



Question - 1
Ways to Sum

An automated packaging system is responsible for packing boxes. A box is certified to hold a certain weight. Given an integer *total*, calculate the number of possible ways to achieve *total* as a sum of the weights of items weighing integer weights from 1 to *k*, inclusive.

Example

total = 8

k = 2

To reach a weight of 8, there are 5 different ways that items with weights between 1 and 2 can be combined:

- [1, 1, 1, 1, 1, 1, 1]
- [1, 1, 1, 1, 1, 1, 2]
- [1, 1, 1, 1, 2, 2]
- [1, 1, 2, 2, 2]
- [2, 2, 2, 2]

Function Description

Complete the function *ways* in the editor below.

ways has the following parameter(s):

int total: the value to sum to

int k: the maximum of the range of integers to consider when summing to *total*

Returns

int: the number of ways to sum to the *total*; the number might be very large, so return the integer modulo 1000000007 (10^9+7)

Constraints

- $1 \leq total \leq 1000$
- $1 \leq k \leq 100$

▼ Input Format For Custom Testing

The first line contains an integer, *total*, that denotes the target sum.
The second line contains an integer, *k*, that denotes the maximum value in the range of integers to be considered, i.e, from 1 to *k*.

▼ Sample Case 0

Sample Input For Custom Testing

STDIN	Function
5	→ total = 5
3	→ k = 3

Sample Output

5

Explanation

The sum required is 5. $k = 3$ so the integers that can be considered to reach the sum are $[1, 2, 3]$.

The 5 ways to reach the target sum are:

1. $1 + 1 + 1 + 1 + 1 = 5$
2. $1 + 1 + 1 + 2 = 5$
3. $1 + 2 + 2 = 5$
4. $1 + 1 + 3 = 5$
5. $2 + 3 = 5$

$5 \text{ modulo } 1000000007 = 5$

▼ Sample Case 1

Sample Input For Custom Testing

STDIN	Function
4	→ total = 4
2	→ k = 2

Sample Output

3

Explanation

The sum required is 4, and the range of integers is $[1, 2]$

There are 3 ways to reach the target sum:

1. $1 + 1 + 1 + 1 = 4$
2. $1 + 1 + 2 = 4$
3. $2 + 2 = 4$

$3 \text{ modulo } 1000000007 = 3.$

Question - 2

String Patterns

Given the length of a word (*wordLen*) and the maximum number of consecutive vowels that it can contain (*maxVowels*), determine how many unique words can be generated. Words will consist of English alphabetic letters a through z only. Vowels are *v*. {*a*, *e*, *i*, *o*, *u*}; consonants are *c*. the remaining 21 letters. In the explanations, *v* and *c* represent vowels and consonants.

wordLen = 1

maxVowels = 1

Patterns: {*v*, *c*}

That means there are 26 possibilities, one for each letter in the alphabet.

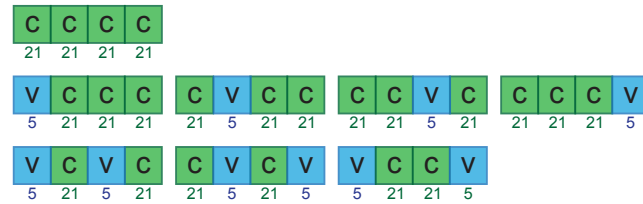
V	or	C
5		21

wordLen = 4

maxVowels = 1

Patterns: {cccc, vccc, cvcc, ccvc, cccv, vcvc, cvcv, vccv}

There are 412,776 possibilities -- see below:



$$\begin{aligned}(21 * 21 * 21 * 21) &= 194481 \\ (5 * 21 * 21 * 21) + (21 * 5 * 21 * 21) + (21 * 21 * 5 * 21) + (21 * 21 * 21 * 5) &= 4 * 46305 = 185220 \\ (5 * 21 * 5 * 21) + (21 * 5 * 21 * 5) + (5 * 21 * 21 * 5) &= 3 * 11025 = 33075 \\ 194481 + 185220 + 33075 &= 412776 \text{ possible solutions.}\end{aligned}$$

wordLen = 4
maxVowels = 2

In this case, all of the combinations from the previous example are still valid.

- There are 5 additional patterns to consider, three with 2 vowels (vvcc, cvvc, ccvv) and 2 with 3 vowels (vvcv and vcvv).
- Their counts are $3 * (5 * 5 * 21 * 21) = 3 * 11025 = 33075$ and $2 * (5 * 5 * 5 * 21) = 2 * 2625 = 5250$.
- The total number of combinations then is $412776 + 33075 + 5250 = 451101$.

The result may be a very large number, so return the answer modulo (10^9+7) .

Note: While the answers will be within the limit of a 32 bit integer, interim values may exceed that limit. Within the function, you may need to use a 64 bit integer type to store them.

Function Description

Complete the function *calculateWays* in the editor below.

calculateWays has the following parameter(s):

int wordLen: the length of a word

int maxVowels: the maximum number of consecutive vowels allowed in a word

Returns

int: the number of well-formed strings that can be created, modulo $1000000007 (10^9+7)$

Constraints

- $1 \leq \text{wordLen} \leq 2500$
- $0 \leq \text{maxVowels} \leq n$

▼ Input Format Format for Custom Testing

Input from stdin will be processed as follows and passed to the function.

The first line contains an integer *wordLen*, the length of the words to create.

The next line contains an integer *maxVowels*, maximum number of consecutive vowels allowed.

▼ Sample Case 0

Sample Input 0

STDIN	Function
-----	-----
2	→ wordLen = 2
1	→ maxVowels = 1

Sample Output 0

651

Explanation 0

Words take the forms $\{vc, cv, cc\}$. There is a vowel in the first position, the second position or no position. The total number of unique words is $(5 * 21) + (21 * 5) + (21 * 21) = 651$ and $651 \text{ modulo } 1000000007 = 651$.

▼ Sample Case 1

Sample Input 1

STDIN	Function
-----	-----
2	→ wordLen = 2
2	→ maxVowels = 2

Sample Output 1

676

Explanation 1

Since the words are 2 characters, and there can be 2 consecutive vowels, each position can contain any character. Words take the forms $\{vv, vc, cv, cc\}$. The total number of unique words is $(26 * 26) = 676$ and $676 \text{ modulo } 1000000007 = 676$.

▼ Sample Case 2

Sample Input 2

STDIN	Function
-----	-----
2	→ wordLen = 2
0	→ maxVowels = 0

Sample Output 2

441

Explanation 2

No vowels are allowed in a word, therefore the words are in the form $\{cc\}$. The total number of unique words is $(21 * 21) = 441$ and $441 \text{ modulo } 1000000007 = 441$.