

Estructuras de datos

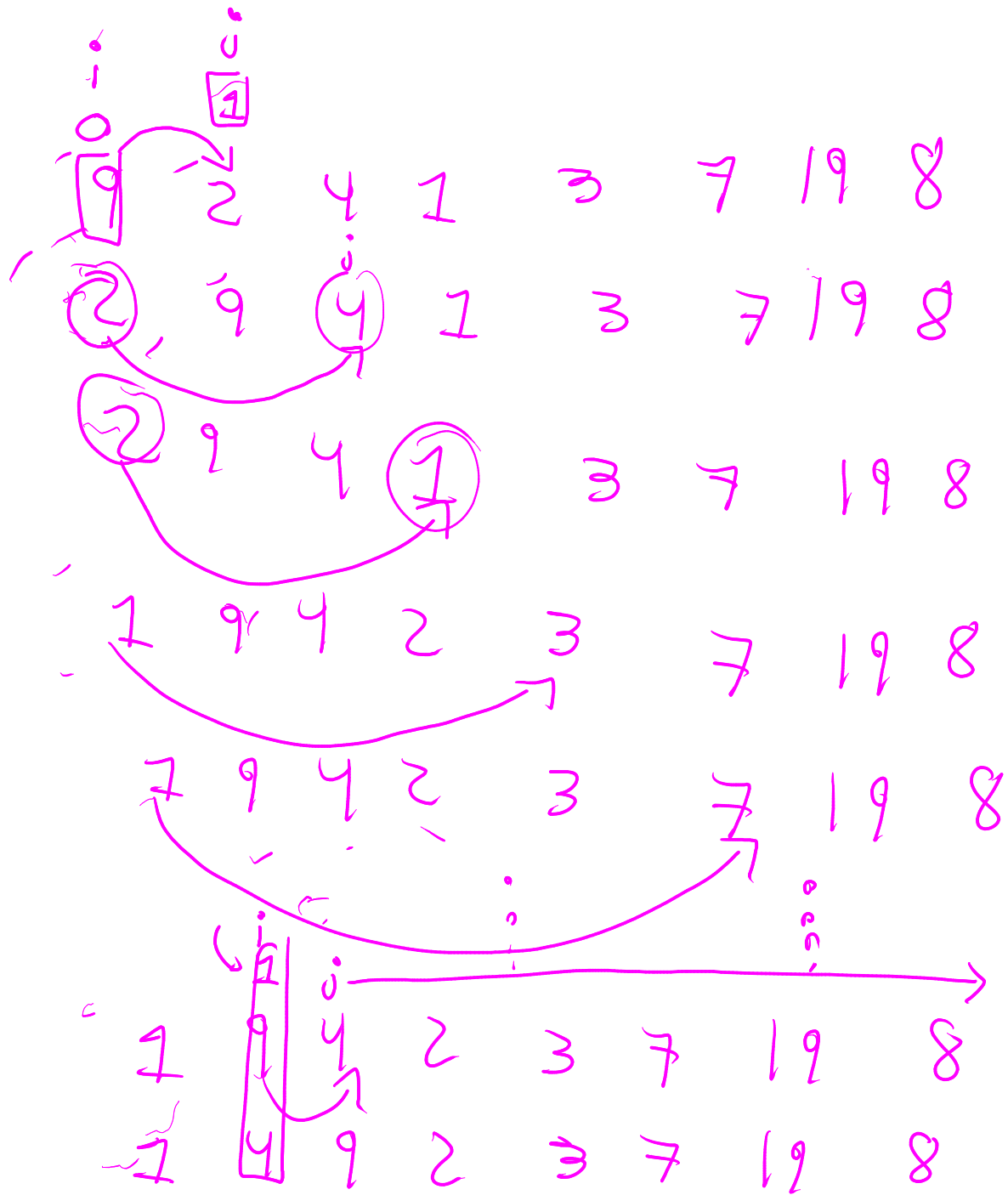
Algoritmos insertionSort

1 4 2 3 7 8 0

0 1 2 3 4 7 8

In place = In situ >> ^{modifican} la estructura

No son in place = No retornan uno nuevo



Algoritmos de Ordenamiento

Analicemos un ejemplo (Algoritmo de ordenamiento insertion-sort)

Instrucción	Costo	Veces que se repite
1 for $j \leftarrow 2$ to $\text{length}[A]$		
2 do $\text{key} \leftarrow A[j]$		
3 $i \leftarrow j-1$		
4 while $i > 0$ and $A[i] > \text{key}$		
5 do $A[i+1] \leftarrow A[i]$		
6 $i \leftarrow i-1$		
7 $A[i+1] \leftarrow \text{key}$		

¡Sin temor!, vamos a explorar este algoritmo.

Windows (CMD, power shell)

Instalado el Python con la opción de PATH

```
py -m pip install matplotlib
```

```
py -m pip install numpy
```

Linux

Debian/Ubuntu

```
sudo apt-get install python3
```

```
sudo apt-get install python3-pip
```

```
sudo pip3 install matplotlib
```

```
sudo pip3 install numpy
```

MAC

```
brew install python3
```


Algoritmos de Ordenamiento

Este algoritmo recibe un arreglo de tamaño n y retorna el mismo arreglo ordenado de menor a mayor.

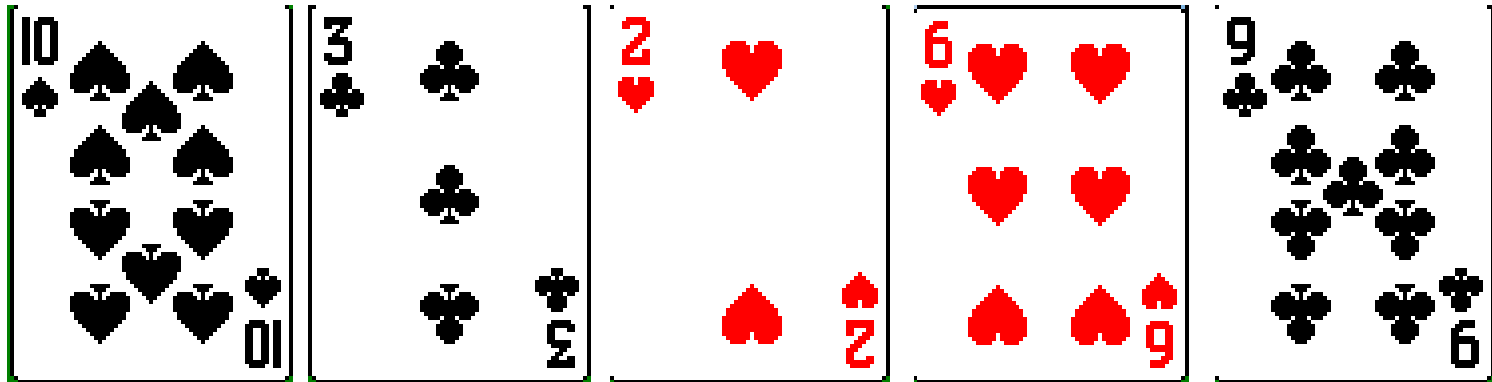
Ejemplo

Entrada = {10,3,2,6,9}

Salida = {2,3,6,9,10}

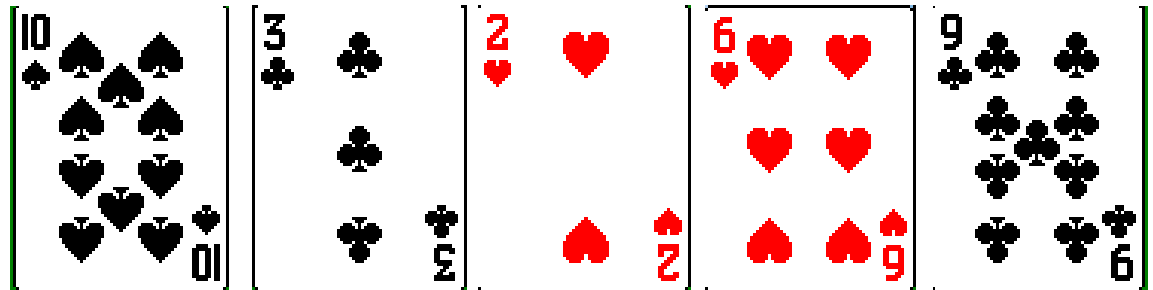
Algoritmos de Ordenamiento

Insertion sort



Algoritmos de Ordenamiento

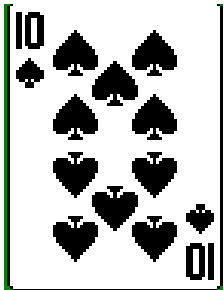
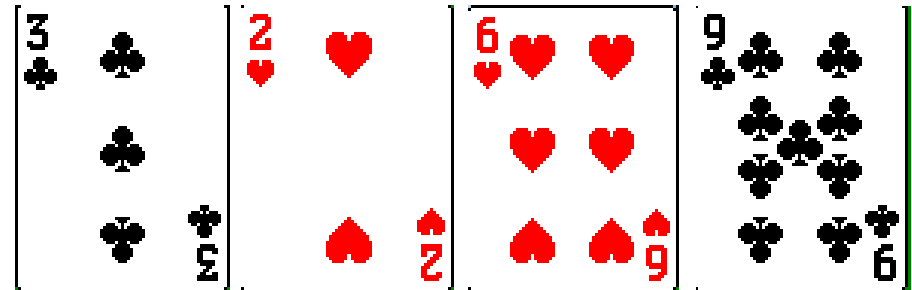
Insertion sort



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Algoritmos de Ordenamiento

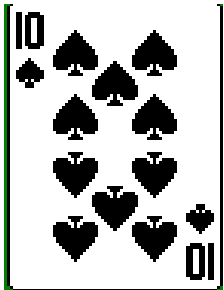
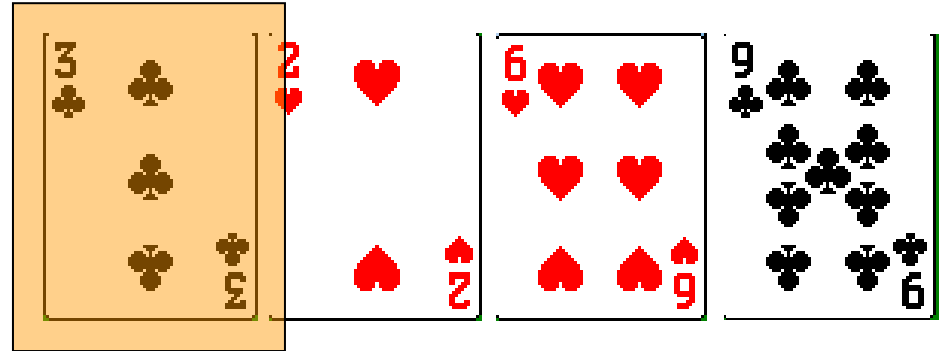
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Algoritmos de Ordenamiento

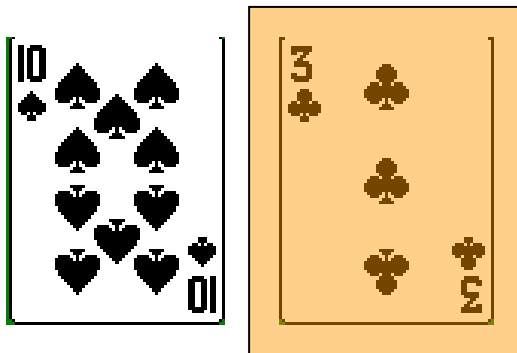
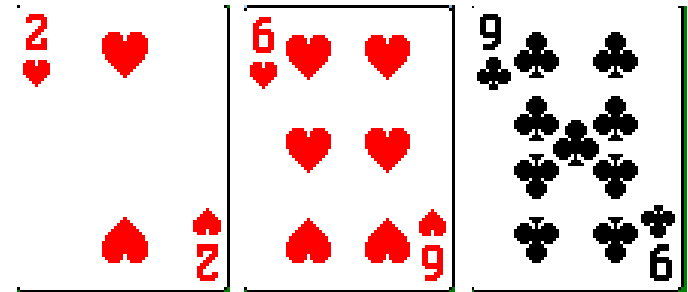
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Algoritmos de Ordenamiento

Insertion sort

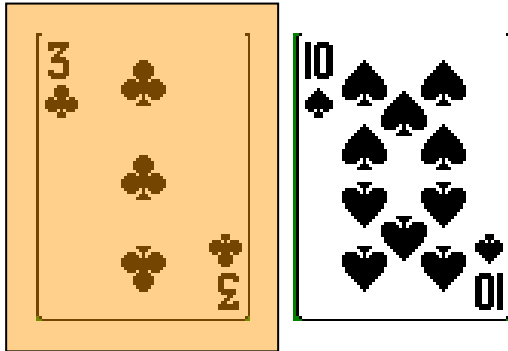
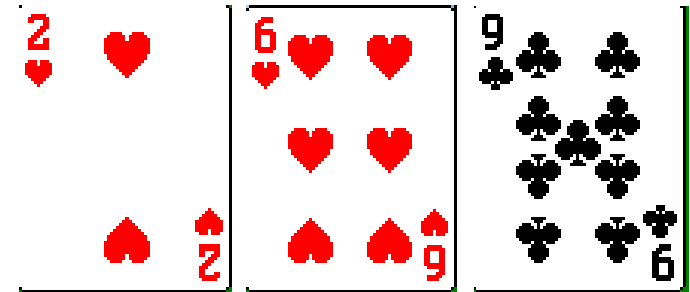


Se recorre de derecha a izquierda buscando el lugar que debe ocupar

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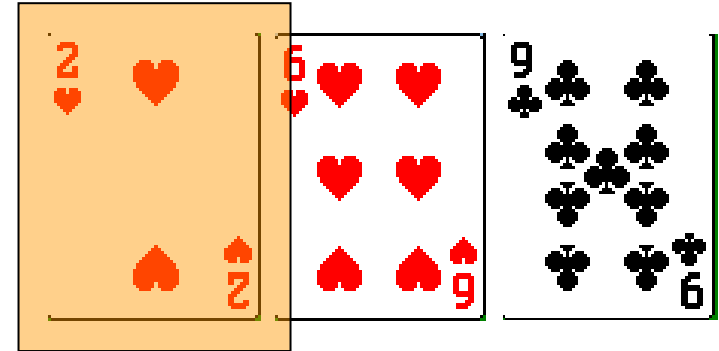
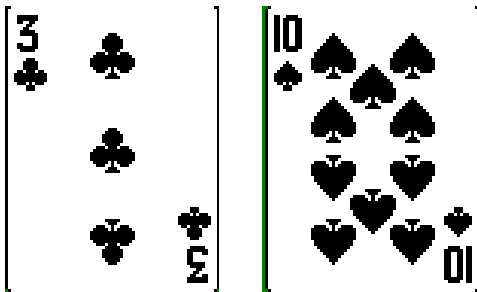
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Algoritmos en la computación

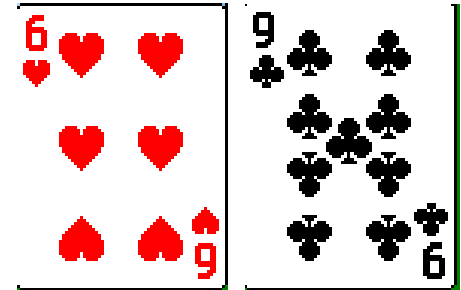
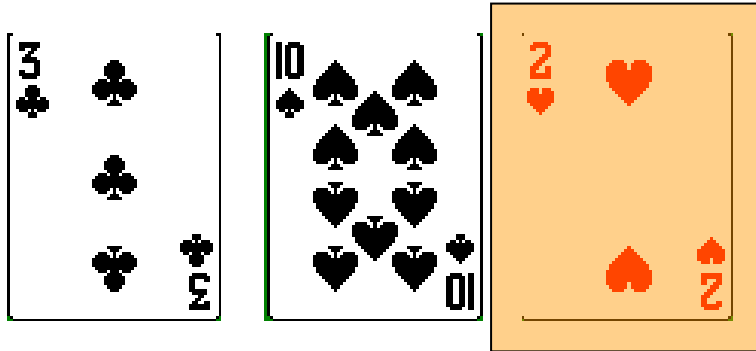
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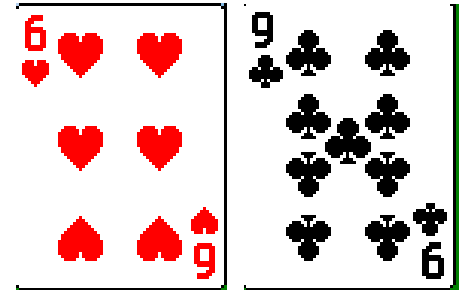
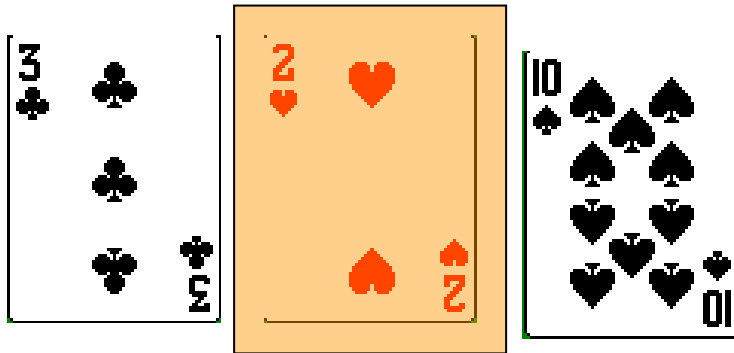
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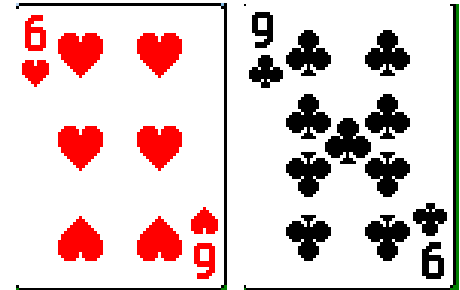
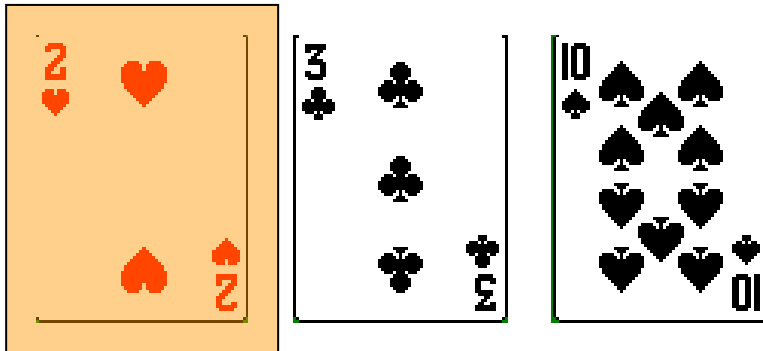
Algoritmos en la computación

Insertion sort



Algoritmos en la computación

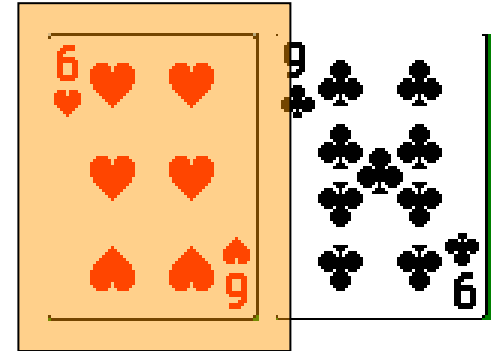
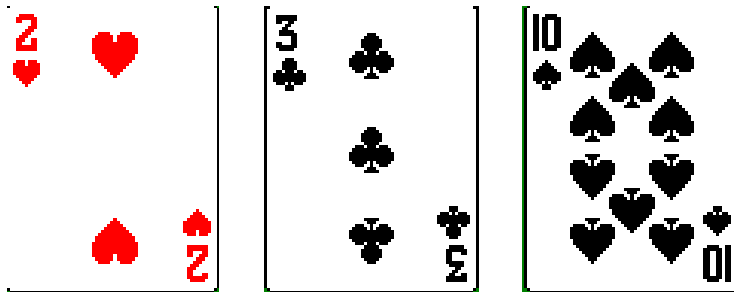
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Algoritmos de Ordenamiento

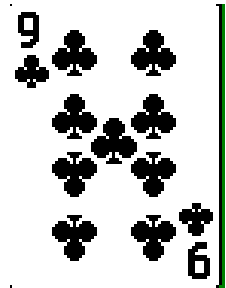
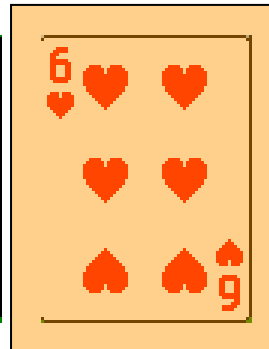
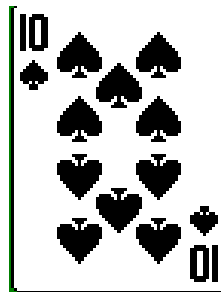
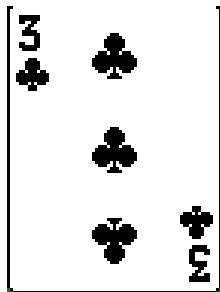
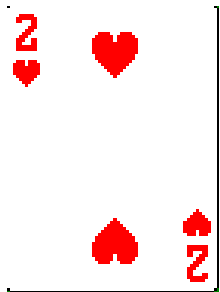
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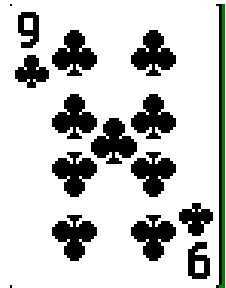
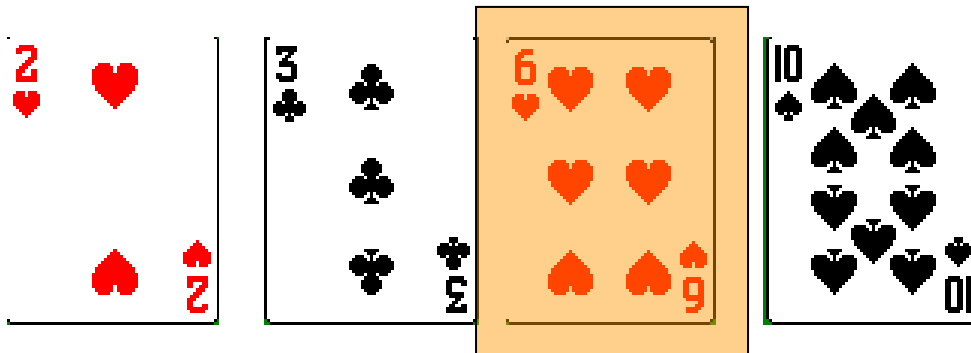
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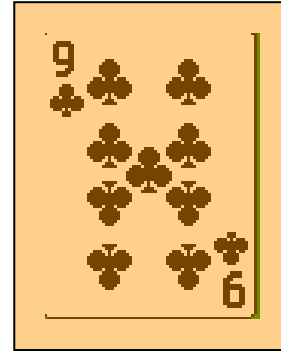
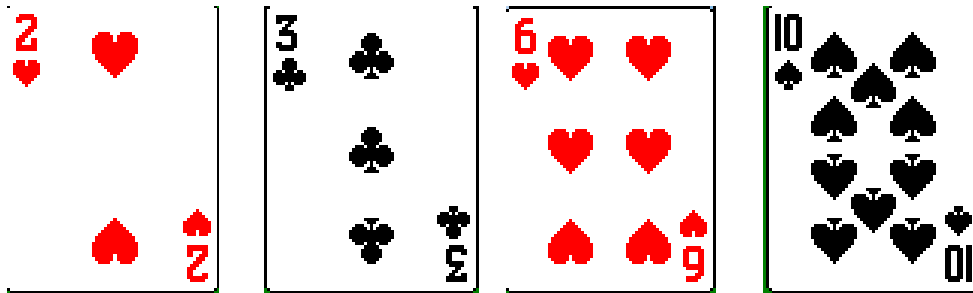
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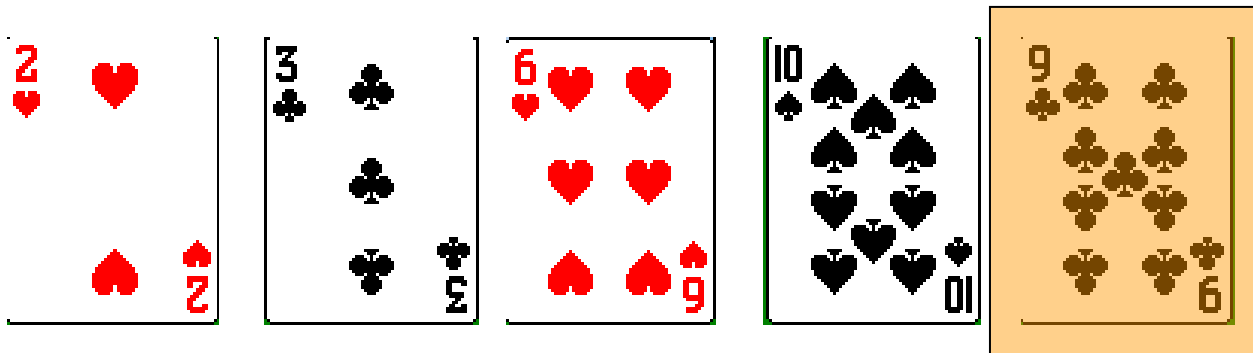
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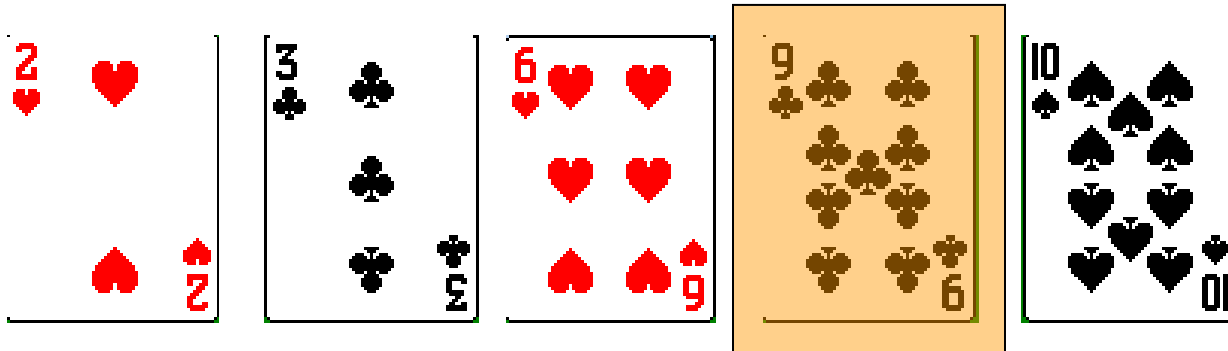
Algoritmos de Ordenamiento

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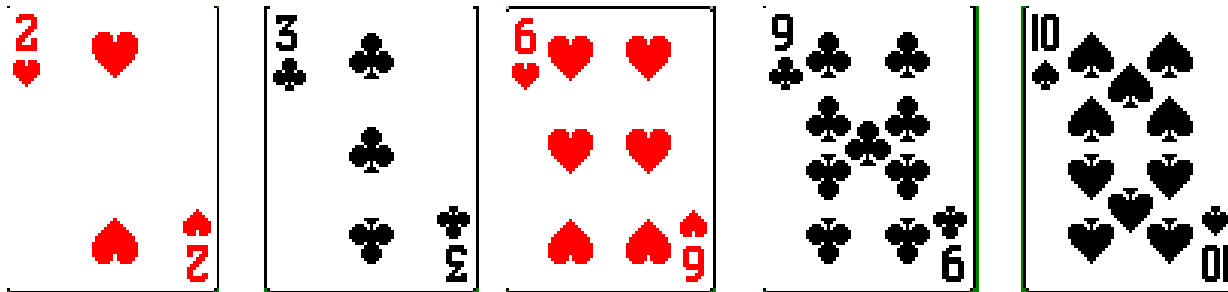
Algoritmos de Ordenamiento

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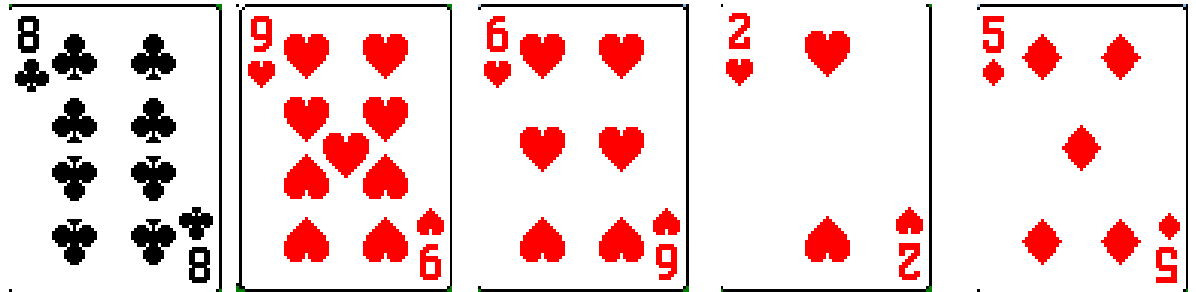
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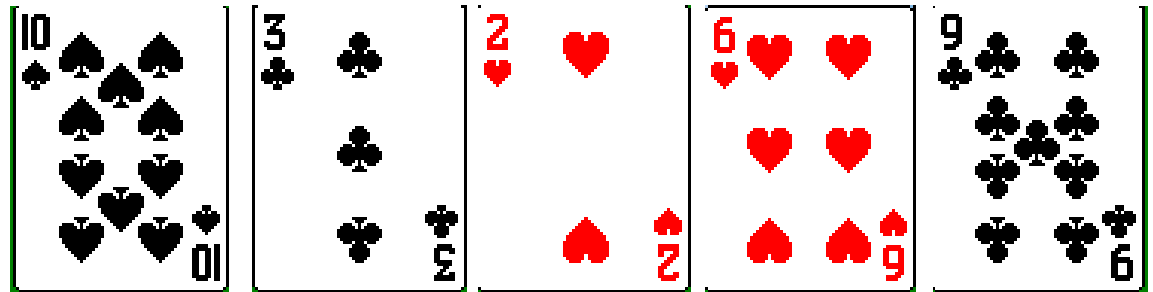
Algoritmos de Ordenamiento

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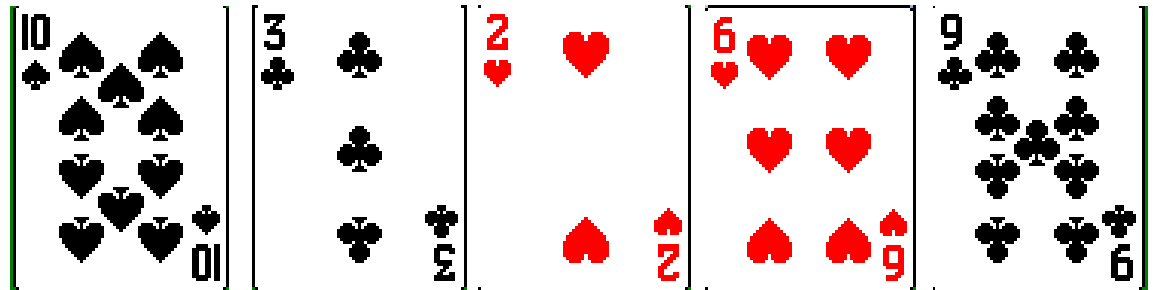
A:

10	3	2	6	9
----	---	---	---	---

Algoritmos de Ordenamiento

Insertion sort

Desarrolle el algoritmo
INSERTION-SORT(A)



A:

10	3	2	6	9
----	---	---	---	---

10 3 2 6 9
↑
ordered

3 10 2 6 9

2 3 10 6 9

ordered

2 3 6 10 9

2 3 6 9 10

1 4 7 10 3 5 0 3
Valor

1) $3 < 10$

1 4 7 10 10 5 0 3

2) $3 < 7$

1 4 7 7 10 5 0 3

3) $3 < 4$

1 4 4 7 10 5 0 3

4) $3 < 1$ ~~X~~ $j = 5$
Rompr

1	3	4	7	10
---	---	---	---	----

 S 0 3

Ejercicio

5 1 8 7 6 2 3

$j=1$ logico

1 5 8 7 6 2 3

$j=2$

1 5 8 7 6 2 3

$j=3$

1 5 7 8 6 2 3

$j=4$

1 5 6 7 8 2 3

$j=5$

1 2 5 6 7 8 3

$j=6$

1 2 3 5 6 7 8

✓

7 9 3 1 4 2 6 8 $j=1$

7 9 3 1 4 2 6 8 $j=2$

3 7 9 1 4 2 6 8 $j=3$

1 3 7 9 4 2 6 8 $j=4$

1 3 4 7 9 2 6 8 $j=5$

1 2 3 4 7 9 6 8 $j=6$

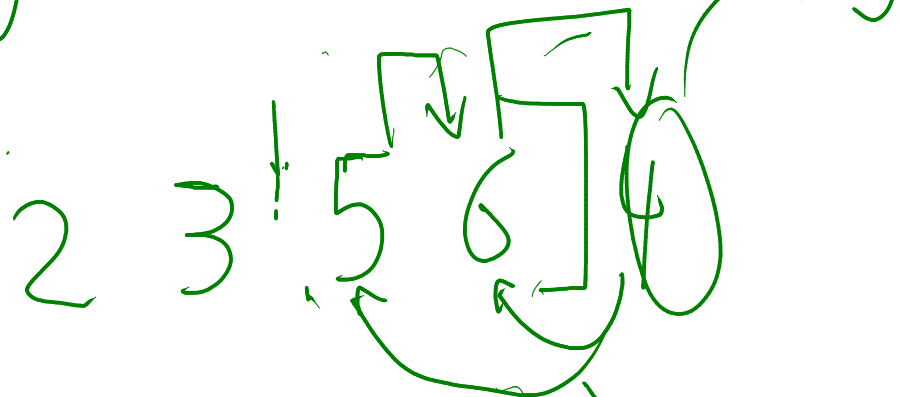
1 2 3 4 6 7 9 8 $j=7$

1 2 3 4 6 7 8 9

3 7 4 2



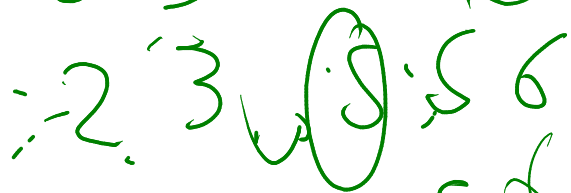
2 3 5 6 7 4



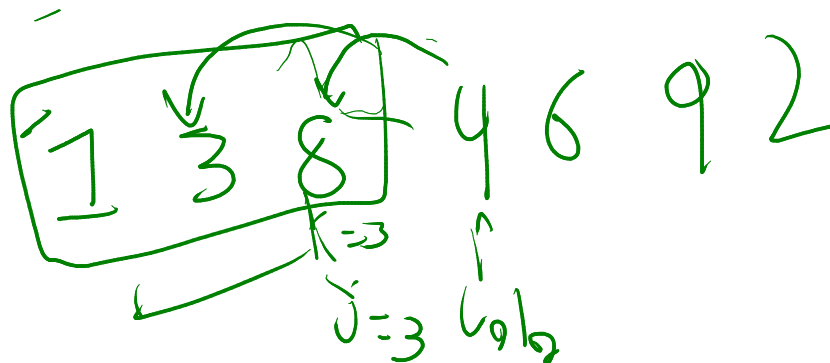
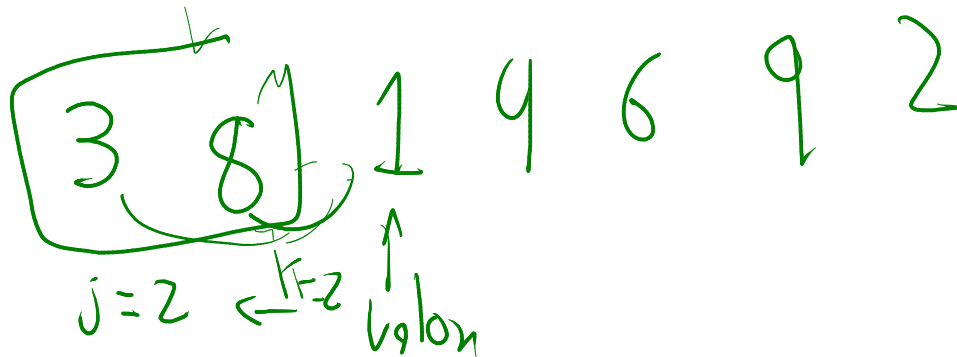
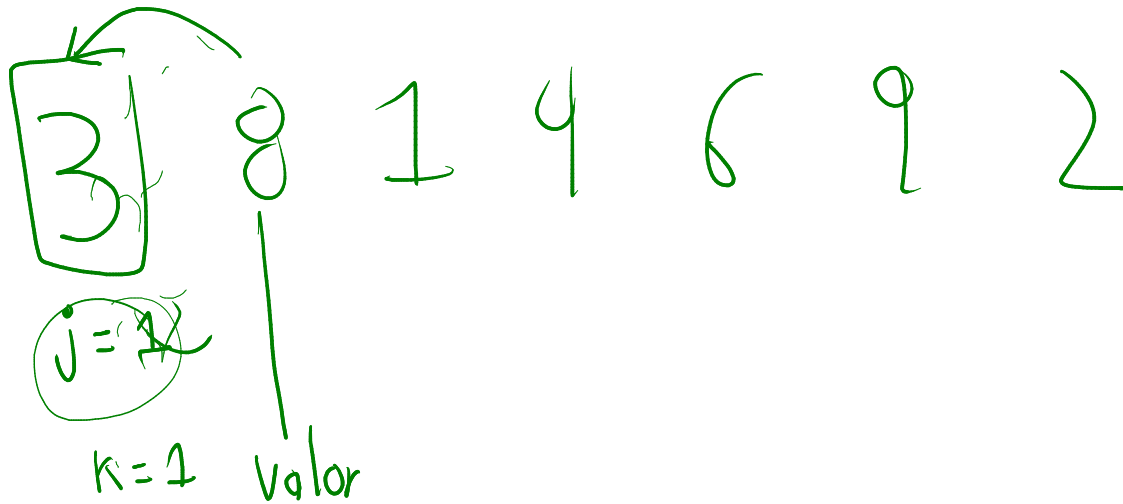
2 3 5 6 7 4



2 3 4 5 6 7



2 3 4 5 6 7



Algoritmos de Ordenamiento

Selection sort

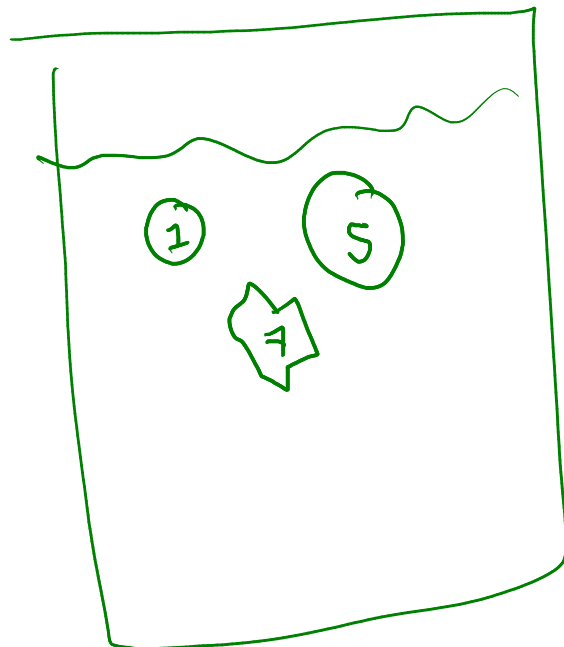
- Considere un arreglo $A[1..n]$
- Encuentre el menor elemento, colóquelo en la posición 1, ahora considere el arreglo $A[2..n]$
- Encuentre el menor elemento de $A[2..n]$, colóquelo en la posición 2.
- Repita el proceso hasta llegar al a posición n

Algoritmos de Ordenamiento

Selection sort

Lista ordenada	Sub lista no ordenada	Menor elemento
()	(11, 25, 12, 22, 64)	11
(11)	(25, 12, 22, 64)	12
(11, 12)	(25, 22, 64)	22
(11, 12, 22)	(25, 64)	25
(11, 12, 22, 25)	(64)	64
(11, 12, 22, 25, 64)	()	

Burbuja



7 2 6 1 8 3 0

2 7 6 1 8 3

2 6 7 1 8 3

2 6 1 7 8 3

2 6 1 7 3 8

2 6 1 7 3 8

2 1 6 7 3 8

2 1 6 3 7 8

↓

1 2 6 3 7 8

1 2 3 6 7 8

5 8 9 3 1 4 $j=1$

1 8 9 3 5 4 $j=2$

1 3 9 8 5 4 $j=3$

1 3 4 8 5 9 $j=4$

1 3 4 5 8 9 $j=5$

$j=6$

$j=7$

Referencias

Thomas H. Cormen, Charles E. Leiserson, Ronald L. Rivest, and Clifford Stein. 2009. Introduction to Algorithms, Third Edition (3rd ed.). The MIT Press. Pages 5-29