Fiscal-Monetary Interactions and the FTPL: "Paper Money" (AER 2013) by Chris Sims

Carlo Galli

uc3m & CEPR

Topics in Macroeconomics A uc3m, spring 2025

Motivation

- Recent developments in CB balance sheets and sovereign debt sizes
- · Fiscal and monetary policy are deeply intertwined
- Conventional (quantity theory) models with
 - non-interest bearing money
 - a "money multiplier"
 - tight relation between P and M

are inadequate for current policy discussions

- The FTPL is a more adequate framework
 - this paper tries to bring FTPL down to earth

First model

Samuelson's consumption loan model with storage

Simple OLG model with gov't debt and storage

Households

$$\begin{aligned} \max_{\{c_t^{\gamma}, c_{t+1}^{o}, B_t, s_t\}} & \log(c_t^{\gamma}) + \log(c_{t+1}^{o}) \\ \text{s.t.} & c_t^{\gamma} + s_t + \frac{B_t}{P_t} = e^{\gamma} \\ & c_{t+1}^{o} = \frac{B_t R}{P_{t+1}} + \theta s_t, \quad \theta \in (0, 1) \end{aligned}$$

Government

$$B_{t+1} = RB_t$$
$$B_t \ge 0$$

can always think of R=1 and of debt as paper money

Optimality

$$rac{c_{t+1}^o}{c_t^y} = heta \quad \text{if } s_t > 0$$
 $rac{c_{t+1}^o}{c_t^y} = R_t rac{P_t}{P_{t+1}} \quad \text{if } B_t > 0$

Let

- $W_t := s_t + \frac{B_t}{P_t}$ denote savings
- ullet ho_t be the real rate of return on W_t

The log-utility assumption implies

$$\frac{c_{t+1}^o}{c_t^y} = \rho_t \quad \Rightarrow \quad \frac{\rho_t W_t}{e^y - W_t} = \rho_t \quad \Rightarrow \quad W_t = c_t^y = e^y/2$$

Equilibrium without storage

Households only save in bonds $W_t = \frac{B_t}{P_t} = e^y/2$

From the goods market clearing condition

$$c_t^y + c_t^o = e^y$$
$$e^y/2 + \rho_t e^y/2 = e^y$$

which implies $\rho_t = 1$, $R = \frac{P_{t+1}}{P_t}$, and $c_{t+1}^o = c_t^y = e^y/2$

The government budget implies that the real value of debt is constant

$$\frac{B_t}{P_t} = \frac{B_{t-1}}{P_{t-1}}$$

and the debt market clearing condition requires it is equal to household savings: $\frac{B_t}{P_t} = e^y/2$

Equilibrium without storage

Consumption of the initial old is given by

$$c_1^o = R \frac{B_0}{P_1} = \frac{B_1}{P_1} = e^y/2$$

so that

$$P_1 = \frac{2}{e^y} RB_0.$$

The price level is uniquely determined.

Equilibrium with storage

By no-arbitrage, $\theta = \rho_t = R \frac{P_t}{P_{t+1}}$ (the inflation rate $\frac{P_{t+1}}{P_t} = \frac{R}{\theta}$ is higher now)

Plugging no-arbitrage into the govt BC

$$\frac{B_t}{P_t} = \theta \frac{B_{t-1}}{P_{t-1}}$$

so in the limit $\frac{B_t}{P_t} o 0$ and in turn $s_t o e^y/2$

In the initial period, storage and real debt are indeterminate. Any

$$c_1^o = R \frac{B_0}{P_1} = \frac{B_1}{P_1} < e^y/2 \quad \Leftrightarrow \quad P_1 > \frac{2}{e^y} R B_0$$

is an equilibrium. The price level is indeterminate.

Note: in any equilibrium with storage, $c_t^o = \theta/2 < 1/2$ for all t, worse than no-storage eqm

Discussion

Remember that we can always think of paper money if R = 1 and $B \equiv M$.

In the equilibria with storage, P_1 is "too high"

- there is too little real debt available for households to save
- they then use storage, rates of return are low because of no-arbitrage,
- government pays negative interest rates (runs surpluses!), future real debt is even scarcer, and so on...

Tax Backing. Now, assume that the young pay lump-sum taxes

$$c_t^y + W_t + \tau = e^y$$
$$\frac{B_t}{P_t} = R \frac{B_{t-1}}{P_t} - \tau$$

Equilibrium with storage and tax backing

Recall that by no-arbitrage $\rho_t=\theta<1$, which implies $\frac{B_t}{P_t}=\theta\frac{B_{t-1}}{P_{t-1}}$

Iterate gBC backwards

$$\frac{B_t}{P_t} = \theta^{t-1} \frac{B_1}{P_1} - \tau \sum_{j=0}^{t-1} \theta^j \quad \text{so that} \quad \lim_{t \to \infty} \frac{B_t}{P_t} = -\frac{\tau}{1-\theta}$$

so $\rho_t < 1$ cannot be an equilibrium: in the limit, gov't would be net saver, which we are ruling out $(B_t \ge 0)$. Intuitively,

- the gov't surpluses now are independent of the size of debt, so it eventually accumulates savings ⇒ fiscal policy now incompatible with arbitrary path of prices
- If $B \equiv M$, the gov't is shrinking the stock of money by raising taxes

In either case, household wealth eventually not enough to finance taxes. The demand for savings \uparrow , $P_1 \downarrow$.

Equilibrium without storage and tax backing

Same idea as equilibrium without tax backing, but now youngs have smaller effective endowment ${\it e}^y-\tau$

- lower savings $W_t = \frac{e^y \tau}{2}$
- higher real rate of return $ho_t = rac{e^y + au}{e^y au} > 1$
- less consumption smoothing: $c_t^y = \frac{e^y \tau}{2}$, $c_{t+1}^o = \frac{e^y + \tau}{2}$
- for the initial old, $c_1^o=\frac{RB_0}{P_1}= au+\frac{B_1}{P_1}= au+\frac{e^y- au}{2}$ so that $P_1=\frac{2}{e_y- au}RB_0$

The government budget is $\frac{B_t}{P_t} = \frac{B_{t-1}}{P_{t-1}} \rho - \tau$, and real debt is constant. The debt valuation equation holds: $\frac{B_t}{P_t} = \frac{\tau}{\rho - 1}$

Taking stock

Without fiscal backing

- 1 eqm without storage, where govt paper is valued as a store of value, and $1 = R \frac{P_t}{P_{t+1}}$ (Wallace (1998): use of money as endogenous outcome rather than assumption)
- ullet ∞ eqa with storage

Govt paper can have value in these models even if it is not backed

With fiscal backing

- ullet equilibria with indeterminate P_t and $B_t/P_t
 ightarrow 0$ are ruled out
- unique eqm has lower welfare, but arbitrarily close to perfect smoothing as au o 0, and $\frac{e^y + \tau}{e^y \tau} = R \frac{P_t}{P_{t+1}}$

Note: you have seen case with no storage technology, $B_t = M$ and $e^o > 0$, which also had

- ullet ∞ eqa where money is valued but its value converges to zero $(P_t o \infty)$
- autarky eqm where money is never valued

Second model Debt as fiscal cushion

Well-known optimal fiscal-monetary policy results:

- 1. With distortionary taxes and state-contingent debt, taxes are smooth and independent of the debt stock, and debt returns absorb shocks (Lucas and Stokey (1983))
- 2. Surprise inflation can make non-contingent nominal debt state-contingent in real terms
 - but that is only optimal when surprise inflation is costless (Siu (2004), Schmitt-Grohé and Uribe (2004))
 - with long-term debt, state-contingency can be achieved through debt valuation effects (i.e. future inflation)

Debt as fiscal cushion

This model

- adds price level determination to Barro (1979)
- shows how nominal debt can be used as a "fiscal cushion" via long-term interest rates and/or inflation

Govt objective

$$egin{aligned} \max_{P_t, \mathcal{B}_t, \mathcal{R}_t, au_t} &- rac{1}{2} \mathbb{E} \left[\sum_{t=0}^{\infty} eta^t \left(au_t^2 + heta(
u_t - 1)^2
ight)
ight] \ ext{s.t.} \quad b_t &= R_{t-1}
u_t b_{t-1} + g_t - au_t \ R_t \mathbb{E}_t [
u_{t+1}] &=
ho \end{aligned}$$

with
$$\nu_t = P_{t-1}/P_t$$
, $b_t = B_t/P_t$ and $\rho = 1/\beta$ g_t is exogenous and random

Optimality

First-order conditions

$$\begin{aligned} \tau_t &= \lambda_t & \text{(taxes)} \\ \lambda_t &= \beta R_t \mathbb{E}[\nu_{t+1} \lambda_{t+1}] & \text{(debt)} \\ \mu_t \mathbb{E}[\nu_{t+1}] &= \beta b_t \mathbb{E}[\nu_{t+1} \lambda_{t+1}] & (R_t) \\ \theta(\nu_t - 1) + \lambda_t R_{t-1} b_{t-1} &= \mu_{t-1} R_{t-1} \beta^{-1} & (\nu_t) \end{aligned}$$

Combine (R_t) and (debt): $\mu_t \rho = b_t \lambda_t$

Combining FOCs for b, R, ν we get tradeoff for ν_t

$$\theta(\nu_t - 1) = (\tau_{t-1} - \tau_t) R_{t-1} b_{t-1}$$

welfare loss at t = budget benefit at (t-1) (lower R_{t-1} via Fisher eq.) — budget cost at t

With $\theta = 0$

- $\tau_t = \tau_{t-1} = \tau$ constant
- iterating the govt BC forward we get

$$b_t = rac{ au}{
ho - 1} - \mathbb{E}_{oldsymbol{t}} \sum_{j=1}^\infty eta^j oldsymbol{\mathsf{g}}_{t+j}$$

- with g_t i.i.d., b_t remains constant
- surprise inflation (swings in ν_t) absorb all effect of g_t shocks

With
$$\theta = \infty$$

- $\nu_t = 1$
- $au_t = \mathbb{E}_t[au_{t+1}]$ (martingale as in Barro (1979))

With $0 < \theta < \infty$

- mix of surprise inflation and tax changes
- compare 1-period with consol debt model

Consol Debt

- let A_t be a consol: never matures, pays 1 dollar every period, has price Q_t
- new govt BC

$$Q_{t} \frac{A_{t} - A_{t-1}}{P_{t}} = \frac{A_{t-1}}{P_{t}} + g_{t} - \tau_{t}$$

• define $b_t := \frac{Q_t A_t}{P_t}$ (real value of consol debt)

$$b_t = b_{t-1}
u_t rac{1 + Q_t}{Q_{t-1}} + g_t - au_t$$

Fisher equation of the private sector

$$\mathbb{E}_t \frac{(1+Q_{t+1})\nu_{t+1}}{Q_t} = \rho$$

Optimal response to a spending shock

Numerical example (local approximation around steady-state) g_t i.i.d. with $\mathbb{E}[g_t]=1, \ \rho=1.1, \ \tau=2, \ \nu=1, \ b=10$

Experiment: one time shock, $\uparrow g_t$ by 1 unit. Study optimal fiscal/monetary policy responses

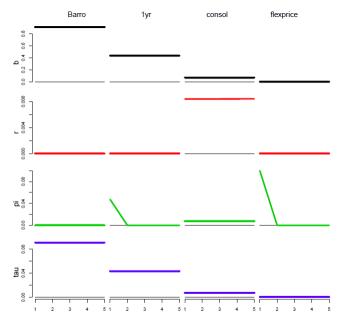
Real debt $(\theta = \infty)$: permanent increase of τ (0.91) and b (0.09)

Increase in au perfectly smoothed over time, enough to service higher debt forever

Flexible prices ($\theta = 0$): one-off surprise $\uparrow \pi$ by 10p.p. (\approx small default) Small one-off reduction in debt service, nothing else changes

Intermediate case ($\theta = 10$):

- One-Year Debt
 - permanent fiscal adjustment $(b \uparrow 0.43, \tau \uparrow 0.043)$, one-off monetary $(\frac{1}{\nu} \uparrow 0.048 \text{ p.p.})$
 - mainly fiscal response, π -default must be immediate so cannot be too large
- Consol Debt
 - both adjustments permanent $(b \uparrow 0.07, \tau \uparrow 0.007 \text{ and } \frac{1}{\nu} \uparrow 0.74 \text{ p.p.})$
 - $-\,$ mainly monetary response, $\pi\text{-default}$ on bondholders spread out to infinity



References

- **Barro, Robert J.**, "On the Determination of the Public Debt," *Journal of Political Economy*, 1979, *87*, 940–971.
- **Jr., Robert E. Lucas and Nancy L. Stokey**, "Optimal Fiscal and Monetary Policy in an Economy without Capital," *Journal of Monetary Economics*, 1983, *12*, 55–93.
- **Schmitt-Grohé, Stephanie and Martin Uribe**, "Optimal fiscal and monetary policy under sticky prices," *Journal of Economic Theory*, 2004, 114 (2), 198–230.
- **Siu, Henry E.**, "Optimal fiscal and monetary policy with sticky prices," *Journal of Monetary Economics*, 2004, *51* (3), 575–607.
- Wallace, Neil, "A dictum for monetary theory," Quarterly Review, 1998, 22 (Win), 20–26.