

Tipos

Manejo de memoria: ¿Que número de bits necesito para almacenar la información?

Número --> 32 bits (integer)

--> 64 bits (long)

--> 128 bits (long long)

Double --> 32 bits (float)

--> 64 (double)

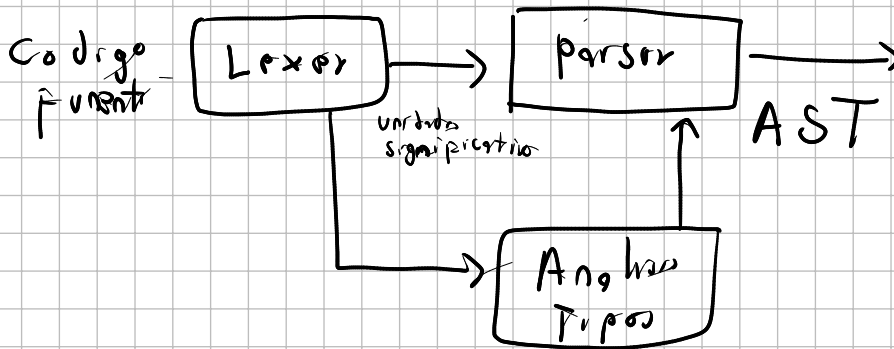
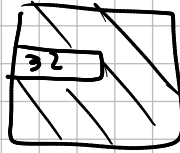
--> 128 (double de doble precisión)

}
Figura

Tipado + Compilado: más rápido { C++
Java

var a = 8;
a = "HolaF"
↓
8

} 32 bits
40 bits



Reglas Tipos

primitivo { + int * int → int and bool * bool → bool
> int * int → bool

condicion { if <test-exp>
then <true-exp>
false <false-exp>

<test-exp> := bool
<true-exp> = <false-exp>

$$\text{proc} \left\{ \begin{array}{l} t_1 * t_2 * t_3 * \dots * t_n \rightarrow t \\ \text{proc}(\underbrace{\hspace{2cm}}_{n \text{ variables}}) \end{array} \right.$$

$$\text{app-exp} \left\{ \begin{array}{l} (F \overbrace{t_1' t_2'}) \\ t_F = t_1 * t_2 * t_3 * \dots * t_n \rightarrow t \\ \underline{t_1 = t_1' \quad t_2 = t_2' \quad t_n = t_n'} \\ t \end{array} \right.$$

$$\text{let} \left\{ \begin{array}{l} f = \text{proc}(\text{int } n, \text{int } m) \\ \quad \text{if } >(n, m) \\ \quad \text{then } t(n, m) \\ \quad \text{else } -(n, m) \end{array} \right. \\ \text{in } (f \ 2 \ 3)$$

$$\begin{array}{l} t_F = \text{int} * \text{int} \rightarrow \text{int} \\ \downarrow \\ (f \ 2 \ 3) \\ \downarrow \quad \downarrow \\ t_F = \text{int} * \text{int} \rightarrow \text{int} \\ \uparrow \quad \uparrow \\ \textcircled{2 = \text{int}} \quad \textcircled{3 = \text{int}} \end{array}$$

int

$$\text{basics} \left\{ \begin{array}{l} \langle \text{int} \rangle = \text{int} \\ \langle \text{bool} \rangle = \text{bool} \end{array} \right.$$

$$\text{let} \left\{ \begin{array}{l} \text{let} \\ \text{in } \textcircled{\langle \text{exp} \rangle} \end{array} \right. \quad T_{\text{exp}}$$

let
 $f = \text{proc } (x, y)$
 if $>(x, y)$
 then x else y
 in
 $(f \ 2 \ 3)$

Inferencia de tipos

Chequeo de tipos

let
 $f = \text{proc } (\text{int } x, \text{int } y)$
 if $>(x, y)$
 then x else y
 in $(f \ 2 \ 3)$

$f = \text{proc } (?x, \text{int } y)$

in

$(f \ 2 \ 3)$

retor

args

$[\text{int}, \text{int}]$

$\text{int} * \text{int} \rightarrow \text{int}$

1. Realice chequeo de tipos en la siguiente expresión:

```
let
  j = proc(int x, (int->bool) y)
    if (y 2) then +(x,2) else -(x,3)
  t = proc((int*int->bool) k, int a, int b, int c)
    (k + (a,b) c)
  s = proc(int w) >(w,6)
in
  let
    p = proc((int->(bool->int)) * int * int->int) m, int->(bool->int) n)
      (m n 1 3 s)
  in
    (p t j)
```

$t_j = \text{int} * (\text{int} \rightarrow \text{bool}) \rightarrow \text{int}$

$t_t = (\text{int} * \text{int} \rightarrow \text{bool}) * \text{int} * \text{int} * \text{int} \rightarrow \text{bool}$

$t_s = \text{int} \rightarrow \text{bool}$

$t_p = \text{int} \rightarrow (\text{bool} \rightarrow \text{int}) * \text{int} * \text{int} \rightarrow \text{int}$

$* \text{int} \rightarrow (\text{bool} \rightarrow \text{int}) \rightarrow \text{int}$

Verifique esta expresión, si hay errores de tipo indique cuales son.

2. Escriba expresiones de tipo que cumplan:

- $(\text{int} * (\text{int} \rightarrow \text{bool}) * (\text{int} \rightarrow (\text{bool} \rightarrow \text{int}))) \rightarrow (\text{int} \rightarrow \text{bool})$
- $(\text{int} * \text{bool} * (\text{int} \rightarrow \text{int}) * \text{int} \rightarrow (\text{bool} \rightarrow \text{int})) \rightarrow (\text{int} \rightarrow (\text{bool} \rightarrow \text{int}))$
- $(\text{int} * (\text{bool} \rightarrow \text{bool}) * (\text{int} \rightarrow (\text{bool} \rightarrow \text{int}))) \rightarrow (\text{bool} \rightarrow \text{int})$

t_p
 t_t

$\text{int} * \text{int} \rightarrow \text{bool}$
 $\text{int} \rightarrow (\text{bool} \rightarrow \text{int})$

2. Escriba expresiones de tipo que cumplan:

- $(\text{int} * (\text{int} \rightarrow \text{bool}) * (\text{int} \rightarrow (\text{bool} \rightarrow \text{int})) \rightarrow (\text{int} \rightarrow \text{bool}))$
- $(\text{int} * \text{bool} * (\text{int} \rightarrow \text{int}) * (\text{int} \rightarrow (\text{bool} \rightarrow \text{int}))) \rightarrow (\text{int} \rightarrow (\text{bool} \rightarrow \text{int}))$
- $(\text{int} * (\text{bool} \rightarrow \text{bool}) * (\text{int} \rightarrow (\text{bool} \rightarrow \text{int}))) \rightarrow (\text{bool} \rightarrow \text{int})$

let

$$f \equiv \text{proc}(\text{int } x, (\text{int} \rightarrow \text{bool}) y, (\text{int} \rightarrow (\text{bool} \rightarrow \text{int}) z)$$

$$\text{if } (y \ x)$$

$$\text{then proc}(\text{int } m) > (x, m)$$

$$\text{else proc}(\text{int } n) > ((\underbrace{(z \ n)}_{\text{bool} \rightarrow \text{int}} \text{ true}), n)$$

$$\text{in } F$$

$$\text{int}$$