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import os
In [ ]:
        # MDP Environment
In [ ]:
        import random
        class MDP(object):
          def __init__(self,Questions,Prob_Rewards):
             self.Questions = Questions
             self.Prob_Rewards = Prob_Rewards
          def InitState(self):
            return 1
          def EndState(self, state):
            return state == self.Questions
          def Actions(self, state):
             if self.EndState(state):
               return []
             else:
               return ['Stay','Quit']
          def SuccProbReward(self, state, action):
            if action == 'Stay':
               if state > self.Questions:
                 return [(state, 1., 0.)]
               else:
                 Probability = self.Prob_Rewards[state][0]
                 Reward = self.Prob Rewards[state][1]
                 return [(state+1,Probability,Reward),(self.Questions+1, 1.-Probability, 0.
             elif action == 'Quit':
               if state > self.Questions:
                 return[(state,1.,0.)]
               else:
                 Probability = 1.0
                 Reward = self.Prob_Rewards[state][1]
                 return [(self.Questions+1, Probability, Reward)]
          def discount(self):
                 return 0.9
          def states(self):
             return range(1,self.Questions+2)
        # Value Iteration for the above Defined MDP environment
        def valueIteration(mdp, epsilon=0.001):
             # initialize values of all states to zero
            V = {s: 0.0 for s in mdp.states()}
            # repeat until convergence
             while True:
                 # set change to zero
                 delta = 0
                 # for each state, update its value using Bellman update
                 for s in mdp.states():
                     if mdp.EndState(s):
                         continue
                     # compute the maximum value over all possible Actions
                     MaxValue = -float('inf')
                     for a in mdp.Actions(s):
                         val = 0
                         for NextState, Probability, Reward in mdp.SuccProbReward(s, a):
                             val += Probability * (Reward + mdp.discount() * V[NextState])
                         MaxValue = max(MaxValue, val)
                     # update value of state
```

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delta = max(delta, abs(MaxValue - V[s]))
                     V[s] = MaxValue
                 # check for convergence
                 if delta < epsilon:</pre>
                     break
             # compute the optimal policy using the computed values
             for s in mdp.states():
                 if mdp.EndState(s):
                     pi[s] = None
                 else:
                    MaxValue = -float('inf')
                     best action = None
                     for a in mdp.Actions(s):
                         val = 0
                         for NextState, Probability, Reward in mdp.SuccProbReward(s, a):
                             val += Probability * (Reward + mdp.discount() * V[NextState])
                         if val > MaxValue:
                             MaxValue = val
                             best action = a
                    pi[s] = best_action
             # return the computed values and policy
            return V, pi
        Questions = 10
        Prob_Rewards = \{1: (0.99, 100),
                         2: (0.9, 500),
                         3: (0.8, 1000),
                         4: (0.7, 5000),
                         5: (0.6, 10000),
                         6: (0.5, 50000),
                         7: (0.4, 100000),
                         8: (0.3, 500000),
                         9: (0.2, 1000000),
                         10: (0.1, 5000000)}
        kbc_MDP = MDP(Questions,Prob_Rewards)
        V, P = valueIteration(kbc_MDP)
        # kbc MDP.MonteCarlo(2)
        print(V)
        print(P)
        {1: 26780.771381760005, 2: 29945.87136000001, 3: 36414.656, 4: 49464.799999999996,
        5: 72960.0, 6: 124000.0, 7: 220000.0, 8: 500000.0, 9: 1000000.0, 10: 0.0, 11: 0.0}
        {1: 'Stay', 2: 'Stay', 3: 'Stay', 4: 'Stay', 5: 'Stay', 6: 'Stay', 7: 'Stay', 8:
         'Quit', 9: 'Quit', 10: None, 11: 'Stay'}
In [ ]: # Policy Iteration for the above Defined MDP environment
        def policyIteration(mdp, epsilon=0.001):
            # initialize values of all states to zero
            V = {s: 0.0 for s in mdp.states()}
             # initialize policy arbitrarily
             pi = {s: mdp.Actions(s)[0] for s in mdp.states() if not mdp.EndState(s)}
             while True:
                 # policy evaluation step
                 while True:
                     delta = 0
                     for s in mdp.states():
                         if mdp.EndState(s):
                             continue
                         # compute the value of the current policy for this state
                         val = 0
                         for NextState, Probability, Reward in mdp.SuccProbReward(s, pi[s])
```

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val += Probability * (Reward + mdp.discount() * V[NextState])
                         # update value of state
                         delta = max(delta, abs(val - V[s]))
                         V[s] = val
                     if delta < epsilon:</pre>
                         break
                 # policy improvement step
                 policy stable = True
                 for s in mdp.states():
                     if mdp.EndState(s):
                         continue
                     old_action = pi[s]
                     # find the best action using the updated values
                     MaxValue = -float('inf')
                     best_action = None
                     for a in mdp.Actions(s):
                         val = 0
                         for NextState, Probability, Reward in mdp.SuccProbReward(s, a):
                             val += Probability * (Reward + mdp.discount() * V[NextState])
                         if val > MaxValue:
                             MaxValue = val
                             best action = a
                     # update policy
                     pi[s] = best_action
                     if old_action != best_action:
                         policy_stable = False
                 # check for convergence
                 if policy_stable:
                     break
             # return the computed values and policy
             return V, pi
        Questions = 10
        Prob_Rewards = \{1: (0.99, 100),
                         2: (0.9, 500),
                         3: (0.8, 1000),
                         4: (0.7, 5000),
                         5: (0.6, 10000),
                         6: (0.5, 50000),
                         7: (0.4, 100000),
                         8: (0.3, 500000),
                         9: (0.2, 1000000),
                         10: (0.1, 5000000)}
        kbc_MDP = MDP(Questions, Prob_Rewards)
        V ,P = policyIteration(kbc MDP)
        print(P)
        print(V)
        {1: 'Stay', 2: 'Stay', 3: 'Stay', 4: 'Stay', 5: 'Stay', 6: 'Stay', 7: 'Stay', 8:
        'Quit', 9: 'Quit', 11: 'Stay'}
        {1: 26780.771381760005, 2: 29945.87136000001, 3: 36414.656, 4: 49464.799999999996,
        5: 72960.0, 6: 124000.0, 7: 220000.0, 8: 500000.0, 9: 1000000.0, 10: 0.0, 11: 0.0}
In [ ]: # Sate
        def generateSARS(kbc_MDP, pi, num_sequences=1, max_steps=100):
             sequences = []
             for i in range(num_sequences):
                 state = kbc MDP.InitState()
                 sequence = []
                 for t in range(max_steps):
                     if kbc_MDP.EndState(state):
                         break
```

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action = pi[state]
            next_states, probabilities, rewards = zip(*kbc_MDP.SuccProbReward(state)
            next_state = random.choices(next_states, probabilities)[0]
            reward = rewards[next_states.index(next_state)]
            sequence.append((state, action, reward, next state))
            state = next_state
        sequences.append(sequence)
    return sequences
sequences = generateSARS(kbc_MDP, P, num_sequences=10, max_steps=10)
for sequence in sequences:
    print(sequence)
    print("\n")
[(1, 'Stay', 100, 2), (2, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.
0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11,
'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 1000, 4), (4, 'Stay', 5000,
5), (5, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Sta
y', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.
0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11,
'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 0.0, 11), (11, 'Stay', 0.0,
11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'St
ay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 0.0, 11), (11, 'Stay', 0.0,
11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'St
ay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 1000, 4), (4, 'Stay', 5000,
5), (5, 'Stay', 10000, 6), (6, 'Stay', 50000, 7), (7, 'Stay', 100000, 8), (8, 'Qui
t', 500000, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 0.0, 11), (11, 'Stay', 0.0,
11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'St
ay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 1000, 4), (4, 'Stay', 0.0,
11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'St
ay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 1000, 4), (4, 'Stay', 5000,
5), (5, 'Stay', 10000, 6), (6, 'Stay', 50000, 7), (7, 'Stay', 100000, 8), (8, 'Qui
t', 500000, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
[(1, 'Stay', 100, 2), (2, 'Stay', 500, 3), (3, 'Stay', 0.0, 11), (11, 'Stay', 0.0,
11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'St
ay', 0.0, 11), (11, 'Stay', 0.0, 11), (11, 'Stay', 0.0, 11)]
```

```
# Monto Carlo Environment for the above problem
import random
class MontoCarlo(object):
    def __init__(self, Questions, Prob_Rewards):
        self.Questions = Questions
        self.Prob Rewards = Prob Rewards
    def play(self, policy):
        # initialize variables
        state = self.InitState()
        done = False
        rewards = []
        # play until the game is over
        while not done:
            # choose an action according to the given policy
            action = policy(state)
            # take the action and observe the next state and reward
            next_state, reward, done = self.SuccProbReward(state, action)[0]
            # store the reward
            rewards.append(reward)
            # update the current state
            state = next_state
        # compute the cumulative rewards for each time step
        cumulative_rewards = [sum(rewards[i:]) for i in range(len(rewards))]
        # create a list of (state, action, cumulative reward) tuples
        episodes = [(self.InitState(), None, 0)]
        for i in range(len(rewards)):
            episodes.append((i+1, policy(i+1), cumulative_rewards[i]))
        return episodes
    def InitState(self):
        return 1
    def EndState(self, state):
        return state == self.Questions + 1
    def Actions(self, state):
        if self.EndState(state):
            return []
        else:
            return ['Stay', 'Quit']
    def SuccProbReward(self, state, action):
        if action == 'Stay':
            if state > self.Questions:
                return [(state, 0, True)]
            else:
                prob, reward = self.Prob_Rewards[state]
                if random.random() <= prob:</pre>
                    return [(state+1, reward, False)]
                else:
                    return [(self.Questions+1, 0, True)]
        elif action == 'Quit':
            if state > self.Questions:
                return [(state, 0, True)]
                reward = self.Prob Rewards[state][1]
                return [(self.Questions+1, reward, True)]
    def discount(self):
        return 0.9
```

```
def states(self):
                                      return range(1, self.Questions+2)
                    # define a random policy
                    def random_policy(state):
                             actions = ['Stay', 'Quit']
                             return random.choice(actions)
                    # create a MontoCarlo environment
                    env = MontoCarlo(10, [(0.99, 100), (0.9, 500), (0.8, 1000), (0.7, 5000), (0.6, 10000)
                    # run a random policy for one episode
                    episode = env.play(random_policy)
                    # print the episode
                    print(episode)
                    [(1, None, 0), (1, 'Stay', 6500), (2, 'Quit', 6000), (3, 'Quit', 5000), (4, 'Qui
                   t', 0)]
In [ ]: import numpy as np
                    # Define the KBC game
                    Questions = 10
                    Prob_Rewards = [(0.99, 100), (0.9, 500), (0.8, 1000), (0.7, 5000), (0.6, 10000), (0.5, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.8, 10000), (0.
                    # # Create the transition matrix
                    num_states = Questions + 1
                    num_actions = 2
                    R = np.zeros(num_states).astype(int)
                    for s in range(num_states):
                             if s == num_states - 1:
                                      R[s] = 0 \# end of game
                             else:
                                      R[s] = Prob_Rewards[s][1]
                    # # Format the output of the transition matrix
                    P1 = np.array([[0.99, 0.01, 0, 0, 0, 0, 0, 0, 0, 0, 0],
                                                         [0, 0.9, 0.1, 0, 0, 0, 0, 0, 0, 0],
                                                         [0, 0, 0.8, 0.2, 0, 0, 0, 0, 0, 0, 0],
                                                         [0, 0, 0, 0.7, 0.3, 0, 0, 0, 0, 0, 0],
                                                         [0, 0, 0, 0, 0.6, 0.4, 0, 0, 0, 0]
                                                         [0, 0, 0, 0, 0, 0.5, 0.5, 0, 0, 0, 0],
                                                         [0, 0, 0, 0, 0, 0, 0.4, 0.6, 0, 0, 0],
                                                         [0, 0, 0, 0, 0, 0, 0, 0.3, 0.7, 0, 0],
                                                         [0, 0, 0, 0, 0, 0, 0, 0, 0.2, 0.8, 0],
                                                         [0, 0, 0, 0, 0, 0, 0, 0, 0, 0.1, 0.9],
                                                           [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1]])
                    print("Transition matrix : \n")
                    for i in range(num_states):
                             for j in range(num_states):
                                      print(P1[i][j], end = "
                             print("\n")
                    print("Rewards Vector : \n")
                    print(R)
                    # Set up the discount factor
                    gamma = 0.9
```

```
# Solve the system of linear equations
A = np.eye(num_states) - gamma * P1
b = R
V = np.linalg.inv(A).dot(b) # value function
# Print the value function vector
print("\n Value function : \n")
print(V)
Transition matrix :
0.99
      0.01 0.0
                  0.0
                        0.0
                                     0.0
                                          0.0
                                                0.0
                                                     0.0
                                                            0.0
                               0.0
0.0
     0.9
           0.1
                 0.0
                       0.0
                             0.0
                                   0.0
                                         0.0
                                               0.0
                                                    0.0
                                                          0.0
0.0
     0.0
           0.8
                 0.2
                       0.0
                             0.0
                                   0.0
                                         0.0
                                               0.0
                                                          0.0
                                                    0.0
0.0
     0.0
           0.0
                 0.7
                       0.3
                             0.0
                                   0.0
                                         0.0
                                               0.0
                                                     0.0
                                                          0.0
0.0
     0.0
           0.0
                 0.0
                       0.6
                             0.4
                                   0.0
                                         0.0
                                               0.0
                                                     0.0
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0.0
     0.0
           0.0
                       0.0
                             0.5
                                   0.5
                 0.0
                                         0.0
                                               0.0
                                                    0.0
                                                          0.0
0.0
     0.0
           0.0
                 0.0
                       0.0
                             0.0
                                   0.4
                                         0.6
                                               0.0
                                                    0.0
                                                          0.0
0.0
     0.0
           0.0
                 0.0
                       0.0
                             0.0
                                   0.0
                                         0.3
                                               0.7
                                                    0.0
                                                          0.0
0.0
     0.0
           0.0
                 0.0
                       0.0
                             0.0
                                   0.0
                                         0.0
                                               0.2
                                                    0.8
                                                          0.0
0.0
     0.0
           0.0
                 0.0
                       0.0
                             0.0
                                   0.0
                                         0.0
                                               0.0
                                                    0.1
                                                          0.9
0.0
     0.0
           0.0
                 0.0
                       0.0
                             0.0
                                   0.0
                                         0.0
                                               0.0
                                                    0.0
                                                          1.0
Rewards Vector:
            500
                   1000
                           5000
                                  10000
                                          50000 100000 500000 1000000
    100
 5000000
             0]
Value function :
[ 63648.10943705 759738.21429313 1598336.23017438 2480745.24693792
 3381021.26432234 4292416.05996743 5135175.18440464 5900948.36670179
```

6043956.04395604 5494505.49450549 0. ]

In [ ]: