

DEALING WITH HETEROGENEOUS CREDITORS IN SOVEREIGN BOND RESTRUCTURINGS

Carlo Galli
UC3M

Stéphane Guibaud
SciencesPo

INTERNATIONAL FINANCE AND MACROECONOMICS
BSE Summer Forum, June 16th 2023

INTRODUCTION

Recent sovereign bond restructurings

- multiple bond series
- heterogeneous exchange offers
- heterogeneous choices by bondholders
- use of 'enhanced' CACs

INTRODUCTION

Recent sovereign bond restructurings

- multiple bond series
- heterogeneous exchange offers
- heterogeneous choices by bondholders
- use of 'enhanced' CACs

Collective Action Clauses (CACs)

- key pillar of debt restructuring framework with private creditors
- in a debt exchange, supermajority of consenting creditors can bind dissenting minority

INTRODUCTION

Recent sovereign bond restructurings

- multiple bond series
- heterogeneous exchange offers
- heterogeneous choices by bondholders
- use of 'enhanced' CACs

Collective Action Clauses (CACs)

- key pillar of debt restructuring framework with private creditors
- in a debt exchange, supermajority of consenting creditors can bind dissenting minority

Enhanced CACs

- inserted in external bond issuances since 2014-15 (ICMA 2014)
- when restructuring multiple bond series, sovereign can choose among 3 voting rules

ENHANCED CACs: DEFINITION

Within a restructuring of multiple bonds, can choose among 3 voting rules

Source: Indenture of Ecuador's 10.75% 2022 Notes

ENHANCED CACs: DEFINITION

Within a restructuring of multiple bonds, can choose among 3 voting rules

- **Series-by-series: within-bond ($\approx 75\%$)**

*In the case of any **Modification** of the terms and conditions of the Notes [...], such Modification may be made with the consent of Ecuador and of holders of **at least 75%** in aggregate principal amount of the Notes then outstanding.*

Source: Indenture of Ecuador's 10.75% 2022 Notes

ENHANCED CACs: DEFINITION

Within a restructuring of multiple bonds, can choose among 3 voting rules

- **Series-by-series: within-bond ($\approx 75\%$)**

In the case of any Modification of the terms and conditions of the Notes [...], such Modification may be made with the consent of Ecuador and of holders of at least 75% in aggregate principal amount of the Notes then outstanding.

- **Two-limb: across-bonds ($\approx 66.6\%$) and within-bond ($\approx 50\%$)**

*[...] any modification to the terms and conditions of **two or more series** may be made [...] with the consent of the Republic, and (x) the holders of **at least $66\frac{2}{3}\%$** of the aggregate principal amount of the outstanding debt securities **of all series [...]** (taken in aggregate); and (y) the holders of **more than 50%** the aggregate principal amount [...] **of each affected series (taken individually)**.*

Source: Indenture of Ecuador's 10.75% 2022 Notes

ENHANCED CACs: DEFINITION

Within a restructuring of multiple bonds, can choose among 3 voting rules

- **Series-by-series: within-bond ($\approx 75\%$)**

In the case of any Modification of the terms and conditions of the Notes [...], such Modification may be made with the consent of Ecuador and of holders of at least 75% in aggregate principal amount of the Notes then outstanding.

- **Two-limb: across-bonds ($\approx 66.6\%$) and within-bond ($\approx 50\%$)**

[...] any modification to the terms and conditions of two or more series may be made [...] with the consent of the Republic, and (x) the holders of at least $66 \frac{2}{3}\%$ of the aggregate principal amount of the outstanding debt securities of all series [...] (taken in aggregate); and (y) the holders of more than 50% the aggregate principal amount [...] of each affected series (taken individually).

- **Single-limb: across-bonds ($\approx 75\%$) + uniform applicability constraint**

*[...] any modification to the terms and conditions of **two or more series** may be made, [...] with the consent of the Republic, and the holders of at least 75% of the aggregate principal amount [...] **of all series** [...] (taken in aggregate), provided that the **Uniformly Applicable condition** is satisfied.*

Source: Indenture of Ecuador's 10.75% 2022 Notes

ENHANCED CACs IN PRACTICE

Adoption

- two-limb CACs inserted in bond contracts since Uruguay 2003
- single-limb introduction in 2014 viewed as key innovation
- wide belief that single-limb would be most effective procedure
 - *more robust ‘aggregation’ feature designed to limit the ability of holdouts to neutralize traditional CACs, which operate on a series-by-series basis (IMF, 2014)*
- Eurozone 2022 Model CACs include single-limb only

ENHANCED CACs IN PRACTICE

Adoption

- two-limb CACs inserted in bond contracts since Uruguay 2003
- single-limb introduction in 2014 viewed as key innovation
- wide belief that single-limb would be most effective procedure
 - *more robust ‘aggregation’ feature designed to limit the ability of holdouts to neutralize traditional CACs, which operate on a series-by-series basis* (IMF, 2014)
- Eurozone 2022 Model CACs include single-limb only

Argentina & Ecuador 2020 debt restructurings

- enhanced CACs tested in practice for the first time
- both opted for two-limb aggregation
- both made differentiated exchange offers across bond series

THIS PAPER

- A theoretical analysis of optimal debt restructuring with
 - multiple bonds
 - heterogeneous creditors
 - enhanced CACs

THIS PAPER

- A theoretical analysis of optimal debt restructuring with
 - multiple bonds
 - heterogeneous creditors
 - enhanced CACs
- Consider **heterogeneity**
 - within each bond
 - across bonds

(e.g. expected litigation cost/outcome, discount rates, coupon/maturity preferences)

THIS PAPER

- A theoretical analysis of optimal debt restructuring with
 - multiple bonds
 - heterogeneous creditors
 - enhanced CACs
- Consider **heterogeneity**
 - within each bond
 - across bonds

(e.g. expected litigation cost/outcome, discount rates, coupon/maturity preferences)
- Characterise
 - optimal offers, for a given voting rule
 - optimal voting rule

for the debtor government

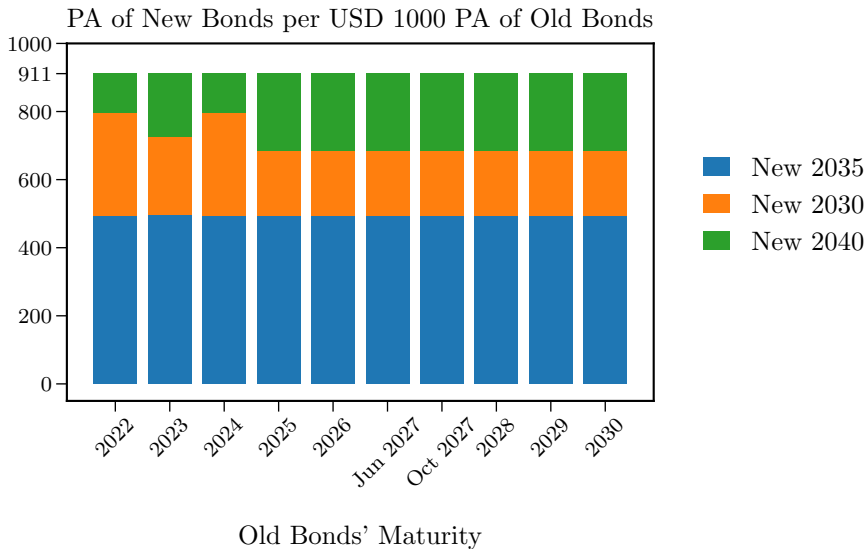
LITERATURE

- Theoretical: single bond restructurings
 - Haldane et al. (2005); Engelen and Lambsdorff (2009); Bi, Chamon and Zettelmeyer (2016); Pitchford and Wright (2012, 2017)
- Empirical: bond-level restructuring outcomes
 - Fang, Schumacher and Trebesch (2021); Asonuma, Niepelt and Ranciere (2023)
- Empirical: effects of CACs on bond prices
 - Becker et al. (2003); Eichengreen Mody (2004); Carletti et al. (2016, 2020); Chung and Papaioannou (2020)

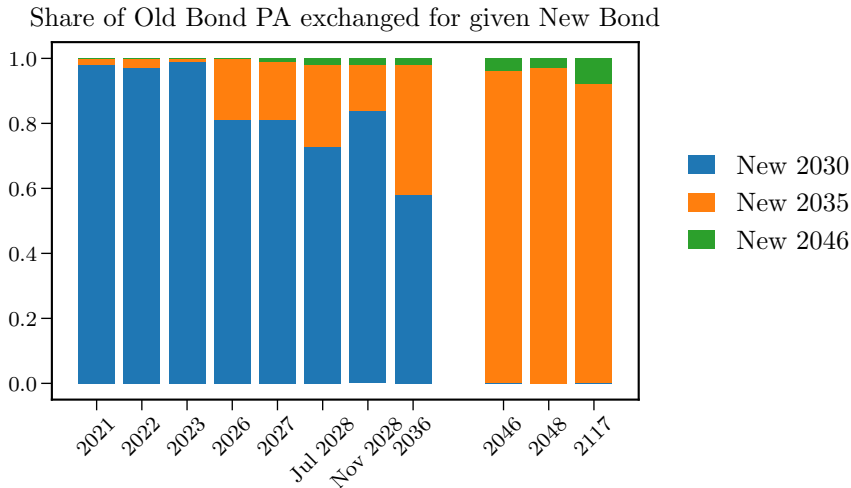
OUTLINE

- Motivating evidence
- Static model, two bonds
 - setup
 - optimal offers given voting rule
 - optimal voting rule
 - comparative statics
- Environments
 - deterministic
 - stochastic

ECUADOR 2020: HETEROGENEOUS OFFERS



ARGENTINA 2020: HETEROGENEOUS OFFERS & CHOICES



Old Bonds' Maturity (2016-Indenture (Macri) USD bonds)

MODEL SETUP

Restructuring pool: 2 bonds

MODEL SETUP

Restructuring pool: 2 bonds

- bond H , relative weight λ
- bond L , relative weight $1 - \lambda$

MODEL SETUP

Restructuring pool: 2 bonds

- bond H , relative weight λ
- bond L , relative weight $1 - \lambda$

Bondholders

- atomistic
- assign *idiosyncratic* reservation value v to holding out of the bond exchange
- holders of bond i have reservation values distributed according to CDF F_i

MODEL SETUP

Restructuring pool: 2 bonds

- bond H , relative weight λ
- bond L , relative weight $1 - \lambda$

Bondholders

- atomistic
- assign *idiosyncratic* reservation value v to holding out of the bond exchange
- holders of bond i have reservation values distributed according to CDF F_i

Exchange offer

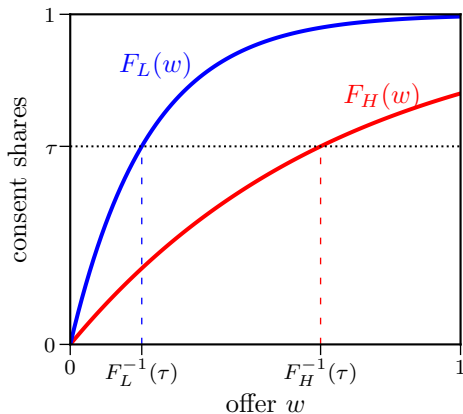
- government makes offer w_i to holders of bond i
- creditor accepts if $w_i \geq v$
- share of consent within bond i is given by $F_i(w_i)$

CREDITOR-BOND HETEROGENEITY

- Holders of bond H have higher reservation values

$$F_H(w) < F_L(w) \quad \text{for any } w$$

\Rightarrow bond H has better payment terms, holders have better litigation skills, ...



GOVERNMENT PROBLEM

- Objective function = restructuring payout

$$\min_{w_H, w_L} \lambda w_H + (1 - \lambda)w_L$$

GOVERNMENT PROBLEM

- Objective function = restructuring payout

$$\min_{w_H, w_L} \lambda w_H + (1 - \lambda)w_L$$

- Participation constraints depend on the voting rule
 - Two-limb

$$F_i(w_i) \geq \tau_2^s \quad \text{for } i \in \{H, L\} \quad (\text{series-by-series})$$

$$\lambda F_H(w_H) + (1 - \lambda)F_L(w_L) \geq \tau_2^a \quad (\text{aggregate})$$

GOVERNMENT PROBLEM

- Objective function = restructuring payout

$$\min_{w_H, w_L} \lambda w_H + (1 - \lambda)w_L$$

- Participation constraints depend on the voting rule
 - Two-limb

$$F_i(w_i) \geq \tau_2^s \quad \text{for } i \in \{H, L\} \quad (\text{series-by-series})$$

$$\lambda F_H(w_H) + (1 - \lambda)F_L(w_L) \geq \tau_2^a \quad (\text{aggregate})$$

- Single-limb

$$w_H = w_L = w \quad (\text{uniform applicability})$$

$$\lambda F_H(w) + (1 - \lambda)F_L(w) \geq \tau_1 \quad (\text{aggregate})$$

GOVERNMENT PROBLEM

- Objective function = restructuring payout

$$\min_{w_H, w_L} \lambda w_H + (1 - \lambda)w_L$$

- Participation constraints depend on the voting rule
 - Two-limb

$$F_i(w_i) \geq \tau_2^s \quad \text{for } i \in \{H, L\} \quad (\text{series-by-series})$$

$$\lambda F_H(w_H) + (1 - \lambda)F_L(w_L) \geq \tau_2^a \quad (\text{aggregate})$$

- Single-limb

$$w_H = w_L = w \quad (\text{uniform applicability})$$

$$\lambda F_H(w) + (1 - \lambda)F_L(w) \geq \tau_1 \quad (\text{aggregate})$$

- We assume $\tau_2^s < \tau_2^a \leq \tau_1$

GOVERNMENT PROBLEM

- Objective function = restructuring payout

$$\min_{w_H, w_L} \lambda w_H + (1 - \lambda)w_L$$

- Participation constraints depend on the voting rule
 - Two-limb

$$F_i(w_i) \geq \tau_2^s \quad \text{for } i \in \{H, L\} \quad (\text{series-by-series})$$

$$\lambda F_H(w_H) + (1 - \lambda)F_L(w_L) = \tau_2^a \quad (\text{aggregate})$$

- Single-limb

$$w_H = w_L = w \quad (\text{uniform applicability})$$

$$\lambda F_H(w) + (1 - \lambda)F_L(w) = \tau_1 \quad (\text{aggregate})$$

- We assume $\tau_2^s < \tau_2^a \leq \tau_1 \Rightarrow$ aggregate constraint binds

‘AUXILIARY’ PROBLEM

- Problem with aggregate constraint only

$$\begin{aligned} \min_{w_H, w_L} \quad & \lambda w_H + (1 - \lambda)w_L \\ \text{s.t.} \quad & \lambda F_H(w_H) + (1 - \lambda)F_L(w_L) = \tau \end{aligned}$$

‘AUXILIARY’ PROBLEM

- Problem with aggregate constraint only

$$\begin{aligned} \min_{w_H, w_L} \quad & \lambda w_H + (1 - \lambda)w_L \\ \text{s.t.} \quad & \lambda F_H(w_H) + (1 - \lambda)F_L(w_L) = \tau \end{aligned}$$

- Additional constraint in full problem depends on voting rule
 - Two-limb: $\tau = \tau_2^a$ and $F_i(w_i) \geq \tau_2^s$ for $i \in \{H, L\}$
 - Single-limb: $\tau = \tau_1$ and $w_H = w_L$

SINGLE-LIMB OFFER

- Optimal uniform offer w_u s.t.

$$\lambda F_H(w_u) + (1 - \lambda)F_L(w_u) = \tau_1$$

- Total government cost

$$C_1 = w_u$$

- Remarks

- $F_H(w_u) < \tau_1 < F_L(w_u)$
- $w_u(\lambda, \tau_1)$ increasing in λ, τ_1

SINGLE-LIMB OFFER

- Optimal uniform offer w_u s.t.

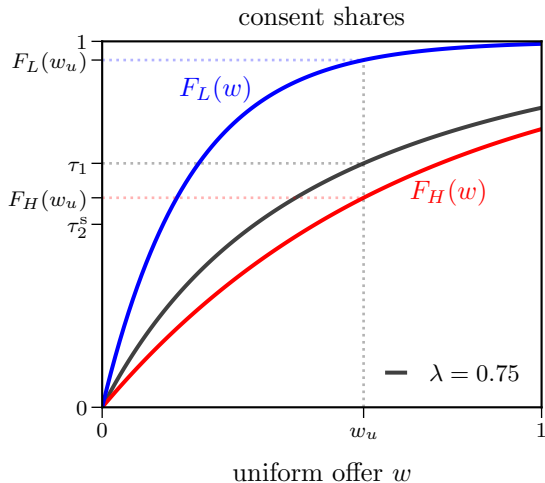
$$\lambda F_H(w_u) + (1 - \lambda)F_L(w_u) = \tau_1$$

- Total government cost

$$C_1 = w_u$$

- Remarks

- $F_H(w_u) < \tau_1 < F_L(w_u)$
- $w_u(\lambda, \tau_1)$ increasing in λ, τ_1



SINGLE-LIMB OFFER

- Optimal uniform offer $w_u(\lambda, \tau_1)$ s.t.

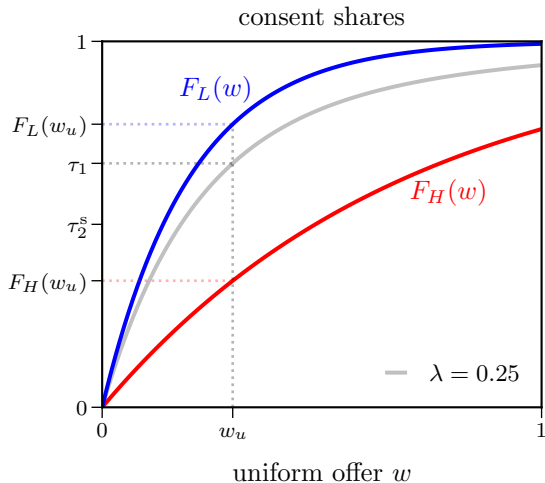
$$\lambda F_H(w_u) + (1 - \lambda)F_L(w_u) = \tau_1$$

- Total government cost

$$C_1 = w_u$$

- Remarks

- $F_H(w_u) < \tau_1 < F_L(w_u)$
- $w_u(\lambda, \tau_1)$ increasing in λ, τ_1



TWO-LIMB OFFER

- Auxiliary problem

$$\min_{w_H} C_2(w_H) := \lambda w_H + (1 - \lambda)g(w_H) \quad \text{where} \quad g(w_H) := F_L^{-1} \left(\frac{\tau_2^a - \lambda F_H(w_H)}{1 - \lambda} \right)$$

TWO-LIMB OFFER

- Auxiliary problem

$$\min_{w_H} C_2(w_H) := \lambda w_H + (1 - \lambda)g(w_H) \quad \text{where} \quad g(w_H) := F_L^{-1} \left(\frac{\tau_2^a - \lambda F_H(w_H)}{1 - \lambda} \right)$$

- Solution $(\hat{w}_H, \hat{w}_L = g(\hat{w}_H))$ such that

$$f_L(\hat{w}_L) = f_H(\hat{w}_H)$$

TWO-LIMB OFFER

- Auxiliary problem

$$\min_{w_H} C_2(w_H) := \lambda w_H + (1 - \lambda)g(w_H) \quad \text{where} \quad g(w_H) := F_L^{-1} \left(\frac{\tau_2^a - \lambda F_H(w_H)}{1 - \lambda} \right)$$

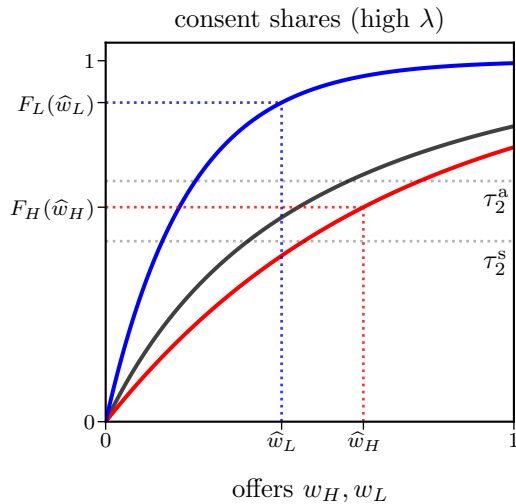
- Solution $(\hat{w}_H, \hat{w}_L = g(\hat{w}_H))$ such that

$$f_L(\hat{w}_L) = f_H(\hat{w}_H)$$

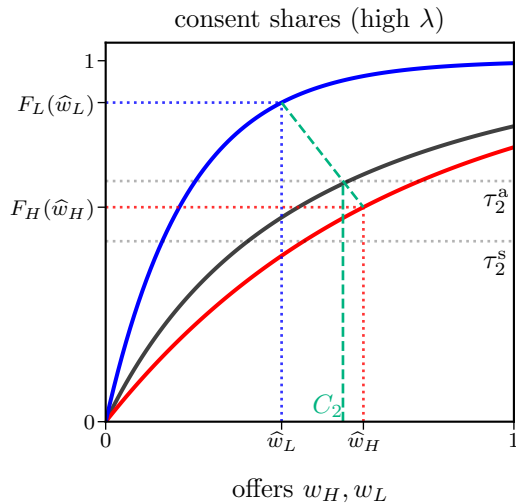
- Full solution (w_H, w_L)
 - = (\hat{w}_H, \hat{w}_L) if series-by-series constraint is satisfied
 - \neq (\hat{w}_H, \hat{w}_L) if *one* series-by-series constraint binds, e.g.

$$F_H(w_H) = \tau_2^s \quad \text{and} \quad w_L = F_L^{-1} \left(\frac{\tau_2^a - \lambda \tau_2^s}{1 - \lambda} \right)$$

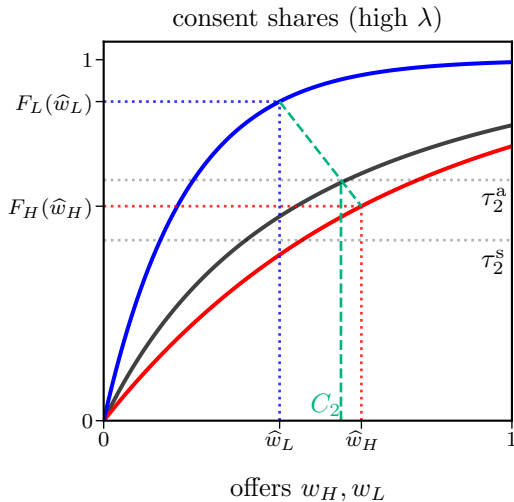
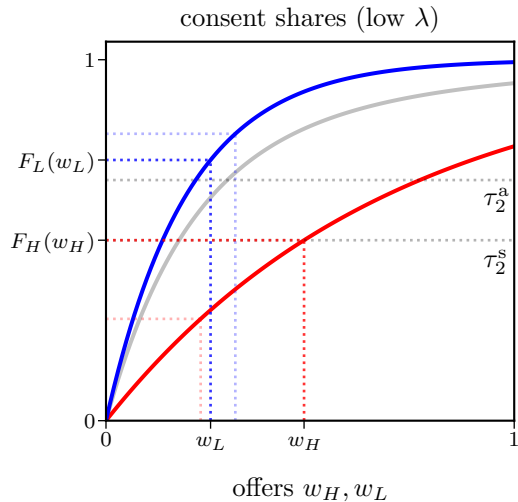
TWO-LIMB OFFER



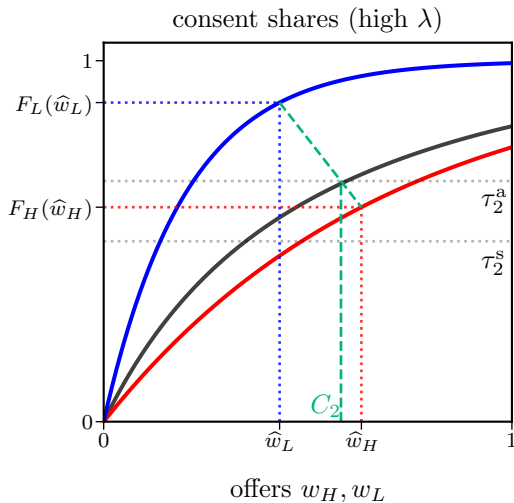
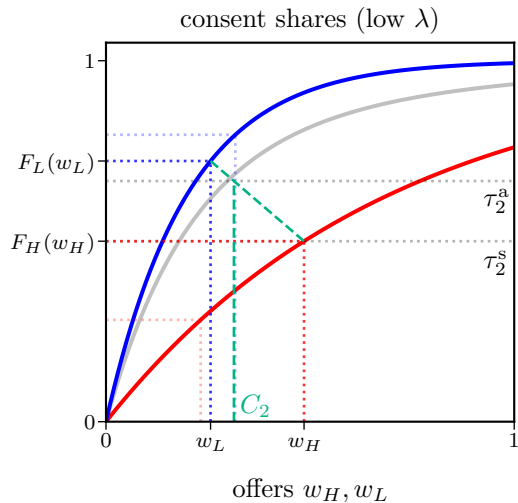
TWO-LIMB OFFER



TWO-LIMB OFFER



TWO-LIMB OFFER



OPTIMAL VOTING RULE

SUFFICIENT CONDITIONS

LEMMA

Two-limb dominates single-limb if

- (i) *the optimal single-limb offer w_u satisfies all series-by-series constraints: $F_i(w_u) \geq \tau_2^s$*
- (ii) *the auxiliary problem solution \hat{w}_i satisfies all series-by-series constraints: $F_i(\hat{w}_i) \geq \tau_2^s$*

OPTIMAL VOTING RULE

SUFFICIENT CONDITIONS

LEMMA

Two-limb dominates single-limb if

- (i) *the optimal single-limb offer w_u satisfies all series-by-series constraints: $F_i(w_u) \geq \tau_2^s$*
- (ii) *the auxiliary problem solution \hat{w}_i satisfies all series-by-series constraints: $F_i(\hat{w}_i) \geq \tau_2^s$*

Remarks

- Advantage of single-limb is lack of series-by-series constraints
 \Rightarrow worthless if not binding
- Result generalises to N -bond case

COMPARATIVE STATICS

SUFFICIENT CONDITIONS

PROPOSITION 1

- Two-limb is optimal if
 - H -bond share (λ) high enough
 - heterogeneity across bonds not too high
 - $\lambda \approx 0$ when $\tau_1 > \tau_2^a$

► λ_S

► γ_S

COMPARATIVE STATICS

SUFFICIENT CONDITIONS

PROPOSITION 1

- Two-limb is optimal if
 - H -bond share (λ) high enough
 - heterogeneity across bonds not too high
 - $\lambda \approx 0$ when $\tau_1 > \tau_2^a$
- Single-limb is optimal if $\tau_1 \approx \tau_2^a$ and
 - around $\tilde{\lambda}$ such that $\hat{w}_H = \hat{w}_L = w_u(\tilde{\lambda}, \tau_1) < F_i^{-1}(\tau_2^s)$ for some i
 - $\lambda \approx 0$ when $\tau_1 = \tau_2^a$

► λ^s

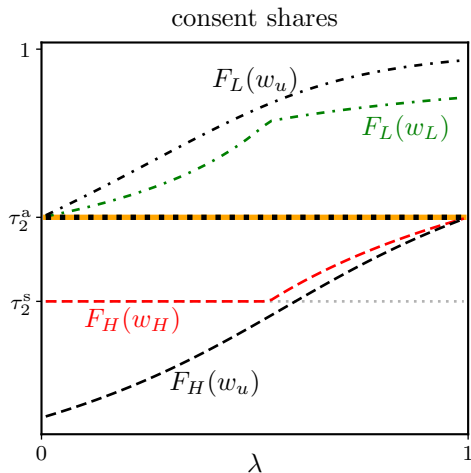
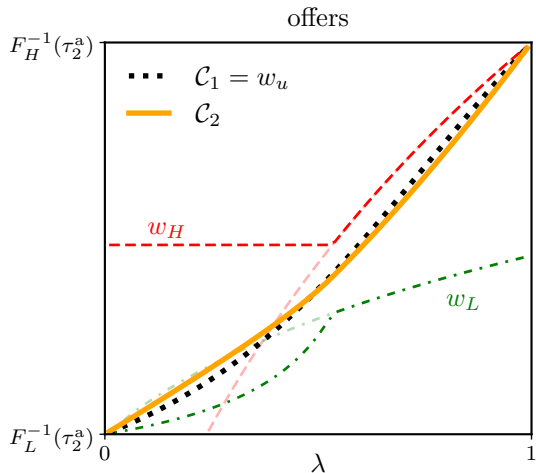
► γ^s

PARAMETRIC EXAMPLE

Assuming: $F_i(w) = 1 - e^{w/\phi_i}$, $\phi_H = 0.7$, $\phi_L = 0.2$ and $\tau_1 = \tau_2^a = 2/3$, $\tau_2^s = 1/2$

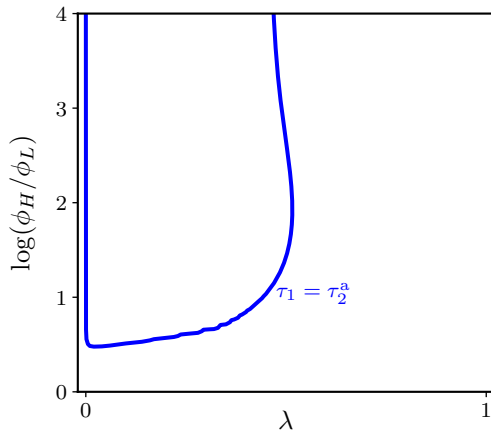
PARAMETRIC EXAMPLE

Assuming: $F_i(w) = 1 - e^{w/\phi_i}$, $\phi_H = 0.7, \phi_L = 0.2$ and $\tau_1 = \tau_2^a = 2/3, \tau_2^s = 1/2$



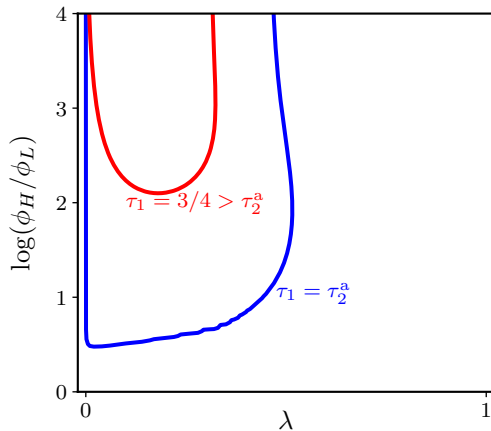
OPTIMAL VOTING RULE

Assuming: $F_i(w) = 1 - e^{w/\phi_i}$ and $\tau_2^a = 2/3, \tau_2^s = 1/2$



OPTIMAL VOTING RULE

Assuming: $F_i(w) = 1 - e^{w/\phi_i}$ and $\tau_2^a = 2/3, \tau_2^s = 1/2$



STOCHASTIC CONSENT SHARES

- Assume there is a bond-specific shock ϵ_i to the consent share

- CACs are triggered if

- aggregate: $\sum_i \lambda_i [F_i(w_i) - \epsilon_i] \geq \tau$

- series-by-series: $F_i(w_i) - \epsilon_i \geq \tau_2^s$

STOCHASTIC CONSENT SHARES

- Assume there is a bond-specific shock ϵ_i to the consent share
- CACs are triggered if
 - aggregate: $\sum_i \lambda_i [F_i(w_i) - \epsilon_i] \geq \tau \quad \Leftrightarrow \quad \sum_i \lambda_i \epsilon_i \leq \sum_i \lambda_i F_i(w) - \tau$
 - series-by-series: $F_i(w_i) - \epsilon_i \geq \tau_2^s \quad \Leftrightarrow \quad \epsilon_i \leq F_i(w) - \tau_2^s$

STOCHASTIC CONSENT SHARES

- Assume there is a bond-specific shock ϵ_i to the consent share
- CACs are triggered if
 - aggregate: $\sum_i \lambda_i [F_i(w_i) - \epsilon_i] \geq \tau \quad \Leftrightarrow \quad \sum_i \lambda_i \epsilon_i \leq \sum_i \lambda_i F_i(w) - \tau$
 - series-by-series: $F_i(w_i) - \epsilon_i \geq \tau_2^s \quad \Leftrightarrow \quad \epsilon_i \leq F_i(w) - \tau_2^s$
- Government minimises expected cost of restructuring
 - single-limb

$$P_a w_u + (1 - P_a)Z$$

STOCHASTIC CONSENT SHARES

- Assume there is a bond-specific shock ϵ_i to the consent share

- CACs are triggered if

- aggregate: $\sum_i \lambda_i [F_i(w_i) - \epsilon_i] \geq \tau \quad \Leftrightarrow \quad \sum_i \lambda_i \epsilon_i \leq \sum_i \lambda_i F_i(w) - \tau$
 - series-by-series: $F_i(w_i) - \epsilon_i \geq \tau_2^s \quad \Leftrightarrow \quad \epsilon_i \leq F_i(w) - \tau_2^s$

- Government minimises expected cost of restructuring

- single-limb

$$P_a w_u + (1 - P_a) Z$$

- two-limb ‘all-or-nothing’

$$P_{a,H,L} (\lambda_H w_H + \lambda_L w_L) + (1 - P_{a,H,L}) Z$$

STOCHASTIC CONSENT SHARES

- Assume there is a bond-specific shock ϵ_i to the consent share

- CACs are triggered if

- aggregate: $\sum_i \lambda_i [F_i(w_i) - \epsilon_i] \geq \tau \quad \Leftrightarrow \quad \sum_i \lambda_i \epsilon_i \leq \sum_i \lambda_i F_i(w) - \tau$
- series-by-series: $F_i(w_i) - \epsilon_i \geq \tau_2^s \quad \Leftrightarrow \quad \epsilon_i \leq F_i(w) - \tau_2^s$

- Government minimises expected cost of restructuring

- single-limb

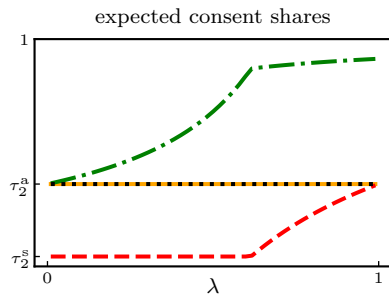
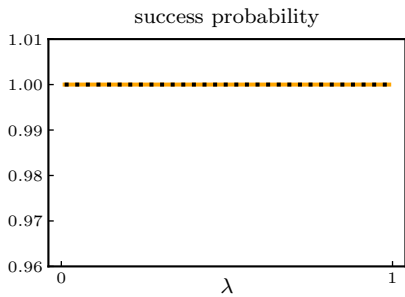
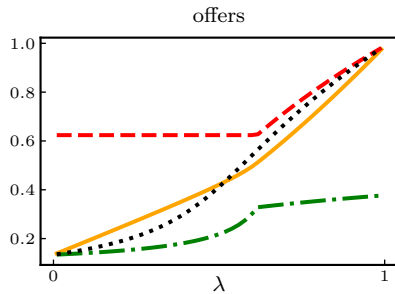
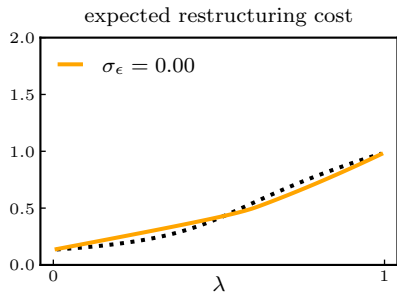
$$P_a w_u + (1 - P_a) Z$$

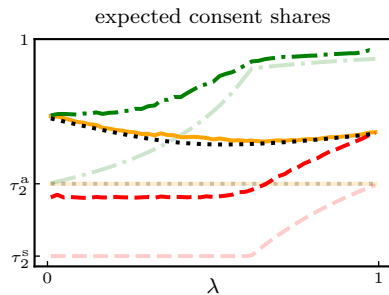
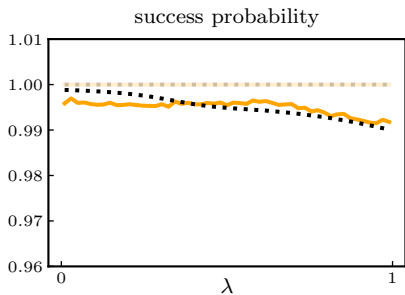
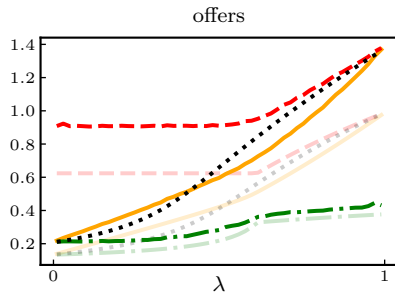
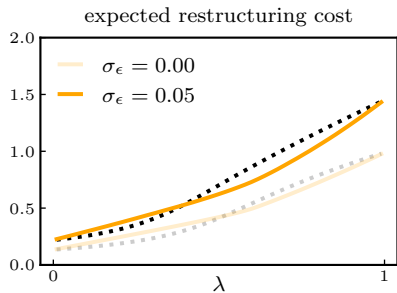
- two-limb ‘all-or-nothing’

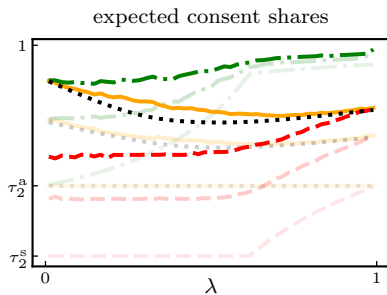
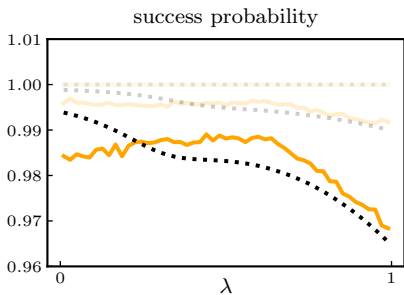
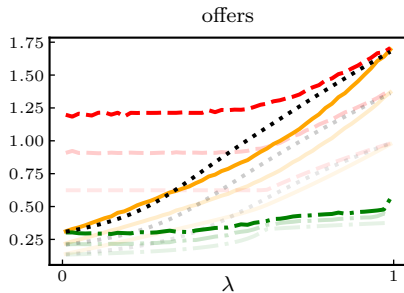
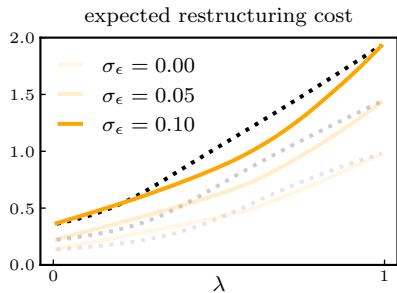
$$P_{a,H,L}(\lambda_H w_H + \lambda_L w_L) + (1 - P_{a,H,L}) Z$$

- two-limb with redesignation

$$\underbrace{P_{a,H,L}(\lambda_H w_H + \lambda_L w_L)}_{\text{both bonds}} + \underbrace{P_{a,H}(\lambda_H w_H + \lambda_L Z)}_{\text{just } H} + \underbrace{P_{a,L}(\lambda_H Z + \lambda_L w_L)}_{\text{just } L} + \underbrace{(1 - P_a) Z}_{\text{failed exchange}}$$







TAKEAWAYS AND AGENDA

Takeaways

- an economic theory of the optimal
 - restructuring of multiple, heterogeneous bonds
 - use of enhanced CACs
- results depend on degree of bond & creditor heterogeneity

TAKEAWAYS AND AGENDA

Takeaways

- an economic theory of the optimal
 - restructuring of multiple, heterogeneous bonds
 - use of enhanced CACs
- results depend on degree of bond & creditor heterogeneity

A lot more to be done with this framework:

- quantitative analysis of ARG and ECU restructurings through the lens of our model
- optimal bond pool designation

and taking a step back

- endogenous investor sorting into bonds ($\Rightarrow F_i$ within and across)
- endogenous government bond issuance/maturity structure

UNIFORM APPLICABILITY

ICMA

- exchange on same terms for same (menu of) instrument(s)
- amendments to principal, accrued interest imply new bonds have same provisions

Euro Area

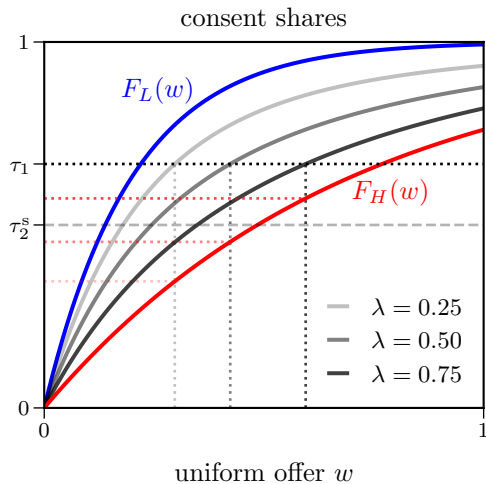
- exchange on same terms for same (menu of) instrument(s)
- reduce face value by same %
- extend maturity by same period or same %



SINGLE-LIMB: COMPARATIVE STATICS WRT λ

Assuming: $F_i(w) = 1 - e^{w/\phi_i}$, $\phi_H = 0.7, \phi_L = 0.2$ and $\tau_1 = \tau_2^a$

[◀ back](#)



SINGLE-LIMB: COMPARATIVE STATICS WRT ϕ_H/ϕ_L

Assuming: $F_i(w) = 1 - e^{w/\phi_i}$ and $\tau_1 = \tau_2^a$

◀ back

