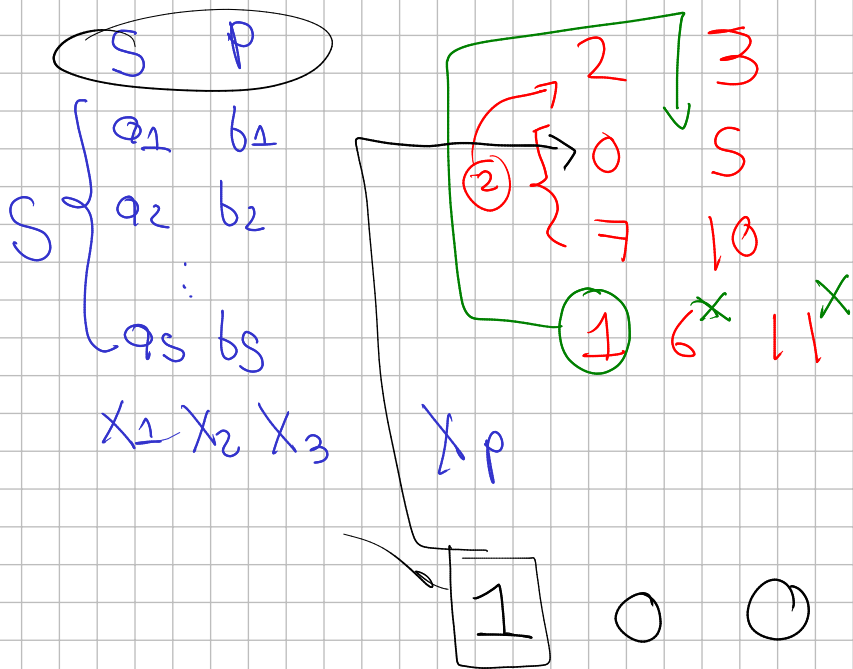


## Explicación punto 1 TI



$$1 \in [0, 5] \cap [7, 10] = \emptyset$$

$$6 \in [0, 8] \cup [7, 10] = \mathbb{P} \quad 0$$

$$11 \in [0, 8] \cup [7, 10] = \mathbb{F}_0$$

## Listas:

**<elemento> :: <lista>**

List(1,2,3)

$$1:2:3:\text{Nil}$$

Nil

$$\{a, b, c\} \xrightarrow{h} \in, a, b, c, aa, ab, ac, \dots$$

$$\Sigma^* = \{ \epsilon, a, b, c, aa, ab, ac, b \dots \}$$

$$\Sigma^* = \{ \text{h}, a, b, c, aa, ab, \dots \}$$

$$L(xh) = \{ h, a, b, \dots \}$$

$$P(y) = |xy| = |x| + |y|$$

$$P(ya) = |xya| = |x| + |ya|$$

$$|xya| = |x| + |y| + |a|$$

$$|xya| = |x| + |y| + \underline{\underline{1}}$$

$$y = \{ \text{h}, a, b, c \}$$

$$ya = \{ a, aa, ba, \dots \}$$

$$y = \{ a, b, c \}$$

$$x = \{ bb, aa, cc \}$$

$$> \{ bba, aab, ccc, \dots \}$$

$a_{m,n}$  se define recursivamente para  $(m,n) \in \mathbb{N} \times \mathbb{N}$  por  $a_{0,0} = 0$  y

$$a_{m,n} = \begin{cases} a_{m-1,n} + 1 & \text{si } n=0 \text{ y } m > 0 \\ a_{m,n-1} + n & \text{si } n > 0. \end{cases}$$

Se  $a_{m,n} = m + n(n+1)/2$  para todo  $(m,n) \in \mathbb{N} \times \mathbb{N}$ , esto es, para todos

$$a_{0,0} = 0$$

$$a_{5,0} = 5$$

$$a_{5,0} = a_{4,0} + 1 = 5$$

$$a_{4,0} = a_{3,0} + 1 = 4$$

$$a_{3,0} = a_{2,0} + 1 = 3$$

$$a_{2,0} = a_{1,0} + 1 = 2$$

$$a_{1,0} = a_{0,0} + 1 = 1$$

$$a_{5,3} = a_{4,2} + 3 = 11$$

$$a_{5,2} = a_{4,1} + 2 = 8$$

$$a_{5,1} = a_{4,0} + 1 = 6$$

$$a_{5,0} = m + \frac{n(n+1)}{2} = 5 + \frac{0(1)}{2} = 5 \checkmark$$

$$a_{5,3} = 5 + \frac{3(4)}{2} = 5 + 6 = 11 \checkmark$$

**Paso inductivo:** Sea  $a_{m',n'} = m' + n'(n'+1)/2$  con  $(m',n')$  menor que  $(m,n)$  en el orden lexicográfico de  $\mathbb{N} \times \mathbb{N}$ .

$$a_{m',n'} < a_{m,n}$$

$$n=0$$

$$a_{m,n} > a_{m-1,n}$$

$$m + \frac{n(n+1)}{2} > m-1 + \frac{n(n+1)}{2}$$

$$m > m-1$$

$$0 > -1$$

$a_{m,n}$  se define recursivamente para  $(m, n) \in \mathbb{N} \times \mathbb{N}$  por  $a_{0,0} = 0$  y

$$a_{m,n} = \begin{cases} a_{m-1,n} + 1 & \text{si } n = 0 \text{ y } m > 0 \\ \underline{a_{m,n-1} + n} & \text{si } n > 0. \end{cases}$$

ie  $a_{m,n} = m + n(n+1)/2$  para todo  $(m, n) \in \mathbb{N} \times \mathbb{N}$ , esto es, para todos

$n > 0$

$$a_{m,n} = a_{m,n-1} + n$$

(m)

$$a_{m,n} > a_{m,n-1}$$

$$\cancel{m} + \cancel{n}(n+1) > \cancel{m} + \cancel{(n-1)}n$$

$n$

$$n(n+1) > (n-1)n$$

$$n+1 > n-1$$

$$1 > -1 \quad \checkmark$$