given the following triangle

```
[
  [2],
  [3,4],
  [6,5,7],
  [4,1,8,3]
]
```

The minimum path sum from top to bottom is **11** (i.e., $2 + 3 + 5 + 1 = 11$).

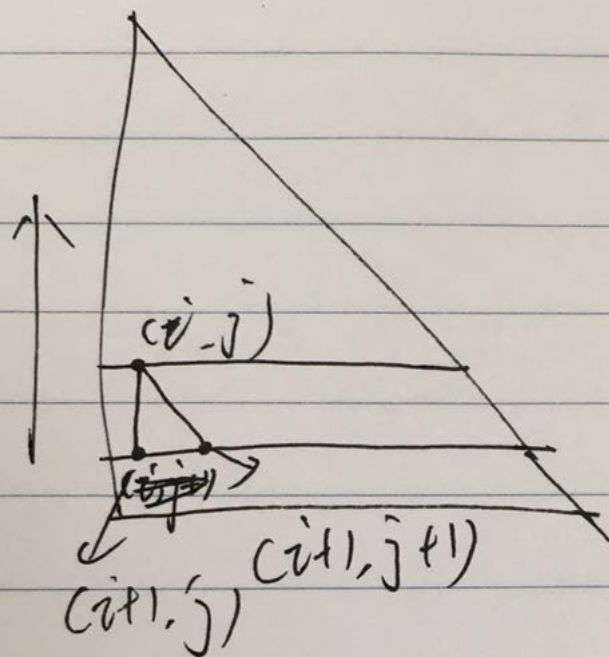
```
/*
 * 这道题目是典型的动态规划题目
 * 递推公式是: res[i][j]=Math.min(res[i-1][j-1],res[i-1][j])+list(i).get(j)
 * 即从上一行能够到达该点的两个点钟选择小的那个点, 然后到达该点加上当前点的值即可
 * 这道题目由于是个三角形, 无需建立二维数组。
 */
public class L120 {
    public int minimumTotal(List<List<Integer>> triangle) {
        if(triangle.size()==1)
            return triangle.get(0).get(0);

        int[] dp = new int[triangle.size()];

        //题目从下到上, 首先dp[i]设置为最后一行的值
        for (int i = 0; i < triangle.get(triangle.size() - 1).size(); i++) {
            dp[i] = triangle.get(triangle.size() - 1).get(i);
        }

        // 然后从倒数第二行开始, 递推上去
        for (int i = triangle.size() - 2; i >= 0; i--) {
            for (int j = 0; j < triangle.get(i).size(); j++) {
                dp[j] = Math.min(dp[j], dp[j + 1]) + triangle.get(i).get(j);
            }
        }

        return dp[0];
    }
}
```



$$dp[i][j] = \min(dp[i+1][j], dp[i+1][j+1]) + \text{triangle}(i, j)$$

这样得到的是 (i, j) 的最小值。从底往上