

Data Structures and Complexity

Memory, Data Structures and Complexity Notations



SoftUni Team
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1. Memory Storage
2. Data Structures – Overview
3. Algorithmic Complexity
 - Asymptotic notations
4. Array Data Structure
5. Data Structure Implementation





Memory Storage

Memory Storage and Hierarchy

What Do We Call Memory?

- Computer **memory** is any physical device capable of storing information temporarily, like **RAM**, or permanently, like **ROM**. Memory devices utilize **integrated circuits** and are used by **operating systems, software, and hardware**.
- The term "memory", meaning "primary storage" or "**main memory**", is often associated with addressable **semiconductor memory**.



What Do We Call Memory?

- In computer science, memory usually is:
 - a continuous, numbered – aka addressed – sequence of bytes
 - storage for variables and functions created in programs
 - random-access – equally fast accessing 5th and 500th byte
 - addresses numbered in hexadecimal, prefixed with 0x

Address	0x0	0x1	0x2	...	0x6afe4c	...
Byte _(binary)	00001101	00101010	01000101	...	00000011	...

Memory Usage by Variables

- A primitive data type takes up a sequence of bytes
 - **byte** is **1** byte, **1** address:

```
byte number = 42; // let's assume number is at address 0x6afe4c
```

Address	...	0x6afe4b	0x6afe4c
---------	-----	----------	----------	-----	-----	-----	-----

Byte _(binary)	00101010
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- Other types & arrays use consecutive bytes, e.g. **4**-byte **int**

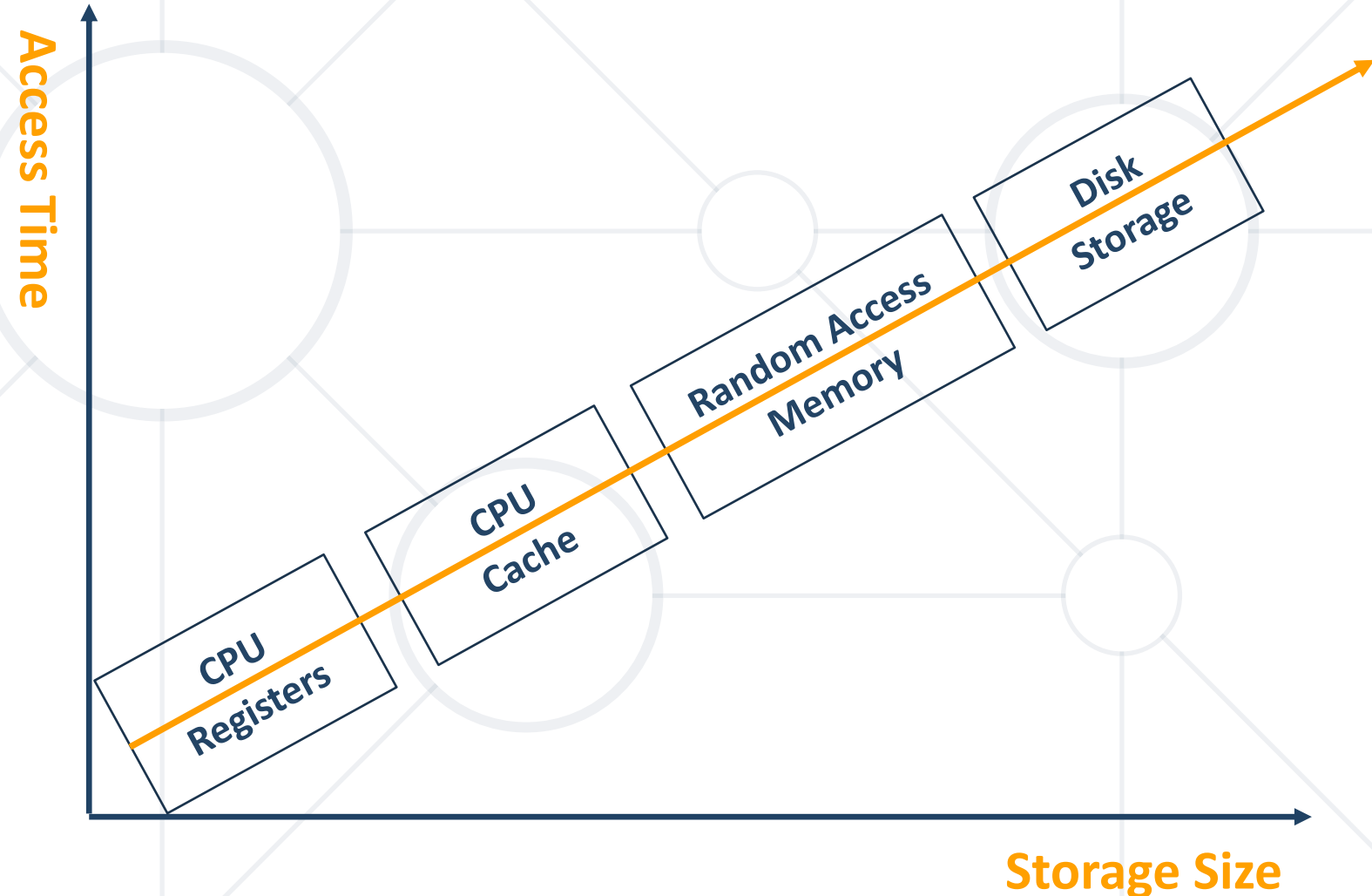
```
int year = 2020; // let's assume year is at address 0x6afe4c
```

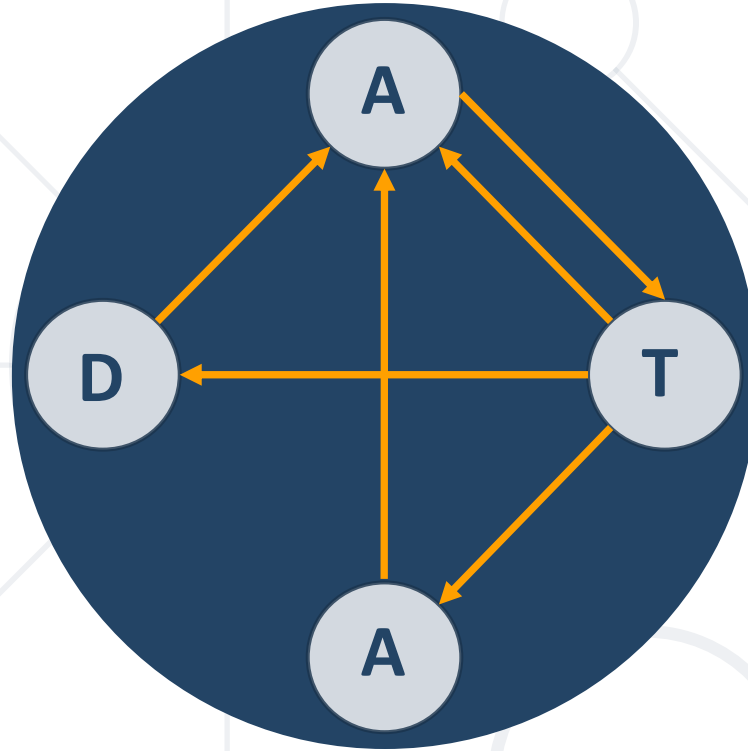
Address	...	0x6afe4b	0x6afe4c	0x6afe4d	0x6afe4e	0x6afe4f	...
---------	-----	----------	----------	----------	----------	----------	-----

Byte _(binary)	11100100	00000111	00000000	00000000	...
--------------------------	-----	-----	----------	----------	----------	----------	-----

Memory Hierarchy

- Each memory level is **faster** and **smaller** than the **next memory level**. At the end we can say we have **nearly infinite memory** storage which **is also infinitely slow**.






Data Structures

Overview

What is Data?

- 
- **"Data"** from Latin – datum, which originally meant "something given." Dates back to the 1600s.
 - Data is **raw, unorganized** facts that need to be processed. Data can be something simple and seemingly **random** and **useless** until it is **organized**.
 - Example:

The history of temperature readings all over the world for the past 100 years is data.

What is Information?


- **"Information"** has Old French and Middle English origins. It has always referred to "the act of informing, " usually in regard to education, instruction, or other knowledge communication.
- When data is **processed, organized, structured or presented** in each **context** to **make it useful**, it is called **information**.
- Example:

The history of temperature readings all over the world for the past 100, when organized and analyzed we find that global temperature is rising.

- Set of **symbols** gathered and translated for **some purpose**.
- Simplified – bits of information stored in memory. If those bits remain **unused**, they don't do anything.
- Example:

Binary Data	Translation
100 0001	65
100 0001	A

- It is easy to notice, that the way we **read** the data **retrieves the information** of the bits in different ways. However those bits have only **0** or **1** as values.
- Example:

Type	Binary Data	Translation
Integer	0000 0100 0001	65
Character	0000 0100 0001	'A'
Double	0000 0100 0001	65.0
Instruction Code	0000 0100 0001	Store 65
Color	0000 0100 0001	

- Data structure – an **object** which takes responsibility for data **organization, storage, management** in **effective** manner.
- Storing items **requires memory consumption**:

Data Structure	Size
int	= 4 bytes
float	= 4 bytes
long	= 8 bytes
int[]	$\approx (\text{Array length}) * 4 \text{ bytes}$
List<double>	$\approx (\text{List size}) * 8 \text{ bytes}$
Dictionary<int, int[]>	$\approx (\text{Dictionary size}) * \text{Entry bytes}$

- An **Abstract Data Structure (ADS)** – the way the real objects will be modulated as **mathematical** objects, alongside the **set of operations** to be executed upon them, **without** the implementation itself.

```
public interface IList<T>
{
    void Add(T item);
    int Count { get; }
    bool Remove(T item);
    void Clear();
}
```

- An **implementation** – definitive way of ADS to be presented inside the computer memory, alongside the implementation of the operations.

```
public class List<T> : IList<T>
{
    public void Add(T item)
    {
        this.Grow();
        this.elements[this.Count++] = item;
    }
}
```

A background network diagram consisting of a grid of light gray lines intersecting at various points. Some of these intersections are marked with small, empty light gray circles. A larger, solid dark blue circle is centered in the upper half of the image, containing the text 'O(n)' in white.

$O(n)$

Algorithmic Complexity

Asymptotic Notation

- Why should we analyze algorithms?
 - Predict the **resources** the algorithm will need
 - Computational time (**CPU** consumption)
 - Memory space (**RAM** consumption)
 - Communication **bandwidth** consumption
 - **Hard disk** operations

- There are three main properties we want to analyze:
 - **Simplicity** – this is really a matter of intuition and of course it is subjective quality
 - **Accuracy** – this seems easy to determine, however it may be very difficult to determine if the algorithm is correct?
 - **Performance** – the consumption of CPU, Memory and other resources (we really care the most for the first two)

- The expected **running time** of an algorithm is:
 - The total number of **primitive operations** executed (machine independent steps)
 - Also known as **algorithm complexity**
 - Compare algorithms **ignoring details** such as **language** or **hardware**

Problem: Get Number of Steps

- Calculate maximum steps to find the result

```
long GetOperationsCount(int n)
{
    long counter = 0;
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            counter++;
    return counter;
}
```

Solution:

$$T(n) = 3(n^2) + 3n + 3$$

- The input(**n**) of the function is the main source of steps growth

- Some parts of the equation **grow much faster** than others
 - $T(n) = 3(n^2) + 3n + 3$
 - We can **ignore** some part of this equation
 - Higher terms **dominate** lower terms – $n > 2$, $n^2 > n$, $n^3 > n^2$
 - Multiplicative constants can be **omitted** – $12n \rightarrow n$, $2n^2 \rightarrow n^2$
- The solution becomes $\approx n^2$

- Worst-case
 - An **upper** bound on the running time
- Average-case
 - **Average** running time
- Best-case
 - The **lower** bound on the running time (the optimal case)

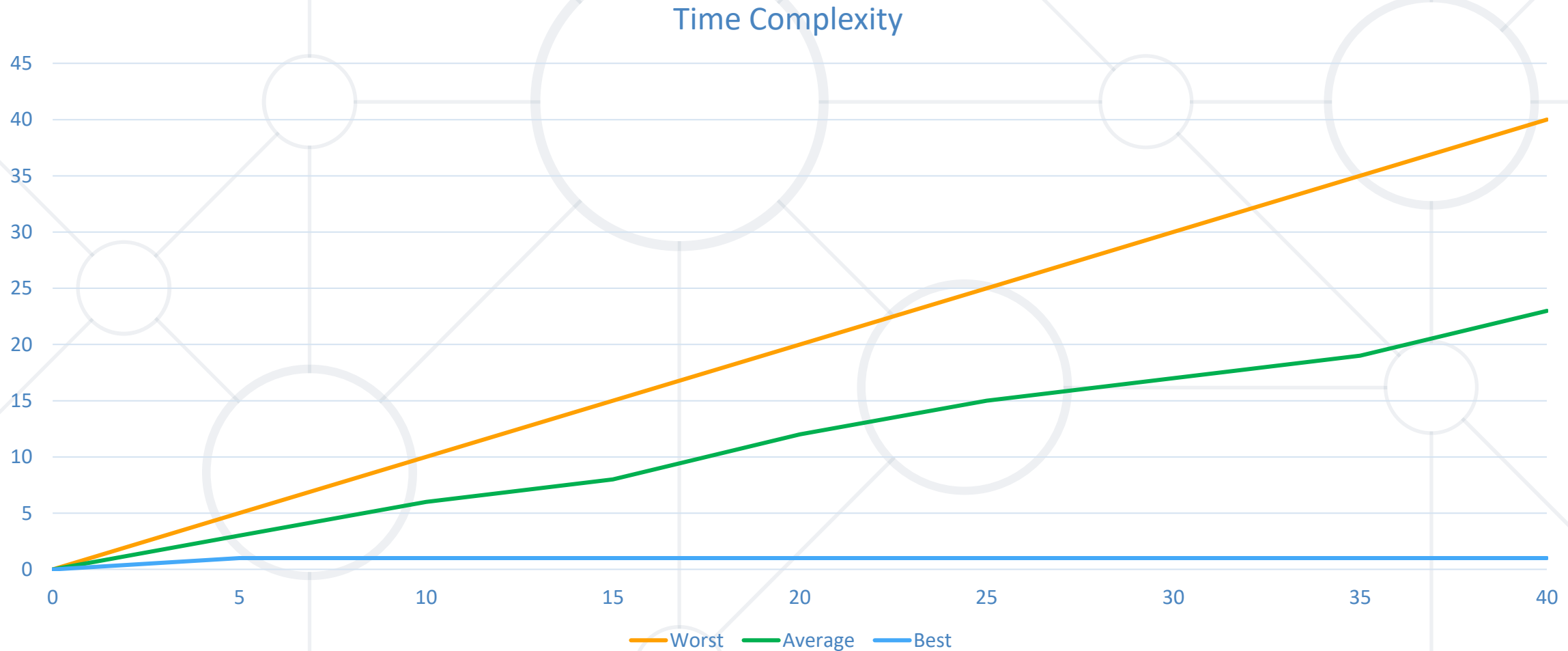
- Define the time complexity of the following code:

```
bool Contains(int[] numbers, int number)
{
    for (int i = 0; i < numbers.Length; i++)
        if (numbers[i] == number)
            return true;

    return false;
}
```


- It is not as simple as the previous, **when** does the code return?

- Therefore, we need to measure **all** the possibilities:



- From the previous chart we can deduce:
 - For smaller size of the input (n) we **don't care much for the runtime**. So we measure the time as n approaches **infinity**
 - If an algorithm **has to scale**, it **should compute** the result within a **finite and practical time**
 - We're concerned about the **order of an algorithm's complexity**, not the actual time in terms of **milliseconds**

Asymptotic Notations

- 
- **Asymptotic notations** are descriptions that allow us to examine an algorithm's running time by expressing its **performance** as the input size (**n**) of an algorithm or a function **f increases**. There are **three** common asymptotic notations:

- Big **O** – $O(f(n))$
- Big **Theta** – $\Theta(f(n))$
- Big **Omega** – $\Omega(f(n))$

- **Algorithmic complexity** – rough estimation of the number of steps performed by given computation, depending on the size of the input
- Measured with asymptotic notation
 - **$O(f(n))$** – upper bound (worst case)
 - **$\Theta(f(n))$** – average case
 - **$\Omega(f(n))$** – lower bound (best case)
 - Where **$f(n)$** is a function of the size of the input data

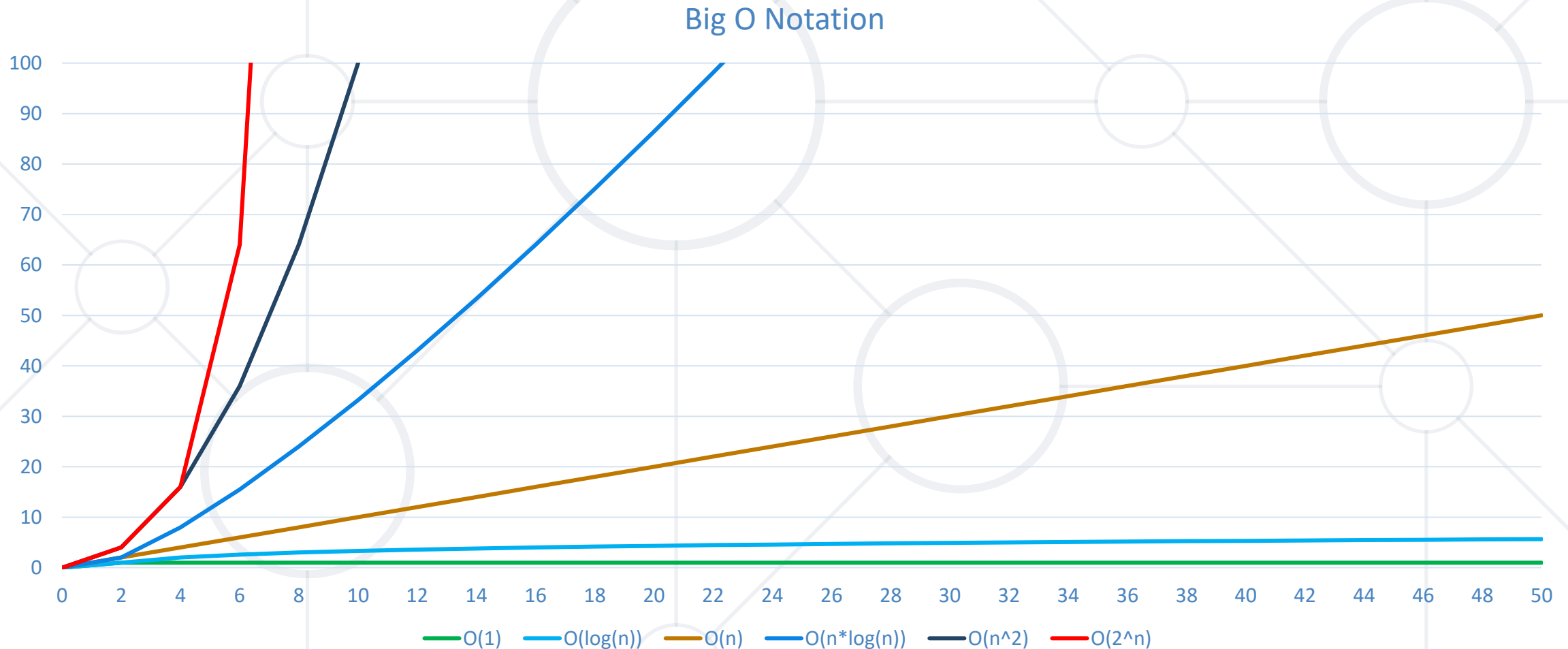
- In this course we will analyze only the Big O – **$O(f(n))$**

```
bool Contains(int[] numbers, int number)
{
    for (int i = 0; i < numbers.length; i++)
        if (numbers[i] == number)
            return true;

    return false;
}
```

- So the code above will have **$O(n)$** or simply **linear** complexity

- Below are some examples of **common algorithmic** grow:



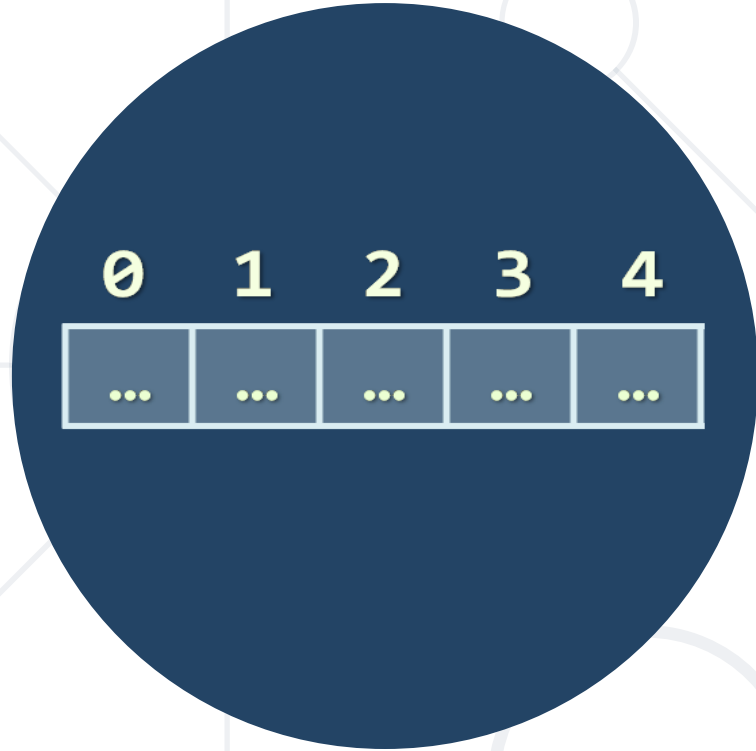
Typical Complexities

Complexity	Notation	Description
constant	$O(1)$	$n = 1\ 000 \rightarrow 1\text{-}2$ operations
logarithmic	$O(\log n)$	$n = 1\ 000 \rightarrow 10$ operations
linear	$O(n)$	$n = 1\ 000 \rightarrow 1\ 000$ operations
linearithmic	$O(n \cdot \log n)$	$n = 1\ 000 \rightarrow 10\ 000$ operations
quadratic	$O(n^2)$	$n = 1\ 000 \rightarrow 1\ 000\ 000$ operations
cubic	$O(n^3)$	$n = 1\ 000 \rightarrow 1\ 000\ 000\ 000$ operations
exponential	$O(n^n)$	$n = 10 \rightarrow 10\ 000\ 000\ 000$ operations

Time Complexity and Program Speed

Complexity	10	20	50	100	1 000	10 000	100 000
$O(1)$	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s
$O(\log n)$	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s
$O(n)$	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s
$O(n \cdot \log n)$	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s
$O(n^2)$	< 1 s	< 1 s	< 1 s	< 1 s	< 1 s	2 s	3-4 min
$O(n^3)$	< 1 s	< 1 s	< 1 s	< 1 s	20 s	5 hours	231 days
$O(2^n)$	< 1 s	< 1 s	260 days	hangs	hangs	hangs	hangs
$O(n!)$	< 1 s	hangs	hangs	hangs	hangs	hangs	hangs
$O(n^n)$	3-4 min	hangs	hangs	hangs	hangs	hangs	hangs

- **Memory consumption** should also be considered, for example:
 - Storing elements in a matrix of size N by N
 - Filling the matrix – Running time $O(n^2)$
 - Get element by index – Running time $O(1)$
 - Memory requirement $O(n^2)$
- However in this course we **won't be optimizing** memory consumption we will only point it out



Array Data Structures

Built-in and Lightweight

- Ordered
- Very **lightweight**
- Has a **fixed size**
- Usually **built into the language**
- Many collections are implemented by using arrays, e.g.
 - **List<T>** in C#
 - **Queue<T>** in C#
 - **Stack<T>** in C#

Why Arrays Are Fast?

- Arrays use a **single block of memory**

int size is 4 bytes

```
int[] array = { 2, 4, 1, 3, 5 };
```

- Uses total of **array pointer + (N * element/pointer size)**

Array starts at this address

		2	4	1	3	5			

Total: 5 * 4 bytes

- Array Address + (Element Index * Size) = Element Address**
- Array Element Lookup – **O(1)**

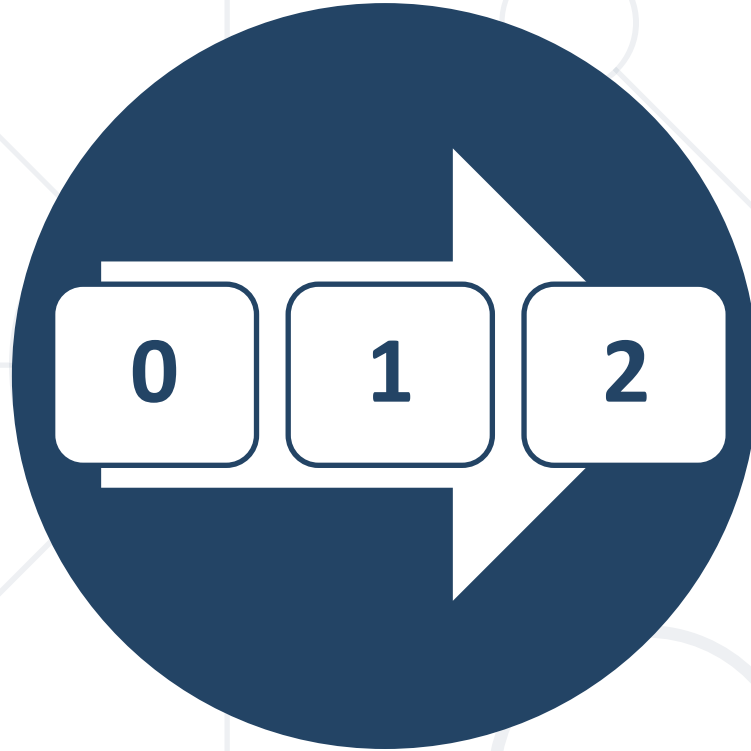
Arrays – Changing Array Size

- Arrays have a **fixed size**
- Memory after the array **may be occupied**
- If we want to resize the array we have to **make a copy**

		2	4	1	3	5			
2	4	1	3	5	0	0	0		

May be occupied

- Array Copy – **$O(n)$**



Data Structure Implementation

Elements Representation Approaches

How Do We Store the Elements?

- **Choose** the way to **store** the elements:
 - By **using an array**:
 - Stores the elements as a **sequence** inside the computer memory
 - By **using a Node<T>** class:
 - Contains the **element** inside the Node.
 - **Must** have **pointer to the next Node**.
 - Can have **more** fields if necessary.



- Store the elements

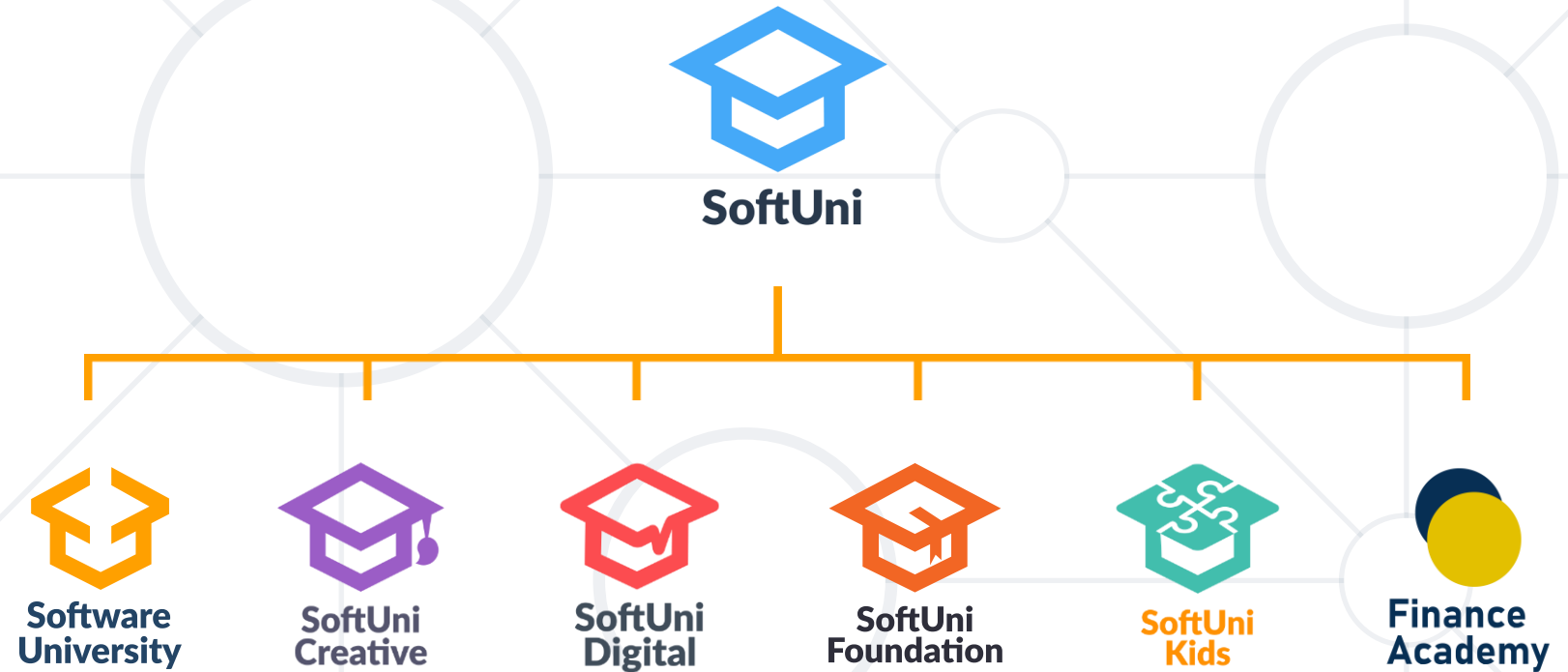
```
public class List
{
    private int[] elements;
}
```

- We can access indices with **$O(1)$** – constant complexity
- The **rest** operations on **unsorted** arrays are **linear**
- Array initial **size**?
- What happens when we **exceed** the **initial** size?

- **Data structures** organize data in computer systems for efficient use
 - Abstract data types (**ADT**) describe a set of operations
- **Algorithm complexity** is a rough estimation of the **number of steps** performed by given computation
- **Arrays** are a **lightweight data structure** that has **constant time access** to elements but has a **fixed size**



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