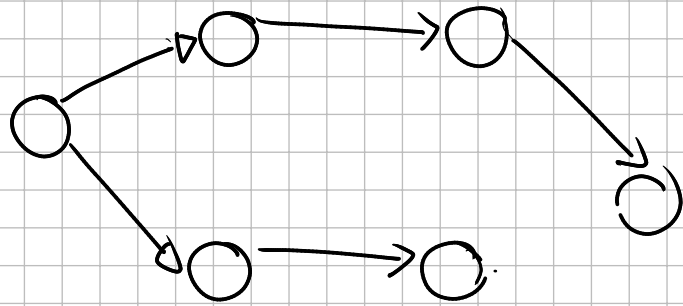
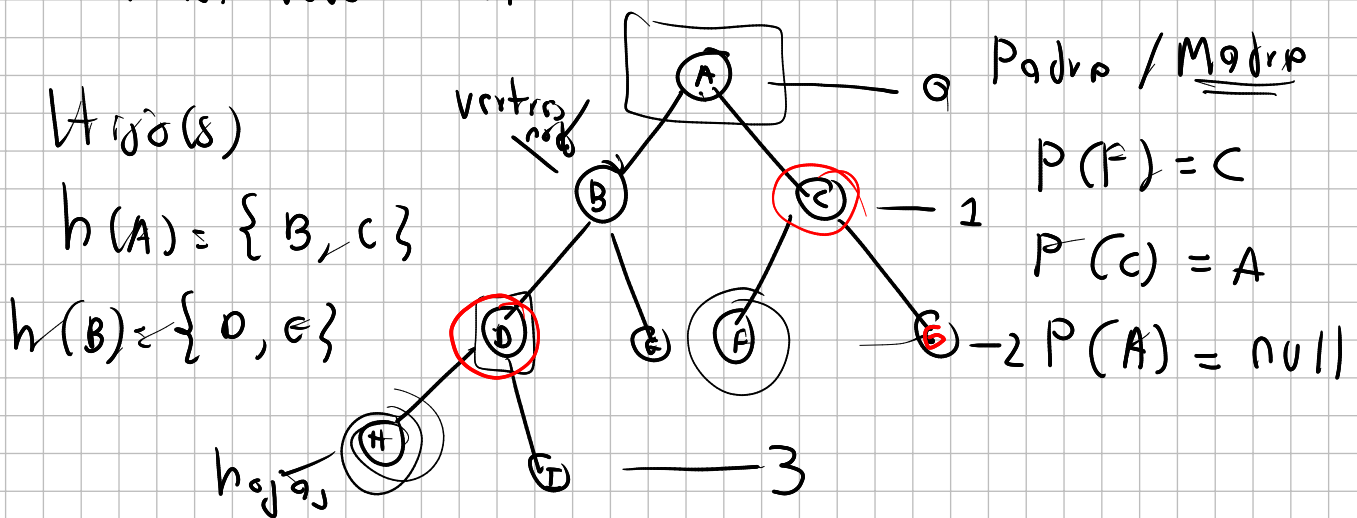


Arboles

Grafos aciclicos dirigidos.



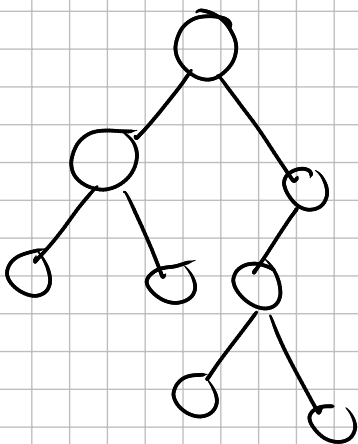
Root, Nodo inicial



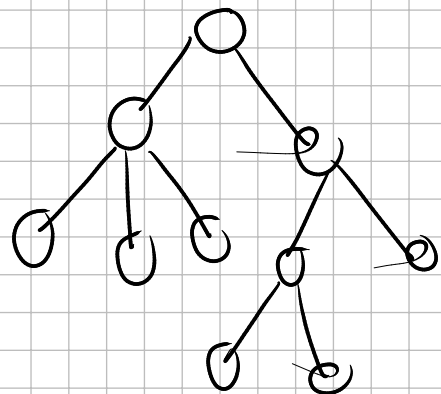
Arboles m-ario

(max m hijos cada nodo)

binario

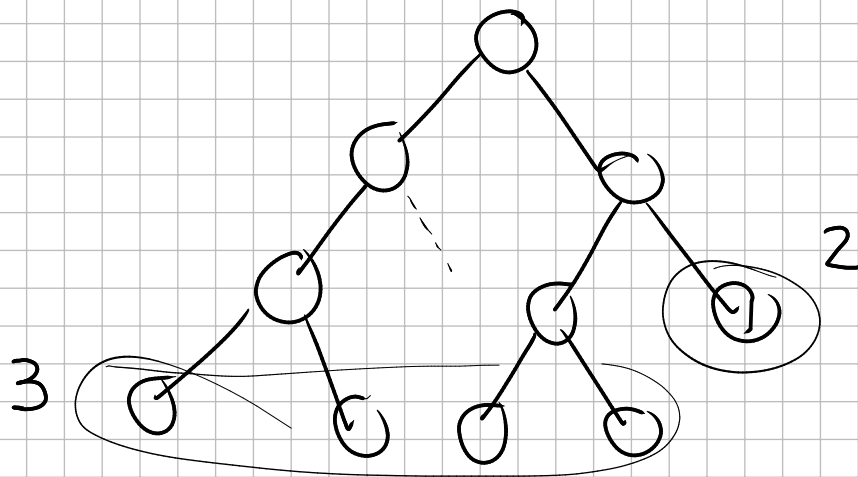


ternario / trinário

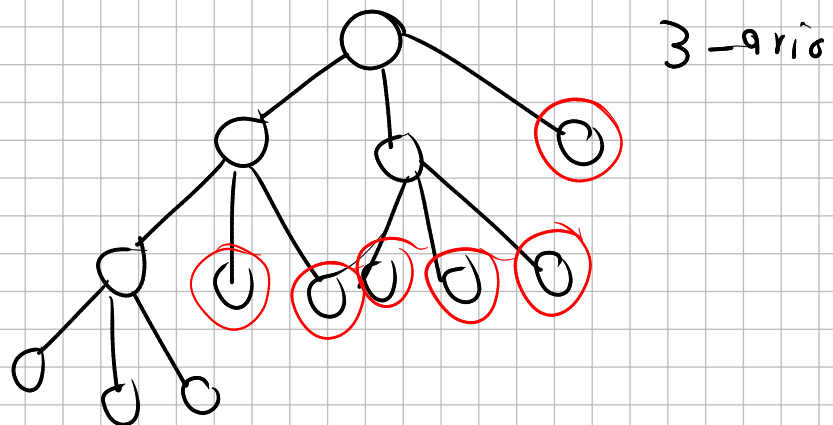


balanceado

hojas: h o $h-1$

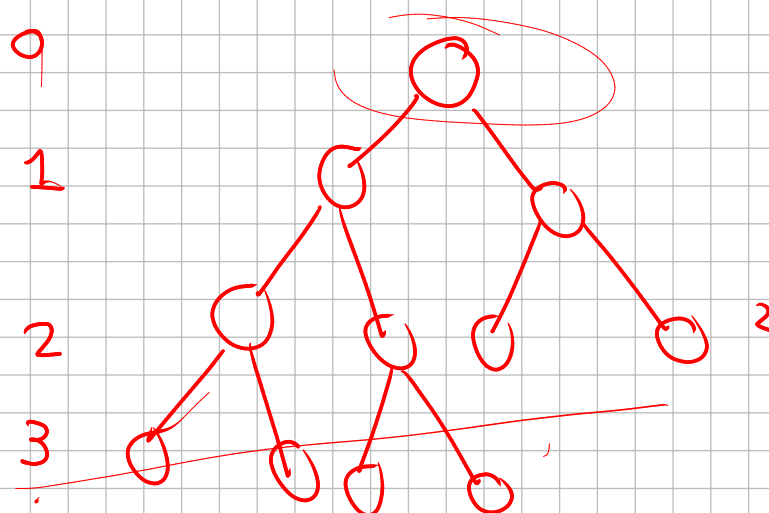


Completo: los nodos/vértices tienen exactamente m hijos



Arbol m-ario completo

Es un arbol completo y es balanceado



$$m^h$$

$$2^0 = 1$$

$$2^1 = 2$$

$$2^2 = 4$$

$$\max(2^3) = \max(8)$$

$\max(m^h)$ hojas

$$m = 10$$

$$h = 15$$

Vertices

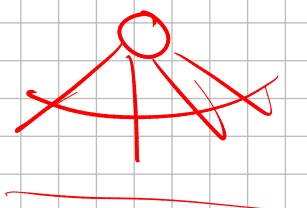
$$h = 8$$

$$10^8$$

hojas

$$\max(10^{15})$$

$$\text{rango}(10^{14}, 10^{15})$$



$$10^0$$

$$10^1$$

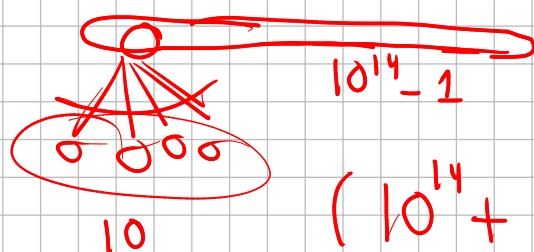
$$10^2$$

$$10^3$$

$$\vdots$$

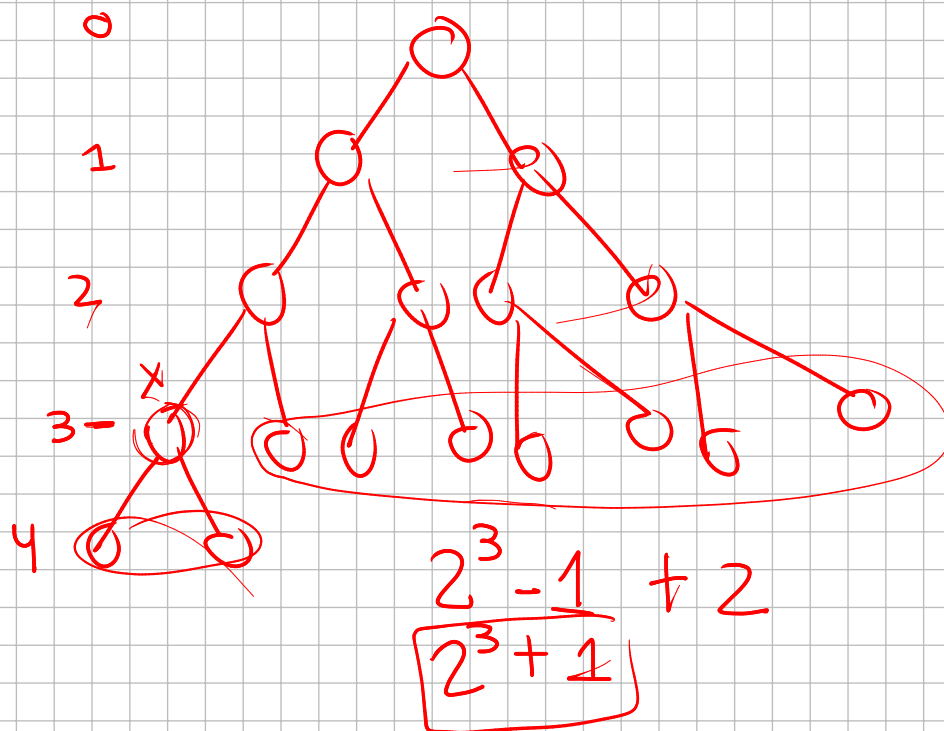
$$10^{14}$$

Completo
m-ario

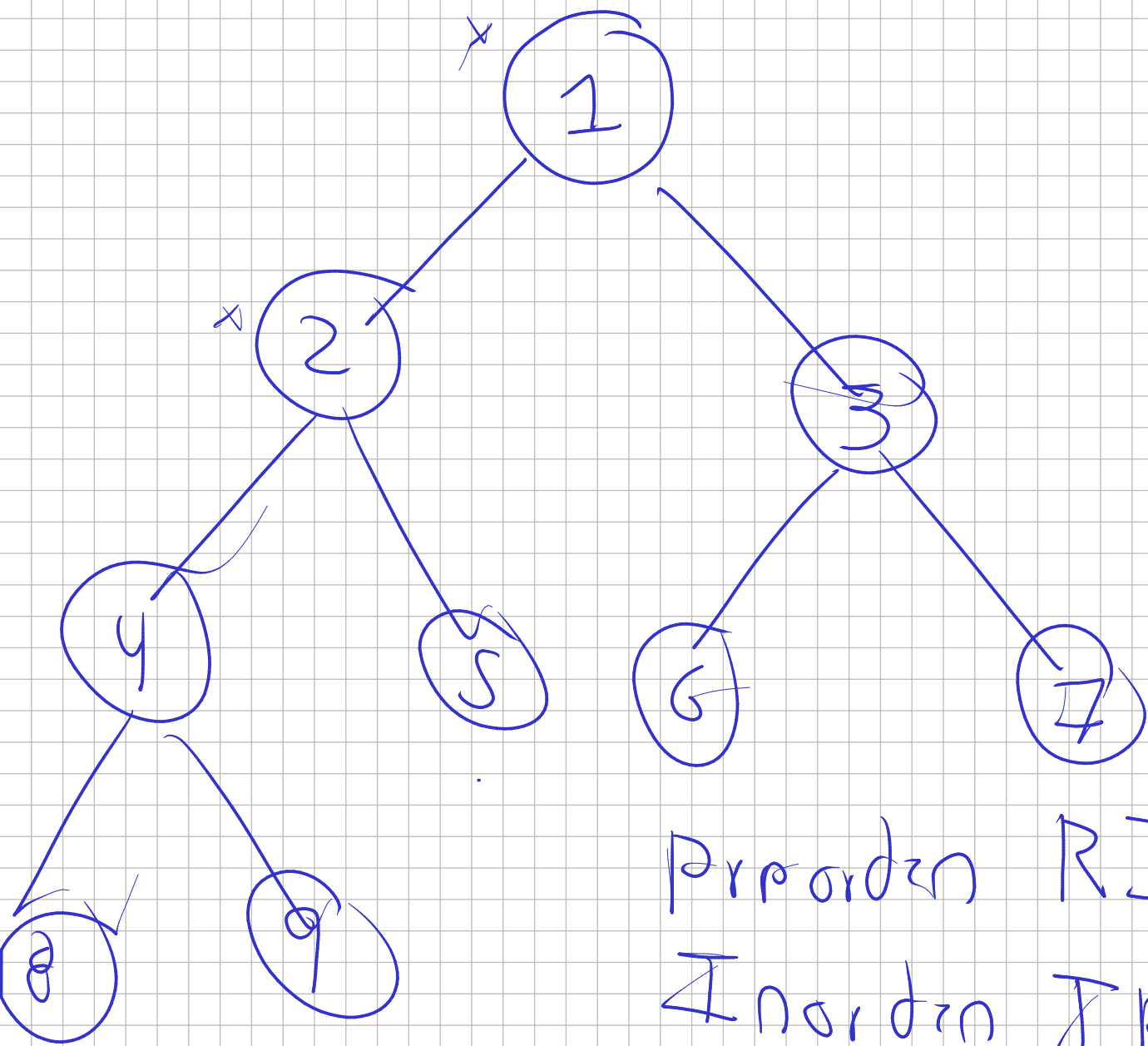


$$10^{14} - 1$$

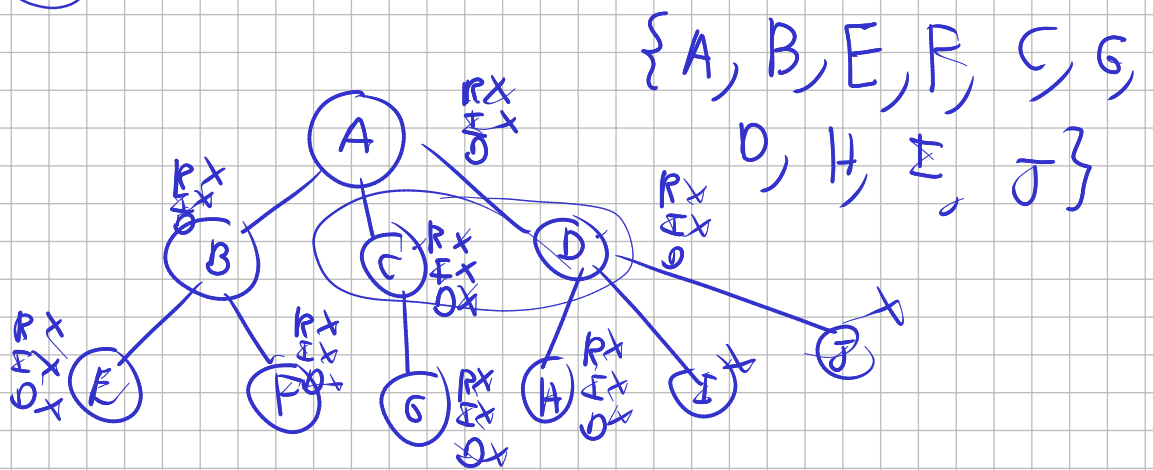
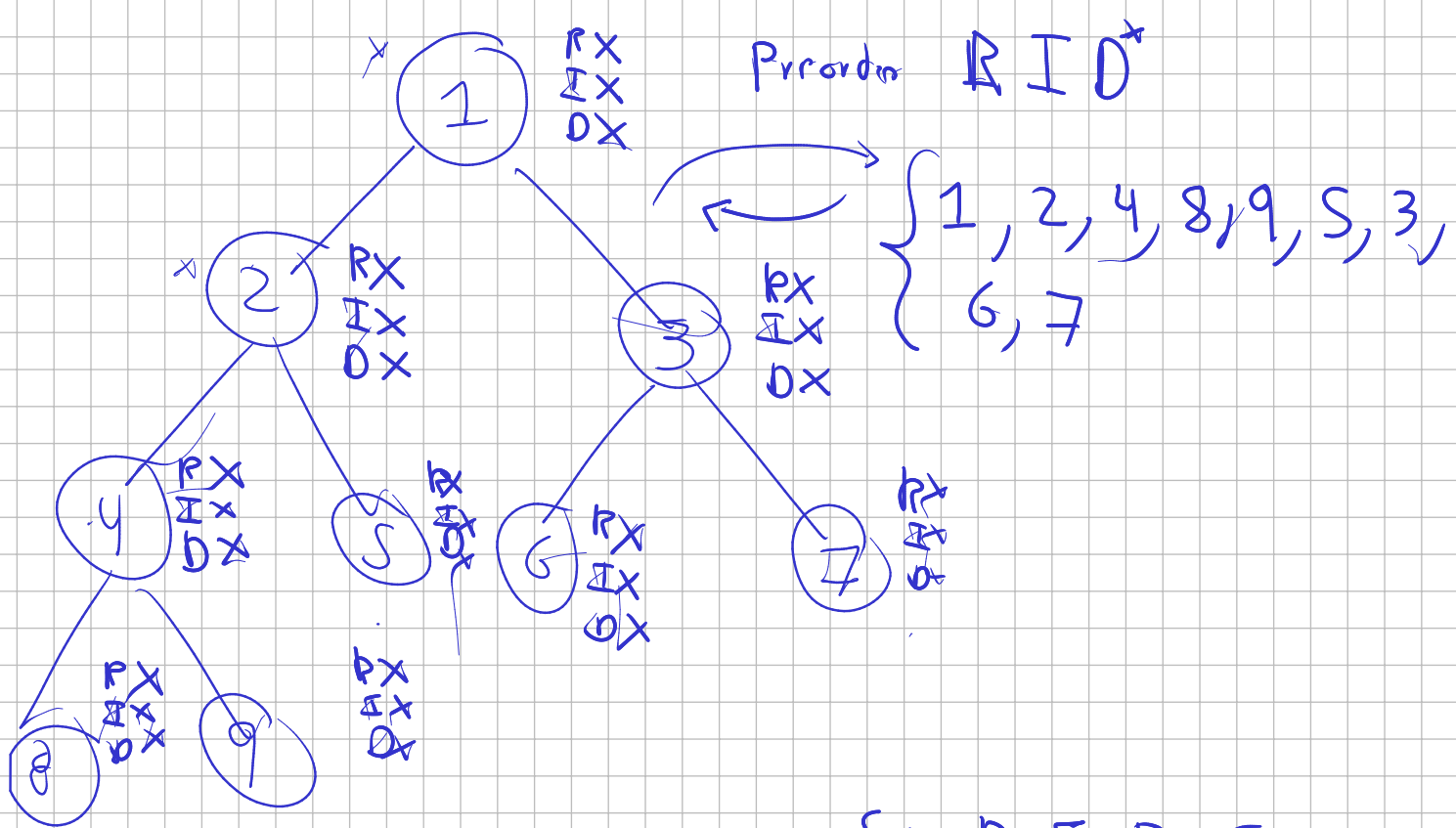
$$(10^{14} + 9, 10^{15})$$

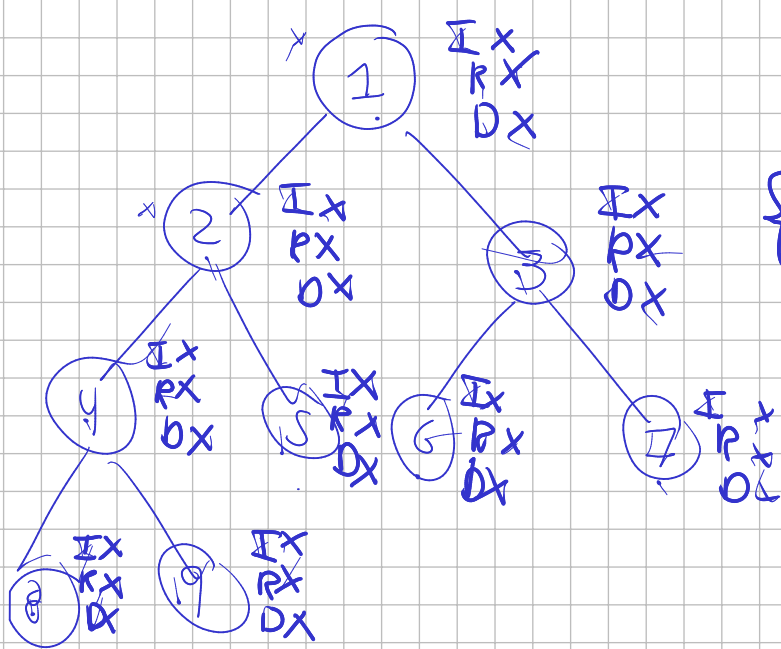


hojas $(m^{h-1} + m - 1, m^h)$
 $(2^3 + 2 - 1, 2^4)$
 $(2^3 + 1, 2^4)$

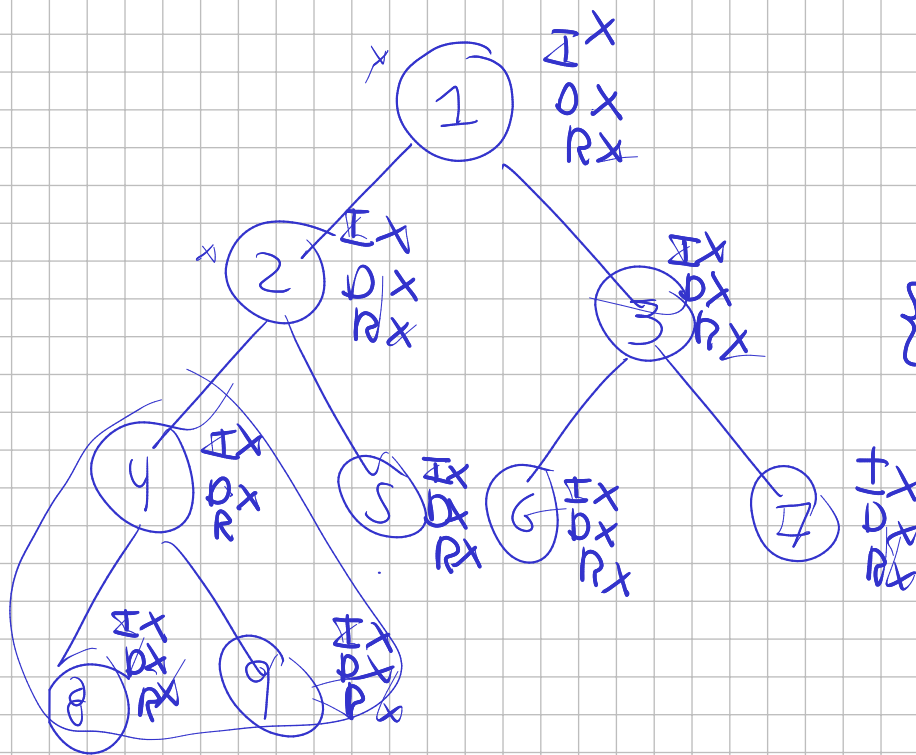


Preorden $RI D^*$
Inorden $IR D^*$
Postorden $IR D$

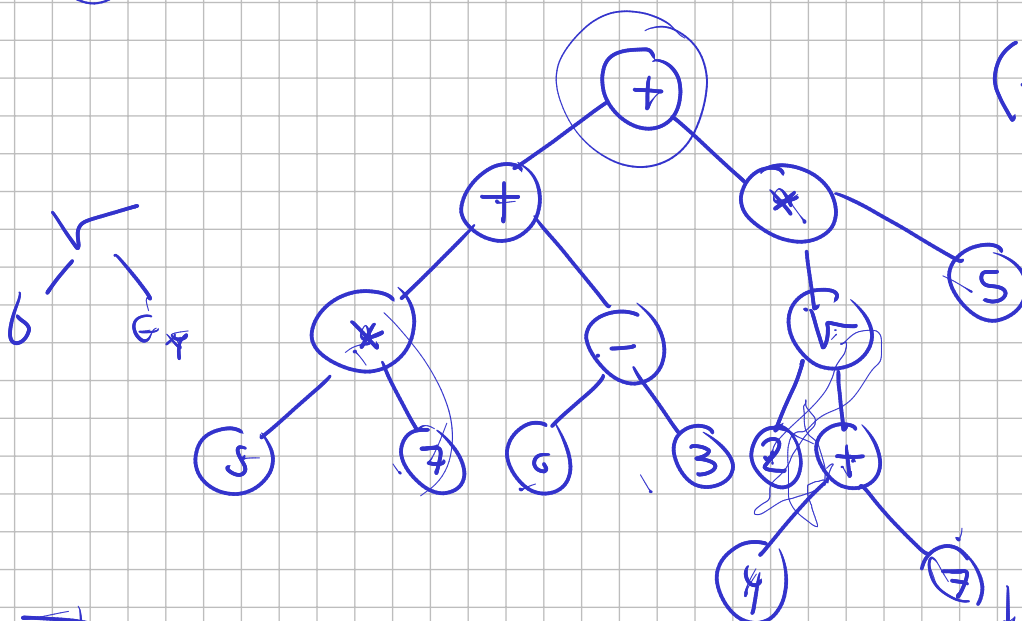




Inorden I
 $\{8, 4, 9, 2, 5, 1, 6, 3, 7\}$



Postorden I, D, R
 $\{8, 9, 4, 5, 2, 6, 7, 3, 1\}$



Präorden R, I, D

$(+ (+ (* 5 7)$
 $(- 6 3))$

$(* (\sqrt{(+ 4 7)})$
 $5)$

Inorden $((5 * 7) + (6 - 3)) + \sqrt{(4 + 7)} * 5$

Postorder ((S 7 *) (6 3 -) +)

((2(4 7 +) 5) S *) +)

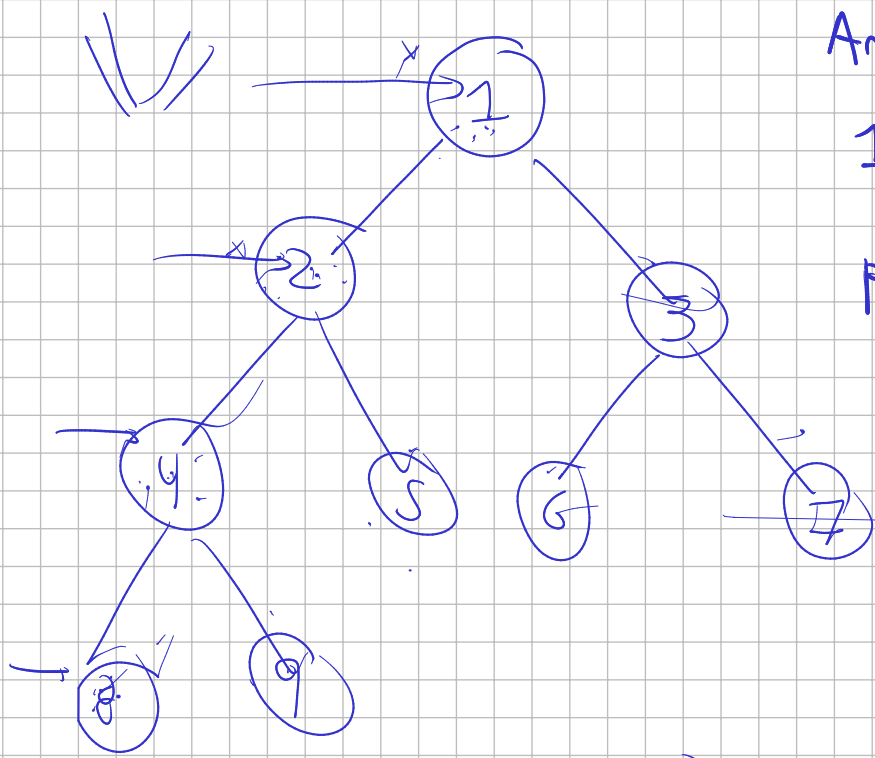
(3 4 4)

3

4
3

+ ←
4
3 |

LIFO
↑ ↑



Amplitud

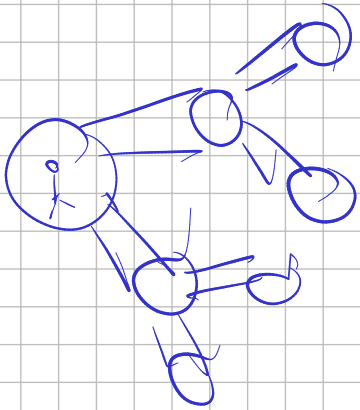
1, 2, 3, 4, ~~5~~, 6, 7, 8, 9

Profundidad I, D

I 1, 2, 4, 8, 9, 5,

~~3, 6, 7~~

D 1, 3, 7, 6, 2, 5,
4, 9, 8

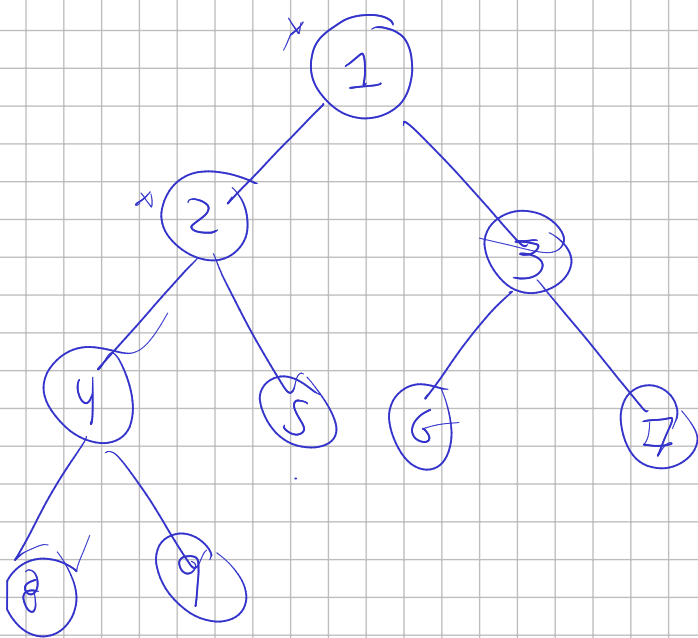


Amplitud

cola

Profundidad

pila



$C = [1]$ $S = \{1\}$

$C = [2, 3]$ $S = \{1, 2\}$

$C = [4, 5]$ $S = \{1, 2, 3\}$

$C = [8, 6, 7]$ $S = \{1, 2, 3, 4\}$

$C = [9, 6, 7, 8, 9]$ $S = \{1, 2, 3, 4, 5\}$

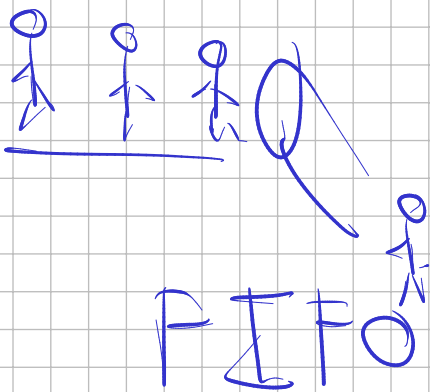
$C = [8, 7, 8, 9]$ $S = \{1, 2, 3, 4, 5, 6\}$

$C = [8, 8, 9]$ $S = \{1, 2, 3, 4, 5, 6, 7\}$

$C = [9, 9]$ $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$

$C = [9]$ $S = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

$C = []$ $S = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

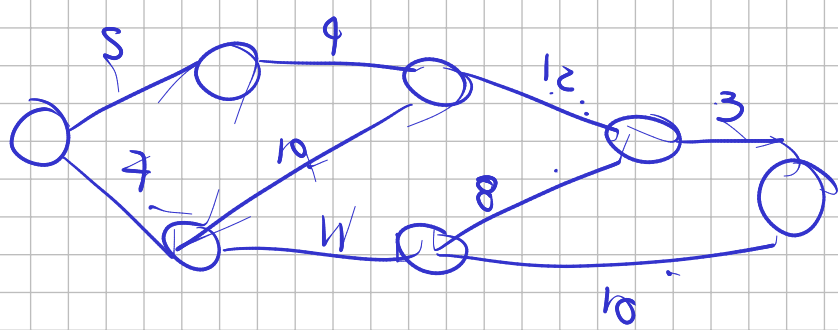


FIFO

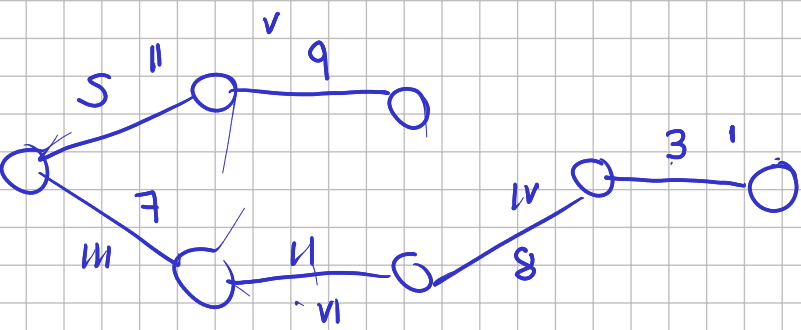
Arboles de expansión

Grafo -> Arbol: Eliminar los ciclos de un grafo para que sea un arbol

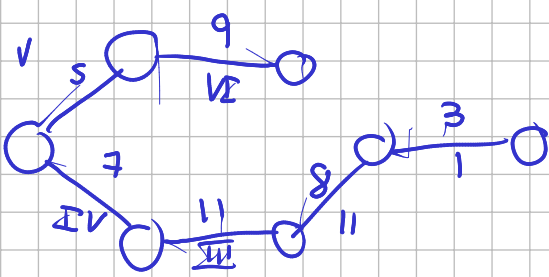
Arboles de expansión minimos: Cuya suma de los valores de las aristas sea mínimo



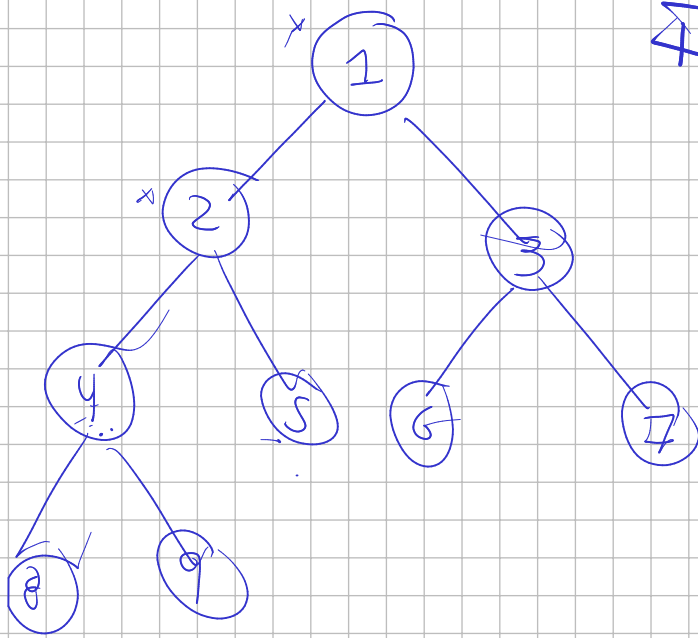
Kruskal



Prim



Δ_{29} Prof



$P = [\cancel{1}]$

$S = \{1\}$

$P = [\cancel{2} \ 3]$

$S = \{1, 2\}$

$P = [\cancel{4} \ 5 \ 3]$

$S = \{1, 2, 4\}$

$P = [\cancel{8} \ 9 \ 5 \ 3]$

$S = \{1, 2, 4, 8\}$

$P = [\cancel{9} \ 5 \ 3]$

$S = \{1, 2, 4, 8, 9\}$

$P = [\cancel{5} \ 3]$

$S = \{1, 2, 4, 8, 9, 5\}$

$P = [\cancel{3}]$

$S = \{1, 2, 4, 8, 9, 5, 3\}$

$P = [\cancel{6} \ 7]$

$S = \{1, 2, 4, 8, 9, 5, 3, 6\}$

$P = [\cancel{7}]$

$S = \{1, 2, 4, 8, 9, 5, 3, 6, 7\}$

$P = []$