

Unreliable Inferences about Unobserved Processes

A Critique of Partial Observability Models^{*}

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Abstract

Methodologists and econometricians advocate the partial observability model as a tool that enables researchers to estimate the distinct effects of a single explanatory variable on two partially observable outcome variables. However, we show that when the explanatory variable of interest influences both partially observable outcomes, the partial observability model estimates are extremely sensitive to misspecification. We use Monte Carlo simulations to show that, under partial observability, minor, unavoidable misspecification of the functional form can lead to substantial large-sample bias, even though the same misspecification leads to little or no bias under full observability.

The data may not contain the answer. The combination of some data and an aching desire for an answer does not ensure that a reasonable answer can be extracted from a given body of data.

John Tukey (1986, p. 74)

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Introduction

Social scientists often face situations, known as “partial observability,” where two (or perhaps more) distinct processes lead to distinct binary outcomes that can only be observed jointly. Braumoeller (2003) provides many examples of established literature theorizing such relationships. For example, survey respondents might self-report turning out to vote because (1) they actually voted or (2) they feel social pressure to do so. Similarly, two states will only sign a treaty if *both* states want the treaty. In these examples, researchers might be interested in modeling the decision to actually vote or the decision of a single state to want a treaty. Econometricians and methodologists argue that researchers can use a partial observability model to parse out the effects of a single explanatory variable on each unobserved outcome (Poirier 1980; Abowd and Farber 1982; Pzeworski and Vreeland 2002; Xiang 2007; Nieman 2015). This partial observability model is also referred to as the split-population logit (Beger et al. 2011) and the Boolean logit or probit (Braumoeller 2003).

Partial observability models inform the literatures on important processes and outcomes such as civil wars (Nieman 2015), international conflict and trade (Xiang 2010), IMF agreements (Knight and Santaella 1997, Przeworski and Vreeland 2000, 2002, Vreeland 2003, and Stone 2008), union membership (Abowd and Farber 1982), regulatory compliance (Feinstein 1990, Stafford 2002, Chen et al. 2006, and Wang 2013), network formation (Comola and Fafchamps 2014), credit ratings (Boyes, Hoffman, and Low 1989), agricultural innovation (Dimara and Skuras 2003), health insurance ownership (Amir 2001), and employment discrimination (Heywood and Mohanty 1990, Logan 1996, and Mohanty 2002). Feinstein (1990) suggests the model’s usefulness for a wide range of policy studies, and the model appears to hold out promise for investigating numerous other subjects, including deterrence, treaty compliance, and attitudes and behaviors that are subject to social desirability bias when measured via a survey report (Beger et al. 2011).

In spite of the optimistic application of the partial observability model, we argue that researchers should view these estimates with skepticism. Seemingly innocuous and unavoidable specification errors that lead to little or no large-sample bias under full observability can lead to a substantial large-sample bias under partial observability. Using a simple example and two simulation studies, we show that minor misspecification of the functional form can lead to large asymptotic biases. Even incorrectly specifying the functional form, a choice that researchers normally view as arbitrary and inconsequential, can lead to large biases with the partial observability model.

Unfortunately, we have no simple solution to this problem. This is not a methodological problem; the data simply do not contain enough information to reliably parse out the effects of a single explanatory variable

on each partially observed outcome variable without strong assumptions about the functional form. Rather than offer a methodological fix, we instead caution scholars to view these partial observability estimates with greater skepticism and urge researchers to collect more complete data, directly observing the outcome of interest. For example, we applaud the Cooperative Congressional Election Studies’ efforts to electronically validate their self-reported voter turnout data.

A Partial Observability Logit Model

Partial observability occurs when the researcher only observes a binary outcome of interest d_{main} jointly with another binary outcome $d_{nuisance}$.¹ The researcher directly observes the binary outcome y_{obs} , which equals one if both d_{main} and $d_{nuisance}$ equal one and zero otherwise.²

To model the observed outcome y_{obs} , we assume that d_{main} and $d_{nuisance}$ are independent events so that $\Pr(y_{obs}) = \Pr(d_{main})\Pr(d_{nuisance})$.³ Next, we assume a standard model relating a set of covariates $X = [1, w_1, w_2, \dots, w_{k_w}, x_1, x_2, \dots, x_{k_x}]$ to $\Pr(d_{main})$ and a set of covariates $Z = [1, w_1, w_2, \dots, w_{k_w}, z_1, z_2, \dots, z_{k_z}]$ to $\Pr(d_{nuisance})$, so that $\Pr(d_{main}) = g^{-1}(X\beta)$ and $\Pr(d_{nuisance}) = g^{-1}(Z\gamma)$. Note that the covariates w_j for $j \in \{1, 2, \dots, k_w\}$ belong to both X and Z . This is crucial—our critique focuses on the situation in which the researcher wishes to parse out the distinct effects of one or more explanatory variables on *both* unobservable outcome variables.⁴ The researcher’s theory rarely offers a compelling rationale for a particular link function g , making the choice essentially arbitrary (King 1998, p. 100, and Berry, DeMeritt, and Esarey 2010). In our partial observability model, we let g be the logit function, but other standard choices include probit, cloglog, and cauchit. Using this form, it is straightforward to find the log-likelihood function for β and γ , although the maximization is not trivial.⁵ We assume that the researcher uses the estimates of β and γ to calculate some quantity of interest (e.g., first difference). As a comparison, we also consider a full observability logit model (i.e., the usual logit model), in which the researcher observes d_{main} and uses the

¹For clarity, we imagine a situation where one outcome is of interest and the other is largely nuisance. However, our ideas generalize to a situation where the researcher’s interest extends to both outcomes.

²One can also employ a partial observability model where y_{obs} equals one if either d_{main} or $d_{nuisance}$ equals one. For simplicity, we focus on a situation where y_{obs} equals one if both d_{main} and $d_{nuisance}$ equal one. Our conclusions do not depend on this choice.

³Especially in the case of the partial observability probit model, the researcher can relax the assumption of independence. We make the assumption of independence to simplify the presentation and the computation.

⁴Even if a researcher *assumes* that each explanatory variable influences only one of the observable outcomes, she usually only has a weak theory guiding the choice and no empirical tools to verify the assumption.

⁵We find that standard hill-climbing optimization routines find local maxima. This presents a separate, perhaps equally concerning problem for substantive applications. To avoid this, we tried an algorithm suggested by Sekhon and Mebane (1998) that relies on a combination of genetic adaptation and hill-climbing to efficiently locate the maximum (Mebane and Sekhon 2011). This approach consistently located the global maximum in several trial examples, but only for a very large population (i.e., computationally prohibitive) of agents. We found that starting a standard hill-climbing algorithm at several sets of random starting values consistently located the global maximum. We use ten sets of starting values in our estimation.

model $\Pr(d_{main}) = \text{logit}^{-1}(X\beta)$ to estimate the quantity of interest.

A Motivating Example

To illustrate the potential bias with a simple example, suppose the researcher wants to estimate β and γ in the stylized model

$$\begin{aligned}\Pr(d_{main}) &= \text{logit}^{-1}(\beta x) \\ \Pr(d_{nuisance}) &= \text{logit}^{-1}(\gamma x - z) \\ \Pr(y) &= \Pr(d_{main}) \Pr(d_{nuisance}),\end{aligned}$$

where y_{obs} represents the observed binary outcome, x and z represent two binary explanatory variables, and β and γ represent parameters to be estimated. Suppose further that $(\beta, \gamma) = (-1, 1)$ or $(\beta, \gamma) = (1, -1)$ so that the researcher knows the absolute value of β and γ is 1, but is not sure which parameter is negative.

Because x and z are binary, there are four conditions, and we can easily compute the expected proportions under each for both sets of possible parameters. Table ?? shows these proportions, where δ represents the logit^{-1} function for compactness. The only difference in the expected proportion occurs when $x = 1$ and $z = 1$, where $(\beta, \gamma) = (-1, 1)$ produces an expected proportion of 0.13 and $(\beta, \gamma) = (1, -1)$ produces an expected proportion of 0.09.

[Table 1 about here.]

This raises the question: How much would we need to alter the logit link function so that we obtain Panel A of Table ?? with parameters $(\beta, \gamma) = \{1, -1\}$? The answer is “not much.”

Our goal is to replace the function logit^{-1} with a new function h^{-1} to obtain Panel A of Table ?? with parameters $(\beta, \gamma) = (1, -1)$. The only time we use $\text{logit}^{-1}(-2)$ in the calculation is for the bottom-right cell. In that case, let $h^{-1}(x) = \text{logit}^{-1}(x)$ for $x \in c\{-1, 0, 1\}$. This ensures that all but the bottom-right cell

remains unchanged. Then we require that

$$\begin{aligned}
h^{-1}(-2)h^{-1}(1) &= 0.13 \\
h^{-1}(-2)\text{logit}^{-1}(1) &= 0.13 \\
h^{-1}(-2) &= \frac{0.13}{\text{logit}^{-1}(1)} \\
h^{-1}(-2) &= \frac{0.13}{0.73} \\
h^{-1}(-2) &= 0.18 \text{ (as opposed to } \text{logit}^{-1}(-2) = 0.12)
\end{aligned}$$

Figure ?? compares the functions logit^{-1} and h^{-1} , which are similar, yet lead to exactly *opposite* inferences about the effects of x on d_{main} and $d_{nuisance}$. If the researcher obtains a large set of data with proportions identical to Panel A of Table ??, then her conclusion about the effects of x on d_{main} and $d_{nuisance}$ depends on her assumption about the link function. If she assumes the logit link function, then she concludes that x has a large, *negative* effect on d_{main} . If she assumes the link function h , then she concludes that x has a large, *positive* effect on d_{main} . This example clearly highlights how minor errors in model specification can lead to large bias. To show the potential for bias in a broader collection of situations, we now turn to two simulation studies.

[Figure 1 about here.]

Simulation Studies

We use two simulation studies to support our claim that partial observability models are highly sensitive to seemingly innocuous specification errors. In the first study, we evaluate the bias in the partial observability logit model estimates as the link function g of the true data-generating process (DGP) varies. We view this as a highly conservative test of our claim, but find that misspecifying the link function can lead to large biases. In the second study, we consider more realistic, but still conservative misspecifications of the functional form. Berry, DeMeritt, and Esarey (2015) observe that few social science theories offer more precision than a simple monotonic relationship between an explanatory variable and the probability of an event. Motivated by their observation, we evaluate the performance of the partial observability logit model for a variety of monotonic DGPs. The simulations clearly show that (1) neither type of misspecification introduces much bias into the estimate under full observability and (2) both types of misspecification can introduce large bias into the estimate under partial observability, including sign errors.

Simulation Study 1: Wrong Link Function

Many researchers view the choice of link function in a model of a binary outcome as an arbitrary, unimportant choice. Berry, DeMeritt, and Esarey (2015) summarize this idea:

In the typical study using binary logit or probit, the theory introduced is not sufficiently specific to imply that logit, probit, or any other functional form is a good fit to the hypothesized DGP. Instead, logit or probit is chosen from among the countless possible functional forms for a model simply because logit and probit have come to be viewed as “default” estimators for a binary dependent variable model—making them convenient estimation choices.⁶

We endorse and echo the authors’ key point: in the social sciences, researchers rarely have a strong theoretical justification for choosing one functional form over another.

Given that researchers seldom have a compelling reason to prefer a logit model over a probit model, a cloglog model, or a cauchit model, we would find it especially troubling if the ability of the partial observability model to recover the quantity of interest depends on the researcher choosing the proper link function. Our simulations show exactly this—if the researcher chooses the wrong link function (e.g., uses a partial observability *logit* model for a *cauchit* DGP), then the large-sample estimates can have substantial bias.

To assess the large-sample bias of the partial observability model we simulate 500 large data sets for each of our DGPs (i.e., 100 million observations for each unique combination of the values for each explanatory variable). Across each data set, we randomly vary k_w (the number of variables explaining both d_{main} and $d_{nuisance}$), k_x (the number of variables explaining only d_{main}), k_z (the number of variables explaining only $d_{nuisance}$), β (the coefficients in the model of d_{main}), and γ (the coefficients in the model of $d_{nuisance}$). The

⁶The authors continue in a footnote:

For example, the 2005 issues of three major journals—*American Journal of Political Science* (AJPS), *American Political Science Review* (APSR), and *The Journal of Politics* (JOP)—contain 49 articles studying binary dependent variables with logit or probit; 30 of these articles offer no defense for their choice of logit or probit; ten other papers defend their choice, but solely by noting that the dependent variable is dichotomous.

parameters are drawn from the following distributions:

$$k_w - 1 \sim \text{Poisson}(0.5)$$

$$k_x \sim \text{Poisson}(1.5)$$

$$k_z \sim \text{Poisson}(1.5)$$

$$\beta^* \sim \text{uniform}(-1, 1)$$

$$\gamma^* \sim \text{uniform}(-1, 1)$$

We also randomly vary the type of each explanatory variable, either binary or continuous, so that each variable is binary with probability 0.5. For computational ease, continuous variables take on values 0.0, 0.2, 0.4, 0.6, 0.8, or 1. For each random set of simulation parameters, we simulate a large data set using logit, probit, cloglog, and cauchit DGPs. For each DGP, we rescale the coefficients β^* and γ^* so that the true first differences are approximately equal across DGPs. For each data set, we use the partial observability logit model to estimate the first difference as the key explanatory variable w_1 varies from its minimum to its maximum (i.e., zero to one). Section ?? of the Appendix summarizes the details of the algorithm.

Figure ?? shows the large-sample estimates of the first difference. The left-hand column shows the relationship between the estimated effect and true effect under full observability, where misspecifying the link function has almost no effect on the inferences. The largest biases under full observability occur for the cauchit DGP, where the average absolute bias is less than 0.01. The average absolute true effect is about 0.1, so the average absolute bias is relatively small. Most importantly, though, the estimate almost always falls close to the true value regardless of the DGP. For the worst-case cauchit DGP, the 95th percentile of the absolute bias is about 0.04 and the maximum is 0.08. The correlations between the estimated effect and the true effect for a cauchit DGP is 0.99. We would expect any biases to be minor; the cauchit link function is nearly indistinguishable from the logit link function and there is almost never a compelling theoretical reason to prefer one over the other.

[Figure 2 about here.]

The results under partial observability, though, tell a different story—the bias can be much larger. For the cauchit DGP, the average absolute bias is about 0.07 when w_1 is continuous and about 0.20 when w_1 is binary—about 7 and 20 times larger under partial observability than under full observability, respectively. Under partial observability, the correlation between the estimated effect and the true effects drops to 0.69 when w_1 is continuous and to 0.32 when w_1 is binary. And remember that standard errors do not reflect this

large-sample bias and that the bias does not shrink as the sample size increases. This performance differential does not occur because the partial observability model requires more information to estimate the parameters; it occurs because the partial observability model is highly sensitive to misspecification.

Unlike the full observability model, the partial observability model does not guarantee an estimate close to the true value. For the cauchit DGP, the 95th percentile for the average absolute bias is about 0.17 and the maximum is about 0.30 when w_1 is continuous. When w_1 is binary, the 95th percentile is 0.83 and the maximum is 1.12. Though the researcher has made only a small specification error, this small error produces a moderate-to-large bias on average and an enormous bias on occasion. Perhaps most informatively, for the cauchit DGP, the partial observability logit model produces sign errors in 24% of the simulations when w_1 is continuous and in 31% of the simulations when w_1 is binary. That is, when using a partial observability logit model to estimate a cauchit DGP, not only does the estimate converge to the wrong value (i.e., is inconsistent), it often converges to a value with the wrong sign! In contrast, the full observability logit model does not produce a single sign error in our simulations, regardless of the DGP.

While the cauchit DGP acts as the worst-case scenario for the partial observability logit model, the biases that emerge for the probit DGP are especially telling. The conventional wisdom suggests that the choice between a logit and probit model is inconsequential. Indeed, King (1998, p. 100) notes in passing that the two link functions “produce almost identical inferences in practical social science problems.” This claim holds in the context of full observability (where King makes the claim), but the partial observability logit model estimates can have substantial bias under a probit DGP. For example, the average absolute bias in the estimates of the partial observability logit model for a probit DGP is about 0.03 for both a continuous and a binary w_1 , which is about three times the worst-case scenario under full observability. Perhaps more importantly, the partial observability model has a much higher likelihood of substantial large-sample bias than the full observability model. The 95th percentile of the absolute bias is 0.12 and the maximum is 0.35 when w_1 is continuous. When w_1 is binary, the 95th percentile is 0.12 and the maximum is 0.55. About 4% of the simulations produce a sign error. While this potential for bias might be small enough or rare enough to ignore, these results highlight the bias that even minor errors in the functional form can produce.

Lastly, notice that substantial large-sample bias does not only occur among models with one or two identifying variables. For the probit DGP, increasing the number of identifying variables ($n_x + n_z$) from one to four shrinks the 95th percentile of the absolute bias from about 0.15 to about 0.10. For the cloglog DGP, this same change shrinks the 95th percentile from 0.21 to 0.15. For the cauchit DGP, the 95th percentile shrinks from 0.73 to 0.69. Even with several identifying variables, the potential for bias remains quite large.

Whereas the full observability logit model can estimate the first difference accurately whether the true DGP is logit, probit, cloglog, or cauchit, the partial observability logit model performs noticeably worse for the probit, cloglog, and cauchit DGPs. In particular, a functional form mismatch leads to moderate-to-large bias on average and dramatically raises the likelihood of an enormous bias, including sign errors. But we view this first study only as a heuristic to illustrate the extreme sensitivity of the partial observability model. In our second simulation, we turn to a more realistic scenario with more general, monotonic DGPs.

Simulation Study 2: A Monotonic Relationship

Our second simulation study mirrors that of Berry, DeMeritt, and Esarey (2015). In these simulations, we assume that the researcher uses the partial observability logit model to estimate a first difference when the DGP is actually some monotonic relationship among the explanatory variables and the probability of an event, so that

$$\begin{aligned}\Pr(d_{main}) &= p(w) \\ \Pr(d_{nuisance}) &= q(w, z) \\ \Pr(y_{obs}) &= \Pr(d_{main}) \Pr(d_{nuisance}),\end{aligned}$$

where p and q are monotonic functions of x and x and z , respectively.

In our view, even the strongest social science theory will not specify the exact functional form relating the explanatory variables to the unobserved outcomes. However, a good theory might specify a monotonic relationship between the explanatory variables and the probability of an event.

In this simulation, the relationships are monotonic and the researcher includes the variables in the appropriate equations, so the misspecification, while always present, remains slight. We view this study as a more realistic, but still conservative evaluation of the partial observability model. While the deviation from the typical link functions (logit, probit, cloglog, cauchit, etc.) can be quite large in this simulation, two features work in favor of the partial observability model. First, we place the variables w and z in the correct equations. In applied research, the researcher must usually make these choices guided only by relatively weak theory. Second, we allow the effects of the identifying variable z to be quite large. In applied work, the researcher might rely on one or more variables that have relatively small effects.

Indeed, this strikes us as a realistic, but best-case scenario for social science research. Following Berry, DeMeritt, and Esarey (2015), we simulate a pool of 2,000 DGPs that meet the monotonicity condition, where

each true DGP can be represented by the nonlinear, interactive equations

$$\begin{aligned}\Pr(d_{main}) &= \beta_{cons} + \beta_w w + \beta_{w^2} w^2 \\ \Pr(d_{nuisance}) &= \gamma_{cons} + \gamma_w w + \gamma_z z + \gamma_{w^2} w^2 + \gamma_{z^2} z^2 + \gamma_{wz} wz \\ \Pr(y) &= \Pr(d_{main}) \Pr(d_{nuisance}).\end{aligned}$$

To choose the coefficients, β and γ are drawn from a uniform($-1, 1$) distribution. Values that do not meet the monotonicity condition are discarded.

As before, we simulate a dataset with 100 million observations for every possible combination of covariate values for each DGP. We use this data set to estimate the full and partial observability logit models. Finally, we compare these large-sample estimates of the quantity of interest to the true value. As before, we focus on the ability of the partial observability model to recover the change in the probability of d_{main} as w moves from its minimum to its maximum (0, 1). Section ?? of the Appendix summarizes the details of the algorithm.

Figure ?? shows the results. The left-hand column shows the full observability logit model estimates of the first difference. These estimates are extremely accurate when w is binary. This occurs because the logit model can perfectly represent the probability of an event, regardless of the “functional form” when the single explanatory variable w is binary. This is not the case for the continuous w , though. In spite of the fact that the full observability model might only roughly approximate $p(w)$, the bottom left-hand panel of Figure ?? shows that the full observability model can estimate the effect of w on $\Pr(d_{main})$ extremely well.

[Figure 3 about here.]

Though the functional form misspecification has almost no influence on the ability of the full observability logit model to estimate the effect of interest, the same misspecification causes substantial bias in the partial observability estimates. For a continuous w , the average absolute bias is about 0.19. The 95th percentile is 0.54, and the maximum bias in our sample is 1.17. For a binary w , the average absolute bias is 0.28, the 95th percentile is 0.85, and the maximum is 1.15. The large-sample absolute bias is larger than 0.1 in 65% of the simulations, larger than 0.3 in 27% of the simulations, and larger than 0.5 in 12% of the simulations. To put this in perspective, many effects of interest to political scientists are smaller than 0.1.

Sign errors are also a substantial problem for the monotonic DGP. When w_1 is binary, 19% of the simulations produce a large-sample sign error. When w_1 is continuous, this only shrinks to about 11%. In applied settings, not only do researchers need to worry about sampling error, they need to worry that the model, even with negligible sampling error, may converge to an estimate with the *wrong sign*.

One might suspect that the magnitude of the bias depends on the magnitude of the effect of the identifying variable. As the magnitude of the effect of the identifying variable increases, the potential for bias does tend to decrease, but it shrinks rather slowly. The 95th percentile of the absolute bias is 1.00 when the effect of z is 0.1. If z has a much larger effect of 0.5, then the 95th percentile of the absolute bias only drops to 0.58.

Conclusion

We highlight an under-appreciated but critical characteristic of partial observability models—they are quite sensitive to seemingly innocuous specification errors. Even small errors in the functional form can lead to a substantial bias in large samples, including sign errors.

Meng and Schmidt (1985) counseled economists early on regarding some of the costs of partial observability, arguing that standard errors are much larger when the outcome of interest is only partially observed. They write, “we would not be surprised to find, in a typical application, t -ratios to be from two to four times as large under full observability as under partial observability” (Meng and Schmidt 1985, p. 83). Yet by design, standard errors only reflect the uncertainty due to sampling error. Other sources of error, such as measurement error, missing data, and specification error create additional uncertainty. In the case of full observability, our simulations show that the functional form has a negligible impact on the large-sample estimates. But in the case of partial observability, uncertainty about the functional form should generate suspicion about the estimates. The bias introduced from specification error of the partial observability model can be quite large, is rarely negligible, and is not captured in the standard errors.

What about the possibility of model specification tests to determine the severity of the misspecification? We are not optimistic about this possibility. The motivating example shows that two models can fit the observed data exactly and still provide opposite inferences. In general, researchers could use a test to determine whether the partial observability model offers a good model of $\Pr(y_{obs})$. But researchers cannot evaluate the quality of the models of $\Pr(d_{main})$ and $\Pr(d_{nuisance})$ because these variables are unobserved. A model might predict the observed data quite well, but offer terrible predictions for the unobserved data. Thus, specification tests cannot resolve the issue when the researcher is interested in explaining d_{main} .

Recent applications are relatively sanguine about employing the partial observability model. For example, Przeworski and Vreeland (2002; see also Przeworski and Vreeland 2000, Vreeland 2003, and Stone 2008) are interested in how surplus in a nation’s budget affects both the IMF’s and the national government’s decisions to enter an agreement. They find that, as a budget surplus increases, a government becomes *less*

likely to enter an IMF agreement, but the IMF becomes *more* likely to enter an agreement. Interestingly, and consistent with our claim, Stone (2008) uses data from a later time period and reports an *opposite* effect of the budget surplus on a government's decision to participate in an agreement. In spite of these and other optimistic applications of the partial observability model, our analysis suggests that skepticism is in order. Indeed, our simulations show that relatively minor and unavoidable model specification errors can lead to a substantial large-sample bias in the estimates. In our view, no easy methodological fix exists. Instead, we encourage scholars to view partial observability estimates with skepticism and encourage researchers to collect more complete data, directly observing the outcome of interest.

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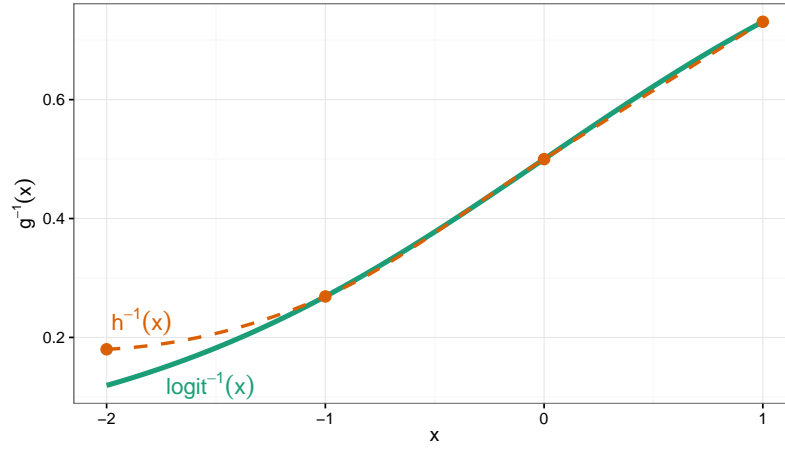


FIGURE 1: This figure compares the link functions logit^{-1} and h^{-1} that lead to exactly opposite inferences in the stylized partial observability model.

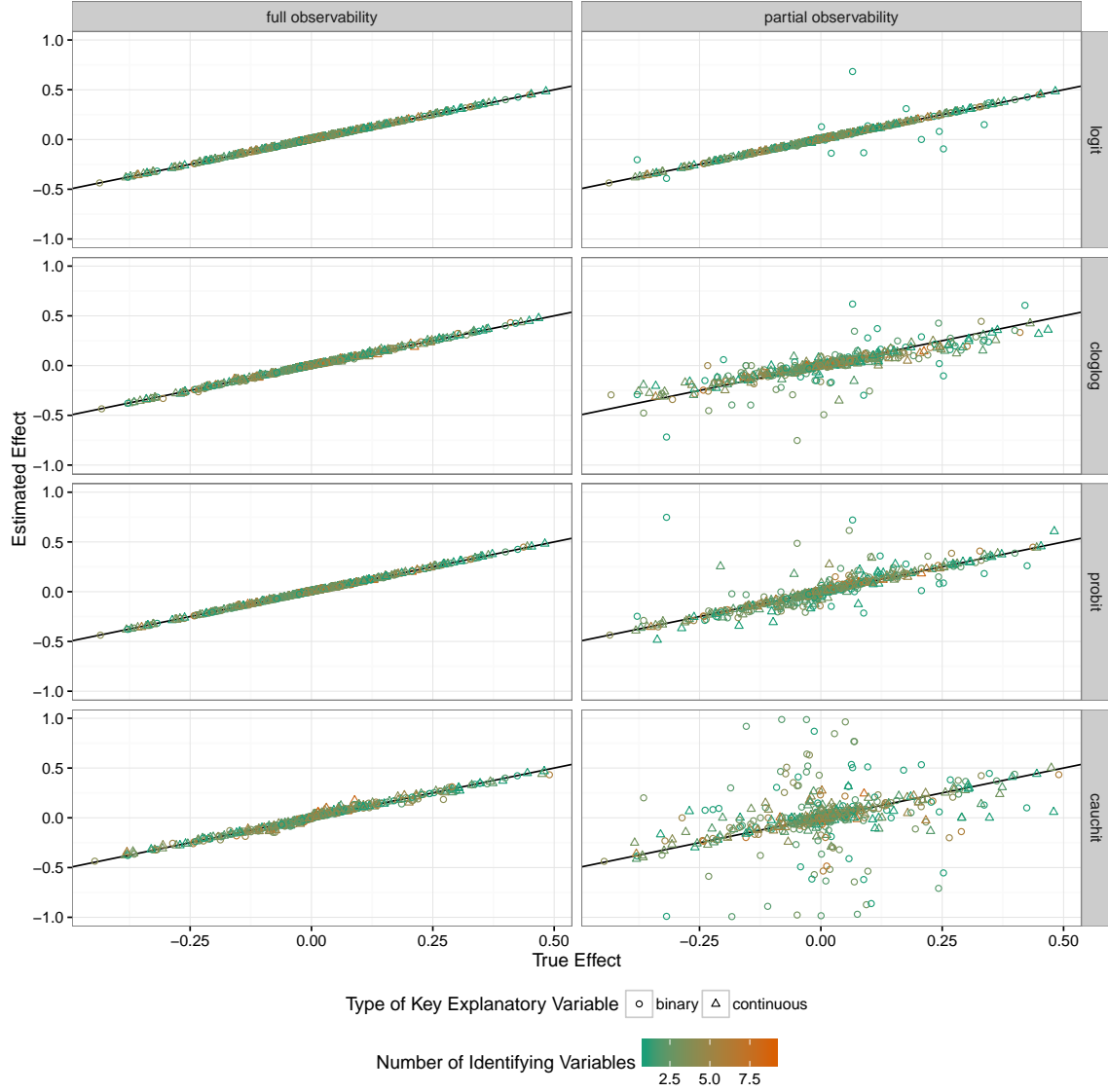


FIGURE 2: These scatterplots show the large-sample estimates of the first difference as the true first difference varies. The left column shows the estimates under full observability (i.e., usual logit model) and the right column shows the estimates under partial observability. The top row shows the estimates when the link function is specified correctly as logit. The remaining rows show the estimates when the link function is not specified correctly (i.e., specified as logit when the DGP is probit, cloglog, and cauchit).

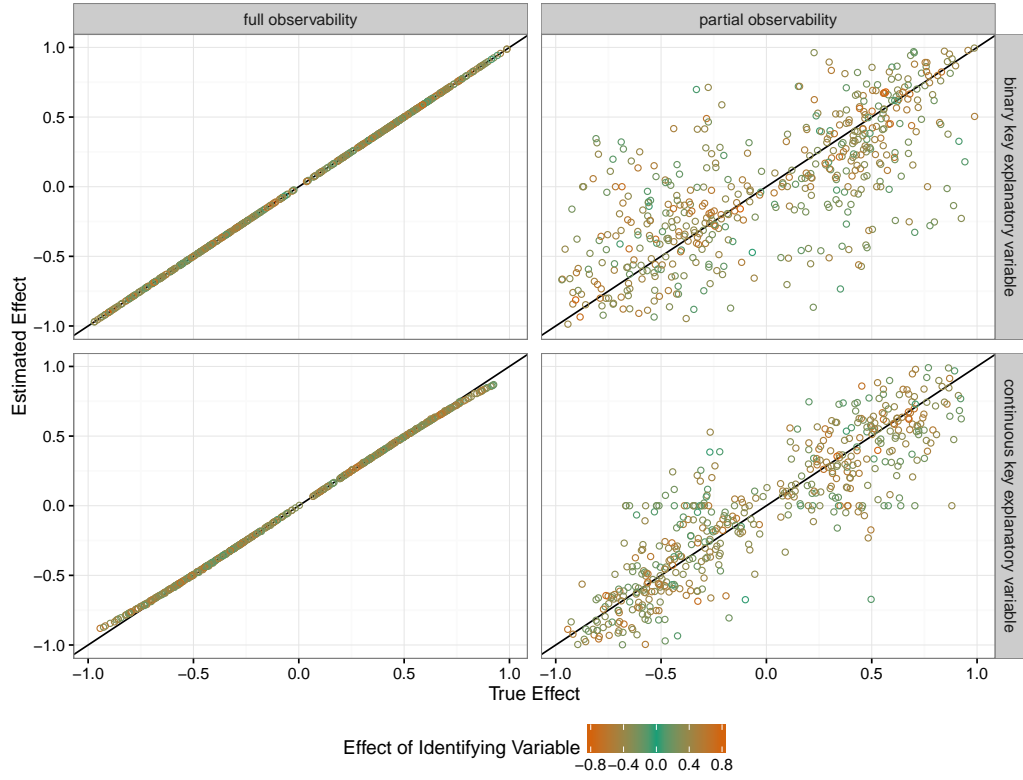


FIGURE 3: These scatterplots show the large-sample estimates of the first difference as the true first difference varies. The left column shows the estimates under full observability (i.e., usual logit model) and the right column shows the estimates under partial observability. The top row shows the estimates when the key explanatory variable is binary and the bottom row shows the estimates when the key explanatory variable is continuous.

(A)			(B)		
$(\beta, \gamma) = (-1, 1)$			$(\beta, \gamma) = (1, -1)$		
	$z = 0$	$z = 1$		$z = 0$	$z = 1$
$x = 0$	$\delta(0)\delta(0) = 0.25$	$\delta(0)\delta(-1) = 0.13$	$x = 0$	$\delta(0)\delta(0) = 0.25$	$\delta(0)\delta(-1) = 0.13$
$x = 1$	$\delta(-1)\delta(1) = 0.20$	$\delta(-1)\delta(0) = \mathbf{0.13}$	$x = 1$	$\delta(1)\delta(-1) = 0.20$	$\delta(1)\delta(-2) = \mathbf{0.09}$

TABLE 1: Expected proportional under the two possible parameter combinations of the stylized partial observability model.