## UNIVERSITY OF EDINBURGH COLLEGE OF SCIENCE AND ENGINEERING SCHOOL OF INFORMATICS

## INFR08012 INFORMATICS 1 - COMPUTATION AND LOGIC

Thursday  $15\frac{\text{th}}{}$  December 2016

14:30 to 16:30

## INSTRUCTIONS TO CANDIDATES

- 1. Note that ALL QUESTIONS ARE COMPULSORY.
- 2. CALCULATORS MAY NOT BE USED IN THIS EXAMINATION.
- 3. You should
  - WRITE YOUR EXAMINATION NUMBER

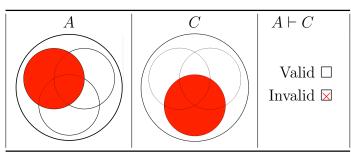
## HERE:

- Write your answers in the spaces provided in this question paper.
- Complete your details on the script book (which is provided for rough-working) and hand it in together with this document.

Convener: I. Simpson External Examiner: I. Gent

THIS EXAMINATION WILL BE MARKED ANONYMOUSLY

- 1. (a) The entailment  $A \vdash C$ , is invalid.
  - $\bullet$   $A \vdash C$



How is this invalidity shown by comparing the two Venn diagrams above?

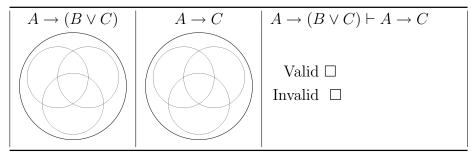
[4 marks]

(b) For each of the following entailments, complete the two Venn diagrams to represent the assumption and conclusion, and place a mark in one of the

check boxes provided to indicate whether the entailment is valid. (You should use the same encoding as in the example above, where each circle represents one of the propositions A, B, C.)

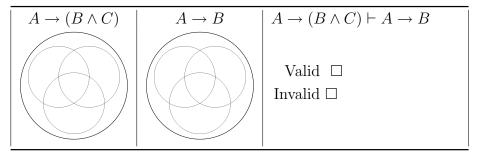
i.  $A \to (B \lor C) \vdash A \to C$ 

[8 marks]



ii.  $A \to (B \land C) \vdash A \to B$ 

[8 marks]



propositional letters $A, B, C, D, E, F, G, H$ . F say how many of the 256 valuations satisfy the reasoning. For example, the expression $D$ is that is 128 of the 256, since for each valua- matching valuation that make $D$ false.	expression, and briefly explain your satisfied by half of the valuations,	
(a) $A \vee B$	Answer	[1 mark]
(b) $(A \wedge B) \vee C$	Answer	[2 marks]
(c) $A \to (B \to C)$	Answer	[2 marks]
(d) $(A \to B) \land (B \to A) \land (C \to D) \land (D \to B)$	$F) \wedge (E \to F) \wedge (F \to G) \wedge (G \to H)$	[5 marks]
(e) $(A \to B) \land (B \to A) \land (C \to D) \land (D \to C)$ (f) $(H \to A) \land (A \to B) \land (B \lor C \to D) \land ($	Answer	[5 marks]
		[5 marks]
	Answer	

2. This question concerns the 256 possible truth valuations of the following eight

3. You are given the following inference rules ( $\Gamma$ ,  $\Delta$  vary over finite sets of expressions; A, B vary over expressions):

(Where A and B are propositional expressions,  $\Gamma$ ,  $\Delta$  are sets of expressions, and  $\Gamma$ , A refers to  $\Gamma \cup \{A\}$ .) This question concerns the use of these rules to prove the following entailment. This is your **goal**.

$$P \to (Q \to R), \ Q \lor \neg P \vdash P \to R$$
 (1)

(a) Which of these rules have a conclusion matching the goal (1)? For each such rule complete a line in the table below showing the name of the rule and the bindings for  $\Gamma, \Delta, A, B$ 

 $[10 \ marks]$ 

Rule	Γ	$\Delta$	A	B	

(b)	Use the rules given to construct a formal proof with the goal as conclusion, making any remaining assumptions as simple as possible.  Label each step in your proof with the name of the rule being applied.	[10 marks]
	$P \to (Q \to R), \ Q \lor \neg P \vdash P \to R$	

(a) What does it mean for an entailment to be valid?			[2 marks		
Answer					
(b) How can resolution be used to determine whether an entailment is valid?					[2 marks]
Answer	,				
		etermine whether	the entailment $(A \rightarrow \text{ole if it is not.})$	$B) \to A \vdash A$	_ [4 marks
	A	B 	C		
Answer	•		Counterexample	?	[2 marks
(d) Use resolution to determine whether $P \to (Q \lor R), (Q \land R) \to S \vdash P \to S$ is valid and produce a counter-example if it is not.				[4 marks	
	P	Q	R S		
Answer			Counterexample	?	[2 marks
. ,	plain what it me	eans to claim tha	the resolution proced	ure is:	[2 marks
Ar	nswer				
ii.	. complete.				[2 marks
Ar	nswer				

5. Each diagram shows an FSM. In each case give a regular expression for the language accepted by the FSM, make a mark in the check box against each string that it accepts (and no mark against those strings it does not accept), make a mark in the DFA check box if it is deterministic, and draw an equivalent DFA if it is not. aab  $\square$ [4 marks] aba 🗆 bab  $\square$ aaa 🗌 a,b a,b (a) bbb  $\square$  $DFA \square$ aab [4 marks] aba 🗆 bab  $\square$ aaa 🗌 a,b a,b (b) bbb  $\square$  $DFA \square$ aab  $\square$ [4 marks] aba 🗌 bab  $\square$ aaa 🗌 (c) b a,b bbb  $\square$  $DFA \square$ aab [4 marks] aba  $\square$ bab  $\square$ aaa 🗆 b (d) bbb  $\square$  $DFA \square$ а aab  $\square$ [4 marks] aba  $\square$ bab  $\square$ aaa 🗆 bbb  $\square$ 

 $DFA \square$