

1) ~~Haristq~~

$$\overline{K_{n,m}}$$

$$K_{n,m} = \{ \underbrace{n, n, n, n, \dots}_m, \underbrace{m, m, m, m}_n \}$$

$$K_{n+m} = \{ \underbrace{n+m-1, n+m-1, n+m-1, \dots}_{n+m} \}$$

$$\overline{K_{n,m}} = \{ \underbrace{m-1, m-1, m-1, \dots}_m, \underbrace{n-1, n-1, \dots}_n \}$$

$$e = \frac{m(m-1) + n(n-1)}{2}$$

$$\overline{w_n} = \left\{ K_{n+1} = \{ \underbrace{n, n, n, \dots}_n \} \right.$$

$$w_n = \{ \underbrace{3, 3, \dots}_n, n \}$$

$$\overline{w_n} = \{ \underbrace{n-3, n-3, \dots}_{n-3}, 0 \}$$

$$e = \frac{n(n-3)}{2}$$

$$C_n = \begin{cases} K_n = \{ \overbrace{n-1, n-1, n-1, n-1 \dots}^{n \text{ vertices}} \} \\ C_n = \{ \overbrace{2, 2, 2, \dots, 2}^{n \text{ vertices}} \} \end{cases}$$

$$e = \frac{n(n-3)}{2}$$

$$\overline{C}_n = \{ \underbrace{n-3, n-3, \dots, n-3}_{n \text{ vertices}} \}$$

2)

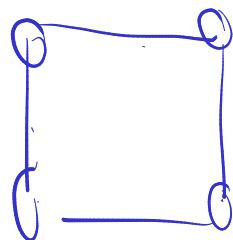
$\Phi_n$



$n=1$

2 vertices  
1 edge

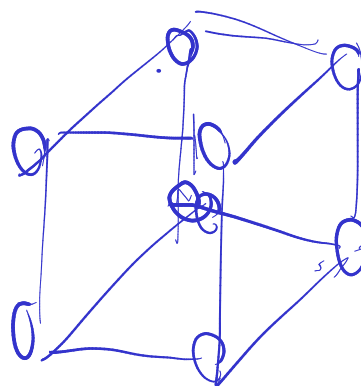
$$V=2^n$$



$n=2$

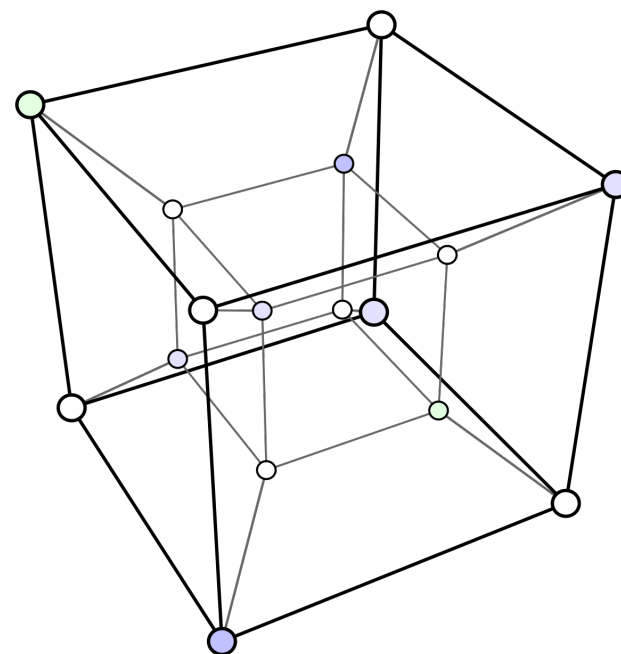
4 vertices,  
4 edges

$$e = \frac{n 2^n}{2}$$



$n=3$

8 vertices,  
12 edges



$n=4$

$$\Phi_n =$$

$$K_{2^n} = \{ \underbrace{2^n - 1, 2^n - 1, 2^n - 1, \dots}_{2^n} \}$$

$$\Phi_n = \{ \underbrace{n, n, n, \dots, n}_{2^n} \}$$

$$\Phi_n = \{ \underbrace{2^n - n - 1, 2^n - n - 1, 2^n - n - 1, \dots}_{2^n - \text{vpcb}} \}$$

$$e = \frac{2^n (2^n - n - 1)}{2}$$

¿Existe un grafo regular con  $n$  vértices tal que sea autocomplementario?

Un grafo regular es aquel que todos el mismo grado.

Para que esto pase la secuencia de grade de  $G$  y  $G$  complemento deben ser iguales, por lo que debo tener en cuenta la secuencia de  $K_n$

$$K_n = \{n-1, n-1, n-1, n-1, \dots\}$$

$$G = \{ \underbrace{d, d, d, d, \dots}_{n \text{ vértices}} \}$$

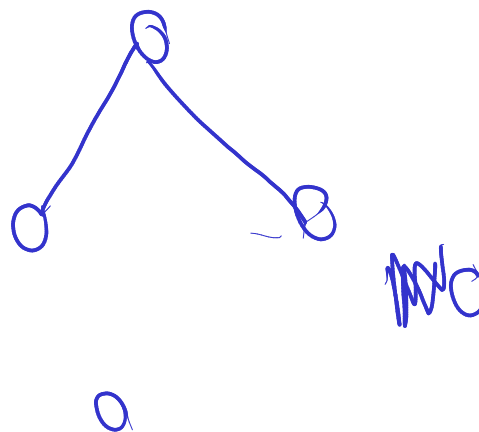
$$\overline{G} = \{ \underbrace{d, d, d, d, \dots}_{n \text{ vértices}} \}$$

$$n-1-d = d$$

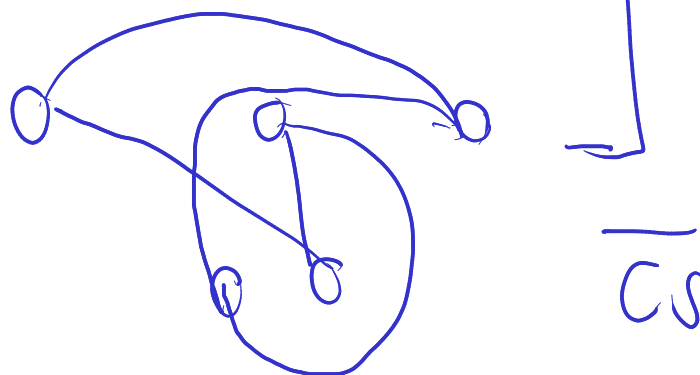
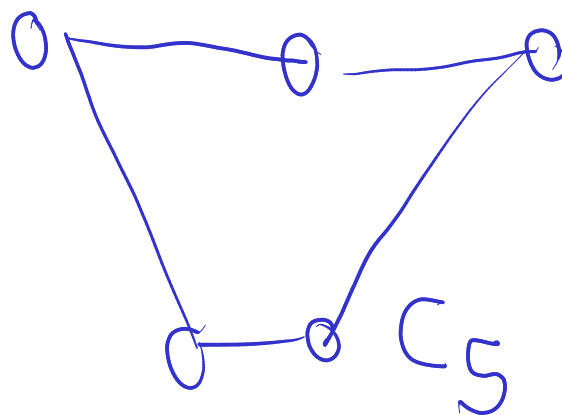
$$n-1 = 2d$$
$$n = 2d + 1$$

$$3 = 2(1) + \underline{1}$$

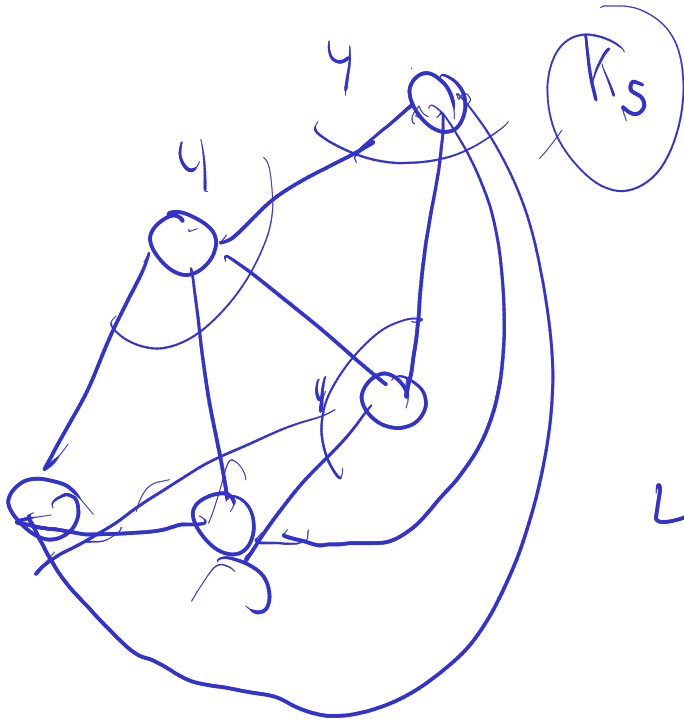
$$\left\{ \begin{array}{l} n=3 \\ d=1 \end{array} \right.$$



$$5 = 2(2) + 1$$



Determinar el número cromático de un grafo regular 5 vértices con grado 4



$K_5$

$$n=5$$

5 colores

$4 \times n$  par