

# Technical Report

## problem declaration:

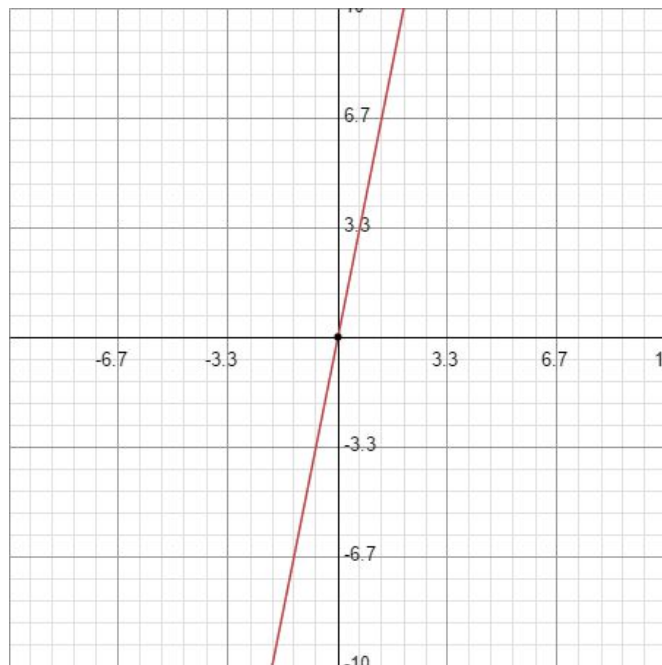
We are going to design a circuit to receive a 4 bit digit number with 4 switches in order to calculate the amount of it's integral.

$$\int 5x \, dx$$

output will display in 7-segments.

## **solution :**

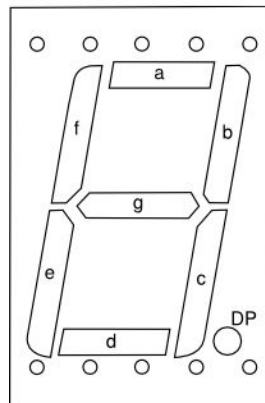
since a 4 bit number in the Decimal system covers a number in range of 0 to 15. According to the definition of integrals, we know that in a function like:  $f_{(x)}=5x$  the answer is the between the  $f_{(x)}$  and the x-axis. So it should be between  $x=0$  to  $x=A$  (A: is the input value to calculate)



$$\int 5x \, dx = 5 (x^2/2) \Rightarrow 5 (A^2/2)$$

We are going to use four 7-segments. So our output will look like xxx.x in the decimal system. The 8th pin of our third seven segment will turn on as DP-point to show the float number.

the 7-segment with common anode display will turn on by 1(TRUE) inputs.



so it will display the numbers according to the below chart:

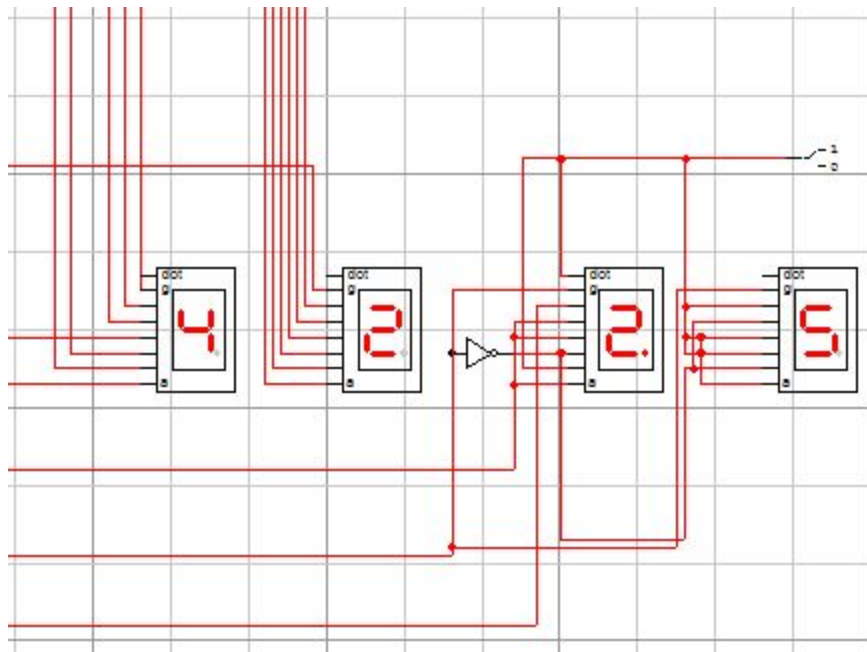
| Digit number | a | b | c | d | e | f | g |
|--------------|---|---|---|---|---|---|---|
| 0            | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
| 1            | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 2            | 1 | 1 | 0 | 1 | 1 | 0 | 1 |
| 3            | 1 | 1 | 1 | 1 | 0 | 0 | 1 |
| 4            | 0 | 1 | 1 | 0 | 0 | 1 | 1 |
| 5            | 1 | 0 | 1 | 1 | 0 | 1 | 1 |
| 6            | 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 7            | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| 8            | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 9            | 1 | 1 | 1 | 0 | 0 | 1 | 1 |

eventually we will have 4 seven segments and 4 tables for each of them to show the output:

the next table demonstrates each potential output for its input for the numbers between 0 to 15(solution for numbers between these 16 digits.)

| inputs |   |   |   |   | O0 |    |    |    |    |    |    |    | O1 |    |    |    |    |    |    |    | O2 |    |    |    |    |    |    |    | O3 |    |    |    |  |  |  |  |
|--------|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|--|--|--|--|
| dec    | a | b | c | d | A0 | B0 | C0 | D0 | E0 | F0 | G0 | A1 | B1 | C1 | D1 | E1 | F1 | G1 | A2 | B2 | C2 | D2 | E2 | F2 | G2 | A3 | B3 | C3 | D3 | E3 | F3 | G3 |  |  |  |  |
| 0      | 0 | 0 | 0 | 0 | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 1      | 0 | 0 | 0 | 1 | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |
| 2      | 0 | 0 | 1 | 0 | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 0  | 1  | 1  | 0  | 0  | 0  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 3      | 0 | 0 | 1 | 1 | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |
| 4      | 0 | 1 | 0 | 0 | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 0  | 1  | 1  | 0  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 5      | 0 | 1 | 0 | 1 | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |
| 6      | 0 | 1 | 1 | 0 | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 0  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 7      | 0 | 1 | 1 | 1 | 0  | 1  | 1  | 0  | 0  | 0  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |
| 8      | 1 | 0 | 0 | 0 | 0  | 1  | 1  | 0  | 0  | 0  | 0  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 9      | 1 | 0 | 0 | 1 | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |
| 10     | 1 | 0 | 1 | 0 | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 11     | 1 | 0 | 1 | 1 | 1  | 1  | 1  | 1  | 0  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |
| 12     | 1 | 1 | 0 | 0 | 1  | 1  | 1  | 1  | 0  | 0  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 13     | 1 | 1 | 0 | 1 | 0  | 1  | 1  | 0  | 0  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |
| 14     | 1 | 1 | 1 | 0 | 0  | 1  | 1  | 0  | 0  | 1  | 1  | 1  | 1  | 1  | 0  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 0  |  |  |  |  |
| 15     | 1 | 1 | 1 | 1 | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 1  | 0  | 1  | 1  | 1  | 1  | 1  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  | 0  | 1  | 1  |  |  |  |  |

SOP form for karnaugh tables will calculate and the functions will deploy in the circuit.



|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 1  | 0  | 1  |
| 11 | 1  | 0  | 1  | 0  |
| 10 | 0  | 1  | 1  | 1  |

$$A_0 = a'b' + a'c' + a'd' + cb' + b'd + bc'd' + cda$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 1  | 1  | 1  |
| 11 | 1  | 1  | 0  | 1  |
| 10 | 1  | 1  | 1  | 1  |

$$B_0 = c' + a' + d' + b'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 1  | 1  | 1  |
| 11 | 1  | 1  | 1  | 1  |
| 10 | 1  | 0  | 1  | 0  |

$$C_0 = a' + b + cd + c'd'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 1  | 0  | 1  |
| 11 | 1  | 0  | 1  | 0  |
| 10 | 0  | 1  | 1  | 1  |

$$D_0 = a'b' + c'a' + b'c + d'a' + db' + bc'd' + cda$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 1  | 0  | 1  |
| 11 | 0  | 0  | 0  | 0  |
| 10 | 0  | 1  | 0  | 1  |

$$E_0 = a'b' + a'c' + d'a' + cd'b' + c'db'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 1  | 0  | 1  |
| 11 | 0  | 1  | 1  | 1  |
| 10 | 0  | 0  | 0  | 0  |

$$F_0 = a'b' + a'c' + d'a' + abc + abd$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 0  | 0  | 0  | 0  |
| 01 | 0  | 0  | 0  | 0  |
| 11 | 1  | 1  | 1  | 1  |
| 10 | 0  | 1  | 1  | 1  |

$$G_0 = ab + ac + ad$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 0  | 1  | 1  | 1  |
| 11 | 1  | 1  | 1  | 1  |
| 10 | 1  | 1  | 1  | 1  |

$$A_1 = a + c + d + a'b'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 0  | 1  | 1  |
| 11 | 0  | 1  | 0  | 1  |
| 10 | 0  | 1  | 1  | 0  |

$$B_1 = a'b' + a'c + a'd' + b'd + cd'b + c'da$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 0  | 1  |
| 01 | 1  | 1  | 0  | 1  |
| 11 | 1  | 0  | 1  | 1  |
| 10 | 1  | 1  | 1  | 1  |

$$C_1 = d' + ab' + ac + a'c'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 0  | 1  | 1  | 0  |
| 11 | 1  | 1  | 1  | 0  |
| 10 | 1  | 1  | 1  | 1  |

$$D_1 = d + b'd' + ac'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 0  | 1  | 1  | 0  |
| 11 | 1  | 1  | 1  | 0  |
| 10 | 1  | 1  | 1  | 0  |

$$E_1 = d + ac' + a'b'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 0  | 1  |
| 01 | 1  | 1  | 0  | 1  |
| 11 | 1  | 0  | 1  | 1  |
| 10 | 1  | 1  | 1  | 1  |

$$F_1 = d' + ab' + a'c' + ac$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 0  | 0  | 1  | 0  |
| 01 | 1  | 1  | 1  | 1  |
| 11 | 1  | 1  | 1  | 1  |
| 10 | 1  | 0  | 0  | 1  |

$$G_1 = b + cda' + ad'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 0  |
| 01 | 1  | 1  | 1  | 1  |
| 11 | 1  | 1  | 1  | 1  |
| 10 | 1  | 1  | 1  | 1  |

$$A_2 = D_2 = E_2 = c' + d + a + b$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 01 | 1  | 1  | 1  | 1  |
| 11 | 1  | 1  | 1  | 1  |
| 10 | 1  | 1  | 1  | 1  |

$$B_2=1$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 0  | 0  | 1  |
| 01 | 1  | 0  | 0  | 1  |
| 11 | 1  | 0  | 0  | 1  |
| 10 | 1  | 0  | 0  | 1  |

$$C_2=d'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 0  | 0  | 0  |
| 01 | 1  | 0  | 0  | 1  |
| 11 | 1  | 0  | 0  | 1  |
| 10 | 1  | 0  | 0  | 1  |

$$F_2=c'd'+d'a+d'b$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 0  | 1  | 1  | 0  |
| 01 | 0  | 1  | 1  | 0  |
| 11 | 0  | 1  | 1  | 0  |
| 10 | 0  | 1  | 1  | 0  |

$$G_2=d$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 1  | 1  | 1  |
| 10 | 1  | 1  | 1  | 1  |
| 11 | 1  | 1  | 1  | 1  |
| 10 | 1  | 1  | 1  | 1  |

$$A_3=C_3=D_3=F_3=1$$



|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 1  | 0  | 0  | 1  |
| 01 | 1  | 0  | 0  | 1  |
| 11 | 1  | 0  | 0  | 1  |
| 10 | 1  | 0  | 0  | 1  |

$$B_3 = E_3 = d'$$

|    | 00 | 01 | 11 | 10 |
|----|----|----|----|----|
| 00 | 0  | 1  | 1  | 0  |
| 01 | 0  | 1  | 1  | 0  |
| 11 | 0  | 1  | 1  | 0  |
| 10 | 0  | 1  | 1  | 0  |

$$G_3 = d$$

some of the functions are reduced and briefed :

$$C_0 = a' + b + (c \oplus d)'$$

$$E_0 = a'b' + a'c' + a'd' + b'(c \oplus d)$$

$$G_0 = a(b + c + d)$$

$$C_1 = d' + ab' + (a \oplus c)' = F_1$$

- to reduce a level from the circuit we use not include gates instead of changing the inputs to FALSE.

.cct file is made by Logic work application.(final circuit design)



