

$$q_0 = A_0$$

$$q_1 = A_1$$

$$q_2 = A_2$$

$$A_0 = a A_1 \cup b A_2$$

$$A_1 = a A_1 \cup (b A_2 \cup \epsilon)$$

$$A_2 = b A_2 \cup a A_1$$

$$aa^* = a^+$$

$$a(a^0 \cup a^1 \cup a^2 \cup \dots)$$

$$(a^1 \cup a^2 \cup a^3 \cup \dots)$$

$$X = aX \cup b$$

$$X = a^*b$$

$$A_1 \rightarrow A_2 \rightarrow A_0$$

$$A_1 = a^*(b A_2 \cup \epsilon)$$

$$\rightarrow A_1 = a^*b A_2 \cup a^*$$

$$A_2 = b A_2 \cup a^+ b A_2 \cup a^+$$

$$A_2 = (b \cup a^+ b) A_2 \cup a^+$$

$$A_2 = (b \cup a^+ b)^* a^+$$

$$A_0 = a A_1 \cup b A_2$$

$$A_0 = a(a^*b A_2 \cup a^*) \cup b(b \cup a^+ b)^* a^+$$

$$A_0 = a(a^*b(b \cup a^+ b)^* a^+ \cup a^*) \cup b(b \cup a^+ b)^* a^+$$

$$A_2 \rightarrow A_1 \rightarrow A_0$$

$$A_2 = b A_2 \cup a A_1$$

$$\bullet A_2 = b^* a A_1$$

$$A_1 = a A_1 \cup b A_2 \cup \epsilon$$

$$A_1 = a^*(b A_2 \cup \epsilon)$$

$$A_1 = a^*b A_2 \cup a^*$$

$$A_1 = a b b^* a \cup a^*$$

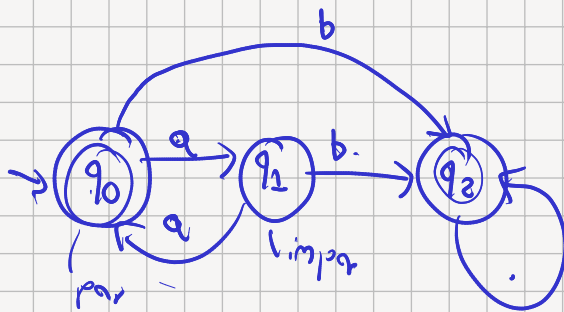
$$\bullet A_1 = a b^+ a \cup a^*$$

$$A_0 = a A_1 \cup b A_2$$

$$A_0 = a(a b^+ a \cup a^*) \cup$$

$$b^* a(a b^+ a \cup a^*)$$

$$b^* a^2 b^+ a \cup b^* a^+$$



$$A_0 = \underline{a A_1} \cup b A_2 \cup \epsilon$$

$$A_1 = \underline{b A_2} \cup a A_0$$

$$A_2 = b A_2 \cup \epsilon$$

$$A_2 = b^* \epsilon = b^*$$

$$A_1 = \underline{b b^* \epsilon} \cup a A_0$$

$$A_1 = b^+ \cup a A_0$$

↓

$$(a^2)^* = \{\epsilon, aa, aaaa, aaaaaa, \dots\}$$

$$(aa)^* = \{(aa)^0 \cup (aa)^1 \cup (aa)^2 \cup \dots\}$$

$$X = \underline{a} X \cup b$$

$$A_0 = \underbrace{a^2 A_0}_{a} \cup \underbrace{(a b^+ \cup b^+ \cup \epsilon)}_b$$

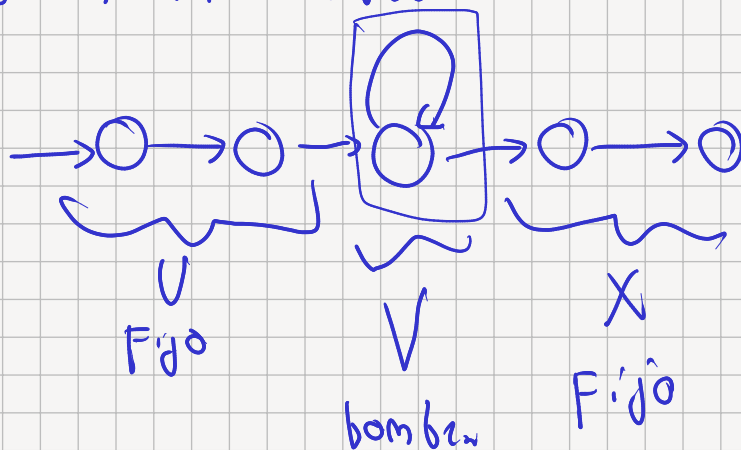
$$A_0 = a(b^+ \cup a A_0) \cup b^+ \cup \epsilon$$

$$\Rightarrow A_0 = \underbrace{a b^+}_{\downarrow} \cup \underbrace{a^2 A_0}_{\downarrow} \cup \underbrace{b^+ \cup \epsilon}_{\downarrow}$$

$$A_0 = (a^2)^* (a b^+ \cup b^+ \cup \epsilon)$$

$$A_0 = (a^2)^* \underbrace{a b^+}_{\downarrow} \cup (a^2)^* b^+ \cup (a^2)^* \underbrace{\epsilon}_{\uparrow}$$

Teorema del bombeo



$$L_1 \rightarrow \begin{matrix} x \in L_1 \\ \textcircled{x_n \in L_1} \\ \uparrow \\ \geq n \end{matrix}$$

$$P(n) \rightarrow P(n+1)$$

Inductiva

$$ab^na \geq \underline{\text{long } n}$$

$$n \text{ es } \underline{\text{long}}$$

$$\underbrace{ab^n}_U \underbrace{b^i}_V \underbrace{a}_X$$

$$i=3$$

$$ab^n b^3 a = ab^{n+3} a \in L$$

$$\left\{ \underbrace{ab^n}_U \underbrace{b^i}_V \underbrace{a}_X \right\} \geq n$$

bomba

$$\textcircled{\underbrace{\epsilon}_U \underbrace{\epsilon^i}_V \underbrace{ab^na}_X}$$

$$\underbrace{a}_U \underbrace{b^n b^i}_V \underbrace{a}_X$$

$$i=4$$

$$a^n b^n \quad n \geq 0$$

$$a^n \underbrace{e^i}_{i=1} b^n \quad n \rightarrow \infty$$

$$\in [a^i a^n] b^n \quad n \rightarrow \infty$$

$$i=4$$

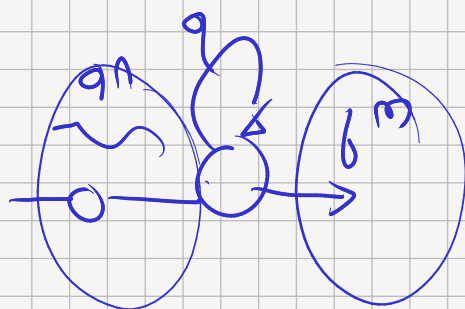
$$\in a^4 a^n b^n$$

$$a^{n+4} b^n \in L? \quad \times \quad n+4 \neq n \quad \times$$

$$a^n b^m \quad n, m \geq 0$$

$$\underbrace{a^n}_{\cup} \underbrace{a^i}_{\cap} \underbrace{b^m}_{\times} \quad i=4$$

$$a^{n+4} b^m \in L?$$



$$S \rightarrow \underset{\substack{\uparrow \\ \text{terminal}}}{a} S \mid \underset{\substack{\uparrow \\ \text{terminal}}}{\epsilon}$$

$$\{\epsilon, a, aa, aaa, \dots\}$$

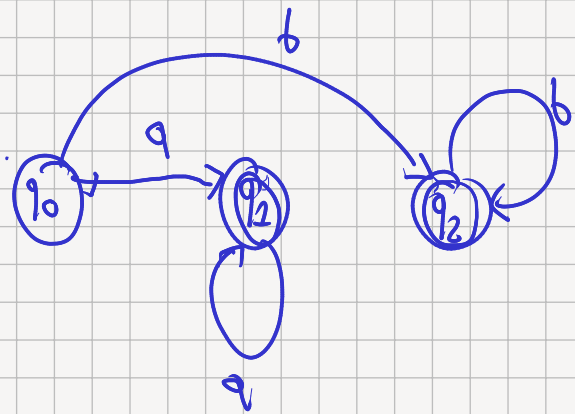
$$S \rightarrow aA \mid bB$$

$$a^+ \cup b^+$$

$$\rightarrow A \rightarrow aA \mid \epsilon$$

$$B \rightarrow bB \mid \epsilon$$

$$A_2 = \{ A_2 \cup E$$



$$A_2 = b^*$$

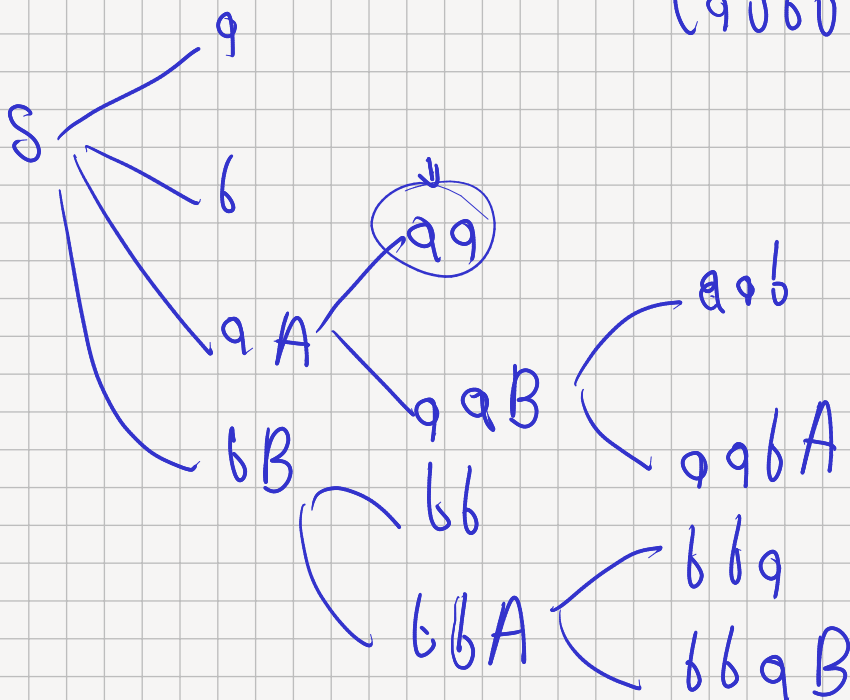
$$A_0 = q^+ \cup l^+ \quad \text{e)}$$

$$A \rightarrow a \mid aB$$

$B \Rightarrow b \mid bA$

$$L = \{ a, b, aaba, aababa, bba \}$$

$$(a \cup b \cup aq(a \cup b)^* \cup b \cup b \cup (b \cup a)^*)$$



$$S \rightarrow \textcircled{a} A \mid b B \mid \underline{a} \mid \underline{b}$$

$$A \rightarrow a \mid a B$$

$$B \rightarrow b \mid b A$$

$$\begin{aligned} & \downarrow \\ & 1) A_0 = a A_1 \cup b A_2 \cup a \cup b \\ & 2) A_1 = \textcircled{a A_2} \cup a \\ & 3) A_2 = b \underline{A_1} \cup b \end{aligned}$$

$$\begin{aligned} A_2 &= b(a A_2 \cup a) \cup b & A_1 &= ab A_1 \cup ab \cup a \\ A_2 &= ba A_2 \cup ba \cup b & \cancel{A_1} &= (ab)^*(ab \cup a) \\ \rightarrow A_2 &= (ba)^*(ba \cup b) \end{aligned}$$

$$A_0 = \textcircled{a} ((ab)^*(ab \cup a)) \cup b((ba)^*(ba \cup \underline{b})) \cup a \cup b$$

$$A_0 = a(ab)^*ab \cup a(ab)^*a \cup b(ba)^*ba \cup b(ba)^*b \cup a \cup b$$

$$A_0 = a(ab)^+ \cup a(ab)^*a \cup b(ba)^+ \cup b(ba)^*b \cup a \cup b$$

$$S \rightarrow \textcircled{a} A \mid b B \mid \underline{a} \mid \underline{b}$$

$$A \rightarrow a \mid a B$$

$$B \rightarrow b \mid b A$$

$$\left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \begin{array}{l} a(ab)^+ \\ aab \\ aabab \end{array}$$