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Deterministic Finite Automata

(Part 1)

Lecture 06
Day 06/31

CS 154
Formal Languages and Computability
Spring 2019

Agenda of Day 06

- Announcement
- Solution and Feedback of Quiz 1
- Summary of Lecture 05
- Lecture 06: Teaching ...
 - Deterministic Finite Automata (Part 1)

Announcement

- Please check your name **spelling** in the **rollcall form** and correct it if it is misspelled.
- **Rollcall** does NOT have any impact on your score.
- I use it for **recommendation, choosing graders, outstanding graduating senior awards, scholarships, and so on.**
- Canvas is supposed to send you a notification for assignments, announcements, etc..
- Sometimes, for some unknown reasons, it doesn't!
- So, that's why **it is your responsibility to check Canvas at least once per day.**

Solution and Feedback of Quiz 1 (Out of 20)

Section	Average	High Score	Low Score
01 (TR 3:00 PM)	13.73	19.5	5
02 (TR 4:30 PM)	13.05	18	6.5
03 (TR 6:00 PM)	14.11	19	6.5

Summary of Lecture 05: We learned ...

Operations on Languages

- Regular set operations

union, intersection, minus

- Complement of L

$$\bar{L} = U - L = \Sigma^* - L$$

- Reverse of L

$$L^R = \{w : w^R \in L\}$$

- Concatenation of L_1 and L_2

$$L_1 L_2 = \{xy : x \in L_1, y \in L_2\}$$

$$\phi L = L \phi = \phi$$

$$\{\lambda\} L = L \{\lambda\} = L$$

- Exponential Operator

$$L^n = L L \dots L \quad (n \text{ times concatenation})$$

$$L L^n = L^n L = L^{n+1}$$

$$L^0 = \{\lambda\}$$

- Some surprising languages were introduced.

- Conclusion:

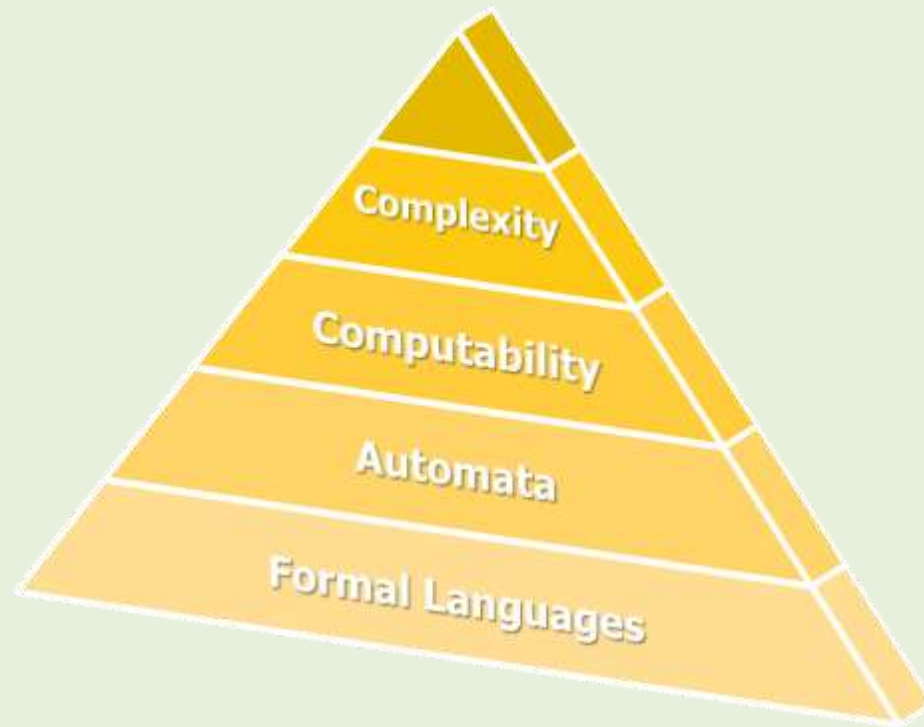
All data in CS are strings.

Any question?

! The Big Picture of the Course

Recap

- We finished the "first round" of Formal Languages!
 - We'll get back to it several times later.
- Let's start "Automata"!



Automata

Objective of Automata Lectures

- In the previous lectures, we defined formal languages.
 - That are the mathematical model of all type of languages.
- From this lecture onward, we start constructing machines.
- These machines are supposed to "understand" formal languages.

Automata

- These machines are called "automata" (plural of automaton).
 - This is a scientific name for computation machines.
- In fact, they are mathematical models of computing devices.

Definition



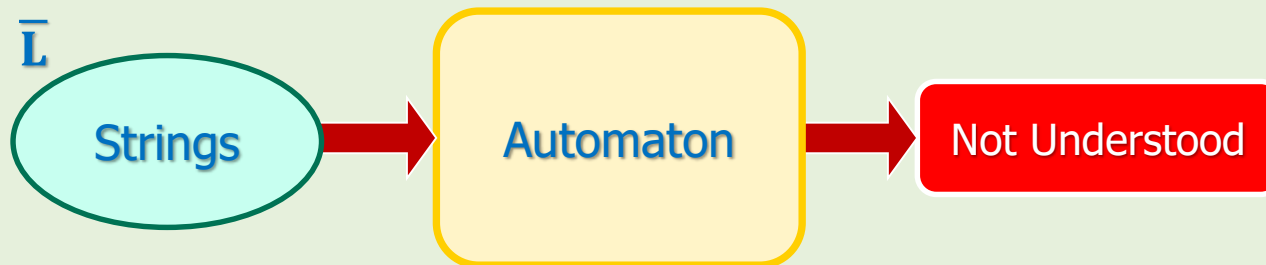
- Automaton is a mathematical model of a computing device.
- In this course, we'll define several "classes of automata".
- Each class has different "power".
 - The definition of "power" will come later.
- In fact, we'll witness the evolution of languages and automata.

Automata: How They Operate on Strings of L and \bar{L}

- When we feed them the strings of language L , they understand (aka **Accept**).



- But when we feed them the strings of \bar{L} , they do not understand (aka **Reject**).



Automata

- We start with the simplest class of automata called:
Deterministic Finite Automata (DFA)
- To introduce a new class of machines, we'll use the next slide template.

Template for Introducing a New Class of Automata

- To construct a new class of automata, we need to deal with the following items:
 1. Why do we need a new class of machines? (Justification)
 2. Name of the new class
 3. Building blocks of the new class
 4. How they work
 - 4.1. What is the starting configuration?
 - 4.2. What would happen during a timeframe?
 - 4.3. When would the machines halts?
 - 4.4. How would a string be Accepted/Rejected?
- 5. The automata in action
- 6. Formal definition
- 7. Their power: this class versus previous class
- 8. What would be the next possible class?

Deterministic Finite Automata

1. Why do we need a new class of machines?

- This is the first class and really we don't need to justify it!
- In fact, the main goal of introducing this class of machines was mentioned in the objective of these lectures:
"These machines are supposed to understand formal languages."

2. Name of the new class

- We name this class of automata as:

Deterministic Finite Automata (DFA)

Where is this name coming from?

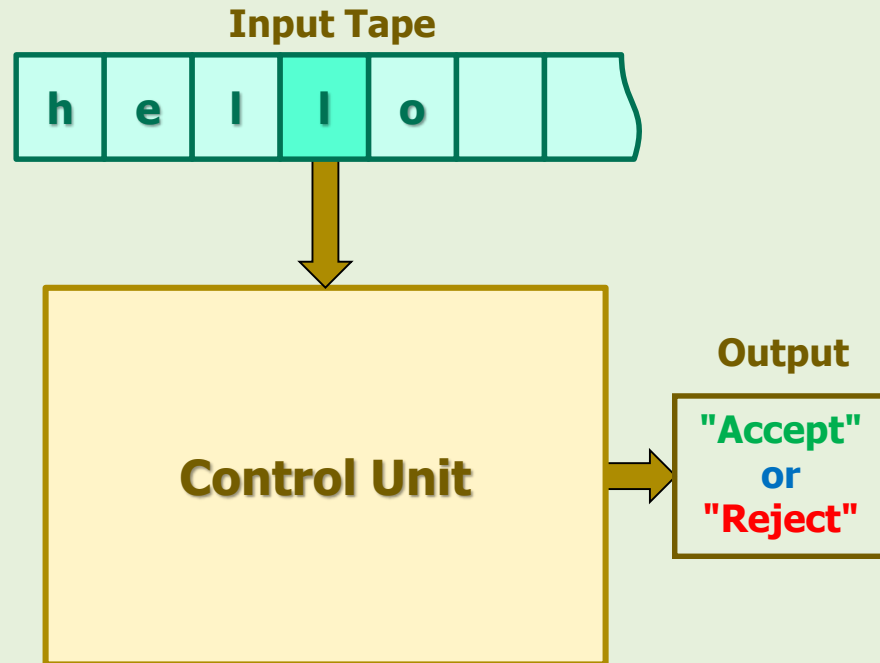
- We have already know that "automata" means machines.
- Also we know the meaning of "finite" but we don't know what part of the machine is finite?
- Also we don't know the meaning of "deterministic".
- Both of these will be explained later.

3. DFAs Building Blocks

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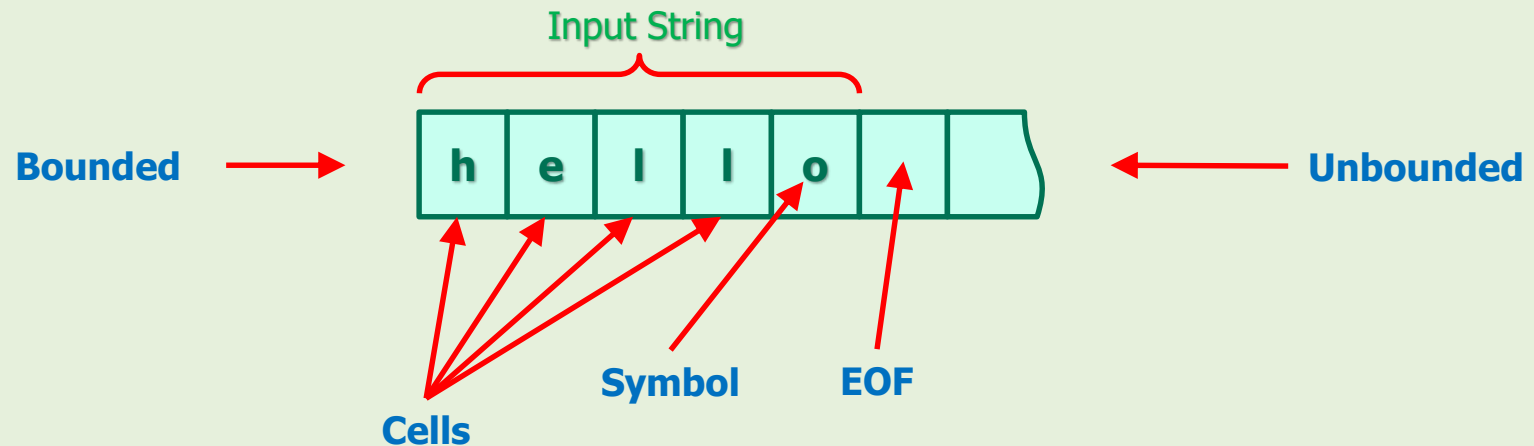
- A DFA has 3 main blocks:

1. Input Tape
2. Control unit
3. Output



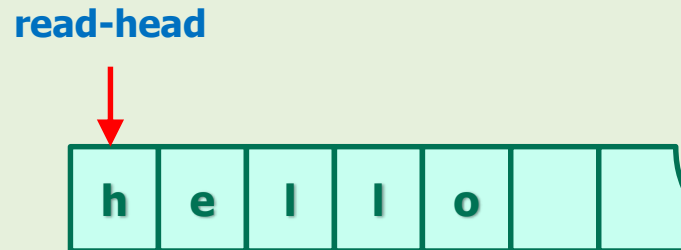
- Let's see each block in detail.

3.1. Input Tape: Structure



- The tape is "unbounded" from the right side and bounded from the left.
- It is divided into "cells".
- Each cell can hold one "symbol".
- The input data is a string written on the tape from the left-most cell.
- We show the end of a string as a blank cell and we call it EOF (stands for "End Of File").

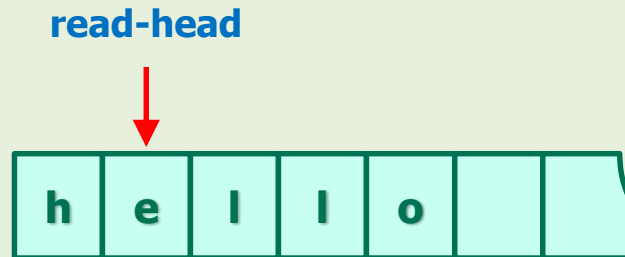
3.1. Input Tape: How It Works



- The tape has a "read-head".
- It can read one symbol at a time.
- The read-head reads the symbol at which it is pointing and sends it to the control unit.
- Then, the control unit commands the head to move one cell to the right.
- We call these two operations as "consuming of the symbol".
- Consuming = reading + moving the read-head to the right



3.1. Input Tape: Notes

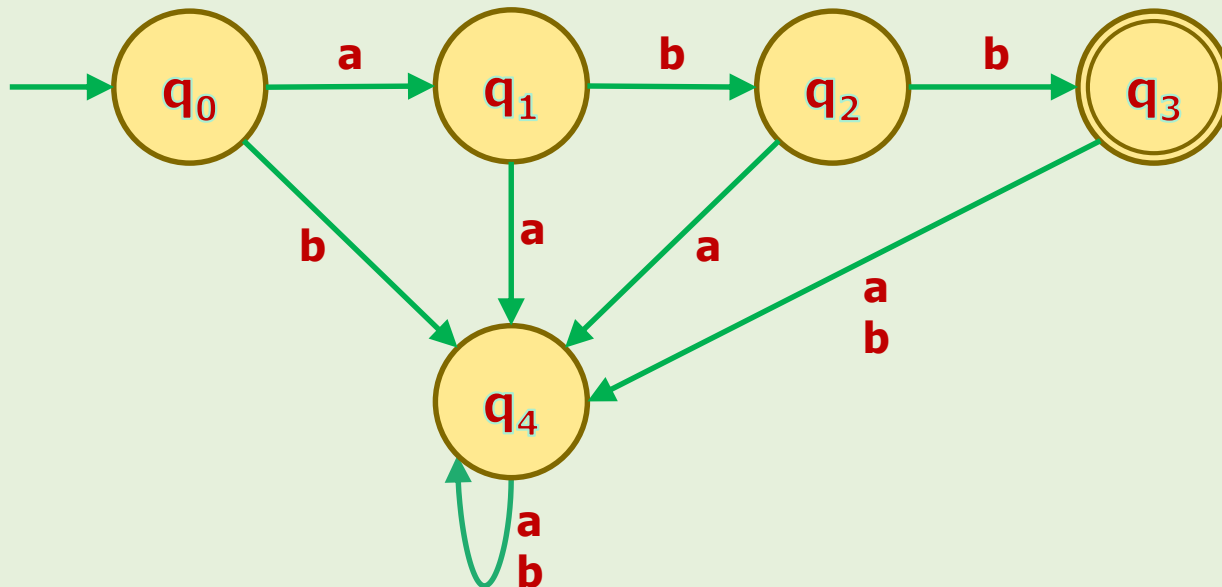


1. We use the words **reading**, and **scanning** interchangeably.
2. DFAs can "**read**" the input string but **cannot change** it.
(**Read-Only Tape**)
3. The head only moves from **left to right**.
 - So, during the machine's operations, when the head moves one symbol to the right, there is no way to move it back. (**Irreversible Operation**)
4. The input mechanism can **detect** the **end of the input string** (EOF).
 - For example, in the above illustration, when the machine **consumes 'o'**, it **knows** that it is the **last symbol** of the string!

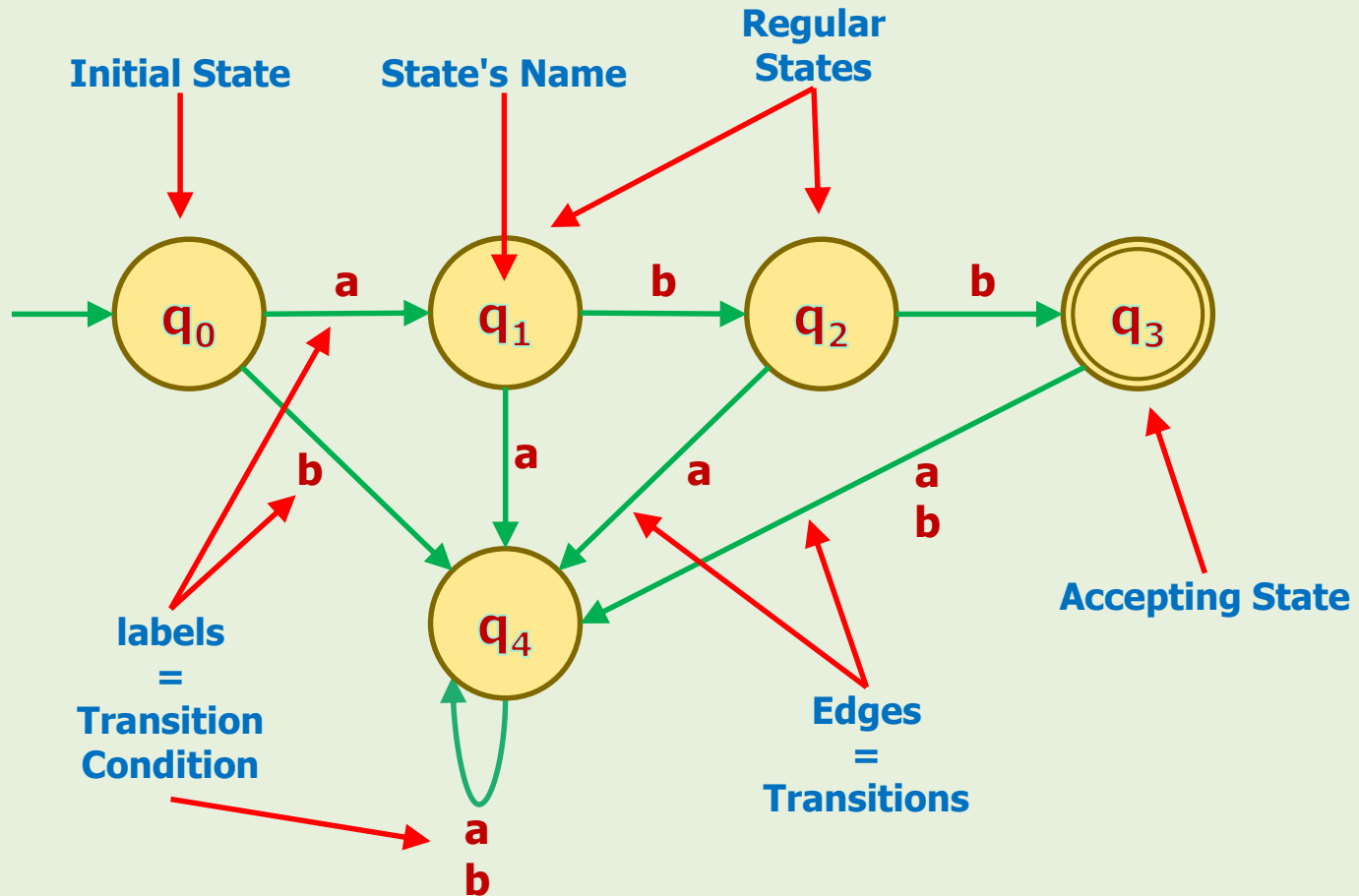
3.2. Control Unit: Structure

- The control unit is the brain (CPU) of DFAs.
- We represent its decision making part by a graph called "transition graph".
- The following example shows an instance of a transition graph.

Example 1



3.2. Control Unit: Transition Graph Ingredients

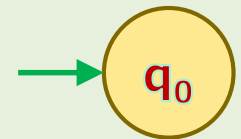


3.2. Control Unit: Transition Graph Ingredients

- A **vertex** of the graph represents a "state of the DFA".
 - The label q_1 is the **name of the state**.



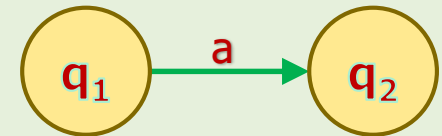
- The "**initial state**" is identified by an incoming **unlabeled** arrow, not originated from any vertex.
 - We **usually** name it q_0 **but** it can be named anything else.



- ⓘ – The machine is **restricted** to have **one and only one** initial state.

3.2. Control Unit: Transition Graph Ingredients

- An **edge** between two vertices represents a "transition".
- The **label** on an edge is the "transition condition".
(will be covered later.)



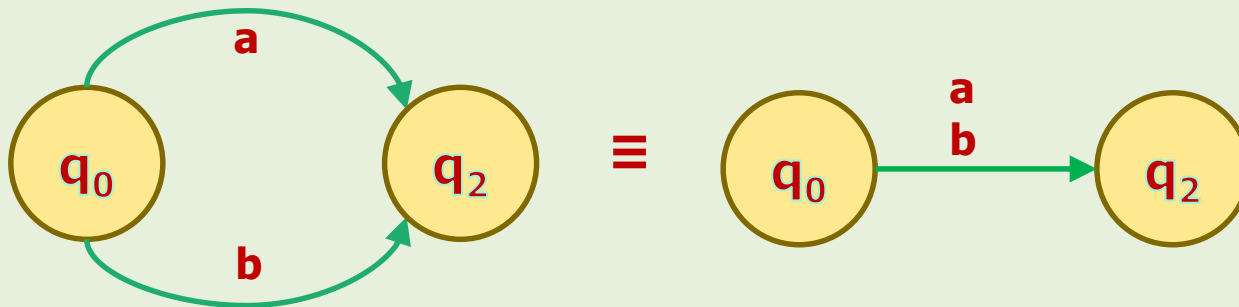
- An "accepting state" (aka "final state") is shown by **double circle**.



- ❗ – Transition graph can have **zero or more** final states.

3.2. Control Unit: Notes

1. We use the following shorthand to simplify the graph.



- Note that $\begin{smallmatrix} a \\ b \end{smallmatrix}$ means "a or b".
- In some books, you might see " a, b " that is confusing.
- Because comma usually means "AND".

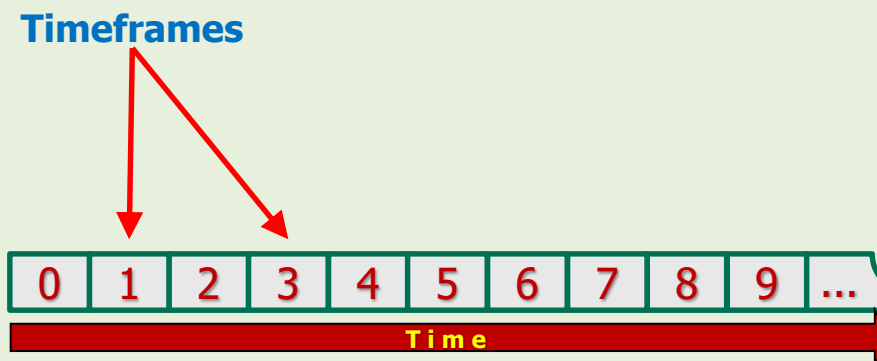


2. DFAs have finite number of states.

- That's where the "finite" in "deterministic finite Automata" comes from.

3.2. Control Unit: Synchronization of Operations

- For **synchronization** of operations, the **control unit** has a **clock** that produces **discrete signals** (ticks).
- We call each signal a "**timeframe**" (aka **timestep**).
 - The **frequency** of the clock **does not matter** in this course.
- In my lecture notes, I use the following figure to show a **clock** and its **timeframes**.



3.3. Output

Output

Accept
or
Reject

- Output of DFAs have two messages:

- ❗ – Accept (aka: understood, recognized, Yes)
- ❗ – Reject (aka: not understood, not recognized, No)

- If the machine understands the input string, the output will be "Accept".
- If the machine does not understand the input string, the output will be "Reject".

References

1. Linz, Peter, "An Introduction to Formal Languages and Automata, 5th ed.," Jones & Bartlett Learning, LLC, Canada, 2012
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3. Michael Sipser, "Introduction to the Theory of Computation, 3rd ed.," CENGAGE Learning, United States, 2013
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