

PBRT: Reflection Models

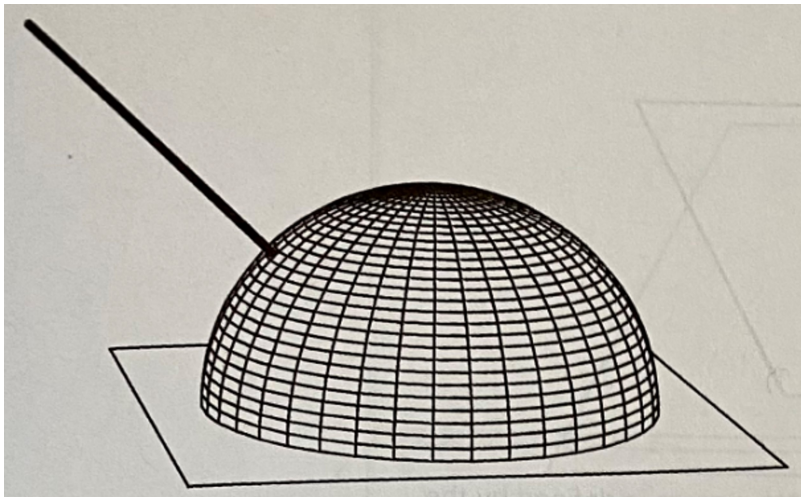
Sunday, January 3, 2021 11:51 AM

8 Reflection models

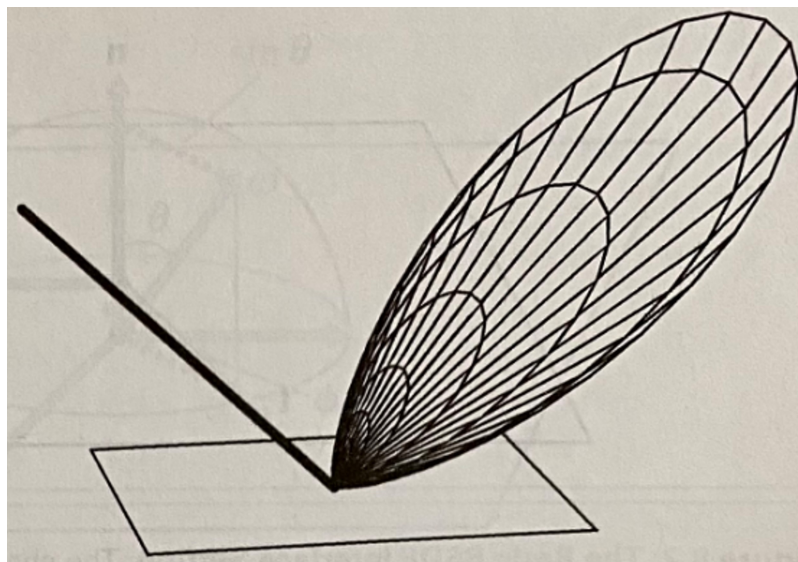
The [BRDF](#) describes light reflection at a surface, the BTDF describes light transmission at a surface, and the BSDF encompasses both of these effects described generally as scattering.

Categories of surface reflection (**IMPORTANT:** most surfaces exhibit a mixture of these 4 types):

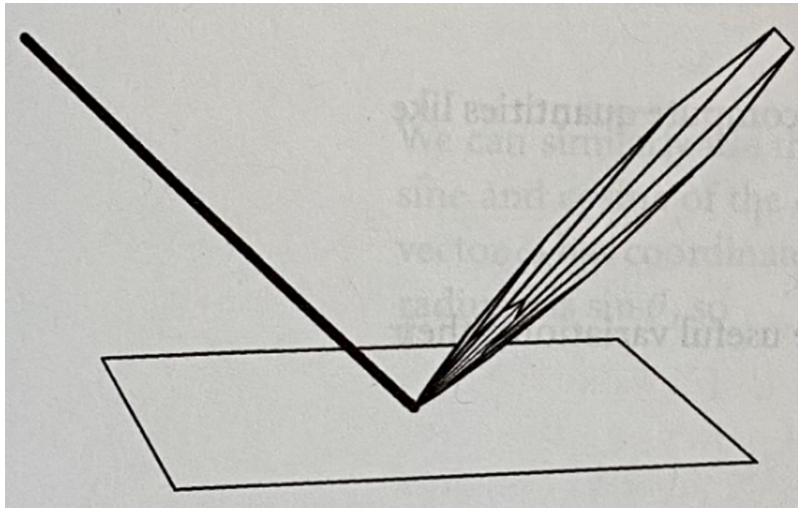
- *Diffuse*: light scatters equally in all directions. Matte paint, dull chalkboards, etc.



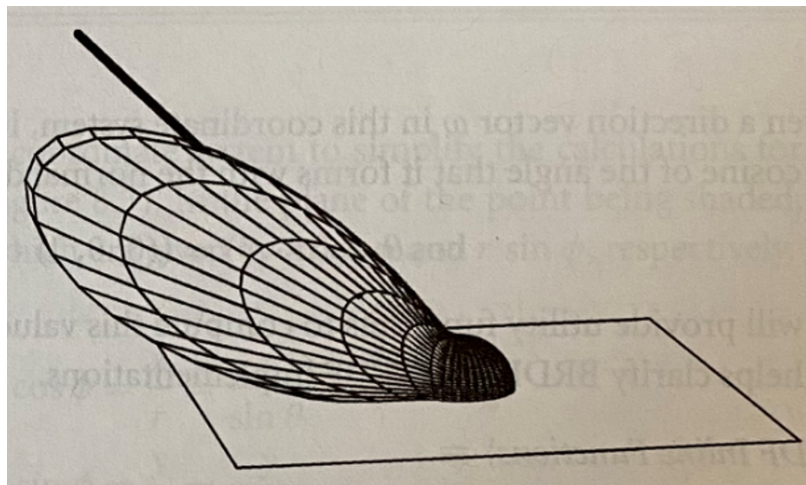
- *Glossy specular*: light scatters preferentially in a set of reflected directions (reflected direction as opposed to back in the incident direction). Plastic, high-gloss paint, etc.



- *Perfect specular*: light scatters in a single reflected direction. Mirrors, glass, etc.



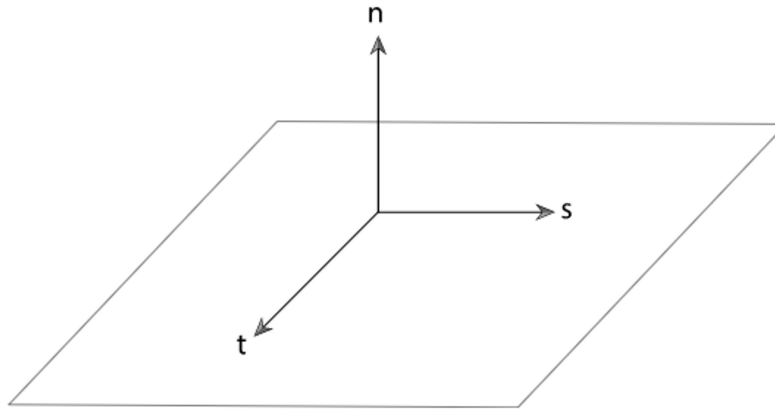
- *Retro-reflective*: light scatters primarily back along the incident direction. Velvet, the moon, etc.



Surface reflection can be further subcategorized as isotropic or anisotropic:

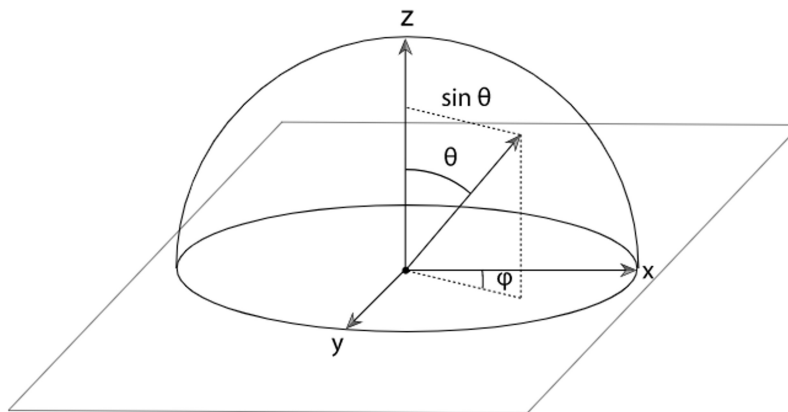
- *Isotropic*: if you rotate the surface about the normal at one point, the reflectance distribution doesn't change.
- *Anisotropic*: if you rotate the surface about the normal at one point, the reflectance distribution changes. Brush metal, compact disks, etc.

The shading coordinate system. Orthonormal basis vectors are 2 vectors tangent to the surface at a point and the normal.



s and t are aligned with x and y , and n with z . (World space x, y , and z ? No. Orientation is such that n points up.)

The spherical coordinates of a direction vector ω are expressed relative to this orthonormal basis. (Note that for computing ϕ , ω is first projected to the xy (st) plane.)



The sine, cosine, and tangent of θ and ϕ are computed using various trigonometric and Pythagorean identities (note the triangles). An interesting thing to note is that the length of the projection of ω onto the xy plane is given by $\sin \theta$.

The ω vector in the shading coordinate system:

- Is a linear combination of $\{s, t, n\}$.
- Is normalized.
- Is outward facing, even if it is an incident direction vector.
- Is an incident one when it is in the same hemisphere as n . And n always points away from the object.

8.1 Basic interface

All categories of surfaces (according to how they reflect light) compute the BRDF (and BTDF) differently. But a **special** note must be made for **perfect specular surfaces**: their directional distribution is a [Dirac delta function](#): only a single incident direction contributes to the reflected radiometric quantity in a given outgoing direction (that is to say that the outgoing direction determines the incident direction uniquely). In contrast, the BRDFs (and BTDF) of other surfaces map a given outgoing direction to multiple (or all) incident directions.

The BxDF is the abstract base class / interface of BRDFs and BTDFs. Among other things, it computes the spectral distribution (Spectrum) of a pair of outgoing and incident directions.

8.1.1 Reflectance

See [here](#).

8.2 Specular reflection and transmission

□ TODO

8.3 Lambertian reflection

The **Lambertian model** models a **perfect diffuse** surface that scatters incident light equally in all directions. Not physically possible.

Its BxDF uses a **reflectance** (a distribution, a spectral distribution, Spectrum) that expresses the fraction of incident light that is scattered ("scattering" is a term that stands for "reflection" or "transmission") at each wavelength in the outgoing direction, which is **equal** for (or **constant** across) all outgoing directions in the hemisphere. (Is the rest of the incident energy absorbed?)

The Lambertian BRDF $f_r(p, \omega_i, \omega_o)$ is a constant spectral distribution commonly called the **diffuse color** c_{diff} or **albedo**.

Since the BRDF is constant across all outgoing directions, the Lambertian **directional-hemispherical reflectance** is constant too:

$$\begin{aligned}
 \rho_{dh}(\omega_i) &= \int_{\Omega=H^2(n):\{\omega_o\}} f_r(p, \omega_i, \omega_o) |\cos \theta_o| d\omega_o \\
 &= f_r(p, \omega_i, \omega_o) \int_{\Omega=H^2(n):\{\omega_o\}} |\cos \theta_o| d\omega_o \\
 &= f_r(p, \theta_o, \phi_o, \theta_i, \phi_i) \int_{\phi_i=0}^{2\pi} \int_{\theta_i=0}^{\pi/2} |\cos \theta_i| \sin \theta_i d\theta_i d\phi_i \\
 &= f_r(p, \theta_o, \phi_o, \theta_i, \phi_i) \pi \\
 &= \pi f_r(p, \omega_i, \omega_o) \\
 &= \pi c_{diff}
 \end{aligned}$$

The value of the double definite integral is π :

Double Integral Calculator

f(x,y)

cos(y)sin(y)

dA

dydx

x from

0

to

2pi

y from

0

to

pi/2

Submit

Definite integral:

More digits

$$\int_0^{2\pi} \int_0^{\frac{\pi}{2}} \cos(y) \sin(y) dy dx = \pi \approx 3.14159$$



2 classes implement the Lambertian model: LambertianReflection is the BRDF and LambertianTransmission is the BTDF.

☐
 TODO: how does Lambertian transmission work? What materials exhibit diffuse transmission?