

# Appendix

## Unreliable Inferences about Unobserved Processes

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### 1 Algorithm for Wrong Link Function Simulations

1. Choose  $n_x$  and  $n_z$  independently from a Poisson distribution with mean 1.5. If both  $n_x$  and  $n_z$  equal zero, then set  $n_z$  equal to one.
2. Choose  $n_w - 1$  from a Poisson distribution with mean 0.5.
3. Assign a type (continuous or binary) to each of the  $n_x + n_z + n_w$  variables with equal probability. To simplify the computation, continuous variables take on the values 0.0, 0.2, 0.4, 0.6, 0.8, or 1.0, and binary variables take on the values 0 or 1.
4. To simplify the computation, create a data set  $WXZ$  that contains each possible combination of all of the explanatory variables.
5. Choose the preliminary coefficients  $\beta^*$  and  $\gamma^*$  from a normal distribution. The intercept coefficients come from a normal distribution with mean 0 and standard deviation 2. The slope coefficients come from a normal distribution with mean 0 and standard deviation 1.
6. If the link function of the DGP is logit, then set  $\beta$  equal to  $\beta^*$  and  $\gamma$  equal to  $\gamma^*$ . If the link function is some other function  $g$ , then (1) simulate a large data set from the logit DGP, (2) estimate a model with link function  $g$  to that data set, and (3) set  $\beta$  and  $\gamma$  equal to the estimates  $\hat{\beta}$  and  $\hat{\gamma}$ , respectively. This step scales the coefficients so that the quantities of interest have comparable magnitude regardless of the DGP.
7. Using the parameters  $\beta$  and  $\gamma$ , simulate 100,000,000 values of  $y_{obs}$  and  $d_{main}$  for each combination of the explanatory variables.
8. Fit a full observability model to the outcome variable  $d_{main}$ . Calculate the first difference as  $w_1$  moves from 0 to 1. Store this large-sample estimate.
9. Fit a partial observability model to the observed outcome variable  $y_{obs}$ . Calculate the first difference as  $w_1$  moves from 0 to 1. Store this large-sample estimate.

### 2 Algorithm for Monotonic Link Function Simulations

1. Choose the coefficients for the non-linear, interactive equations.

$$\Pr(d_{main}) = \beta_{cons} + \beta_w w + \beta_{w^2} w^2$$

and

$$\Pr(d_{nuisance}) = \gamma_{cons} + \gamma_w w + \gamma_z z + \gamma_{w^2} w^2 + \gamma_{z^2} z^2 + \gamma_{wz} wz.$$

from a uniform distribution that ranges from -1 to 1.

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2. Check that this link function produces a monotonic relationship between the  $w$  and  $\Pr(d_{main})$  and between  $w$  and  $z \Pr(d_{nuisance})$ .
3. Set  $w$  as either binary or continuous. For computational ease, continuous variables take on the values 0.0, 0.2, 0.4, 0.6, 0.8, or 1.0, and binary variables take on the values 0 or 1.
4. Create a data set  $WZ$  that contains each possible combination of  $w$  and  $z$ .
5. For each row in  $WZ$ , simulate 100,000,000 values of  $y_{obs}$  and  $d_{main}$ .
6. Fit a full observability model to the outcome variable  $d_{main}$ . Calculate the first difference as  $w_1$  moves from 0 to 1. Store this large-sample estimate.
7. Fit a partial observability model to the outcome variable  $y_{obs}$ . Calculate the first difference as  $w_1$  moves from 0 to 1. Store this large-sample estimate.