Electroweakinos

Carl Martin Fevang

November 23, 2022

1 Background

$\mathbf{2}$ Mixing Matrices

2.1**Neutralino Mixing**

Neutralinos are generally comprised of the three Standard Model neutrinos and the neutral component of the fermion partners to the U(1) and SU(2) gauge fields B^0, W^0 and the neutral fermion partners to the Higgs fields H_d, H_u . Neglecting the neutrino mixing into these states, we can summarise the mass terms from the superpotential, putting the fermion fields into a vector $\psi_0^T = (\tilde{B}^0, \tilde{W}^0, \tilde{H}_d^0, \tilde{H}_u^0)$,

$$\mathcal{L}_{\tilde{\chi}^0 - \text{mass}} = -\frac{1}{2} \psi_0^T M_{\tilde{\chi}^0} \psi_0 + \text{c. c.}, \tag{1}$$

where

$$M_{\tilde{\chi}^{0}} = \begin{bmatrix} M_{1} & 0 & -\frac{1}{\sqrt{2}}g'v_{d} & \frac{1}{\sqrt{2}}g'v_{u} \\ 0 & M_{2} & \frac{1}{\sqrt{2}}gv_{d} & -\frac{1}{\sqrt{2}}gv_{u} \\ -\frac{1}{\sqrt{2}}g'v_{d} & \frac{1}{\sqrt{2}}gv_{d} & 0 & -\mu \\ \frac{1}{\sqrt{2}}g'v_{u} & -\frac{1}{\sqrt{2}}gv_{u} & -\mu & 0 \end{bmatrix}$$

$$= \begin{bmatrix} M_{1} & 0 & -c_{\beta}s_{W}m_{Z} & s_{\beta}s_{W}m_{Z} \\ 0 & M_{2} & c_{\beta}c_{W}m_{Z} & -s_{\beta}c_{W}m_{Z} \\ -c_{\beta}s_{W}m_{Z} & c_{\beta}c_{W}m_{Z} & 0 & -\mu \\ s_{\beta}s_{W}m_{Z} & -s_{\beta}c_{W}m_{Z} & -\mu & 0 \end{bmatrix}.$$
(2a)

$$= \begin{bmatrix} M_1 & 0 & -c_{\beta}s_W m_Z & s_{\beta}s_W m_Z \\ 0 & M_2 & c_{\beta}c_W m_Z & -s_{\beta}c_W m_Z \\ -c_{\beta}s_W m_Z & c_{\beta}c_W m_Z & 0 & -\mu \\ s_{\beta}s_W m_Z & -s_{\beta}c_W m_Z & -\mu & 0 \end{bmatrix}.$$
 (2b)

$$M_{\tilde{\chi}^{\pm}} = \begin{bmatrix} 0 & 0 & M_2 & gv_d \\ 0 & 0 & gv_u & \mu \\ M_2 & gv_u & 0 & 0 \\ gv_d & \mu & 0 & 0 \end{bmatrix}$$
(3a)

$$= \begin{bmatrix} 0 & 0 & M_2 & \sqrt{2}c_{\beta}c_W m_Z \\ 0 & 0 & \sqrt{2}s_{\beta}c_W m_W & \mu \\ M_2 & \sqrt{2}s_{\beta}c_W m_W & 0 & 0 \\ \sqrt{2}c_{\beta}c_W m_Z & \mu & 0 & 0 \end{bmatrix}$$
(3b)

$$m_{\tilde{\chi}_{1,2}^{\pm}} = \frac{1}{2} \left(|M_2|^2 + |\mu|^2 + 2m_W^2 \mp \sqrt{(|M_2|^2 + |\mu|^2 + 2m_W^2)^2 - 4|\mu M_2 - m_W^2 s_\beta^2|^2} \right)$$
(4)