Problem Set #09

November 14, 2019

3. A.)

use an enumerator to find every possible permutation of nodes then test whether it contains all edges Since we know if there's an enumerator there's a decider we will use an enumerator to find all the different permutations of nodes that we could find.

N = "on input $\langle G \rangle$, where G is a graph.

- 1. for i 1...|V|
 - 2. simulate enumerator E to find every subset c of i nodes of G.
 - 3. test each subset whether G contains all edges connecting nodes in c.
 - 4. if yes, output c.

Running time: This construction is correct because we will test every possible permutation of nodes and output all of the accepting sets.

- step 1: runs for how ever many nodes there are in the graph (will always be finite)
- step 2: finds every permutation of i nodes. This is large but still a finite number
- step 3. This check if each node is connected to every other node therefore this will be $O(n^2)$
- step 4. O(1).

step 3 is based on step 2 and step 2 is based on step 1. However since these are all finite steps based on i they will not grow exponentially.

Therefore the worst case running time is still polynomial $O(n^k)$

Validation:

B.) Since we can pass anything in for k for regular clique, we can pass something in that makes it grow exponentially fast. For example we could pass n in for k. Then it would no longer be polynomial on a deterministic machine. However for clique_k since our user cannot pass in a k, we know that k cannot grow larger than the number of nodes, therefore it will always be finite, making the running time of clique_k polynomial.