





# Smallest Subarray with a given sum (easy)

#### We'll cover the following

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  - Space Complexity

## Problem Statement #

Given an array of positive numbers and a positive number 'S,' find the length of the **smallest contiguous subarray whose sum is greater than or equal to 'S'**. Return 0 if no such subarray exists.

### Example 1:

Input: [2, 1, 5, 2, 3, 2], S=7

Output: 2

Explanation: The smallest subarray with a sum great than or equa

l to '7' is [5, 2].

### Example 2:

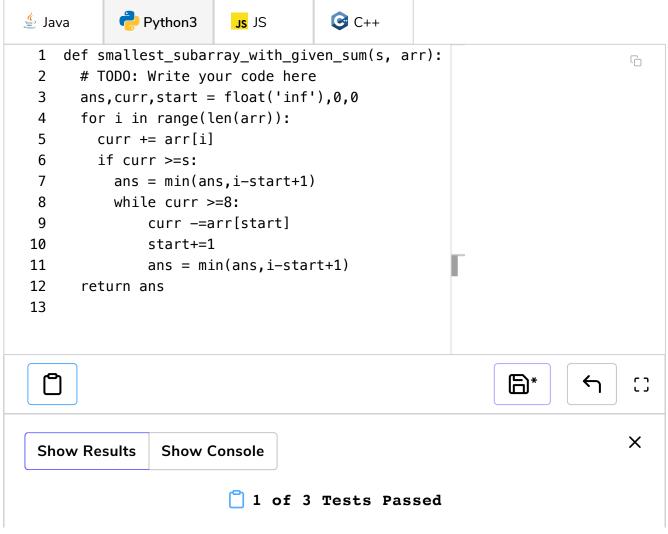
Input: [2, 1, 5, 2, 8], S=7
Output: 1
Explanation: The smallest subarray with a sum greater than or equal to '7' is [8].

#### Example 3:

```
Input: [3, 4, 1, 1, 6], S=8
Output: 3
Explanation: Smallest subarrays with a sum greater than or equal t
o '8' are [3, 4, 1] or [1, 1, 6].
```

# Try it yourself #

Try solving this question here:



Result	Input	Expected Output	Actual Output	Reason
×	<pre>smallest_subarray_with_given_sum(7,</pre>	1	0	Incorrect Output
×	<pre>smallest_subarray_with_given_sum(8,</pre>	3	2	Incorrect Output
<b>~</b>	<pre>smallest_subarray_with_given_sum(7,</pre>	2	2	Succeeded

0.17s

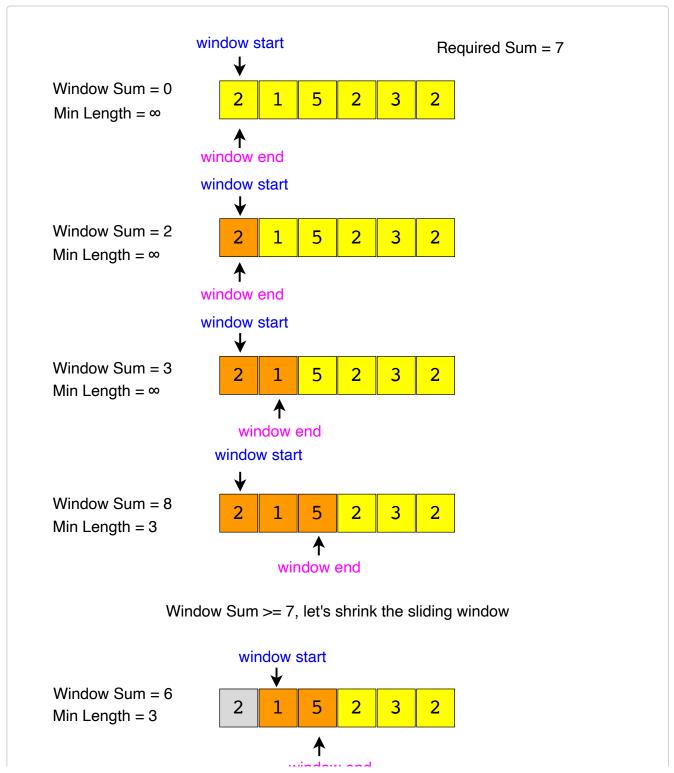
## Solution #

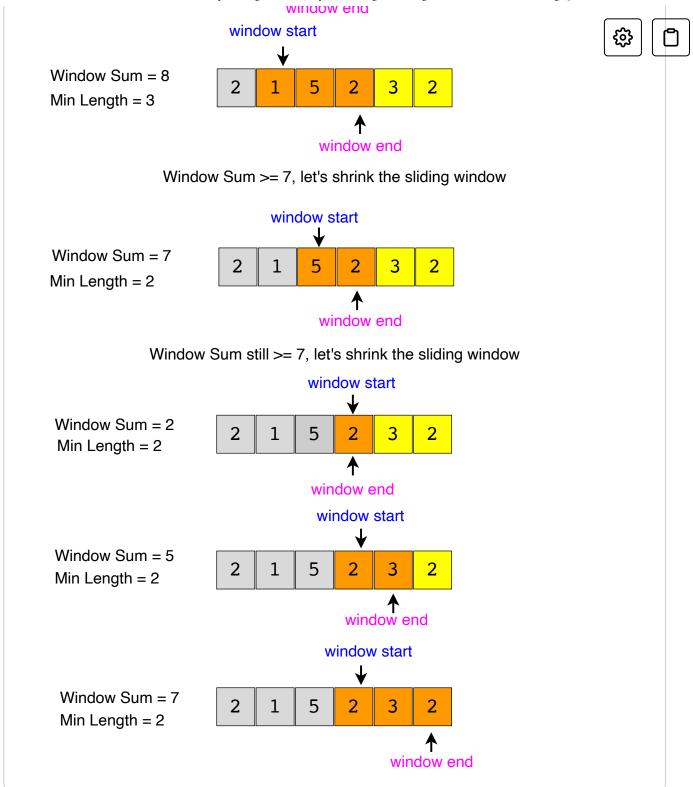
This problem follows the **Sliding Window** pattern, and we can use a similar strategy as discussed in Maximum Sum Subarray of Size K (https://www.educative.io/collection/page/5668639101419520/5671464854355 968/5177043027230720/). There is one difference though: in this problem, the sliding window size is not fixed. Here is how we will solve this problem:

- 1. First, we will add-up elements from the beginning of the array until their sum becomes greater than or equal to 'S.'
- 2. These elements will constitute our sliding window. We are asked to find the smallest such window having a sum greater than or equal to 'S.' We will remember the length of this window as the smallest window so far.
- 3. After this, we will keep adding one element in the sliding window (i.e., slide the window ahead) in a stepwise fashion.
- 4. In each step, we will also try to shrink the window from the beginning. We will shrink the window until the window's sum is smaller than 'S' again. This is needed as we intend to find the smallest window. This shrinking will also happen in multiple steps; in each step, we will do two things:

- o Check if the current window length is the smallest so far, and if so remember its length.
- Subtract the first element of the window from the running sum to shrink the sliding window.

Here is the visual representation of this algorithm for the Example-1





## Code #

Here is what our algorithm will look:



```
import math
 1
 2
 3
    def smallest_subarray_with_given_sum(s, arr):
 4
 5
      window_sum = 0
      min_length = math.inf
 6
      window_start = 0
 7
 8
 9
      for window_end in range(0, len(arr)):
        window_sum += arr[window_end] # add the nex
10
11
        # shrink the window as small as possible unt
12
        while window_sum >= s:
          min_length·=·min(min_length,·window_end·-·
13
14
          window_sum -= arr[window_start]
          window_start += 1
15
      if min_length == math.inf:
16
17
        return 0
18
      return min_length
19
20
21
    def main():
      print("Smallest subarray length: " + str(small
22
      print("Smallest subarray length: " + str(small
23
      print("Smallest subarray length: " + str(small
24
25
26
27
    main()
28
                                                            \leftarrow
D
```

### Time Complexity #

The time complexity of the above algorithm will be O(N). The outer for loop runs for all elements, and the inner while loop processes each element only once; therefore, the time complexity of the algorithm will be O(N+N), which is asymptotically equivalent to O(N).

## Space Complexity #

The algorithm runs in constant space O(1).





Maximum Sum Subarray of Size K (ea...

Longest Substring with K Distinct Cha...



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