

AHSANULLAH UNIVERSITY OF SCIENCE AND TECHNOLOGY

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

LAB REPORT

COURSE NO : EEE 2226

COURSE NAME : Numerical Technique Laboratory

EXPERIMENT NO : 07

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Submitted by:

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Section : D(2)

Exercise1.

Integrate the function tabulated in Table 7.1 over the interval from x=1.6 to x=3.8 using composite trapezoidal rule with (a) h=0.2, (b) h=0.4 and (c) h=0.6

Table 7.1

X	f(x)	X	f(x)
1.6	4.953	2.8	16.445
1.8	6.050	3.0	20.086
2.0	7.389	3.2	24.533
2.2	9.025	3.4	29.964
2.4	11.023	3.6	36.598
2.6	13.468	3.8	44.701

Exercise 2.

- (a) Integrate the function tabulated in Table 7.1 over the interval from x=1.6 to x=3.6 using Simpson's composite 1/3 rule.
- (b) Integrate the function tabulated in Table 7.1 over the interval from x=1.6 to x=3.4 using Simpson's composite 3/8 rule.

Exercise 3.

(a) Find (approximately) each integral given below using the composite trapezoidal rule with n = 12.

(i)
$$\int_{-1}^{1} (1+x^2)^{-1} dx$$

(ii)
$$\int_{0}^{4} x^{2}e^{-x}dx$$

(b) Find (approximately) each integral given above using the Simpson's composite 1/3 and 3/8 rules with n = 12.

Exercise 4.

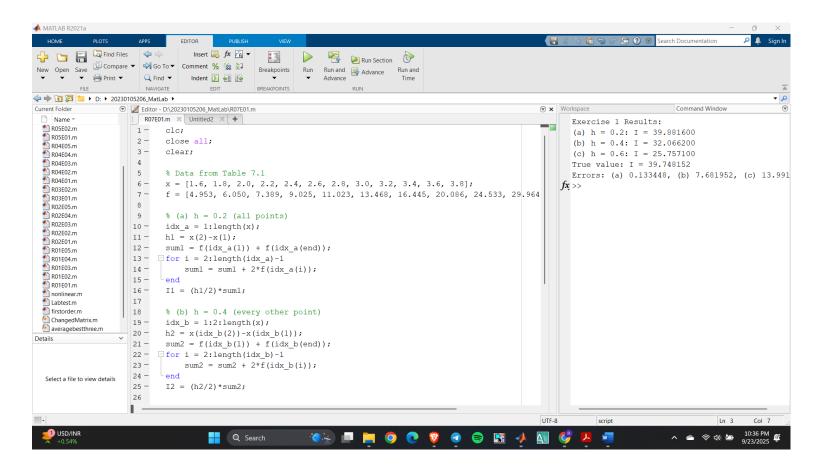
Evaluate the integral of xe^{-2x^2} between x=0 and x=2 using a tolerance value sufficiently small as to get an answer within 0.1% of the true answer, 0.249916 (Use adaptive integration for both Ex 4 & 5).

Exercise 5.

Evaluate the integral of $\sin^2(16x)$ between x = 0 and $x = \pi/2$. Why the result is erroneous? How can this be solved? (The correct result is $\pi/4$)

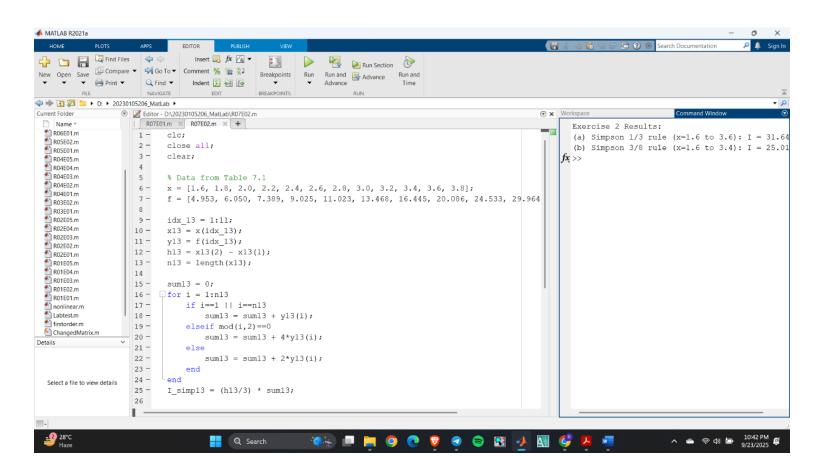
The data in Table 7.1 are for $f(x) = e^x$. Find the true value of the integral and compare this with those found in (a), (b) and (c).

Excercise01:



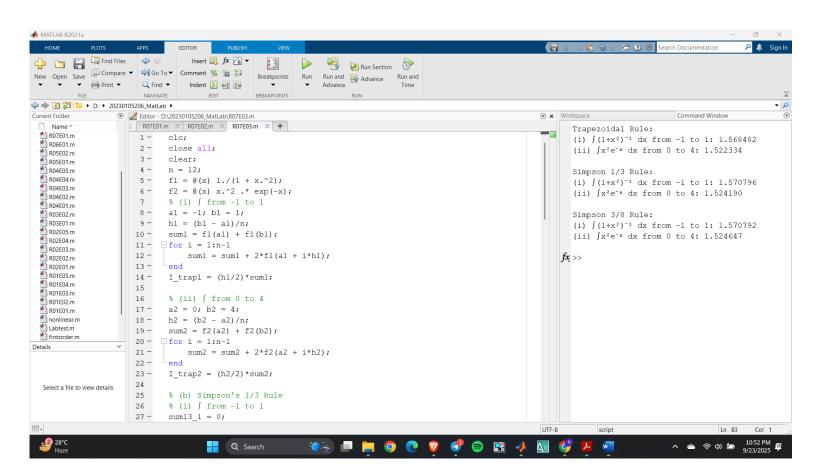
```
26
27
       % (c) h = 0.6 (every third point)
28 -
       idx c = 1:3:length(x);
29 -
       h3 = x(idx c(2)) - x(idx c(1));
       sum3 = f(idx c(1)) + f(idx c(end));
30 -
     \Box for i = 2:length(idx c)-1
32 -
           sum3 = sum3 + 2*f(idx c(i));
33 -
      -end
34 -
       I3 = (h3/2) * sum3;
35
       % True value (f(x) = e^x)
36
37 -
       true val = \exp(3.8) - \exp(1.6);
38
39 -
       fprintf('Exercise 1 Results:\n');
40 -
       fprintf('(a) h = 0.2: I = %.6f \ ', I1);
       fprintf('(b) h = 0.4: I = %.6f \ , I2);
41 -
       fprintf('(c) h = 0.6: I = %.6f \ , I3);
42 -
43 -
       fprintf('True value: I = %.6f\n', true val);
44 -
       fprintf('Errors: (a) %.6f, (b) %.6f, (c) %.6f\n', ...
45
                abs(I1-true val), abs(I2-true val), abs(I3-true val));
46
```

Excercise02:



```
26
       idx_38 = 1:10;
27 -
       x38 = x(idx_38);
28 -
29 -
       y38 = f(idx_38);
30 -
       h38 = x38(2) - x38(1);
       n38 = length(x38);
31 -
32
33 -
       sum38 = y38(1) + y38(end);
34 -
     \Box for i = 2:n38-1
35 -
           if \mod (i-1,3) == 0
                sum38 = sum38 + 2*y38(i);
36 -
37 -
           else
38 -
                sum38 = sum38 + 3*y38(i);
39 -
           end
40 -
       I simp38 = (3*h38/8) * sum38;
41 -
42
43 -
       fprintf('Exercise 2 Results:\n');
44 -
       fprintf('(a) Simpson 1/3 rule (x=1.6 to 3.6): I = %.6f\n', I_simp13);
45 -
       fprintf('(b) Simpson 3/8 rule (x=1.6 to 3.4): I = %.6f n', I simp38);
```

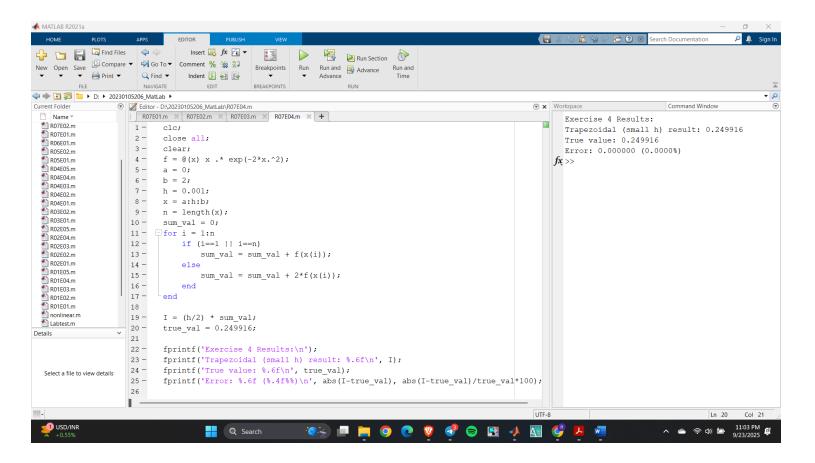
Exercise 03:



```
25
       % (b) Simpson's 1/3 Rule
26
      % (i) \int from −1 to 1
27 -
      sum13_1 = 0;
28 -
       x1 = a1:h1:b1;
29 -
       fx1 = f1(x1);
30 -
       m1 = length(x1);
31 - \bigcirc \text{for i} = 1:m1
32 -
           if i==1 || i==m1
33 -
               sum13_1 = sum13_1 + fx1(i);
34 -
           elseif mod(i, 2) == 0
35 -
               sum13_1 = sum13_1 + 4*fx1(i);
36 -
           else
37 -
                sum13_1 = sum13_1 + 2*fx1(i);
38 -
           end
39 -
      end
40 -
       I_simp1_13 = (h1/3)*sum13_1;
41
42
       % (ii) ∫ from 0 to 4
43 -
       sum13 2 = 0;
44 -
       x2 = a2:h2:b2;
45 -
       fx2 = f2(x2);
46 -
     m2 = length(x2);
47 - \Box \text{ for i} = 1:m2
48 -
           if i==1 || i==m2
49 -
               sum13_2 = sum13_2 + fx2(i);
50 -
          elseif mod(i,2) == 0
```

```
50 -
            elseif mod(i, 2) == 0
51 -
                sum13_2 = sum13_2 + 4*fx2(i);
52 -
53 -
                sum13 2 = sum13 2 + 2*fx2(i);
54 -
            end
55 -
      L end
        I simp2 13 = (h2/3)*sum13 2;
56 -
57
       % (c) Simpson's 3/8 Rule
58
       % (i) ∫ from -1 to 1
59
       sum38 1 = f1(a1) + f1(b1);
60 -
61 -
     \neg for i = 1:n-1
62 -
            xi = a1 + i*h1;
63 -
           if mod(i,3) == 0
64 -
                sum38 1 = sum38 1 + 2*f1(xi);
65 -
            else
66 -
                sum38 1 = sum38 1 + 3*f1(xi);
67 -
            end
68 -
      end
69 -
       I simpl 38 = (3*h1/8)*sum38 1;
70
71
       % (ii) ∫ from 0 to 4
72 -
        sum38 2 = f2(a2) + f2(b2);
73 - \bigcirc \text{for i} = 1:n-1
74 -
           xi = a2 + i*h2;
75 -
            if mod(i,3) == 0
                sum38 2 = sum38 2 + 2*f2(xi);
76 -
76 -
                sum38_2 = sum38_2 + 2*f2(xi);
77 -
78 -
                sum38 2 = sum38 2 + 3*f2(xi);
79 -
            end
80 -
       I_{simp2_38} = (3*h2/8)*sum38_2;
81 -
82
       %Results
83
84 -
       fprintf('Trapezoidal Rule:\n');
85 -
       fprintf('(i) \int (1+x^2)^{-1} dx from -1 to 1: %.6f\n', I trap1);
86 -
       fprintf('(ii) \int x^2 e^{-x} dx from 0 to 4: %.6f\n\n', I trap2);
87
88 -
       fprintf('Simpson 1/3 Rule:\n');
89 -
       fprintf('(i) \int (1+x^2)^{-1} dx from -1 to 1: %.6f\n', I simpl 13);
       fprintf('(ii) \int x^2 e^{-x} dx from 0 to 4: %.6f\n\n', I simp2 13);
90 -
91
       fprintf('Simpson 3/8 Rule:\n');
92 -
       fprintf('(i) \int (1+x^2)^{-1} dx from -1 to 1: %.6f\n', I simpl 38);
93 -
94 -
       fprintf('(ii) \int x^2 e^{-x} dx from 0 to 4: %.6f\n\n', I simp2 38);
```

Exercise 04:



Exercise 05:

