

```

let g = proc (int x, int y, bool z, bool w)
  if < (x, y) then and(z, w)
  else w
  { f = proc (int * int * bool * bool → bool h,
    int → bool p, int m, int n, bool o)
    if (p m) then false
    else (h n m (p n) (p * (2, m)))
  }
  { q = proc (int a)
    > (a, 4)
  }
  i = false
in
  (f g q 1 5 i)

```

$(p\ m)$
 $t_p = t_m \rightarrow \text{bool}$
 $t_o = \text{int} \rightarrow \text{bool}$

$t_m = \text{int}$

$(h\ n\ m\ (p\ n)\ (p * (2, m)))$

$(p\ n)\ t_n = \text{int}$

$(p * (2, m))$
 \uparrow
 int

$(f\ g\ q\ 1\ 5\ i)$

$t_f = t_g * t_q * \text{int} * \text{int} * \text{bool}$

$t_f = (\text{int} * \text{int} * \text{bool} * \text{bool} \rightarrow \text{bool}) * (\text{int} \rightarrow \text{bool}) * \text{int} * \text{int} * \text{bool} \rightarrow \text{bool}$

$t_g = (\text{int} * \text{int} * \text{bool} * \text{bool} \rightarrow \text{bool})$

$t_g = (\text{int} * \text{int} * \text{bool} * \text{bool} \rightarrow \text{bool})$
 $< (x, y)$

$t_x * t_y \rightarrow \text{bool}$

$\text{int} * \text{int} \rightarrow \text{bool}$

$t_x = \text{int}$

$t_y = \text{int}$

$\text{and}(z, w)$

$t_z * t_w \rightarrow \text{bool}$

$\text{bool} * \text{bool} \rightarrow \text{bool}$

$t_g = \text{int} \rightarrow \text{bool}$

$t_g \rightarrow \text{int} \rightarrow \text{bool}$

$t_g = \text{int}$

(b) [26 pts.] El tipo de la expresión

```

let g = proc (x, y, z, t, w)
  if (z y t) then (x true t)
  else (x false w)
  f = proc (j, k)
    if j then *(k, k) else k
  a = 2
in
  let fun1 = proc (l, m)
    if >(l, m) then true
    else false
  in
    let v2 = (g f 3 fun1 4 * (2, a))
    in
      (fun1 v2 (f true a))

```

Exp		V _{tp}
g	*	t _g
x	bool × int → int	t _x
y	int	t _y
z	int × int → bool	t _z
t	int	t _t
w	int	t _w
f	bool × int → int	t _f
j	bool	t _j
k	int	t _k
a	int	t _a
fun1	int × int → bool	t _{fun1}
m	int	t _m
v2	int	t _{v2}

in (fun1 v2 (f true a))
 (z y t) bool t₁
 (x true t) int t₂
 (x false w) int t₃
 *(k, k) int t₄
 >(l, m) bool t₅
 *(2, a) int t₆
 (g f 3 fun1 4 *(2, a)) int t₇
 (f true a) int t₈

$t_g = (\text{bool} \times \text{int} \rightarrow \text{int}) * \text{int} * (\text{int} \times \text{int} \rightarrow \text{bool}) * \text{int} \times \text{int} \rightarrow \text{int}$

$$v_2 = (g \ f \ 3 \ fun_1 \ 4 \ * \ (2, a))$$

$$v_2 = t_7$$

$$t_g = t_f * int * t_{fun_1} * int * t_6 \rightarrow t_7$$

$g = \text{proc } (x, y, z, t, w)$
 $\text{if } (z \ y \ t) \text{ then } (x \ \text{true} \ t)$
 $\text{else } (x \ \text{false} \ w) \} t_3$

$$t_g = t_x * t_y \vee t_z * t_t * t_w \rightarrow t_2$$

$$t_g = t_x * t_y \vee t_z * t_t * t_w \rightarrow t_3$$

$$t_g = (bool * int \rightarrow int) * int * (int * int \rightarrow bool) * int * int$$

$$(z \ y \ t)$$

$$t_z = t_y * t_t \rightarrow bool$$

$$t_z = int * int \rightarrow bool$$

$$(x \ \text{true} \ t)$$

$$t_x = bool * t_t \rightarrow t_2$$

$$t_x = bool * int \rightarrow t_2$$

$$(x \ \text{false} \ w) \} t_3$$

$$t_x = bool * t_w \rightarrow t_3$$

$$Q = 3$$

$$t_a = int$$

$$\begin{cases} t_x = t_f \\ t_y = int \\ t_z = t_{fun_1} \\ t_t = int \\ int = t_w = t_6 \\ t_2 = t_3 \end{cases}$$

$$t_7 = t_2 = t_3$$

$$t_x = bool * int \rightarrow int$$

$$t_2 = int$$

$$t_3 = int$$

$$t_7 = int$$

$$t_w = int$$

$$t_{v_2} = int$$

(f true a)

$$t_F = \text{bool} \times t_a \rightarrow t_8$$

$$t_F = \text{bool} \times \text{int} \rightarrow t_8$$

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f = proc (j, k)

if j then *(k, k) else k

$$t_F = t_j \times t_k \rightarrow t_k \quad (k \neq z)$$

$$t_F = t_j \times t_k \rightarrow t_4$$

*(k, k)

$$t_k \times t_k \rightarrow t_4$$

$$\text{int} \times \text{int} \rightarrow \text{int}$$

$$t_j = \text{bool}$$

$$t_k = \text{int}$$

$$t_k = t_4 = \text{int}$$

$$t_F = \text{bool} \times \text{int} \rightarrow \text{int}$$

$$t_4 = t_8$$

$$t_8 = \text{int}$$

(fun₁ v₂ (f true a))

$$t_{F_{v_2}} = t_{v_2} \times t_8 \rightarrow t_p$$

$$t_{F_{v_2}} = t_{v_2} \times \text{int} \rightarrow t_p$$

$$t_{F_{v_2}} = \text{int} \times \text{int} \rightarrow t_p^*$$

fun₁ = proc (l, m)

if >(l, m) then true
else false

$$t_{F_{v_2}} = t_l \times t_m \rightarrow \text{bool}$$

$$t_{F_{v_2}} = \text{int} \times \text{int} \rightarrow t_p$$

$$t_p = \text{bool}$$

$$t_l = \text{int}$$

$$t_m = \text{int}$$

>(l, m)

$$t_l \times t_m \rightarrow \text{bool}$$

$$\text{int} \times \text{int} \rightarrow \text{bool}$$

$$t_l \times t_m \rightarrow t_5$$