

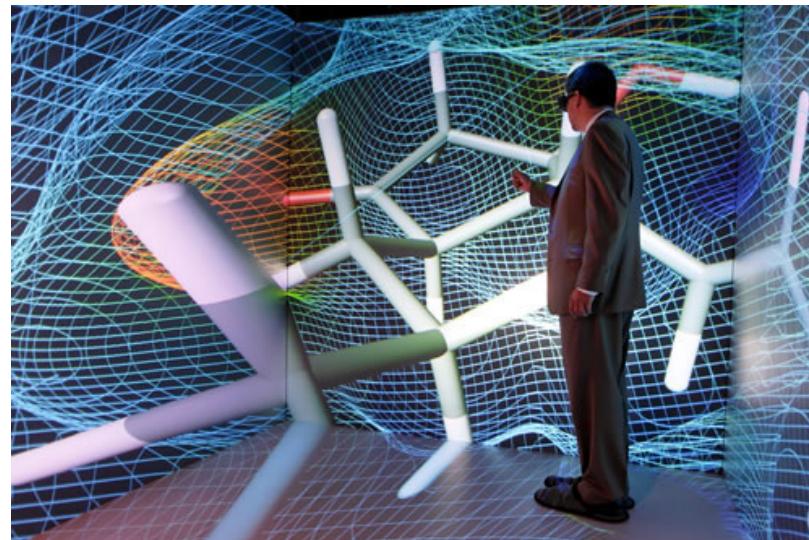
# Stereoscopy

C. Andujar

Sep 2020

# Motivation

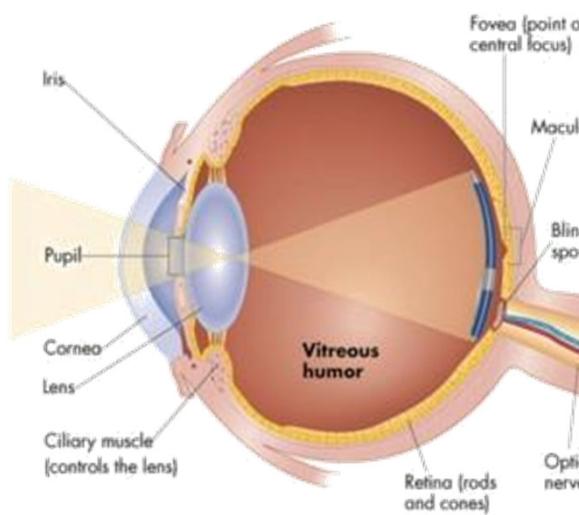
- One of the most important depth cues
- Key in all VR applications
- Influences both software and hardware



# **DEPTH PERCEPTION**

# Depth perception

- Our retinas only capture planar images
- The HVS is able to recover depth information by combining multiple depth cues.
- Depth cues = features that help the HVS obtain depth information.



# Depth cues

- In the real-world, all depth cues agree.
- In VR, some depth cues might disagree!
  - Poor stereo → poor depth, eye strain (visual fatigue)
  - Conflicting stimuli → motion sickness

# Depth cues

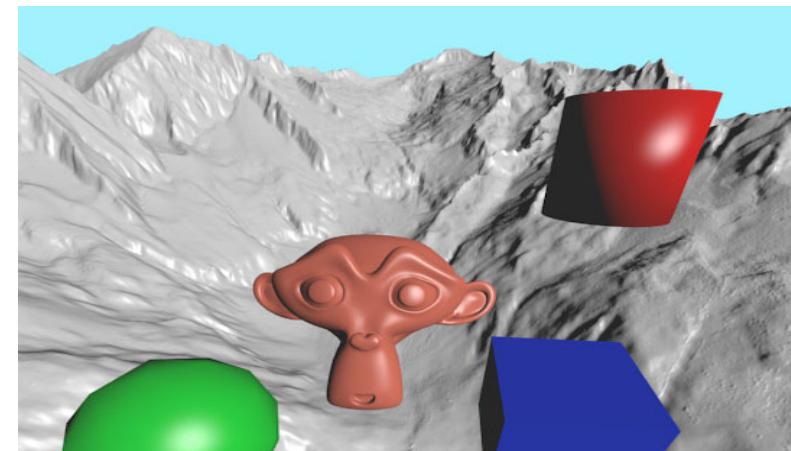
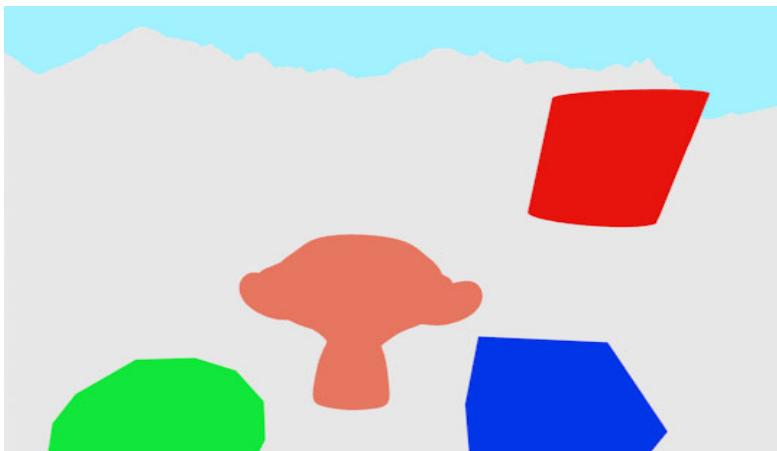
## Depth cue classification

- Monocular
  - Shading, Shadows, Relative size, Perspective, Texture gradient, Atmospheric perspective, Motion parallax, Occlusion, Accommodation
- Binocular
  - Convergence, retinal disparity

1

# Shading

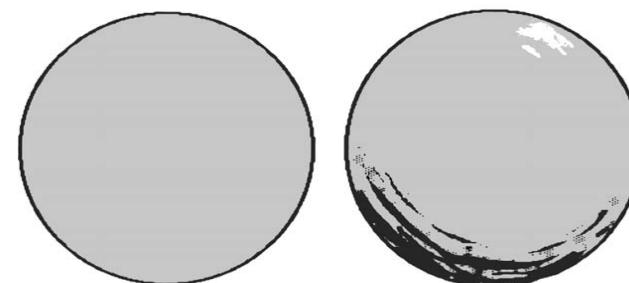
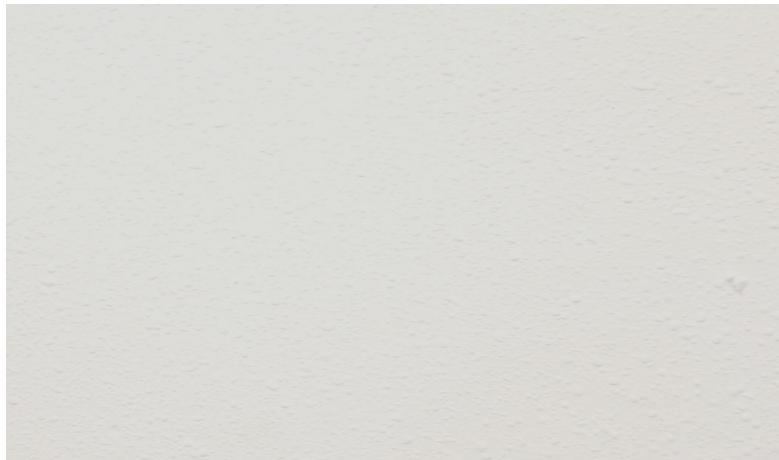
Shading provides shape and depth information because it largely depends on the surface orientation



1

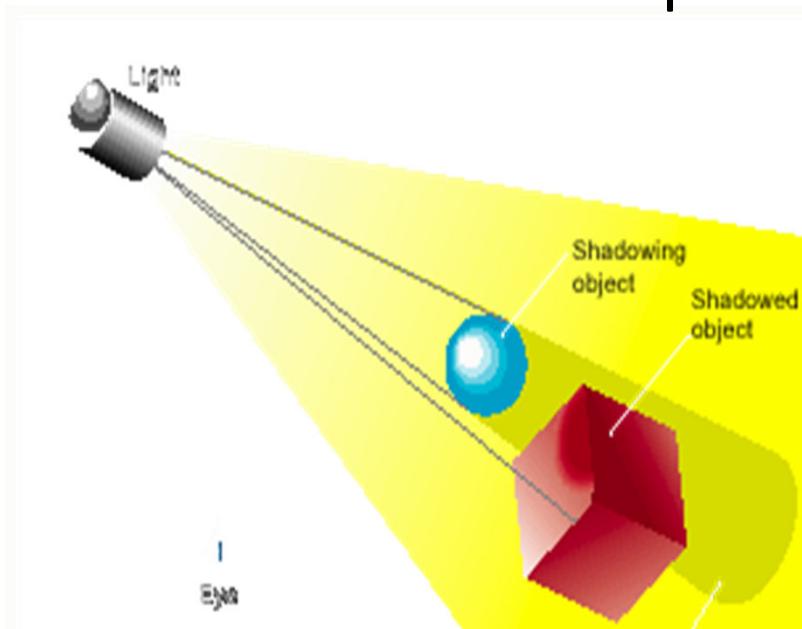
# Shading

Shading provides shape and depth information because it largely depends on the surface orientation

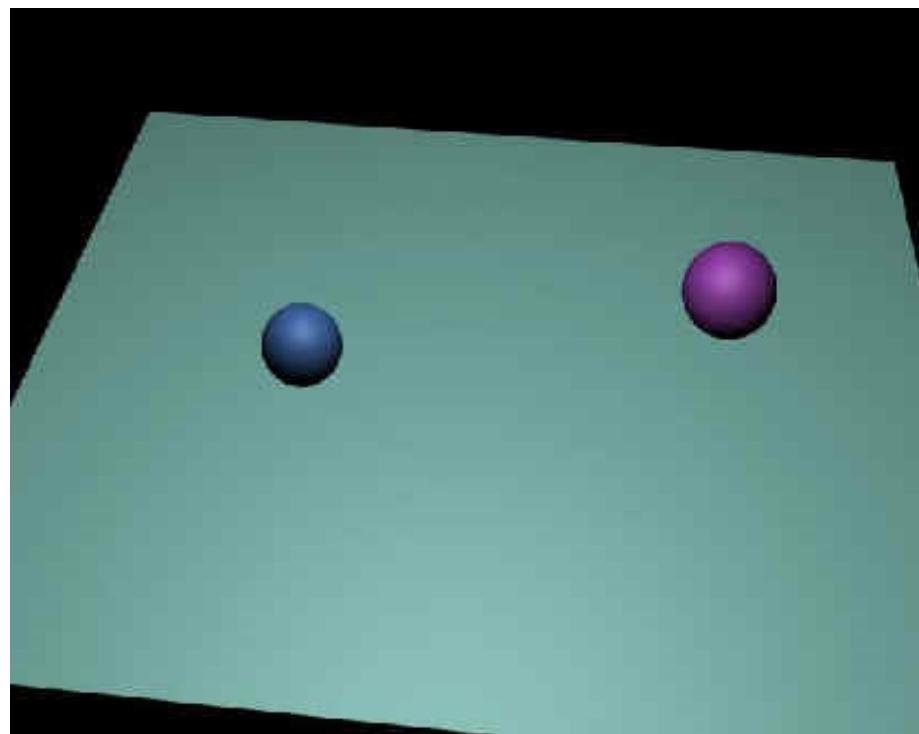


# Shadows

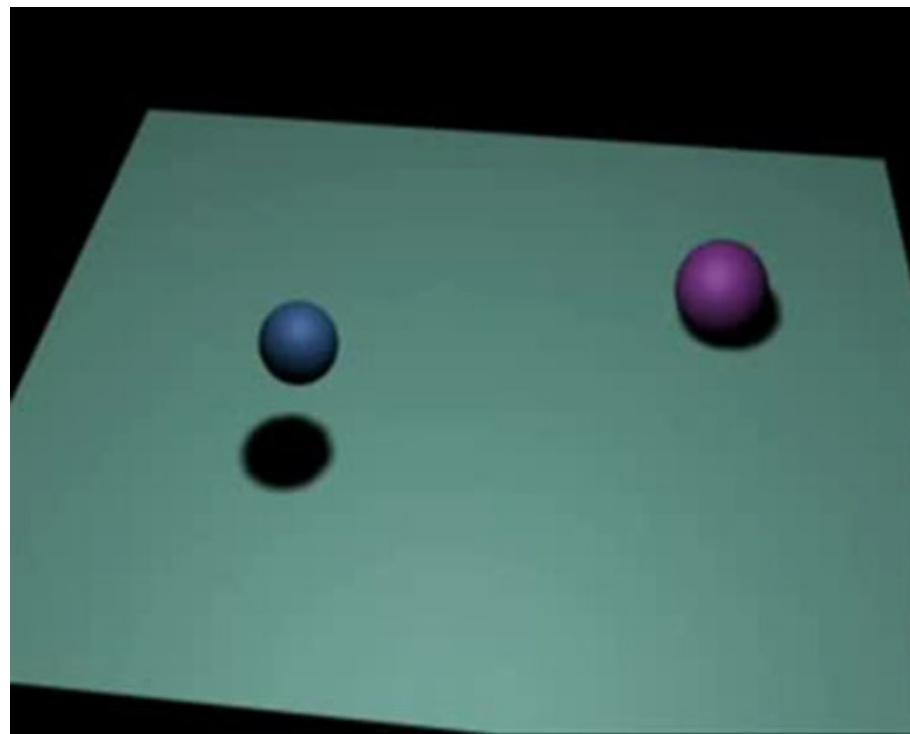
Shadows cast by objects play an important role in depth perception



# Shadows



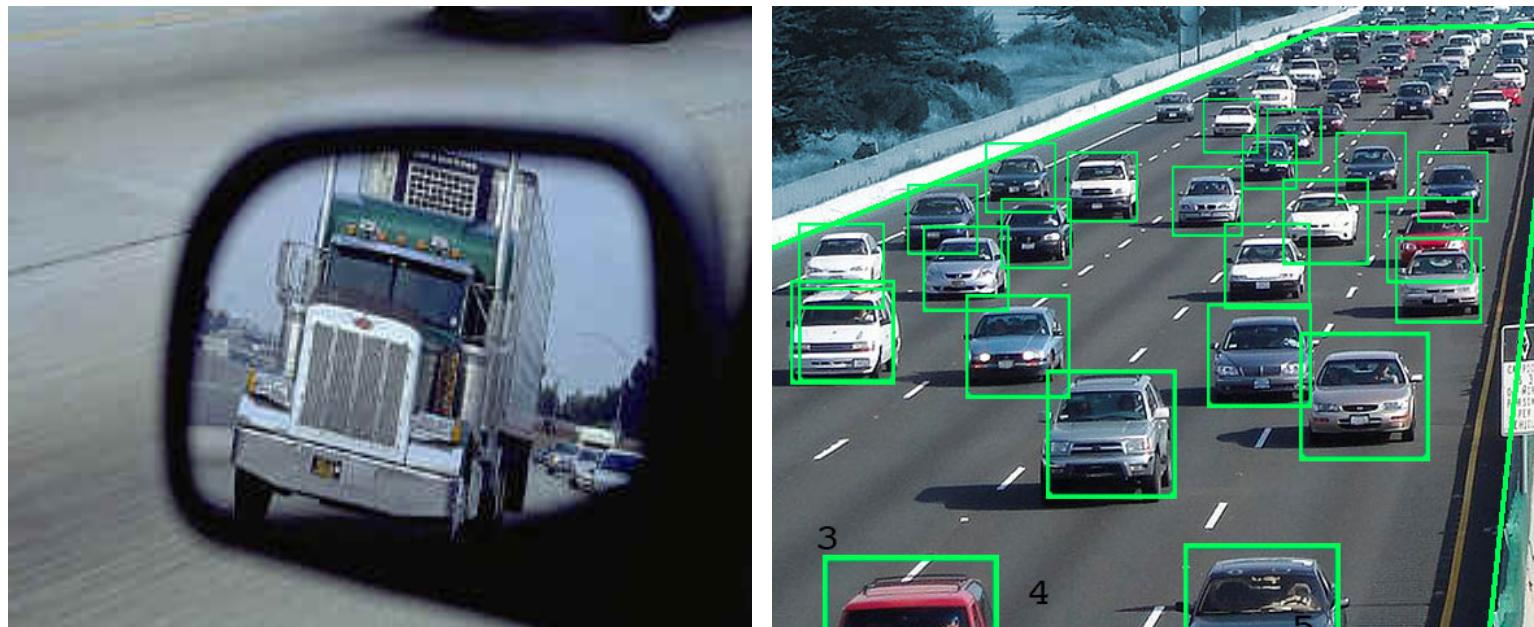
# Shadows



3

## Retinal image size

The visual system exploits the relative size of familiar objects to judge distance.



## 4

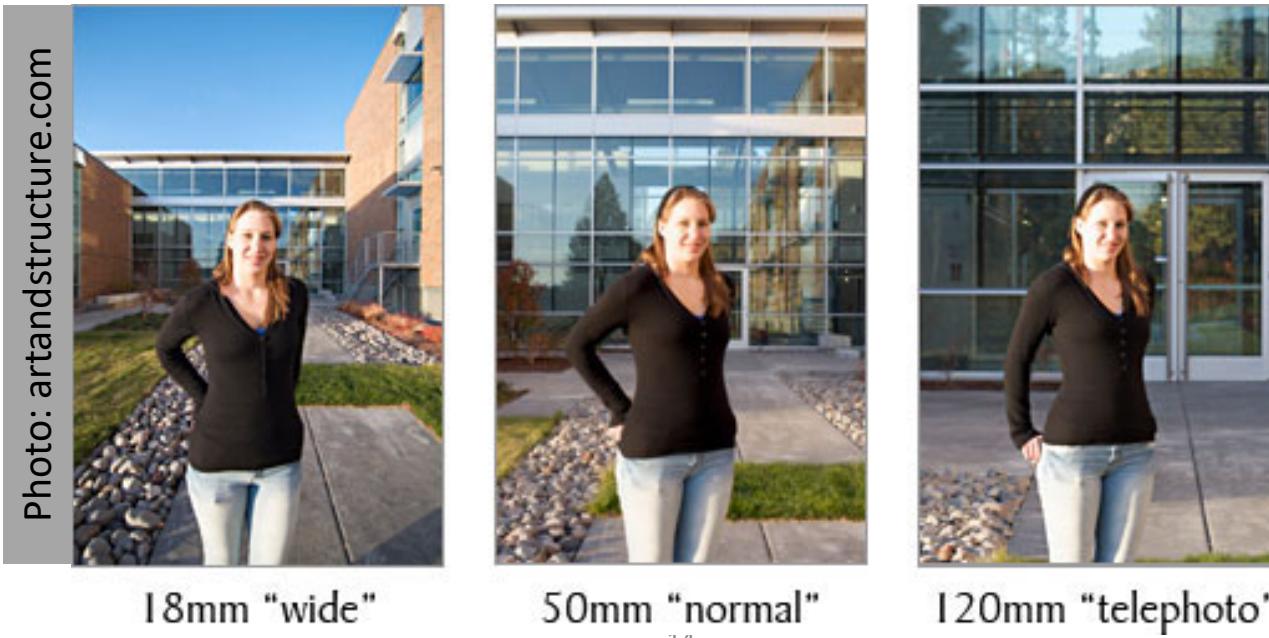
## Perspective (linear perspective)

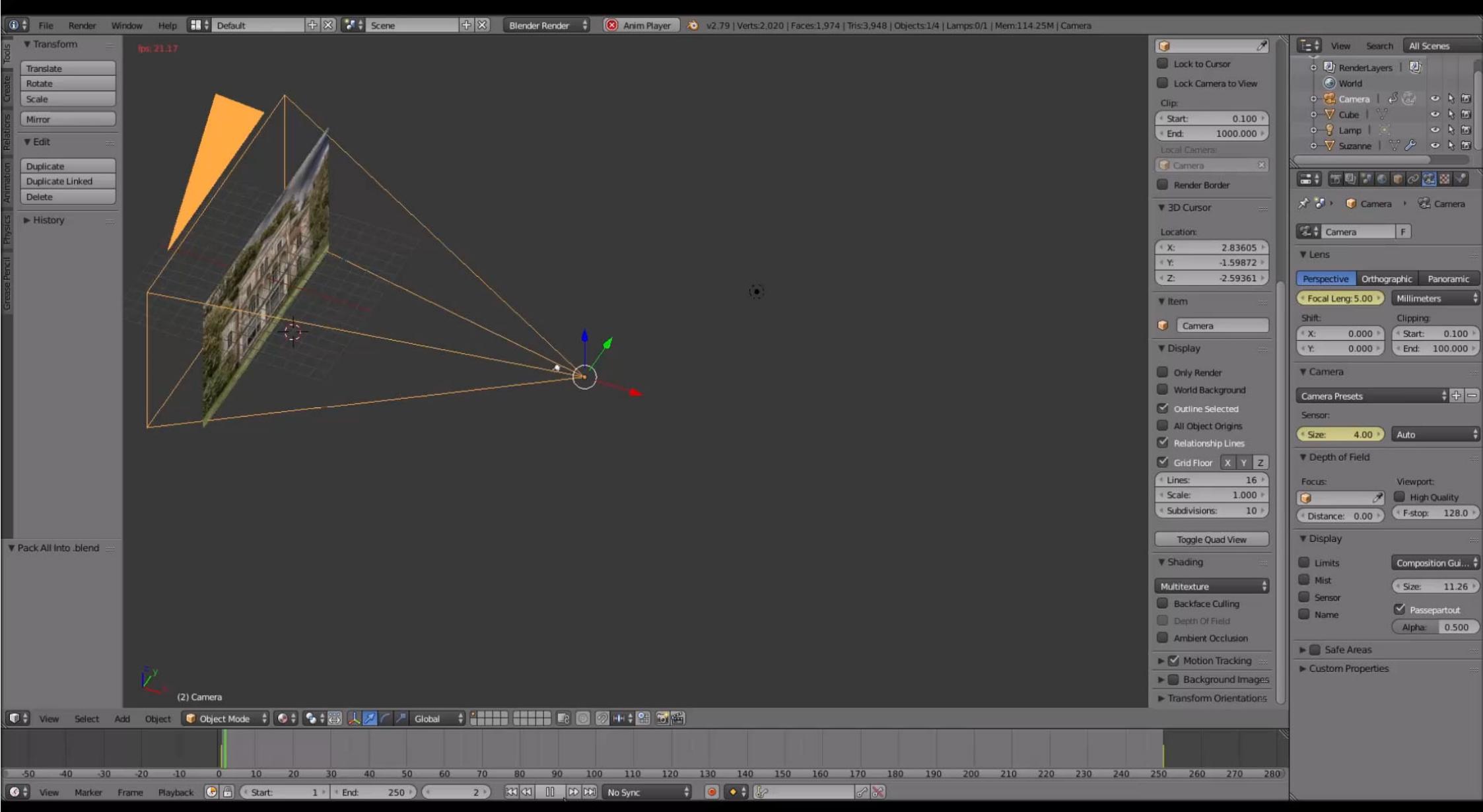
- As objects become more distant, they appear smaller because their visual angle decreases.
- Parallel lines appear to be meeting at a distant point (the vanishing point) on the horizon.



# Perspective (linear perspective)

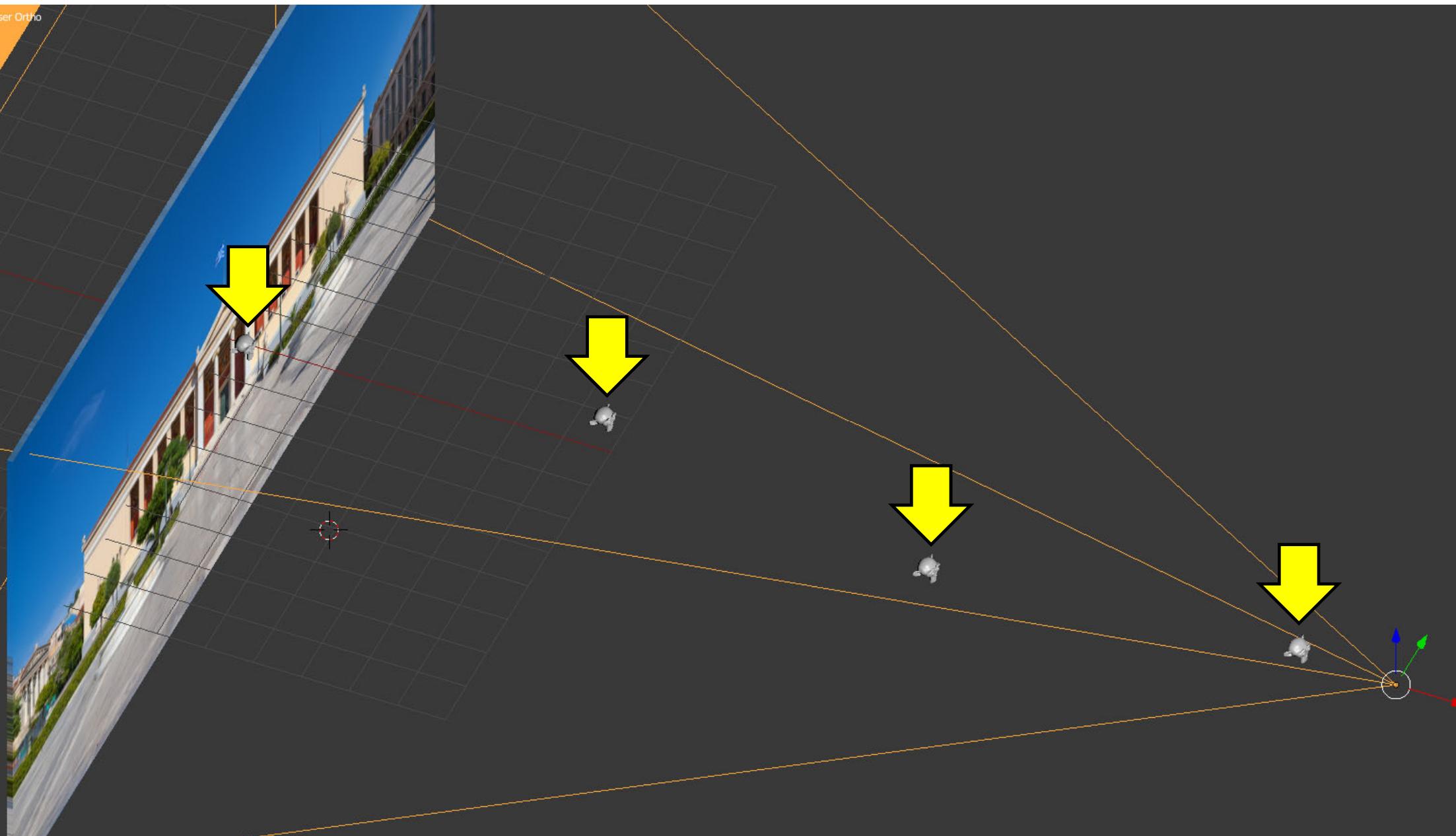
We can compress depth by increasing focal length (photos) or decreasing field-of-view (non-VR renders)







User Ortho





# Telephoto lenses

Some lenses reach 500 mm focal length!



## 5

# Texture gradient

The further apart an object, the higher the spatial frequency of its texture



## 6

# Atmospheric perspective (fog)

Objects that are a great distance away look hazier due to light scattering by the atmosphere

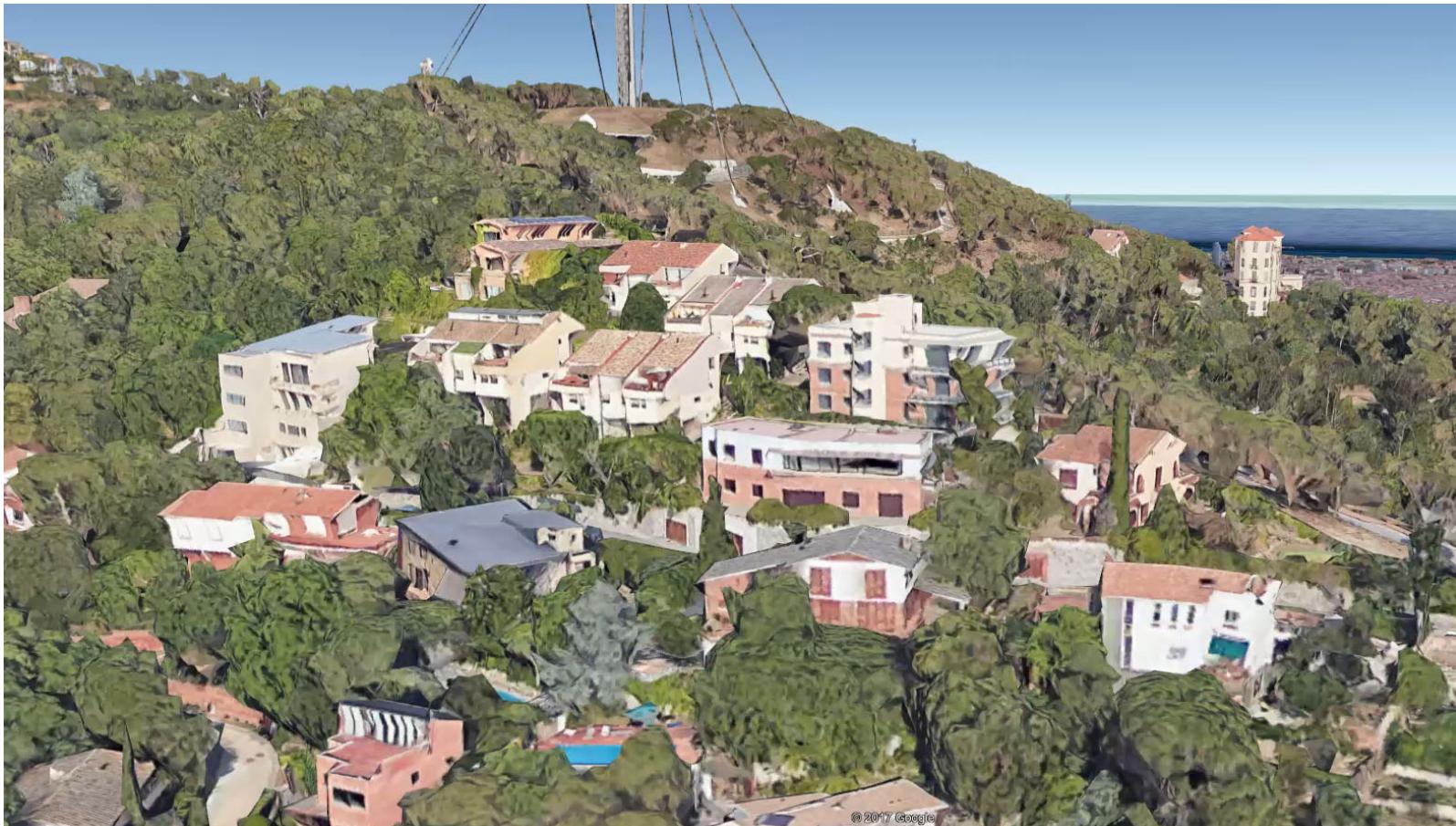


# Atmospheric perspective (fog)



7

# Motion parallax



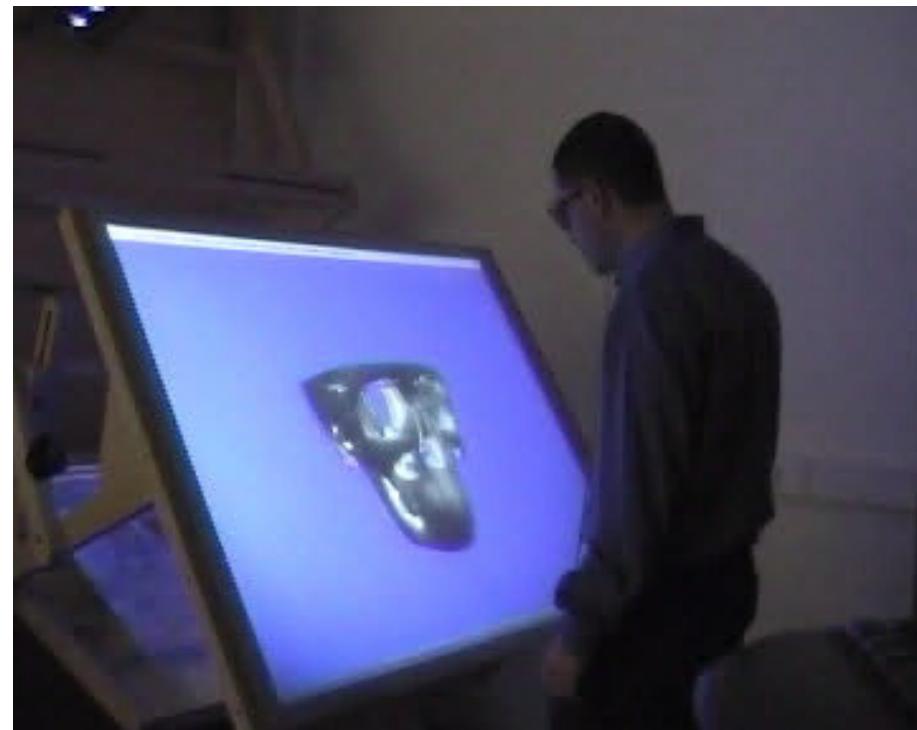


## Occlusion (interposition)

Objects that block other objects appear to be closer.



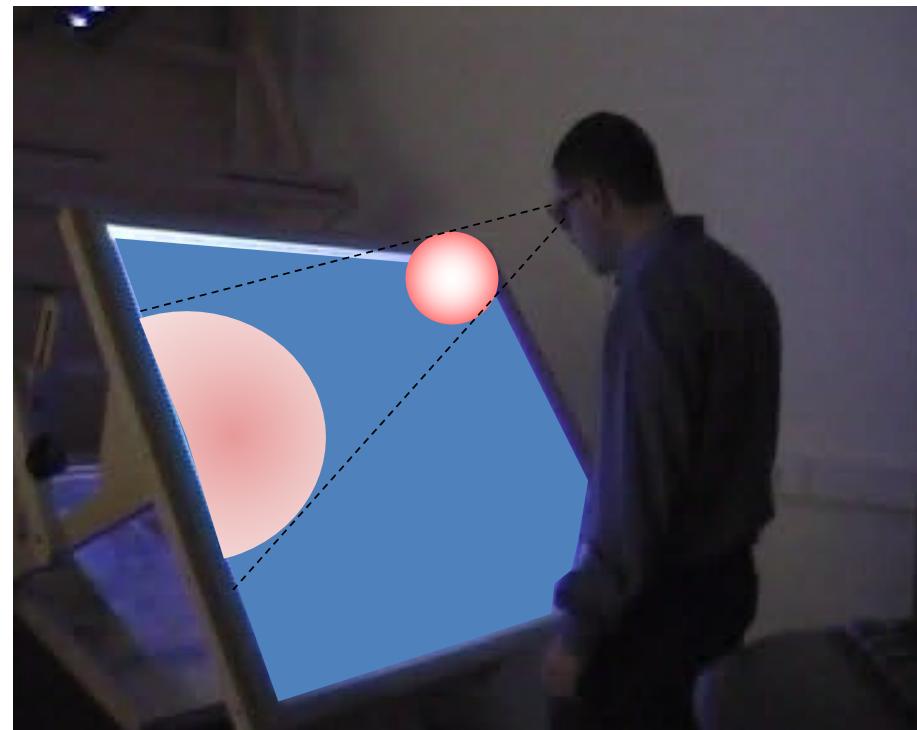
# Occlusion – screen surround



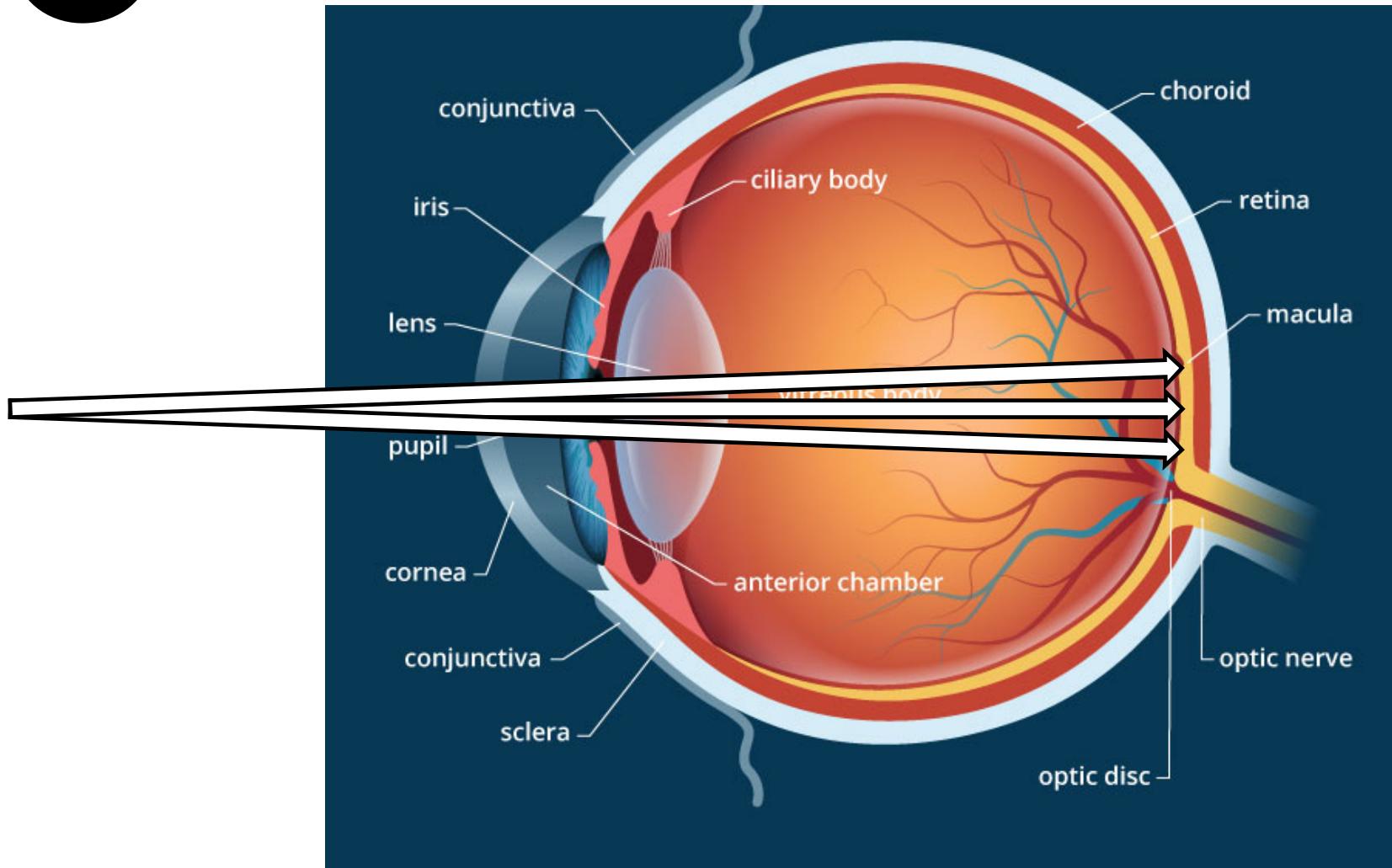
# Occlusion – screen surround



# Occlusion – screen surround

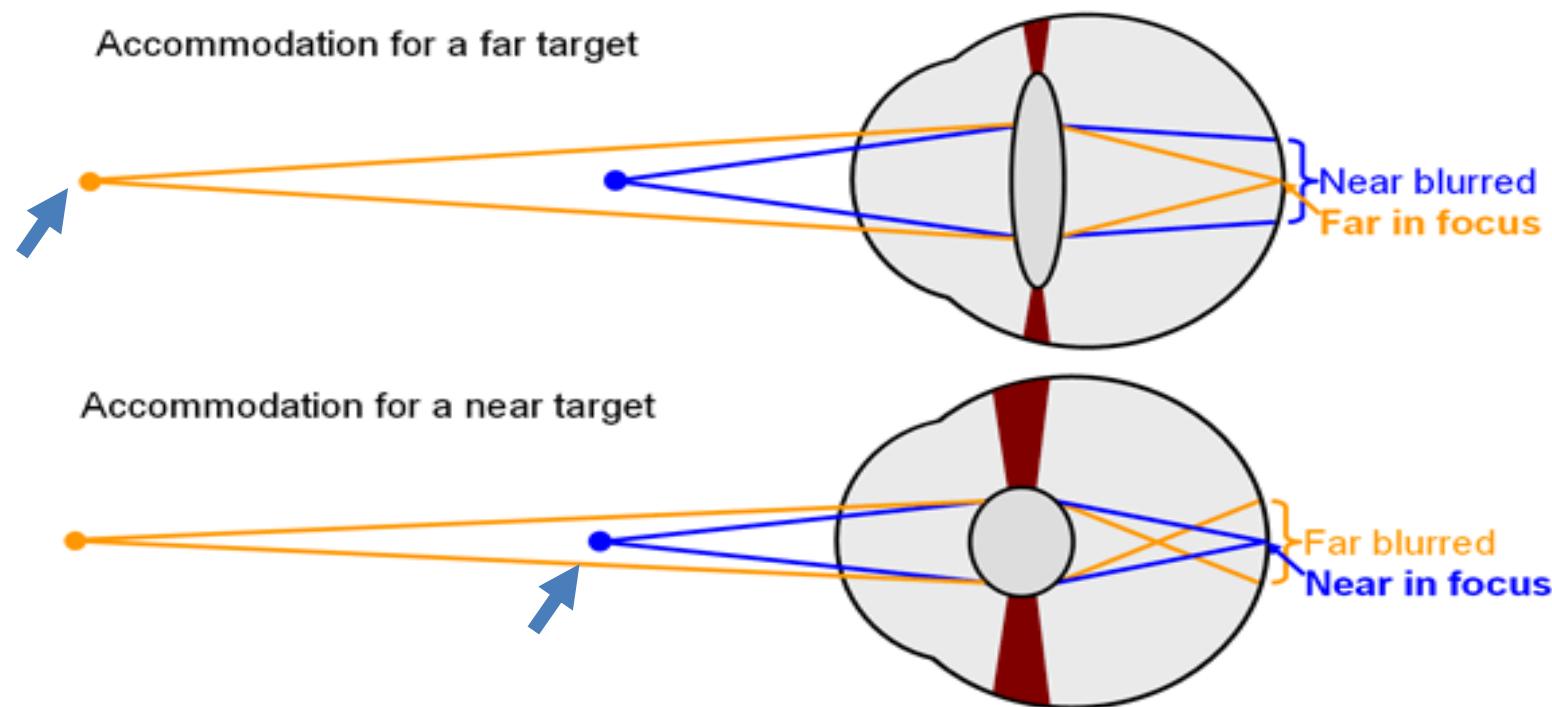
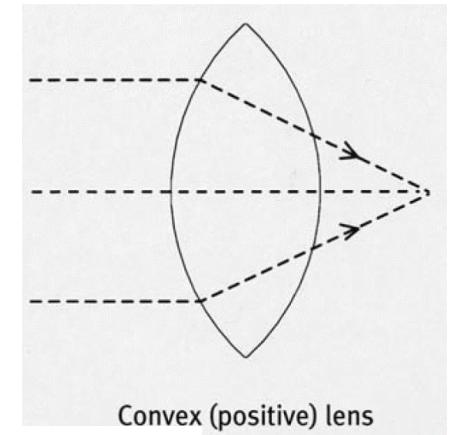


# Accommodation

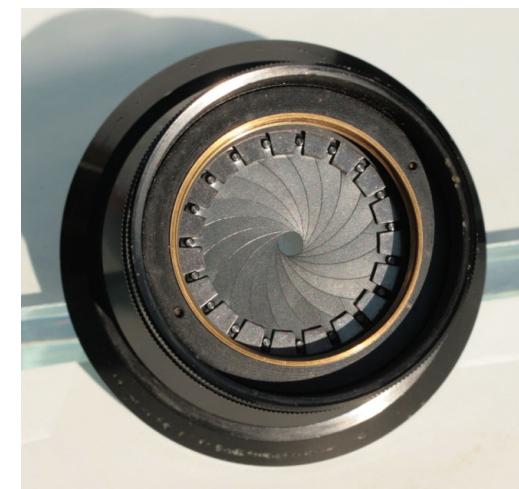
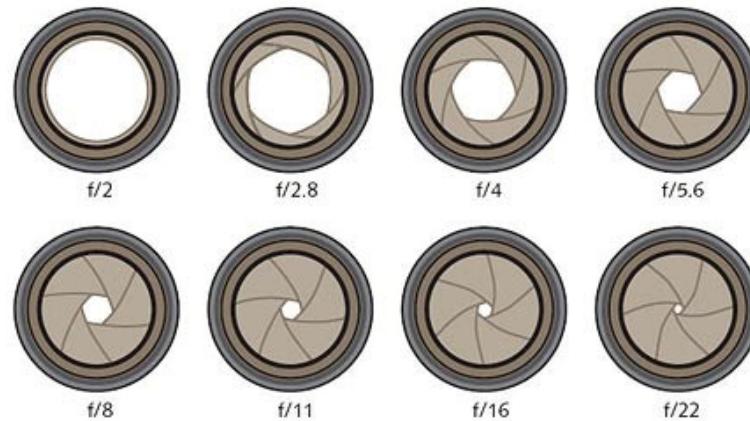
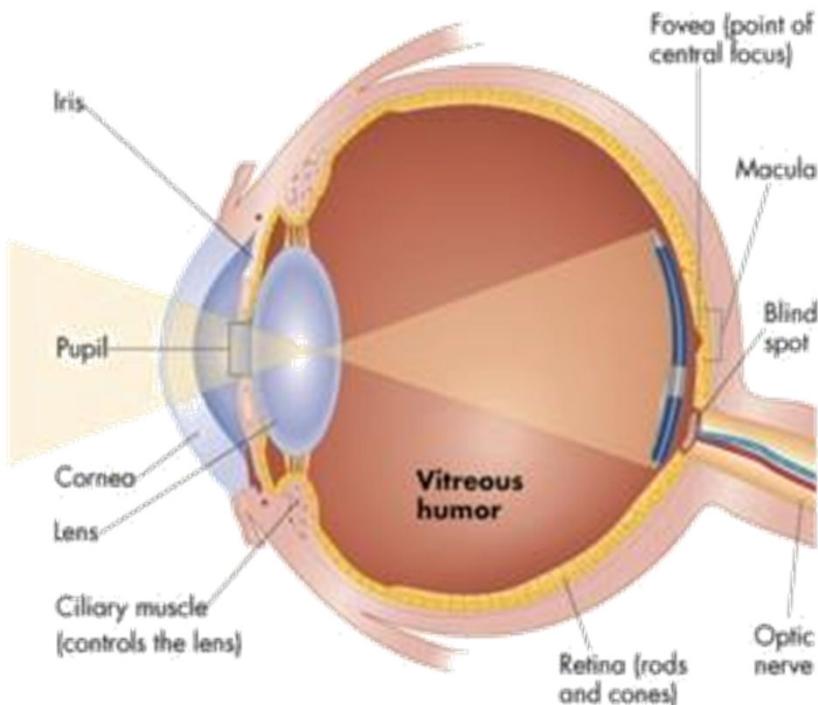


# Accommodation

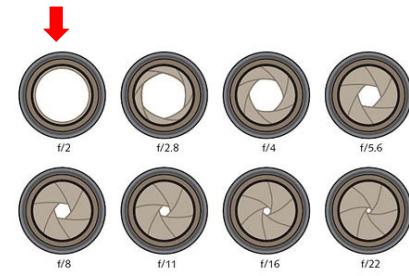
- Deformation of the eye lens (*cristalino*)
- Allows to **focus objects** at some distance



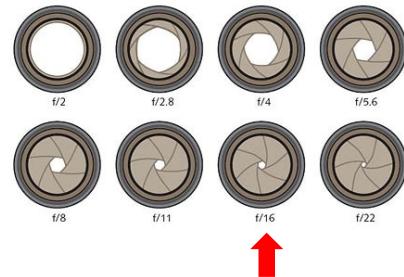
# Accommodation vs pupil size (camera analog)



# Accommodation



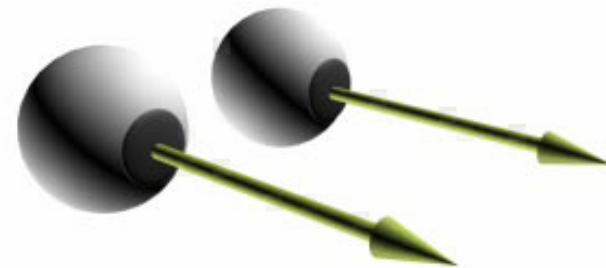
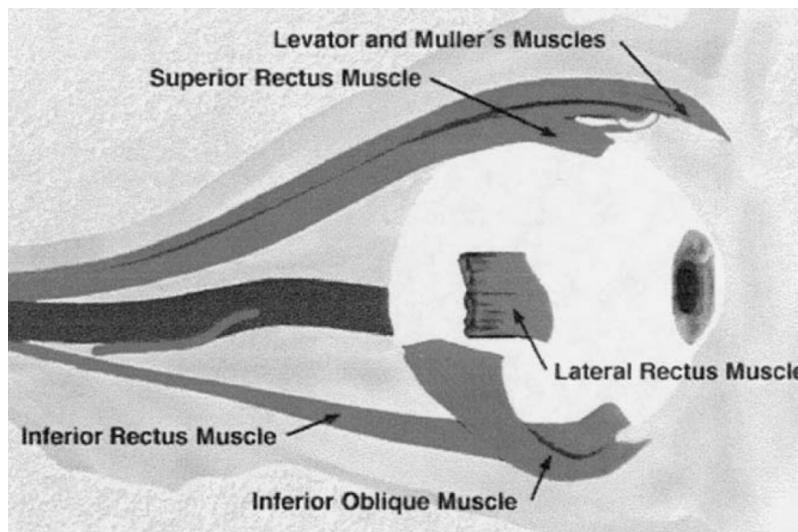
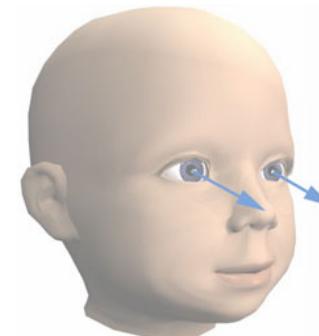
# Accommodation



10

# Convergence

- **Rotation of the eye balls**
- Allows us to place the target at the fovea



# Accommodation & convergence

Points in common:

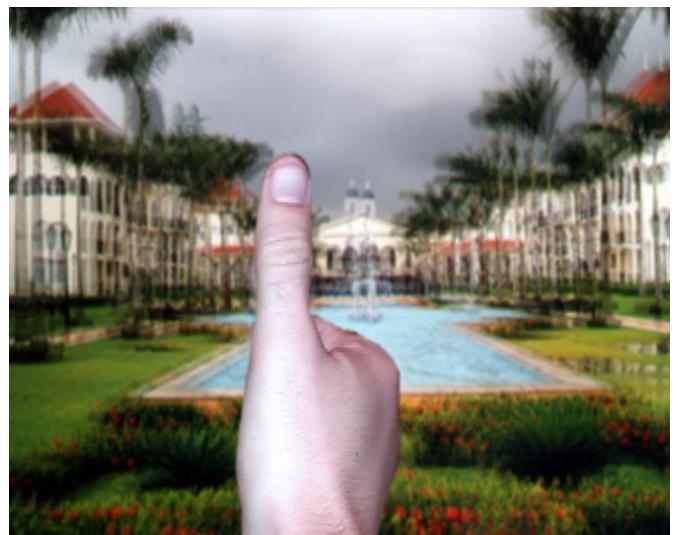
- Both depend on the depth of the fixation point
- Both are depth cues
- There is a natural relationship between accommodation and convergence
- In most VR stereo displays, this relationship is broken → **vision decoupling**

# **RETINAL DISPARITY**

## 11

# Retinal disparity

Difference in the L/R images of an object due to the eyes' horizontal separation

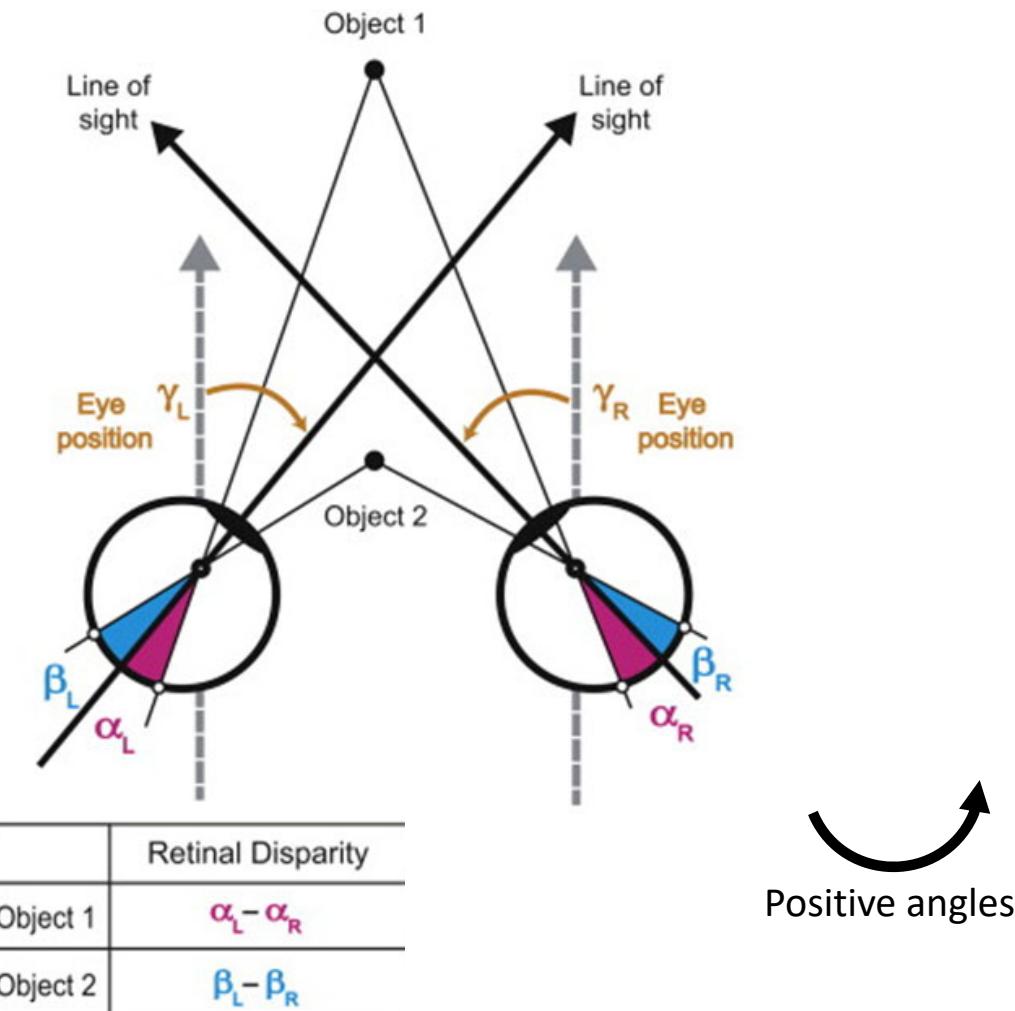


# Fusion and stereopsis

- The HVS combines two images with disparity into a single image with depth.
- This ability is called **fusion** and the resulting sense is called **stereopsis**.

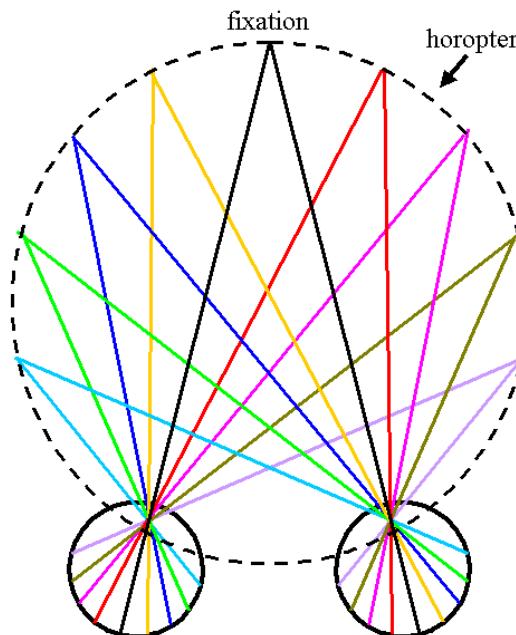


# Retinal disparity (more formally)



# Retinal disparity (more formally)

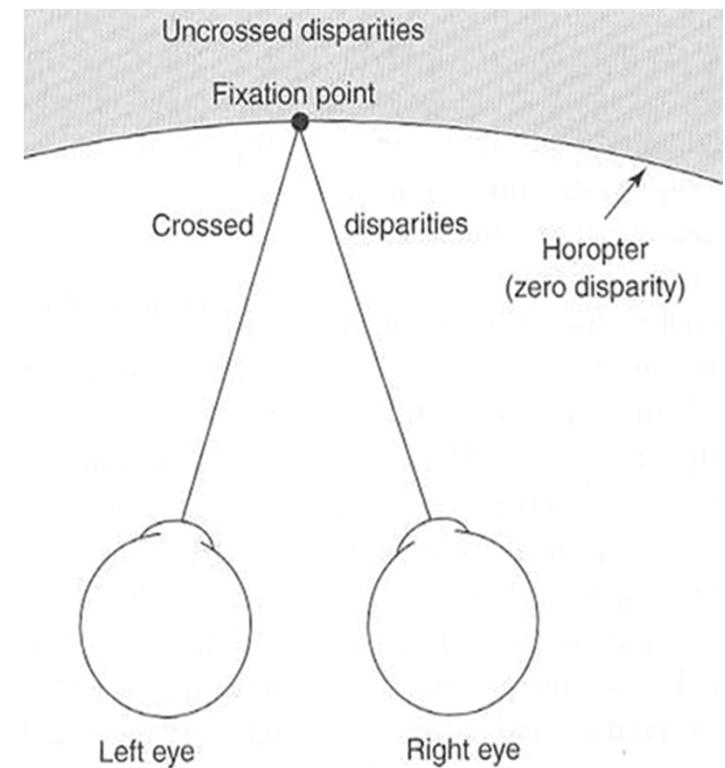
**Horopter:** surface defined by points that, for a given convergence, are projected onto points with **no disparity**



# Retinal disparity (more formally)

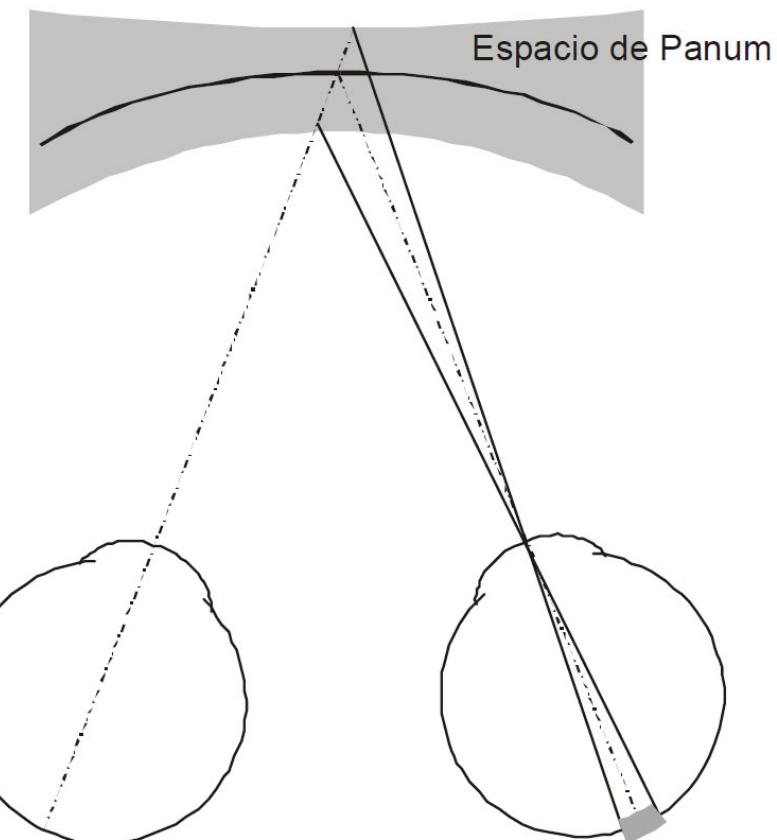
Points closer than the Horopter have **crossed disparity** (negative disparity)

Points farther than the Horopter have **uncrossed disparity** (positive disparity)



# Retinal disparity (more formally)

- **Panum's fusion area:** Space around the horopter where fusion is feasible.
- **Within Panum** points can be fused (resulting in a single image with depth).
- **Outside Panum** fusion fails, producing double images.
- Near the fovea, the maximum binocular disparity resulting in fusion corresponds to a visual angle of about **1/6 of one degree**.



# Retinal disparity

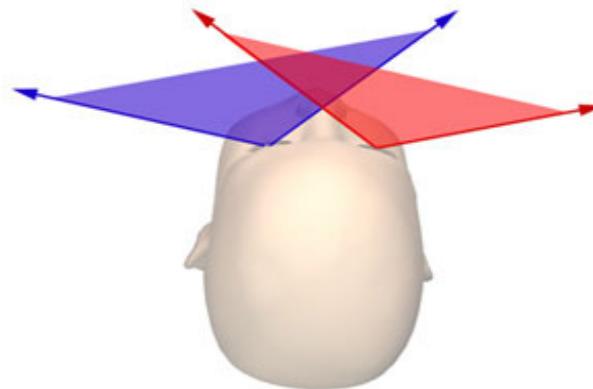
Remember:

- Every scene point has its own retinal disparity.
- If we change fixation point, we change retinal disparities.



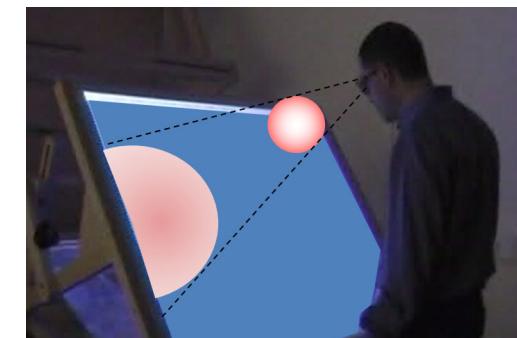
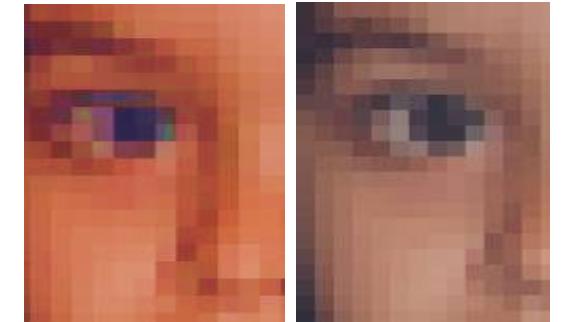
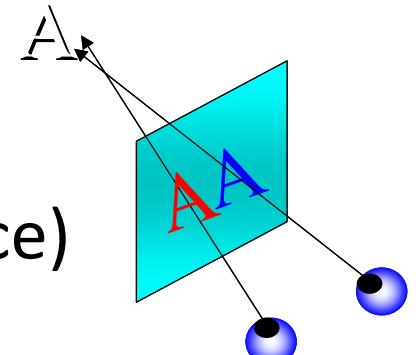
# Human eye fact sheet

- Range IOD: 5 - 7.5 cm
- Average IOD: 6.3 – 6.6 cm
- Eye field-of-view: 160°-180° hor, 130° vert
- Horizontal overlap: 140°



# Summary of issues

- Vision-decoupling (accommodation vs convergence)
- Image congruence (correspondence problem)
- Depth cue conflicts (e.g. Screen surround)



Two screens, one screen, no screen

# TAXONOMY OF 3D DISPLAYS

# According to number of screens

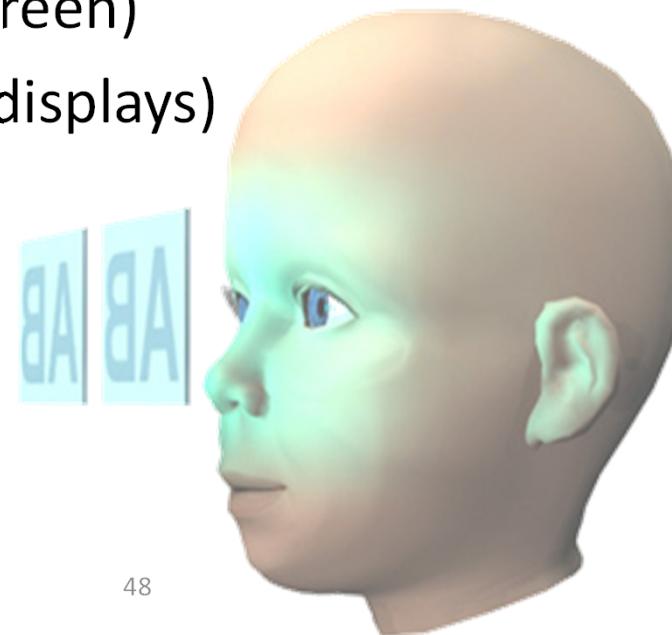
Where are the L/R images projected onto?

- Two independent screen regions (eg HMD)
- A single screen (3D TV, 3D cinema, CAVE...)
- Directly onto the retina (no screen)
- Spinning screen (holographic displays)

# According to number of screens

Where are the L/R images projected onto?

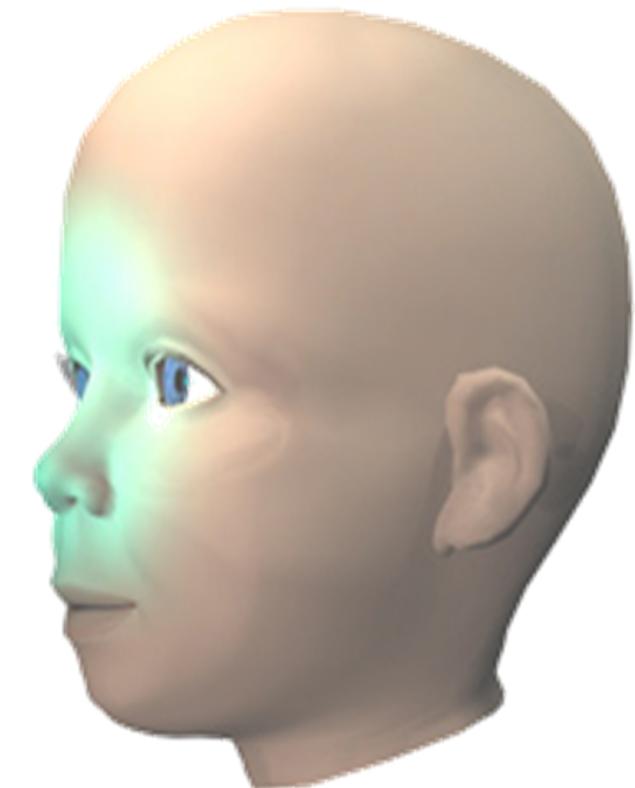
- **Two independent screen regions (eg HMD)**
- A single screen (3D TV, 3D cinema, CAVE...)
- Directly onto the retina (no screen)
- Spinning screen (holographic displays)



# According to number of screens

Where are the L/R images projected onto?

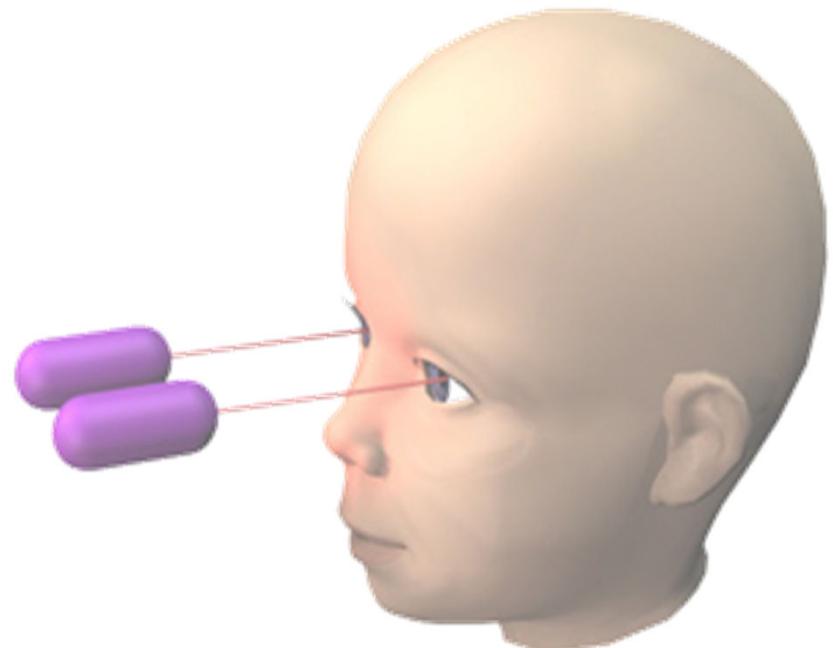
- Two independent screen regions (eg HMD)
- **A single screen (3D TV, 3D cinema, CAVE...)**
- Directly onto the retina (no screen)
- Spinning screen (holographic displays)



# According to number of screens

Where are the L/R images projected onto?

- Two independent screen regions (eg HMD)
- A single screen (3D TV, 3D cinema, CAVE...)
- **Directly onto the retina (no screen)**
- Spinning screen (holographic displays)



- Laser emitters
- Virtual Retinal Display, VRD

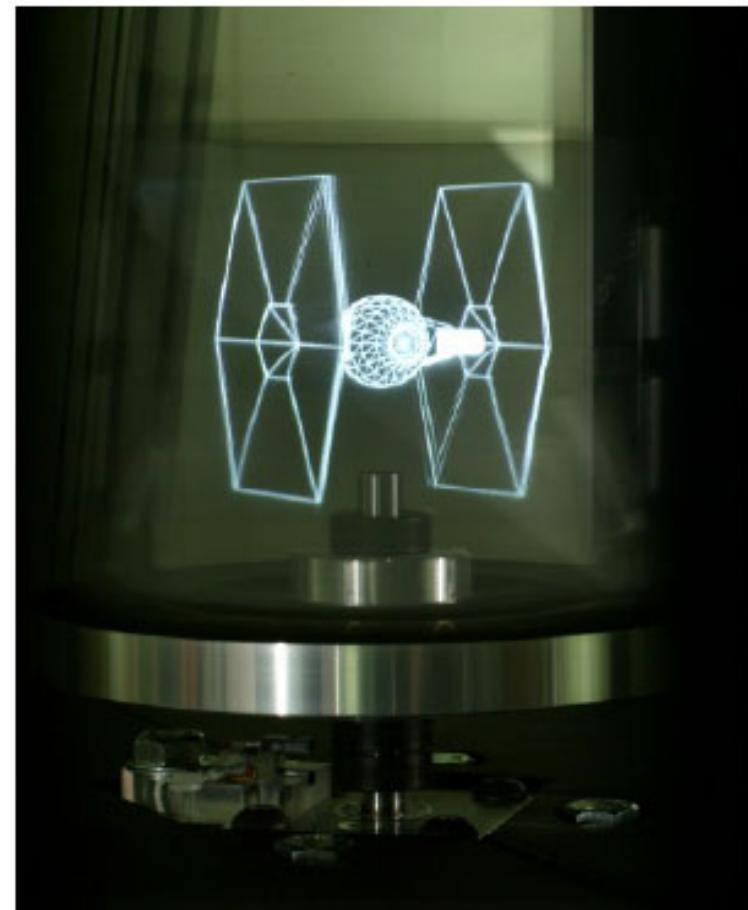
<http://www.hitl.washington.edu/projects/vrd/project.html>

# According to number of screens

Where are the L/R images projected onto?

- Two independent screen regions (eg HMD)
- A single screen (3D TV, 3D cinema, CAVE...)
- Directly onto the retina (no screen)
- **Spinning screen (holographic displays)**
  - Lab prototypes
  - Example: spinning mirror with a high-speed projector

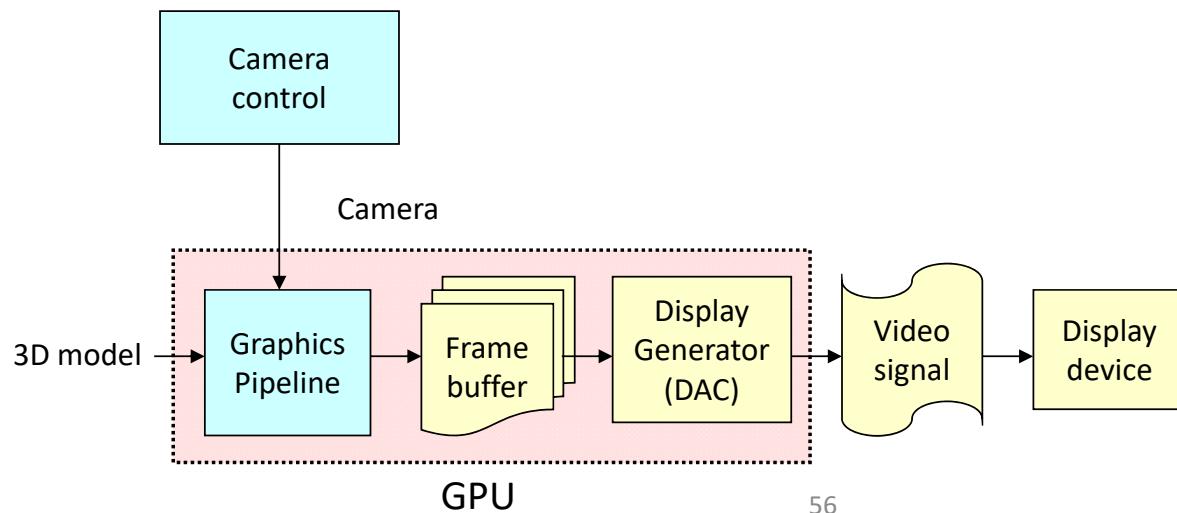
<https://www.youtube.com/watch?v=8gvPS1m40gw>



# **SYNTHESIS OF STEREO IMAGES**

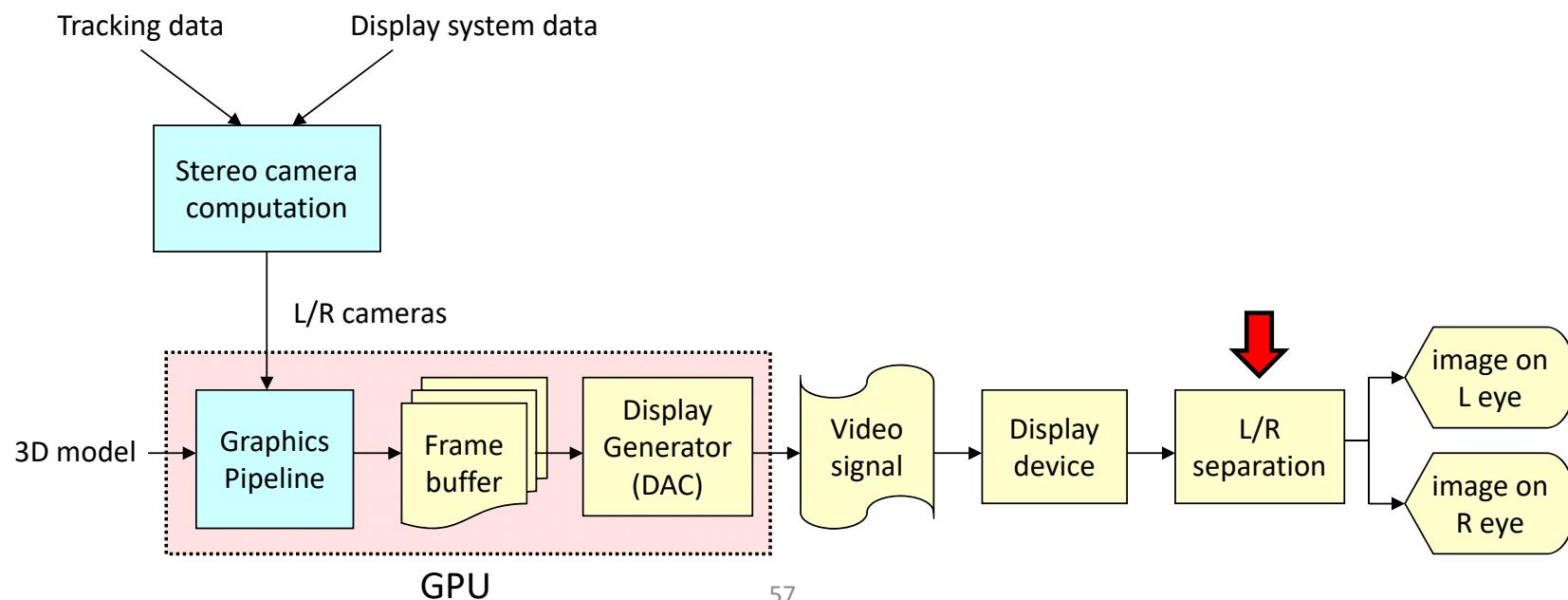
# Synthesis of non-stereo images

- Input: 3D model, tracking data, display system data
- Output: images with retinal disparity



# Synthesis of stereo images

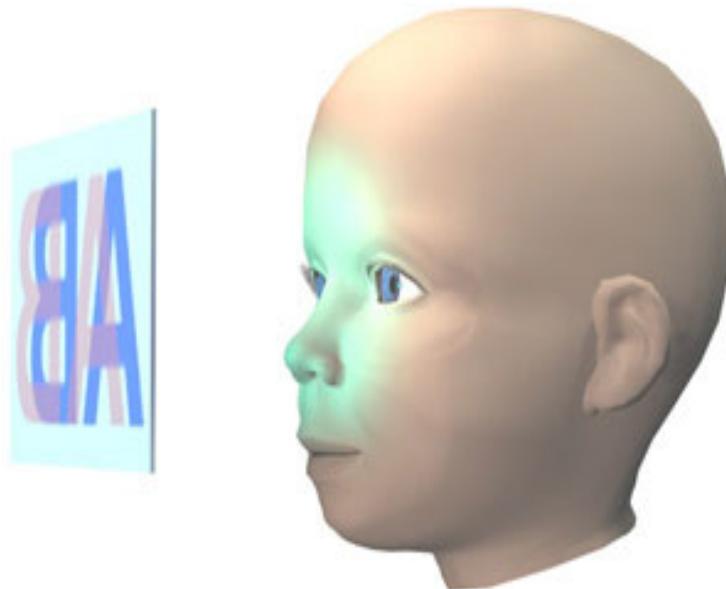
- Input: 3D model, tracking data, display system data
- Output: images with retinal disparity



# **IMAGE SEPARATION**

# Image separation

- Separation = means for providing each eye with its needed image (and rejecting the unnecessary image).
- Required when a single screen surface contains both images.



# Image separation

## Classification

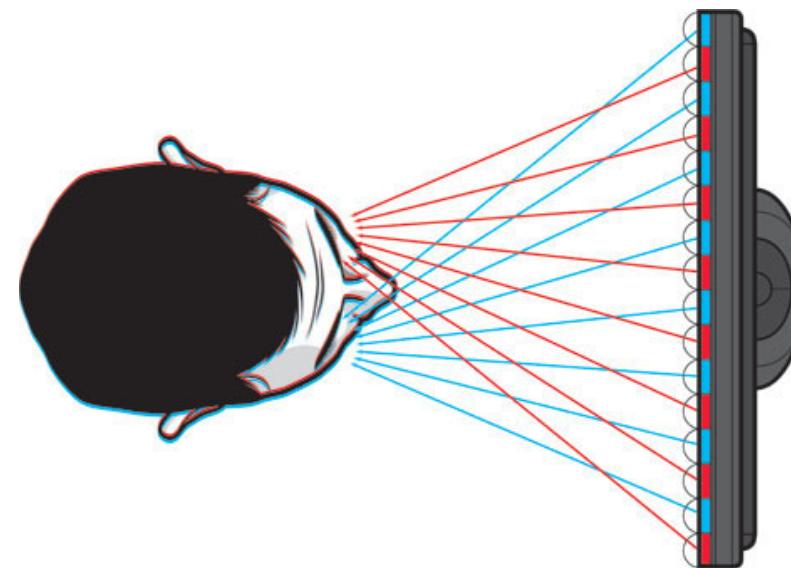
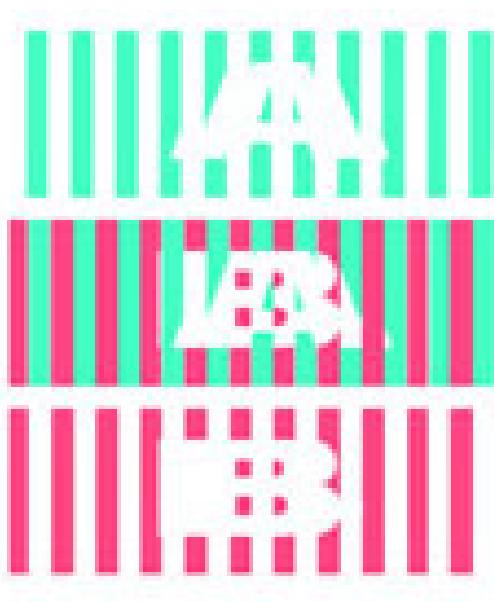
- Autostereoscopic displays
  - Glasses
    - Anaglyph glasses
    - Infitec glasses
    - Polarizing glasses
    - Shutter-glasses
- 
- ```
graph TD; A[Image separation] --> B[Glasses]; B --> C[Autostereoscopic displays]; B --> D[Glasses]; D --> E[Anaglyph glasses]; D --> F[Infitec glasses]; D --> G[Polarizing glasses]; D --> H[Shutter-glasses]; C --- D; D --- E; D --- F; D --- G; D --- H; G --- I[Passive stereo]; H --- J[Active stereo]
```

# Image separation

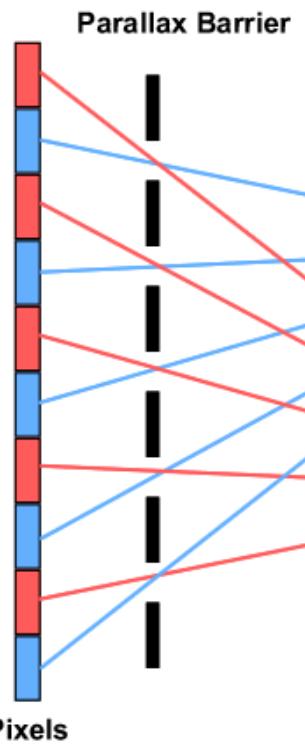
## Classification

- **Autostereoscopic displays**
  - Glasses
    - Anaglyph glasses
    - Infitec glasses
    - Polarizing glasses
    - Shutter-glasses
- 
- ```
graph LR; Glasses[Glasses] --> Passive[Passive stereo]; Glasses --> Active[Active stereo]; Passive --- Anaglyph["Anaglyph glasses"]; Passive --- Infitec["Infitec glasses"]; Passive --- Polarizing["Polarizing glasses"]; Active --- Shutter["Shutter-glasses"];
```

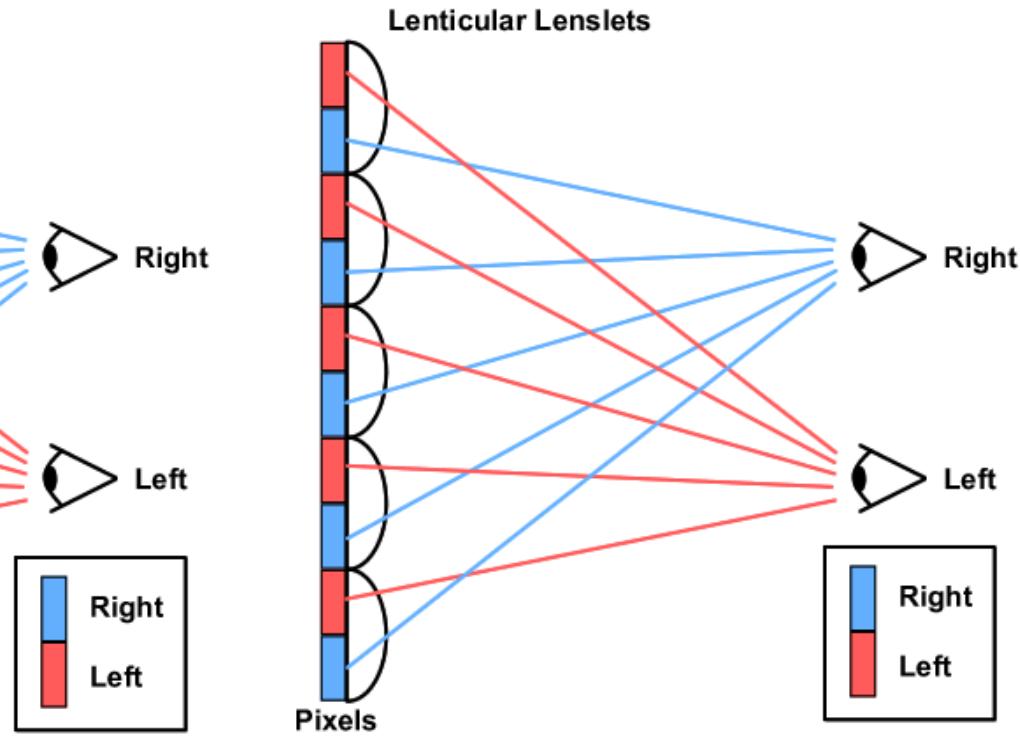
# Autostereoscopic displays



# Autostereoscopic displays



[www.3d-forums.com](http://www.3d-forums.com)



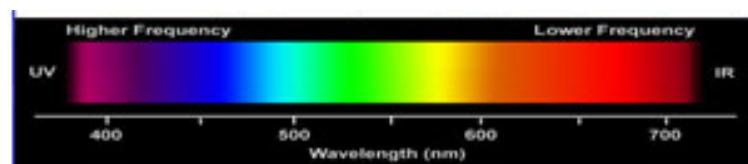
[www.3d-forums.com](http://www.3d-forums.com)

# Image separation

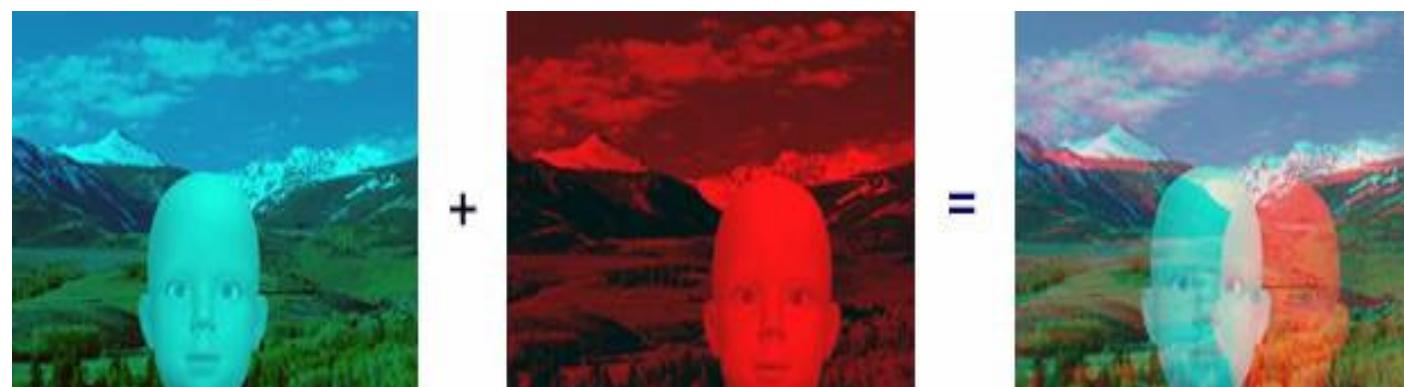
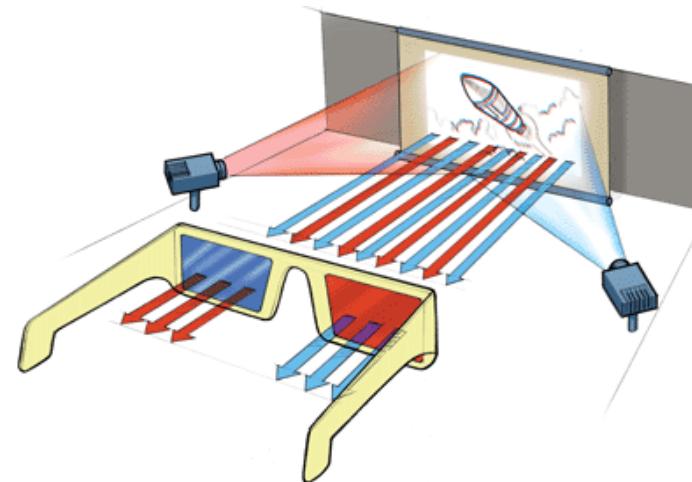
## Classification

- Autostereoscopic displays
  - Glasses
    - **Anaglyph glasses**
    - Infitec glasses
    - Polarizing glasses
    - Shutter-glasses
- 
- ```
graph LR; A[Glasses] --> B[Anaglyph glasses]; A --> C[Infitec glasses]; A --> D[Polarizing glasses]; A --> E[Shutter-glasses]; B --- F[Passive stereo]; E --- G[Active stereo]
```

# Anaglyph filters

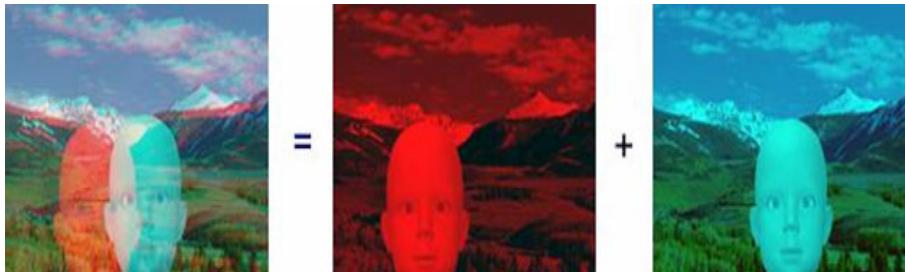


Visible Light



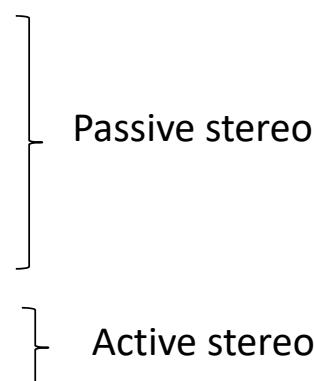
# Anaglyph filters

- Based on complementary colors:
  - R-GB, G-RB, B-RG
- Example: red-cyan, left filter blocks G and B; leaves R.
- Cheap
- Obvious color problems



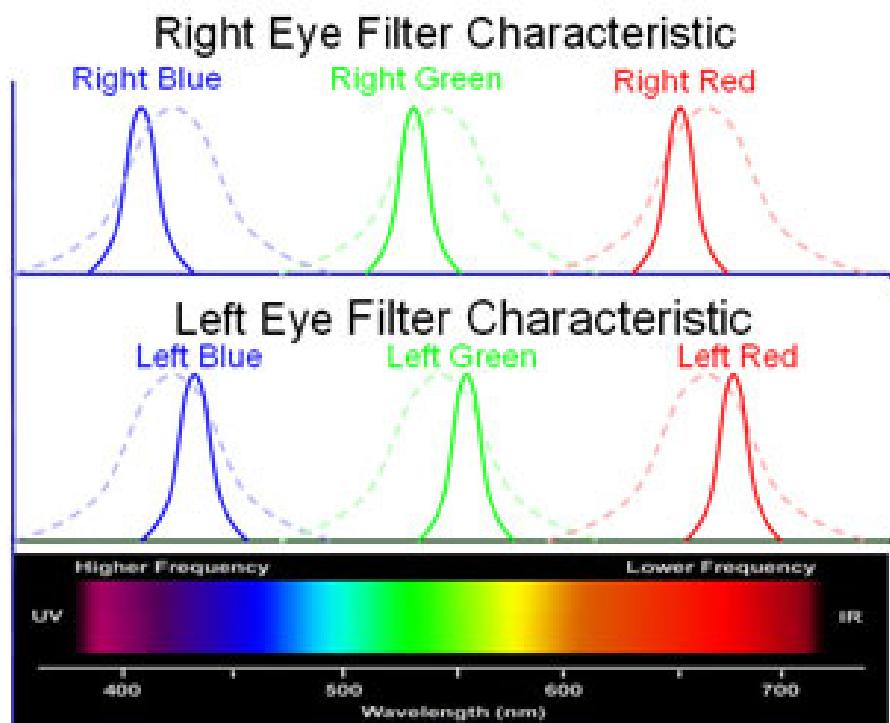
# Image separation

## Classification

- Autostereoscopic displays
  - Glasses
    - Anaglyph glasses
    - **Infitec glasses**
    - Polarizing glasses
    - Shutter-glasses
- 
- Passive stereo
- Active stereo

# Infitec glasses (Dolby 3D digital cinema)

Improved version of anaglyph glasses



Visible Light

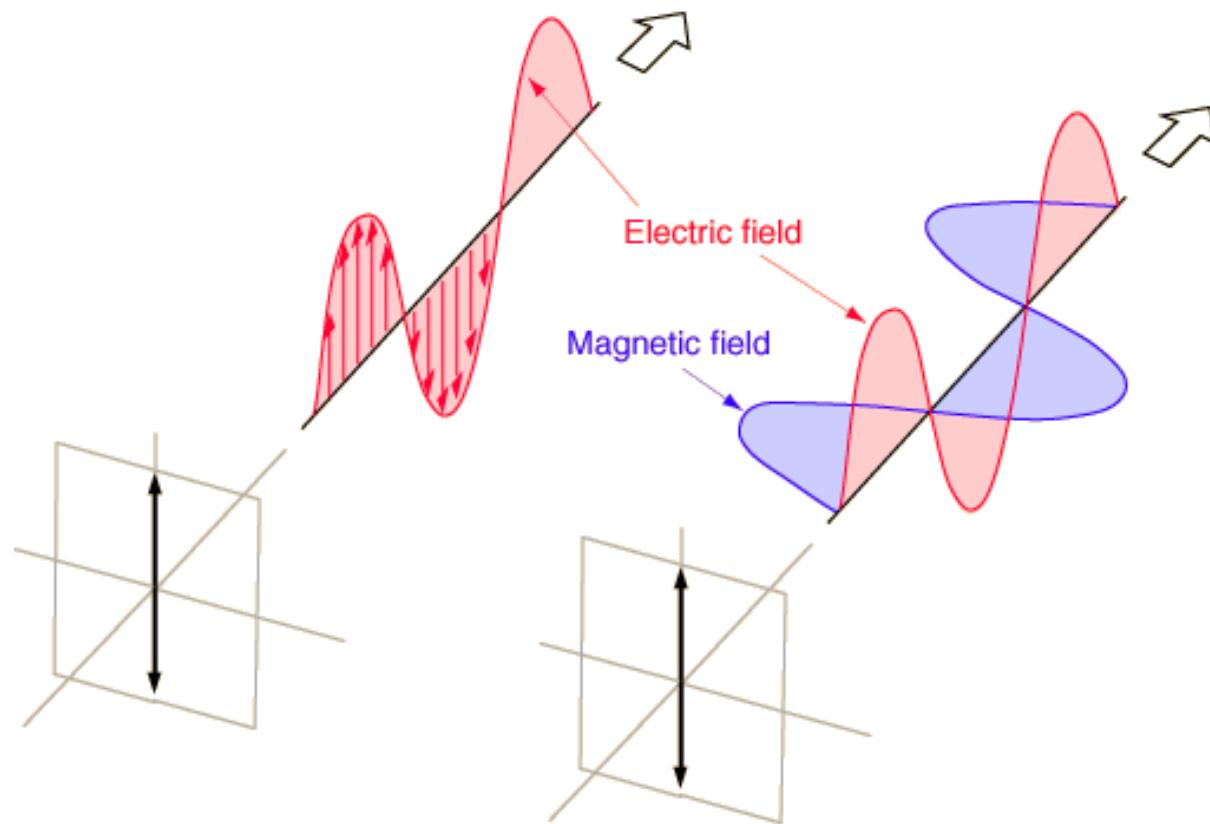


# Image separation

## Classification

- Autostereoscopic displays
  - Glasses
    - Anaglyph glasses
    - Infitec glasses
    - **Polarizing glasses**
    - Shutter-glasses
- 
- ```
graph LR; Glasses[Glasses] --> Passive[Passive stereo]; Glasses --> Active[Active stereo]; Passive --- Anaglyph["– Anaglyph glasses"]; Passive --- Infitec["– Infitec glasses"]; Passive --- Polarizing["– Polarizing glasses"]; Active --- Shutter["– Shutter-glasses"];
```

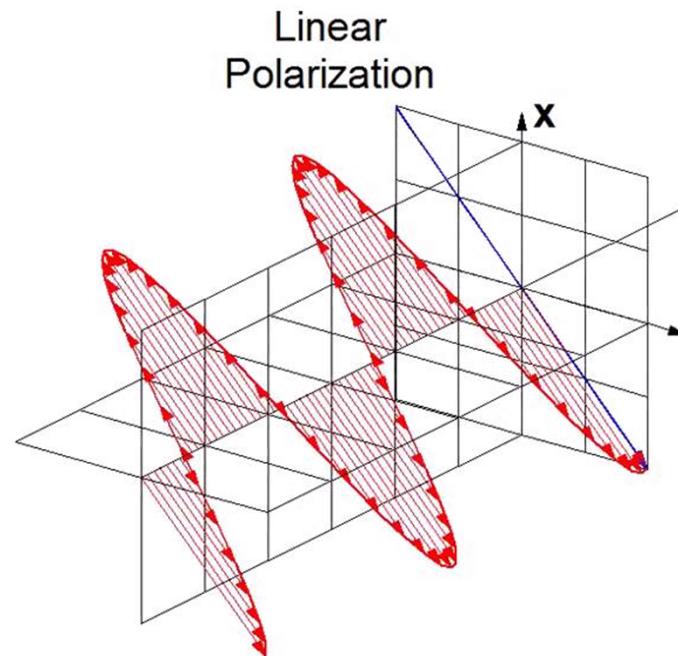
# Polarization



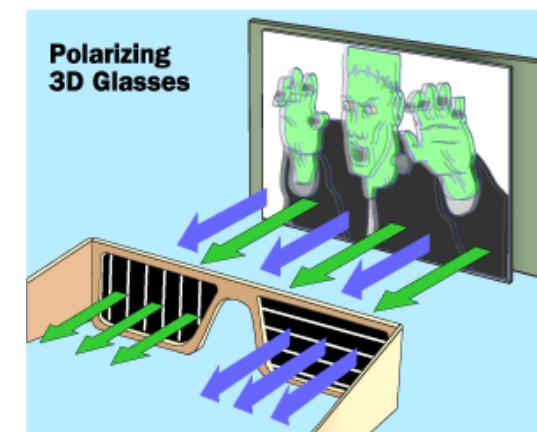
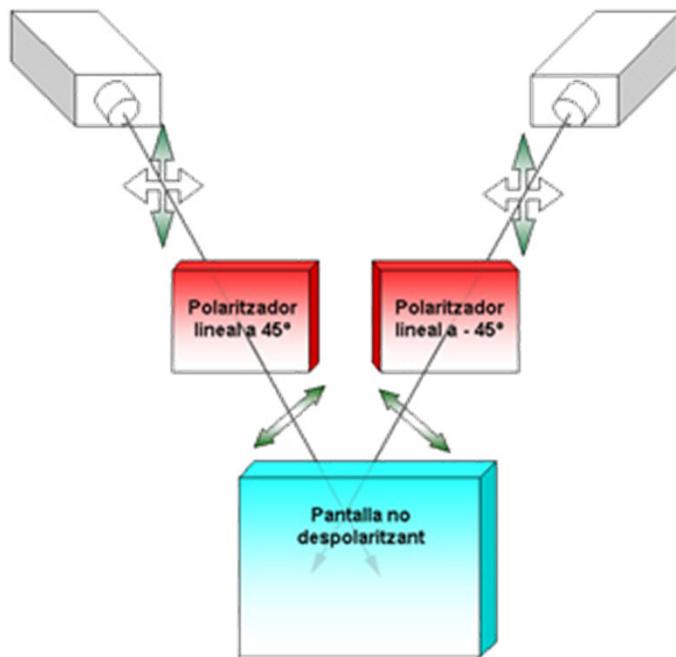
See this video: <https://www.youtube.com/watch?v=8YkfEft4p-w>

# Linear polarizing glasses

- Based on linear polarization filters
  - In the projectors
  - In the glasses
- Oriented at 90°
- Cheap
- Sensible to head tilt

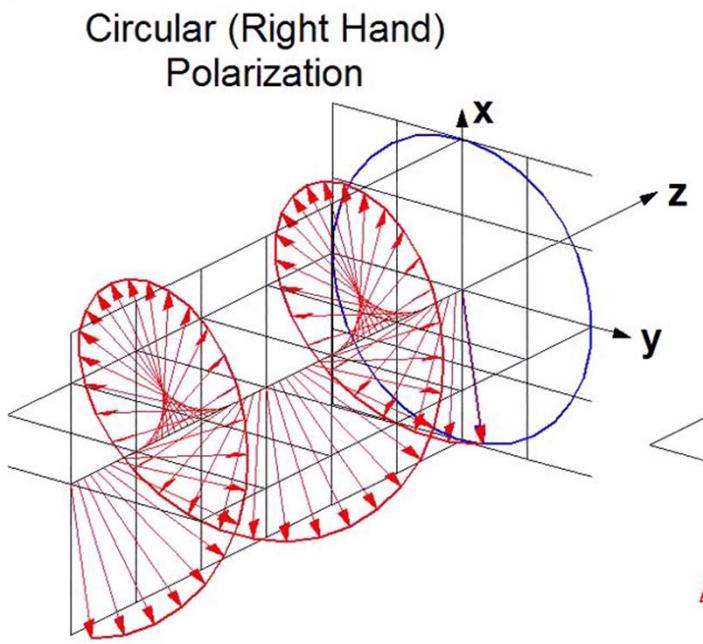


# Linear polarizing glasses



# Circular polarizing glasses

- Based on circular polarization filters (projectors & glasses)
- Cheap
- Almost head-tilt insensitive



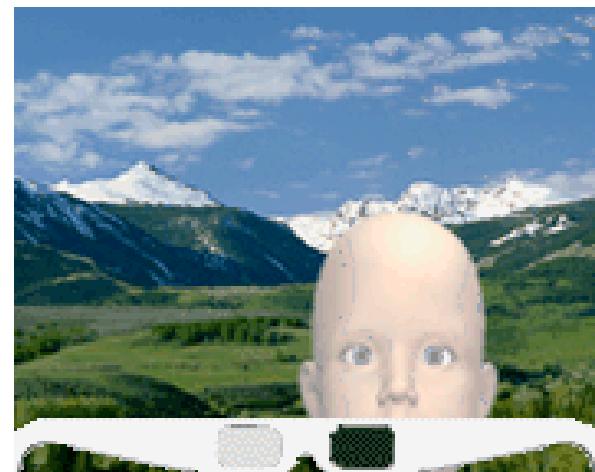
# Image separation

## Classification

- Autostereoscopic displays
  - Glasses
    - Anaglyph glasses
    - Infitec glasses
    - Polarizing glasses
    - **Shutter-glasses**
- 
- ```
graph LR; Glasses[Glasses] --> Passive[Passive stereo]; Glasses --> Active[Active stereo]; Passive --- Anaglyph["– Anaglyph glasses"]; Passive --- Infitec["– Infitec glasses"]; Passive --- Polarizing["– Polarizing glasses"]; Active --- Shutter["– Shutter-glasses"];
```

# Shutter glasses

- LC shutter blocks light, sync with the video signal.
- In any given time, one filter is in *transparent state* and the other in *opaque state*.
- Requires a display running at >100 Hz
- Sync types:
  - Infrared signal
  - Wired



# Shutter glasses

Sync source:

- Stereo-readycards
  - Dedicated signal (eg VESA mini DIN-3)
- Non-stereo-ready cards:
  - VGA connector (pass-through)

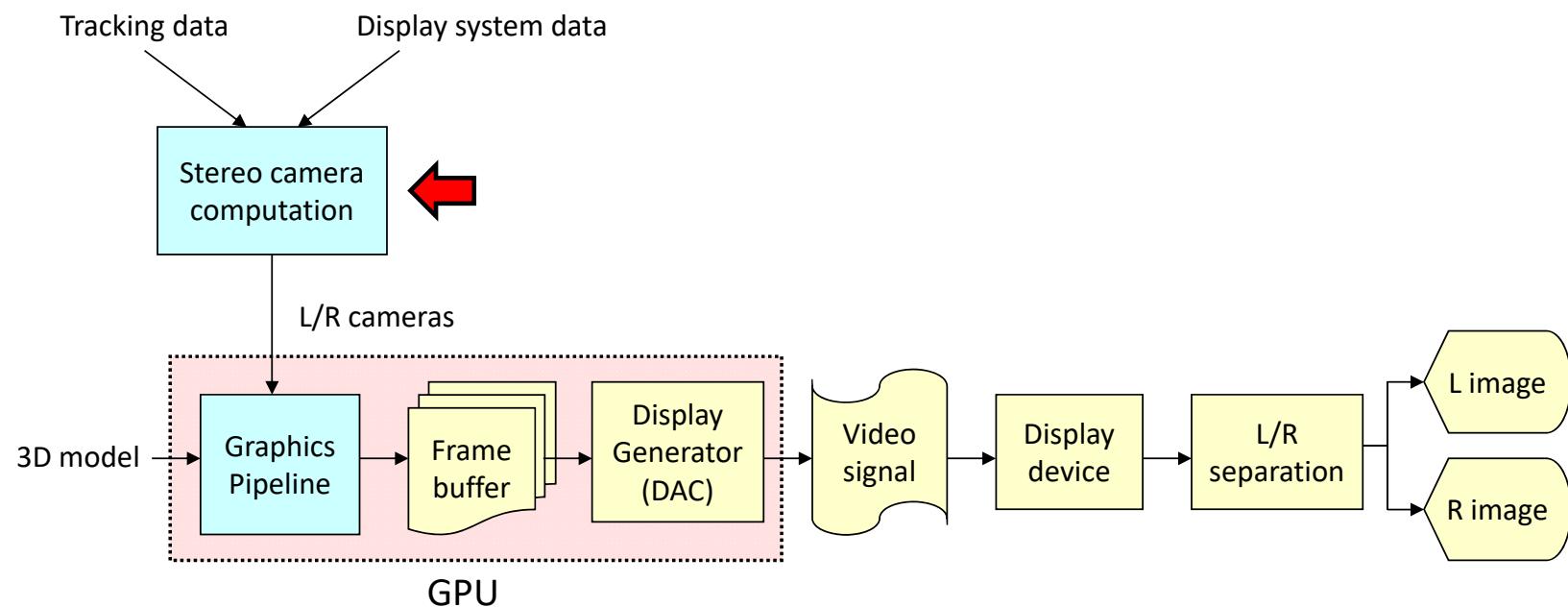


# Comparison

| Technology     | Glasses            | Sensitive to... |           | Glasses Cost | Suitable for      |
|----------------|--------------------|-----------------|-----------|--------------|-------------------|
|                |                    | Head Pos        | Head Tilt |              |                   |
| Lenticular     | No glasses         | Y               | Y         | -            | TV, Nintendo-like |
| Anaglyph       | Red/Cyan           | N               | N         | Low          | Photos            |
| Infitec        | Infitec            | N               | N         | High         | VR, cinema        |
| Passive stereo | Polarizing glasses | N               | Y         | Mid          | VR, TV, cinema    |
| Active stereo  | Shutter glasses    | N               | N         | High         | VR, TV            |

# **STEREO CAMERA COMPUTATION**

# Synthesis of stereo images



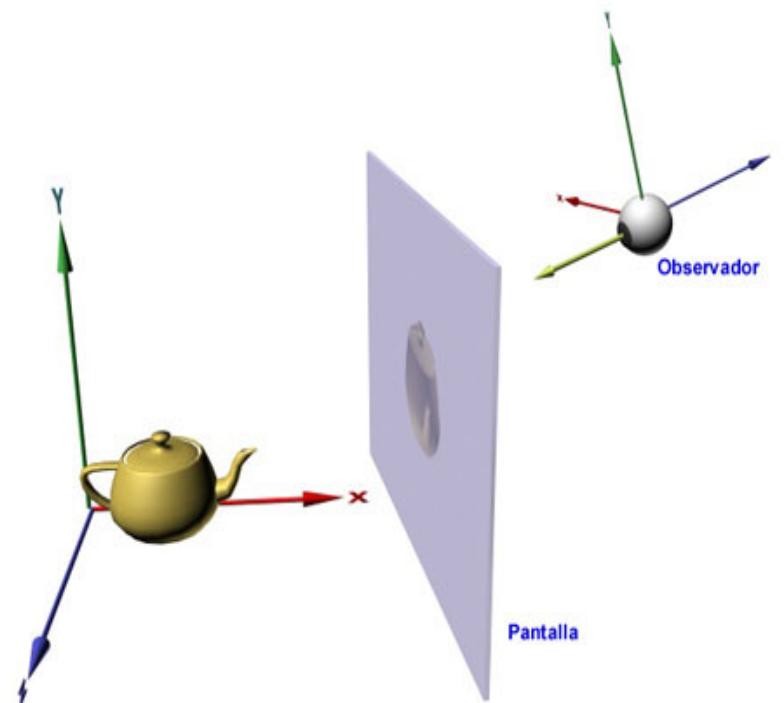
# Stereo camera computation

Output: Left and Right cameras:

- Extrinsic parameters: Eye (OBS), target (VRP), up (VUV) → `lookAt(eye.x, eye.y, eye.z, target.x, target.y, target.z, up.x, up.y, up.z);`
- Intrinsic parameters: view frustum geometry → `frustum(left, right, bottom, top, near, far);`

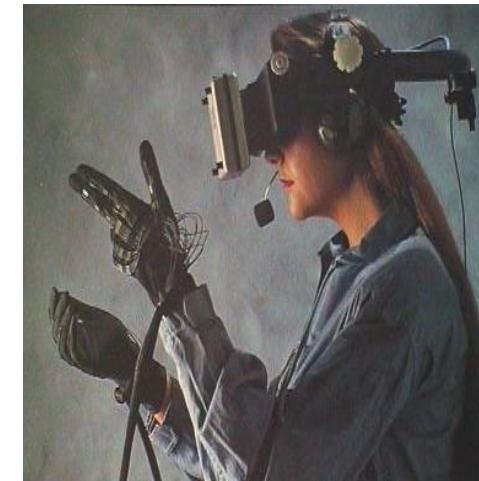
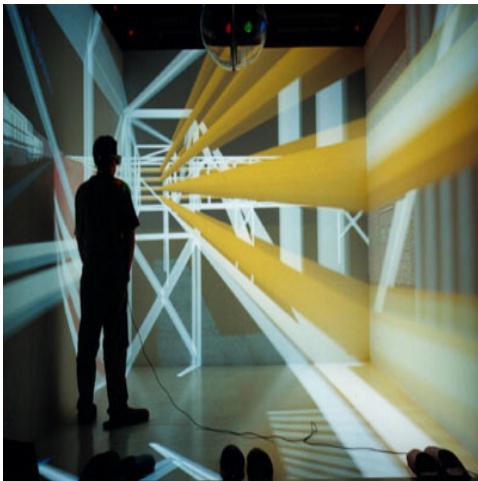
# Stereo rendering

- The virtual camera must be computed taking into account:
  - Screen geometry (size, position, orientation)
  - The eye position with respect to the screen.
- This is absolutely required:
  - On tiled-displays
  - On multi-screen displays
  - On head-tracked displays



# Configurations

- Projection-based VR (+ head-tracking)
- VR monitor (without head tracking)
- Head-Mounted displays



# Projection-based systems

Applies to CAVEs, Stereowalls...

Parameters:

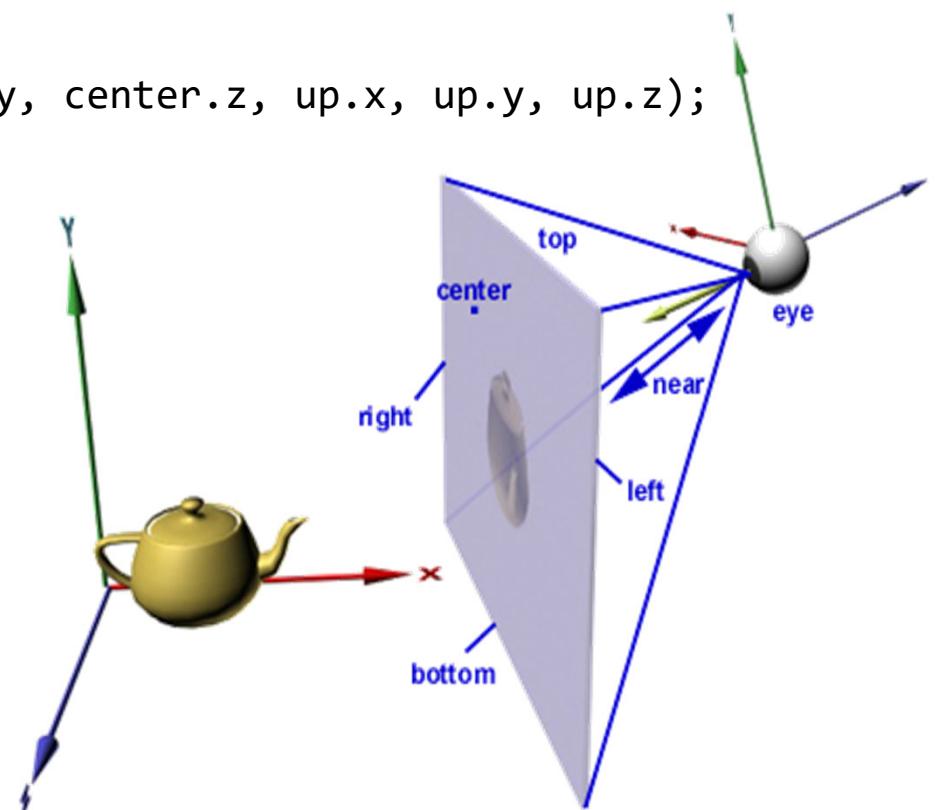
- Tracking data: L/R eye position
  - Two position trackers (3DOF each)
  - One 6DOF tracker (head, glasses...)
- Display system data
  - Screen geometry



# Projection-based systems

```
// Using OpenGL Compatibility mode for clarity...
glMatrixMode(GL_MODELVIEW);
glLoadIdentity();
gluLookAt(eye.x, eye.y, eye.z, center.x, center.y, center.z, up.x, up.y, up.z);

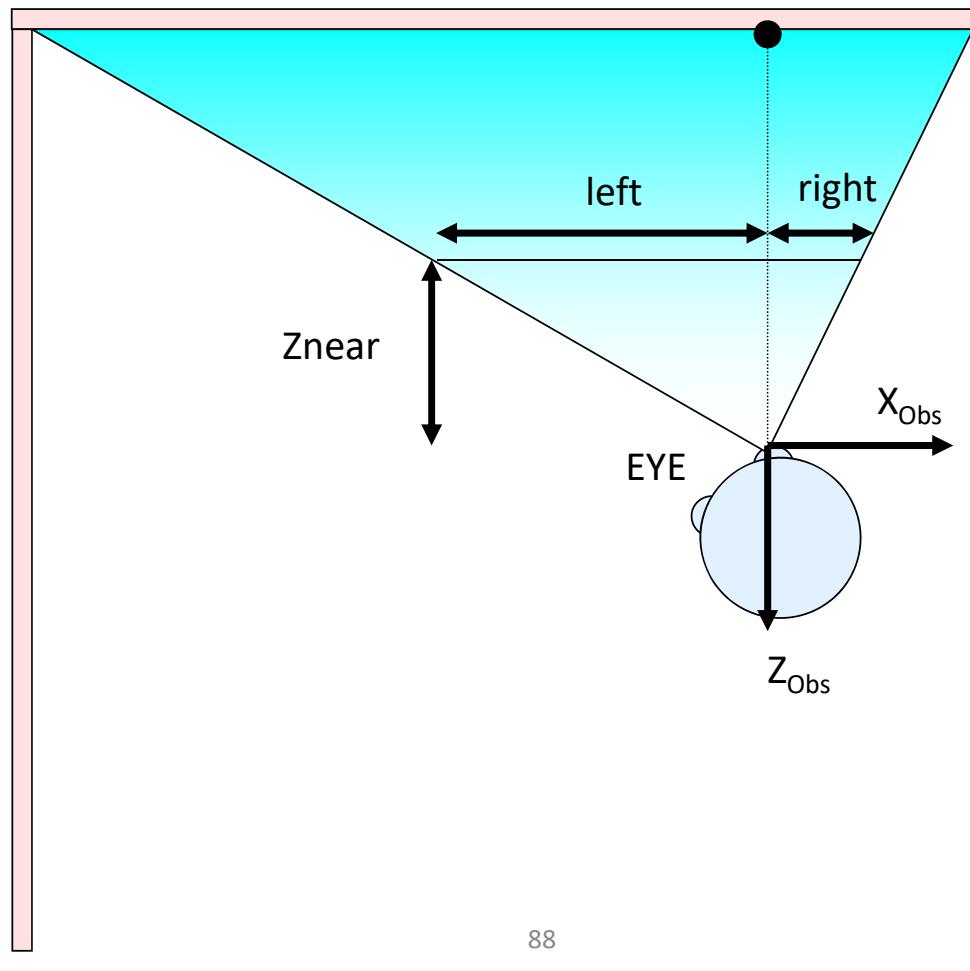
glMatrixMode(GL_PROJECTION);
glLoadIdentity();
glFrustum(left, right, bottom, top, near, far);
```



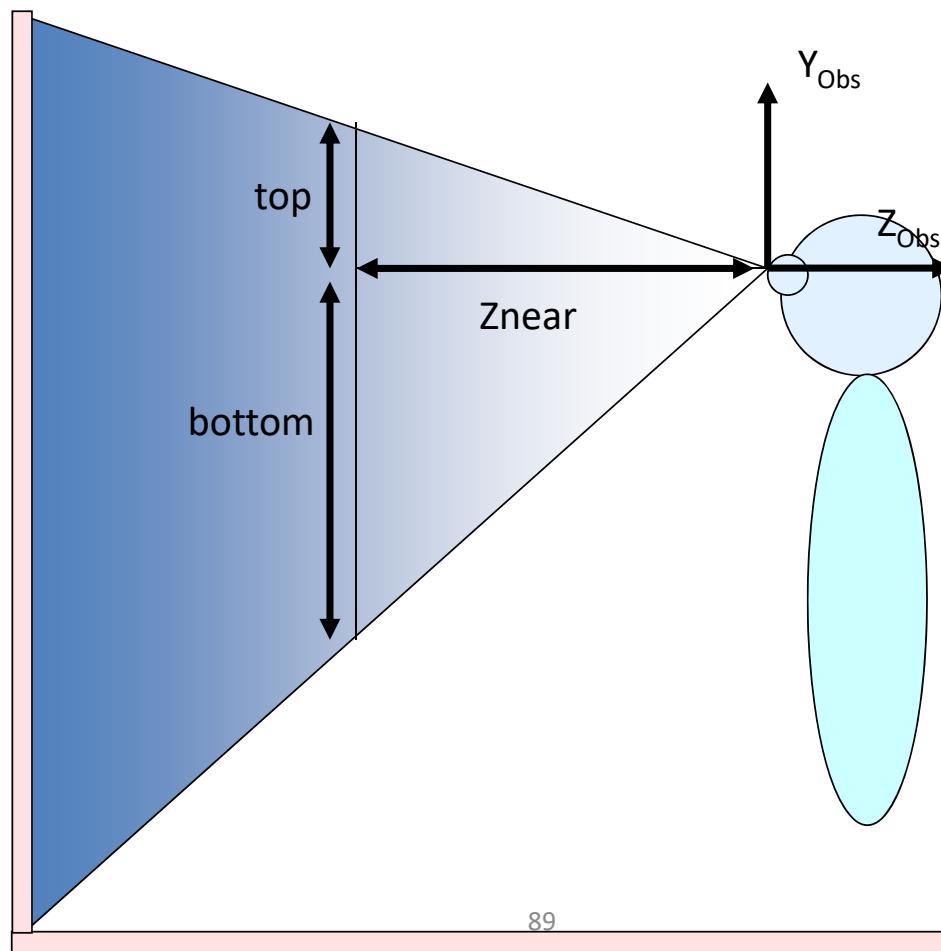


# Projection-based systems

Target

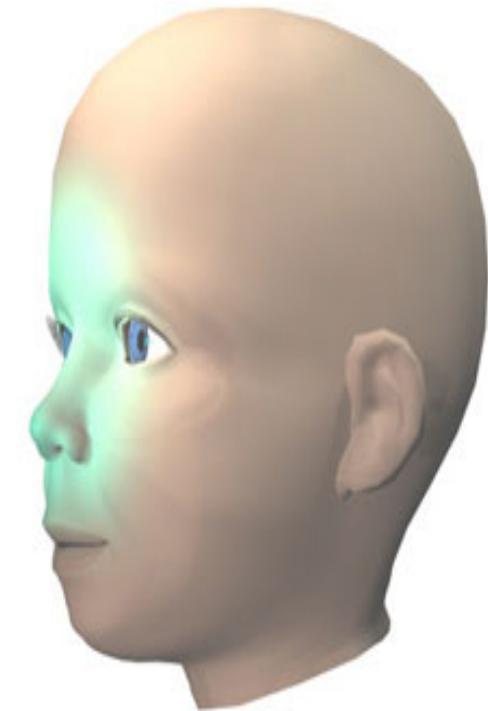
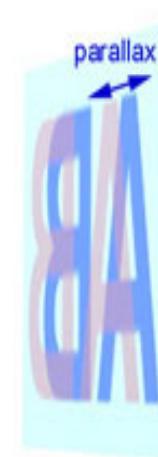


# Projection-based systems



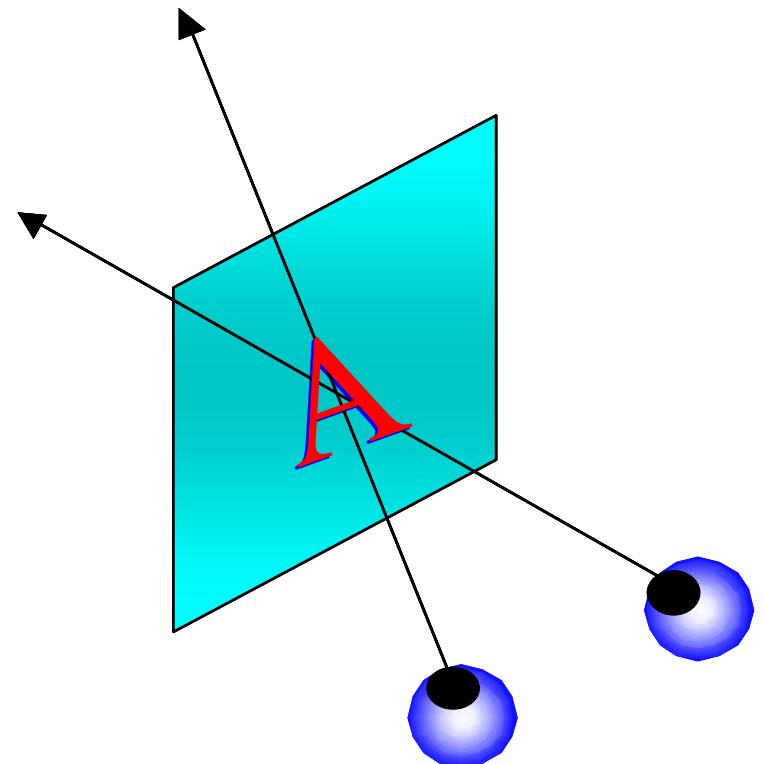
# Parallax

- **Parallax** is a 3D stereo concept.
- Related to (but distinct from!) **retinal disparity**.
- **Parallax:** distance between L/R points **measured on the screen**.
- Unlike retinal disparity, **parallax does not depend on eye convergence**.



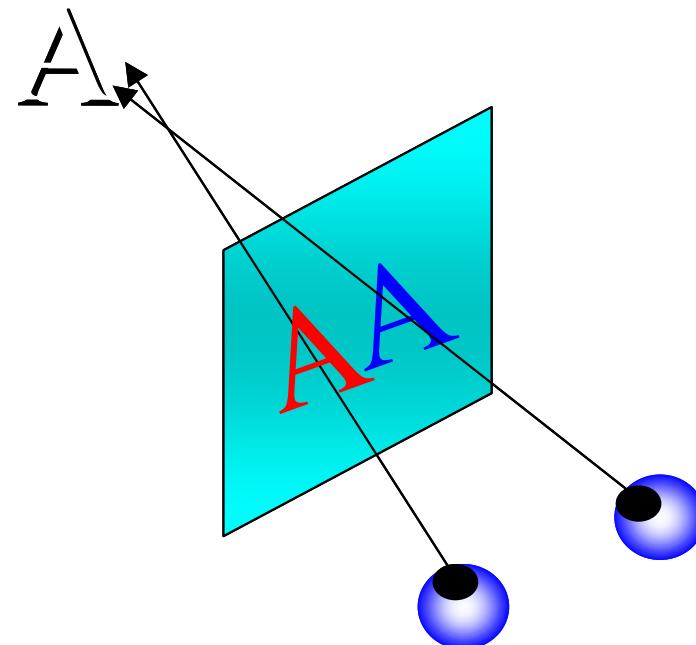
# Zero parallax

- An object has zero parallax when the corresponding L/R points overlap.
- When looking at the object, the eyes converge in the screen plane.
- The object appears to be **on the screen plane**.



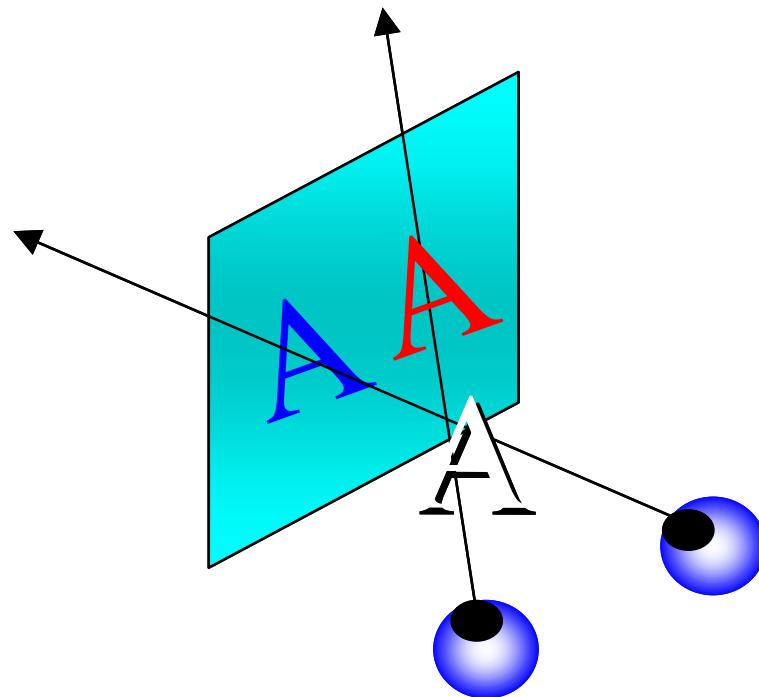
# Positive parallax

- An object has **positive parallax** when the corresponding L/R points have positive distance (**L point is to the left of the R point**).
- When looking at the object, the eyes converge at a point **behind the screen plane**.
- The object appears to be behind the screen.
- It should be in [0, 6.3cm]
- If stereo cameras are computed correctly using actual eye positions, parallax wont be greater than the IOD.



# Negative parallax

- An object has **negative parallax** when the corresponding L/R points have negative distance (**L point is to the right of the R point**).
- When looking at the object, the eyes converge at a point **in front of the screen plane**.
- The object appears to be **in front of the screen**.
- Some studies recommend not to exceed 1.5 degrees (object is too close).



# Desktop system

- Used in low-cost systems (fish-tank VR)
- As in projection-based systems but guessing user's location.



# HMD

- The screens follow the head movements, so they are fixed with respect to the eyes.
- Parameters:
  - Head orientation
  - Head position (optional)
  - HMD frustum **+ distortion**

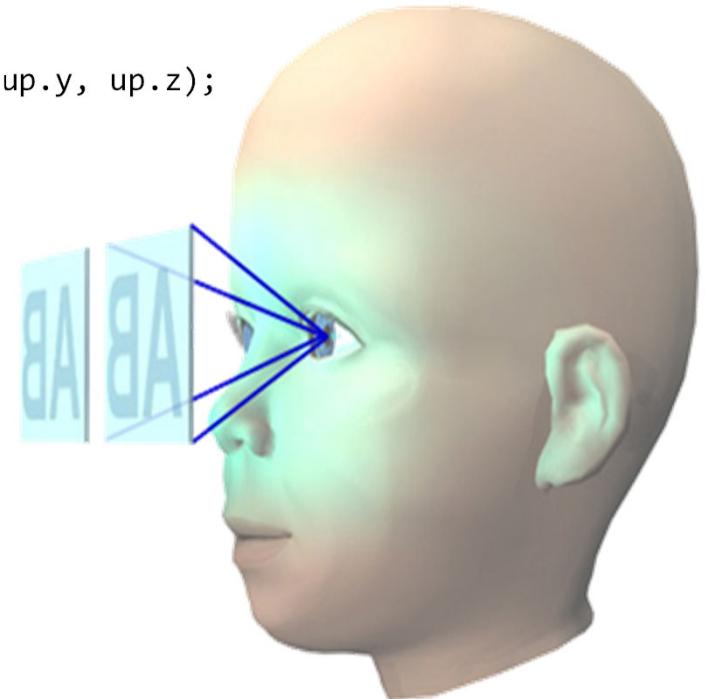


# HMD

If we could neglect lens distortion:

For each eye

```
glMatrixMode(GL_MODELVIEW);
glLoadIdentity();
gluLookAt(eye.x, eye.y, eye.z, center.x, center.y, center.z, up.x, up.y, up.z);
glMatrixMode(GL_PROJECTION);
glLoadIdentity();
glFrustum(left, right, bottom, top, near, far);
```

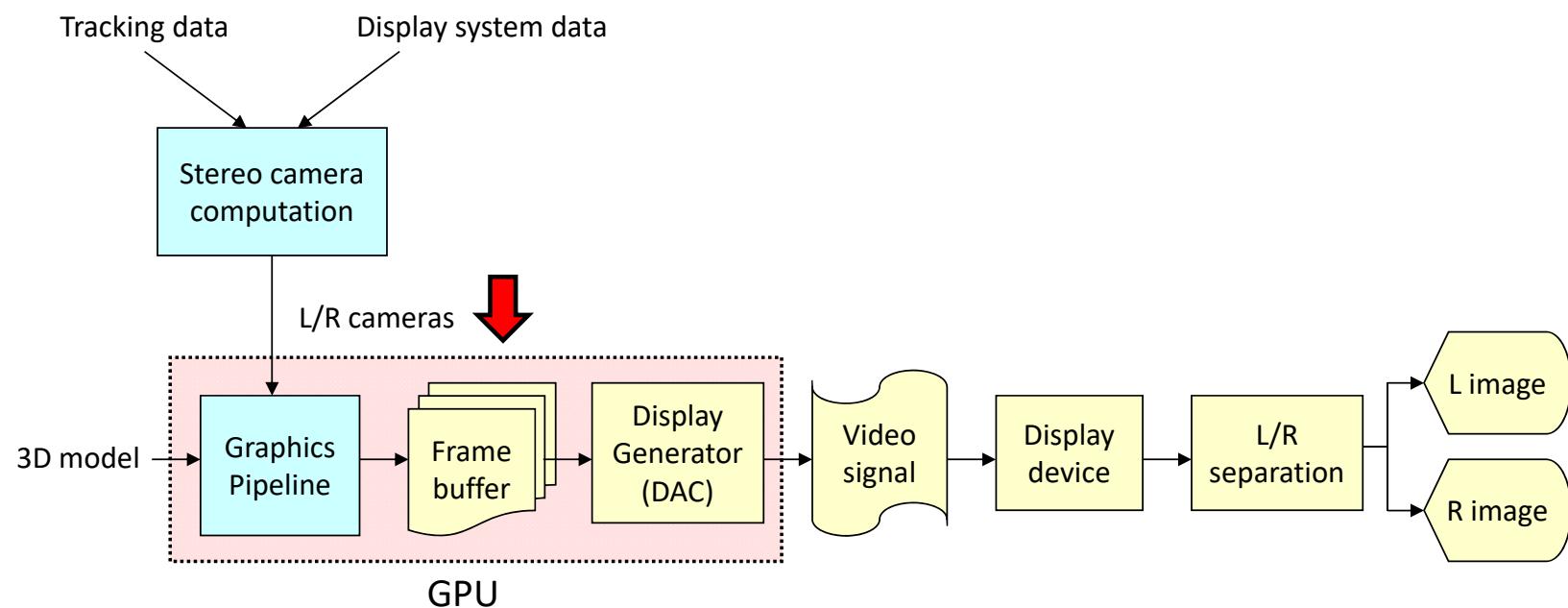


# HMD



# **FRAME BUFFER FORMATS (+ RENDERING)**

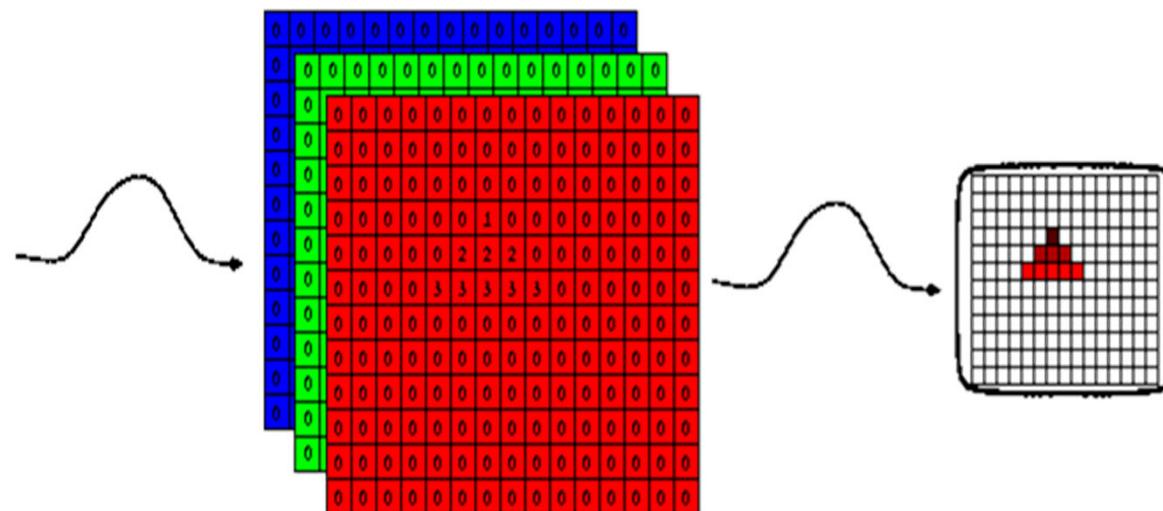
# Synthesis of stereo images



# Frame buffer: review

Frame buffer:

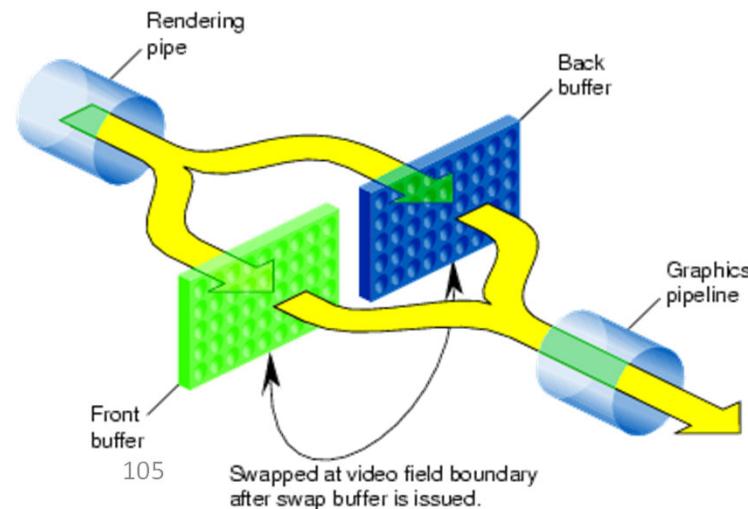
- Color buffer(s)
- Depth buffer
- Stencil buffer



# Frame buffer: review

## Double buffering

- Two color buffers: GL\_FRONT, GL\_BACK
- Depth buffer
- Stencil buffer



# Frame buffer formats

- Encoding a stereo pair in the color buffer (required when a single FB has to hold both L/R images)
- Not required e.g. when each image is generated by a different PC.
- Linked with *image separation*

# Frame buffer formats

Classification:

- Color based
  - Anaglyph stereo
- Frame-based:
  - Above-and-below, or Side-by-side
  - Quad buffering
- Line-based and column-based
  - Line-interlived (line sequential), column-interlived

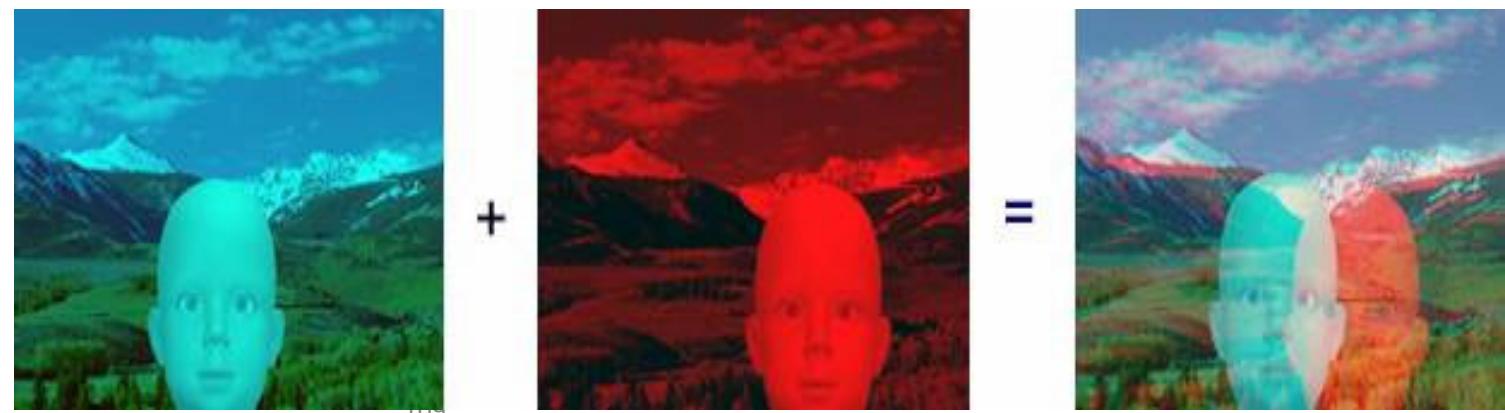
# Frame buffer formats

Classification:

- Color based
  - **Anaglyph stereo**
- Frame-based:
  - Above-and-below, or Side-by-side
  - Quad buffering
- Line-based and column-based
  - Line-interlived (line sequential), column-interlived

# Anaglyph stereo

```
glColorMask(GL_TRUE, GL_FALSE, GL_FALSE, GL_TRUE);  
setupCamera(left);  
drawScene();  
  
glColorMask(GL_FALSE, GL_TRUE, GL_TRUE, GL_TRUE);  
setupCamera(right);  
drawScene();
```



# Frame buffer formats

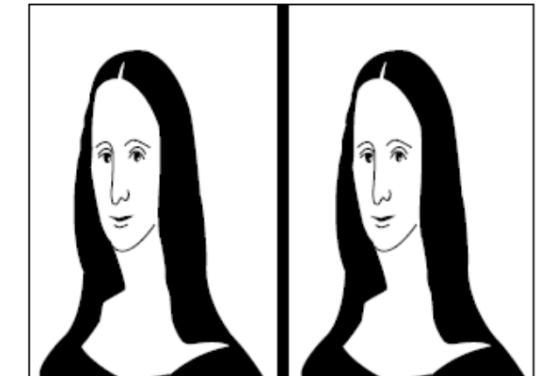
Classification:

- Color based
  - Anaglyph stereo
- Frame-based:
  - Above-and-below, or **Side-by-side**
  - Quad buffering
- Line-based and column-based
  - Line-interlived (line sequential), column-interlived

# Side-by-side

- Left half → left image
- Right half → right image
- Example, assuming a 2048x768 desktop:

```
glViewport(0, 0, 1024, 768);
setupCamera(left);
drawScene();
glViewport(1024,0,1024,768);
setupCamera(right);
drawScene();
```



# Frame buffer formats

Classification:

- Color based
  - Anaglyph stereo
- Frame-based:
  - Above-and-below, or Side-by-side
  - **Quad buffering**
- Line-based and column-based
  - Line-interlived (line sequential), column-interlived

# Quad buffering

## Frame buffer

- Color buffers: GL\_FRONT\_LEFT, GL\_FRONT\_RIGHT, GL\_BACK\_LEFT, GL\_BACK\_RIGHT
- Depth buffer
- Stencil buffer

Quad buffering is used in *active stereo*

- *Why two front buffers?* We need to provide both images during the time the application takes to draw the next frame.
- *Why two back buffers?* Both L/R buffers are swapped simultaneously!
- Supported by *stereo-ready* graphics cards
- Common format when using a single monitor/projector.

# Quad buffering: sample code

Setup a stereo format (Qt sample code):

```
QGLFormat f;  
f.setStereo(true);  
QGLFormat::setDefaultFormat(f);
```

Rendering:

```
glDrawBuffer(GL_BACK_LEFT);  
setupCamera(left);  
drawScene();  
glDrawBuffer(GL_BACK_RIGHT);  
setupCamera(right);  
drawScene();
```

# Frame buffer formats

Classification:

- Color based
  - Anaglyph stereo
- Frame-based:
  - Above-and-below, or Side-by-side
  - Quad buffering
- **Line-based and column-based**
  - Line-interlived (line sequential), column-interlived

# Line/column-interlived

- Example:
  - Even lines encode the left image
  - Odd lines encode the right image
- Limitation: each eye sees half the number of lines (or columns).

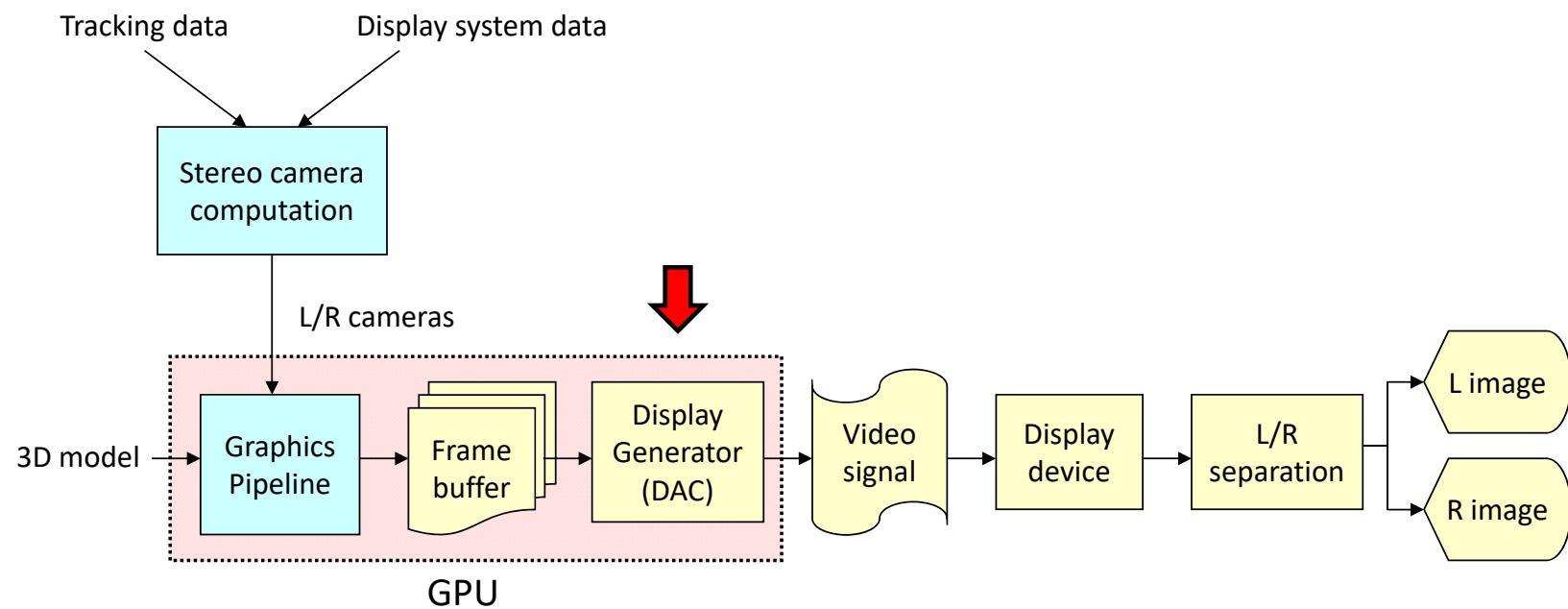
Rendering:

```
shaders.setUniformValue(eye, 0);
setupCamera(left);
drawScene();
shaders.setUniformValue(eye, 1);
setupCamera(right);
drawScene();
```

Fragment Shader:

```
uniform int eye; // 0 = left eye; 1 = right eye
void main()
{
    int parity = int(gl_FragCoord.y) % 2;
    if (parity == eye) discard;
    ...
}
```

# Synthesis of stereo images



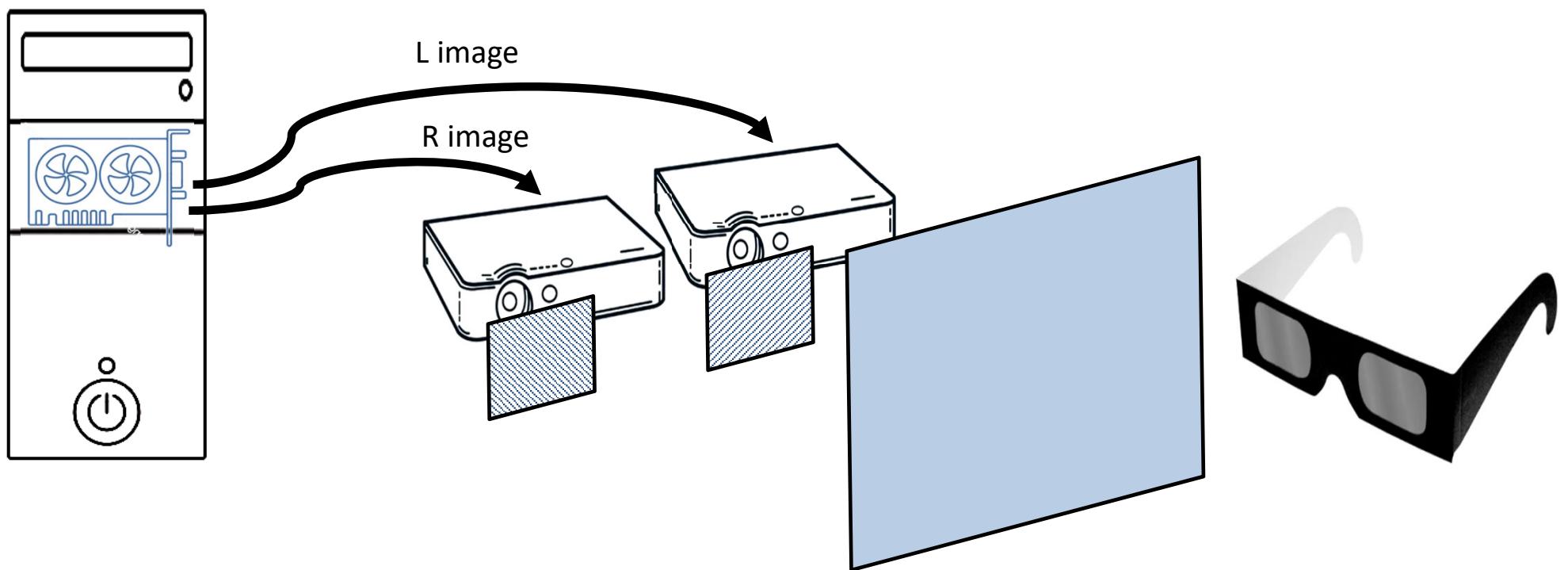
# Display generator

- Converts the contents of the (FRONT) color buffer(s) into a video signal.
- Multiple configurations:
  - **Stereo-ready cards:** one video signal, encoding sequentially left and right images.
  - **Dual-head PCs** (most current graphics cards): two independent video signals (often DVI+VGA or DVI+DVI connectors)
  - **Quad-head PCs** (high-end graphics cards)



# **SAMPLE CONFIGURATIONS**

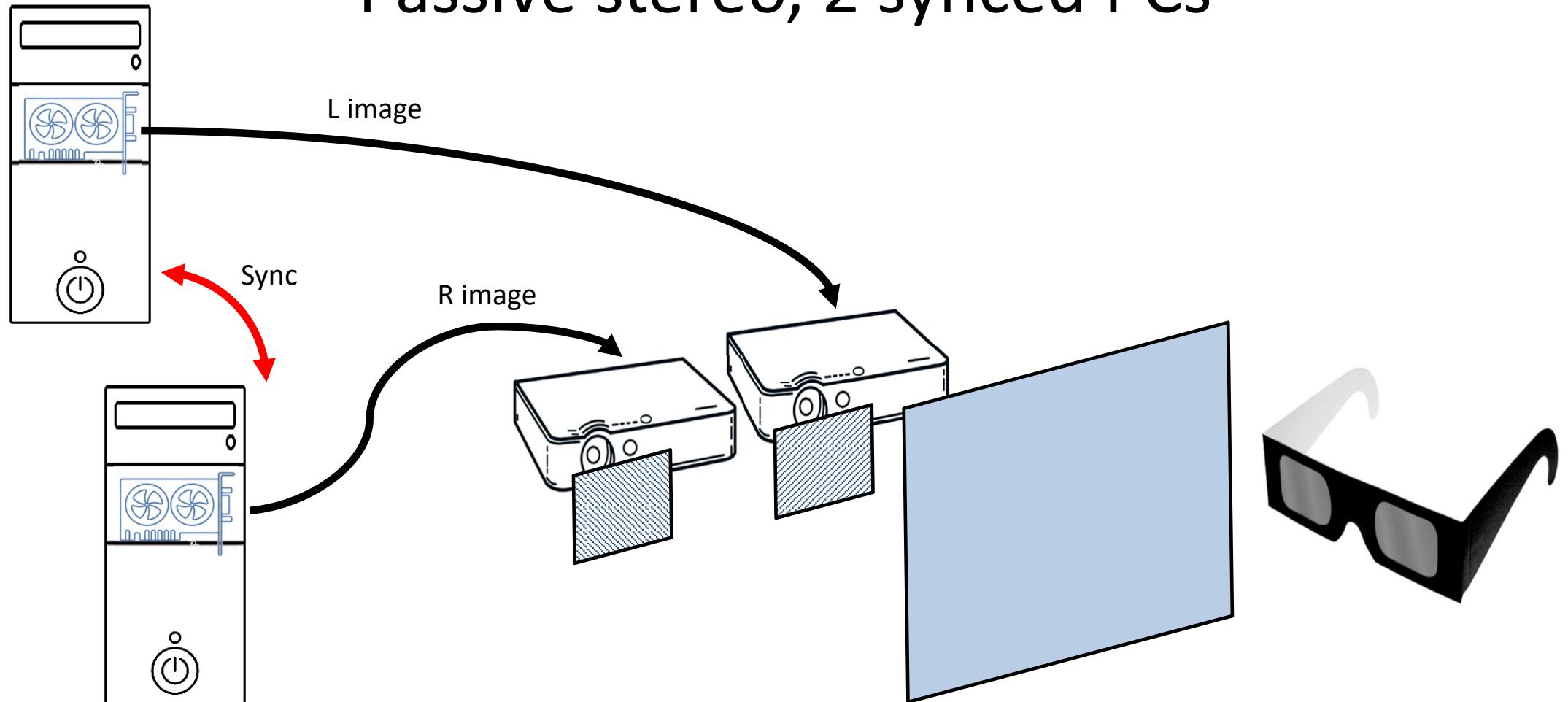
# Passive stereo, 1 PC



# Sample configurations

| # PC | # Gfx cards   | FB format      | # Projectors       | Filter            | # Screens | Glasses            | Comment                          |
|------|---------------|----------------|--------------------|-------------------|-----------|--------------------|----------------------------------|
| 1    | 1 (dual-head) | Side-by-side   | 2 (passive, 60 Hz) | Polarizing filter | 1         | Polarizing glasses | Passive stereo                   |
| 2    | 2             | Normal         | 2 (passive, 60 Hz) | Polarizing filter | 1         | Polarizing glasses | Passive stereo;<br>Needs PC sync |
| 1    | 1             | Quad buffering | 1 (active, 120Hz)  | -                 | 1         | Shutter glasses    | Active stereo                    |
| 4    | 4             | Quad buffering | 4 (active, 120 Hz) | -                 | 4         | Shutter glasses    | Active CAVE<br>Needs gfx sync!   |

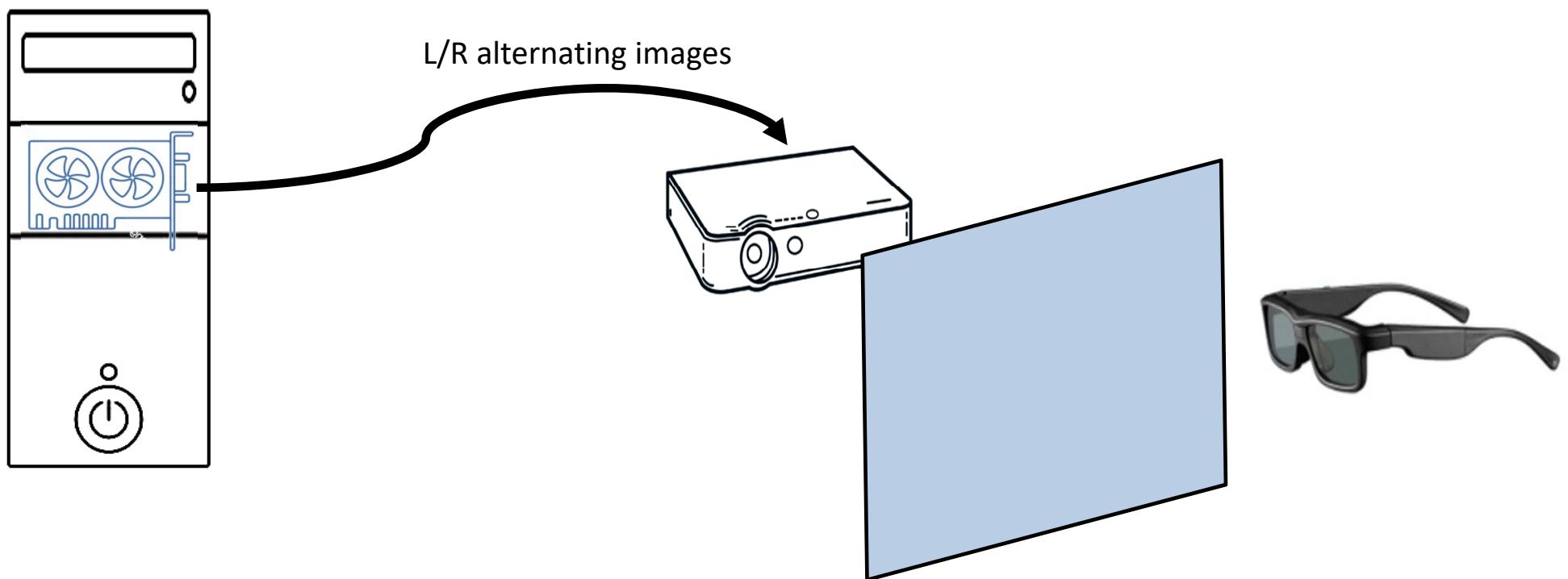
# Passive stereo, 2 synced PCs



# Sample configurations

| # PC | # Gfx cards   | FB format      | # Projectors              | Filter                   | # Screens | Glasses                   | Comment                              |
|------|---------------|----------------|---------------------------|--------------------------|-----------|---------------------------|--------------------------------------|
| 1    | 1 (dual-head) | Side-by-side   | 2 (passive, 60 Hz)        | Polarizing filter        | 1         | Polarizing glasses        | Passive stereo                       |
| 2    | 2             | Normal         | <b>2 (passive, 60 Hz)</b> | <b>Polarizing filter</b> | <b>1</b>  | <b>Polarizing glasses</b> | <b>Passive stereo; Needs PC sync</b> |
| 1    | 1             | Quad buffering | 1 (active, 120Hz)         | -                        | 1         | Shutter glasses           | Active stereo                        |
| 4    | 4             | Quad buffering | 4 (active, 120 Hz)        | -                        | 4         | Shutter glasses           | Active CAVE<br>Needs gfx sync!       |

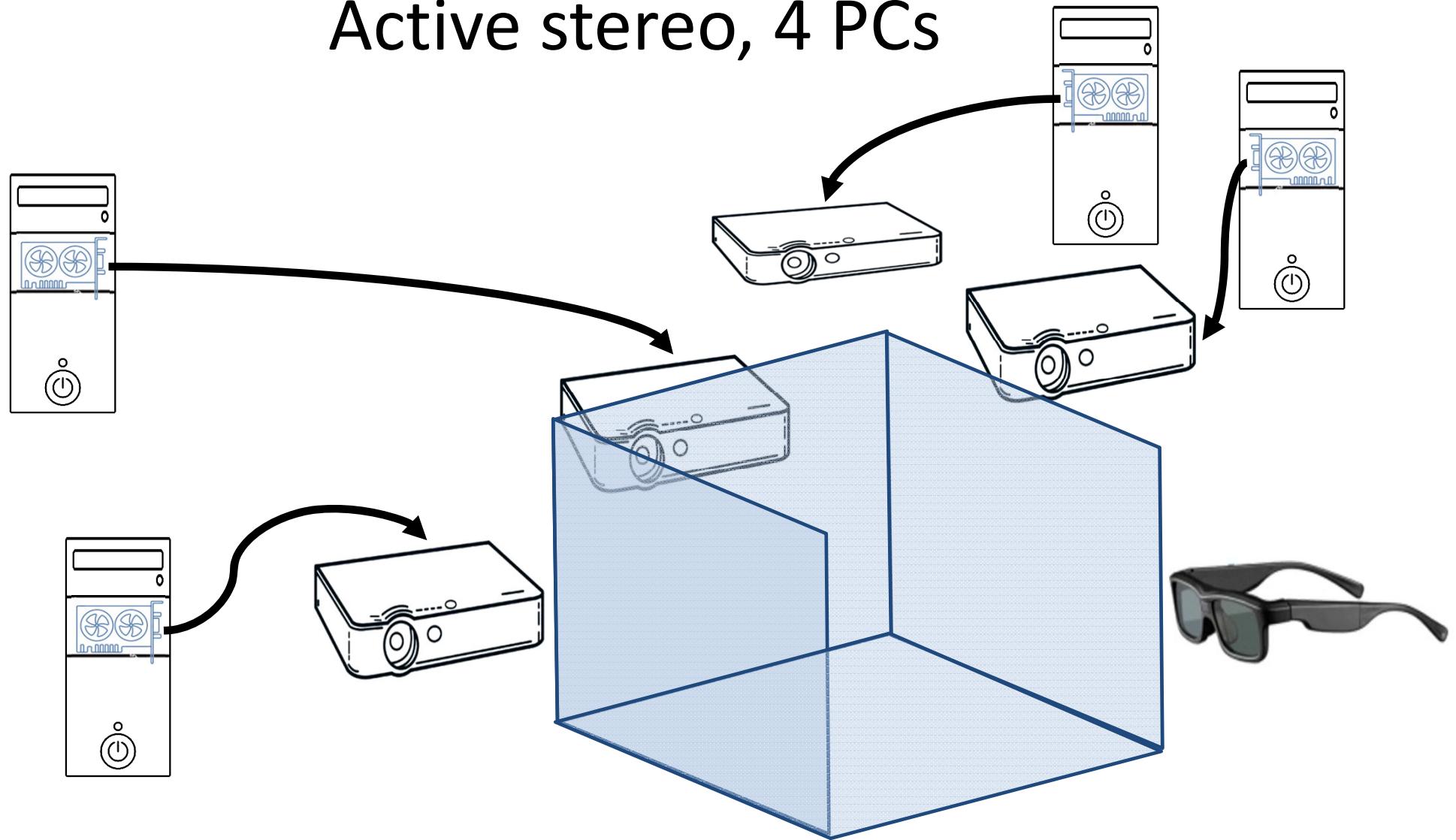
# Active stereo, 1 PC



# Sample configurations

| # PC | # Gfx cards   | FB format             | # Projectors             | Filter            | # Screens | Glasses                | Comment                          |
|------|---------------|-----------------------|--------------------------|-------------------|-----------|------------------------|----------------------------------|
| 1    | 1 (dual-head) | Side-by-side          | 2 (passive, 60 Hz)       | Polarizing filter | 1         | Polarizing glasses     | Passive stereo                   |
| 2    | 2             | Normal                | 2 (passive, 60 Hz)       | Polarizing filter | 1         | Polarizing glasses     | Passive stereo;<br>Needs PC sync |
| 1    | 1             | <b>Quad buffering</b> | <b>1 (active, 120Hz)</b> | -                 | 1         | <b>Shutter glasses</b> | <b>Active stereo</b>             |
| 4    | 4             | Quad buffering        | 4 (active, 120 Hz)       | -                 | 4         | Shutter glasses        | Active CAVE<br>Needs gfx sync!   |

# Active stereo, 4 PCs



# Sample configurations

| # PC | # Gfx cards   | FB format      | # Projectors       | Filter            | # Screens | Glasses            | Comment                                |
|------|---------------|----------------|--------------------|-------------------|-----------|--------------------|----------------------------------------|
| 1    | 1 (dual-head) | Side-by-side   | 2 (passive, 60 Hz) | Polarizing filter | 1         | Polarizing glasses | Passive stereo                         |
| 2    | 2             | Normal         | 2 (passive, 60 Hz) | Polarizing filter | 1         | Polarizing glasses | Passive stereo;<br>Needs PC sync       |
| 1    | 1             | Quad buffering | 1 (active, 120Hz)  | -                 | 1         | Shutter glasses    | Active stereo                          |
| 4    | 4             | Quad buffering | 4 (active, 120 Hz) | -                 | 4         | Shutter glasses    | <b>Active CAVE<br/>Needs gfx sync!</b> |