

# HW 2

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## 1 Implementation Using MPI Natives

Here, MPI treats `MPI_COMM_WORLD` as a single, asymmetric tree.  $P_0$  simply does `MPI_Scatter` on the array, then each process performs its integration, and finally, each process does `MPI_Gather` into  $P_0$ .  $P_0$  eventually receives an array of doubles of size  $np$ , and it adds all their elements to get the final integral value.

## 2 Custom Implementation

My custom implementation assigns each process to a tree of size a power of 2. Then,  $P_0$  (which has the entire workload stored in memory), sends the appropriate chunks to each tree root (virtual rank = 0). Figure 1 shows an example with 13 processes. This method is expected to be fast because the number of processes is usually sub-exponential, so the burden that  $P_0$  carries in distributing and collecting each tree's data, on the order  $\log np$ , is insignificant.

First,  $P_0$  sends the data corresponding to ranks  $8 \rightarrow 11$  ( $T_1$ ) to process 8, whose virtual rank is 0.  $P_0$  also sends the data corresponding to rank 12 ( $T_2$ ) to process 12 (also virtual rank 0). Every process that is not  $P_0$  is blocked on a `MPI_Probe` call.  $P_8$  and  $P_{12}$  are return from `MPI_Probe` when  $P_0$  sends them data, and they `MPI_Get_count` to allocate space for it. Then, propagate in a loop to processes in their tree. The processes targeted by their propagation return from their `MPI_Probe`, and also propagate in a loop. The stopping condition for the propagation is that the array of data being propagated contains only that processor's share of computation. Then, the entire tree's processes begin integrating at approximately the same time (horizontal dashed lines in Figure 1).

After the integration, the tree begins gathering into its corresponding virtual rank 0 process ( $P_0$ ,  $P_8$ , and  $P_{12}$ ). During this time,  $P_0$  is continuously performing `MPI_Recv` (from senders in its own tree). Even as it does this,  $P_{12}$  and  $P_8$  asynchronously complete their gathers, and send to  $P_0$  their tree sum. However, there is no need for barriers because they send to  $P_0$  via a unique tag, which  $P_0$  does not listen on until after it gathers all of tree 0.  $P_0$  then waits for

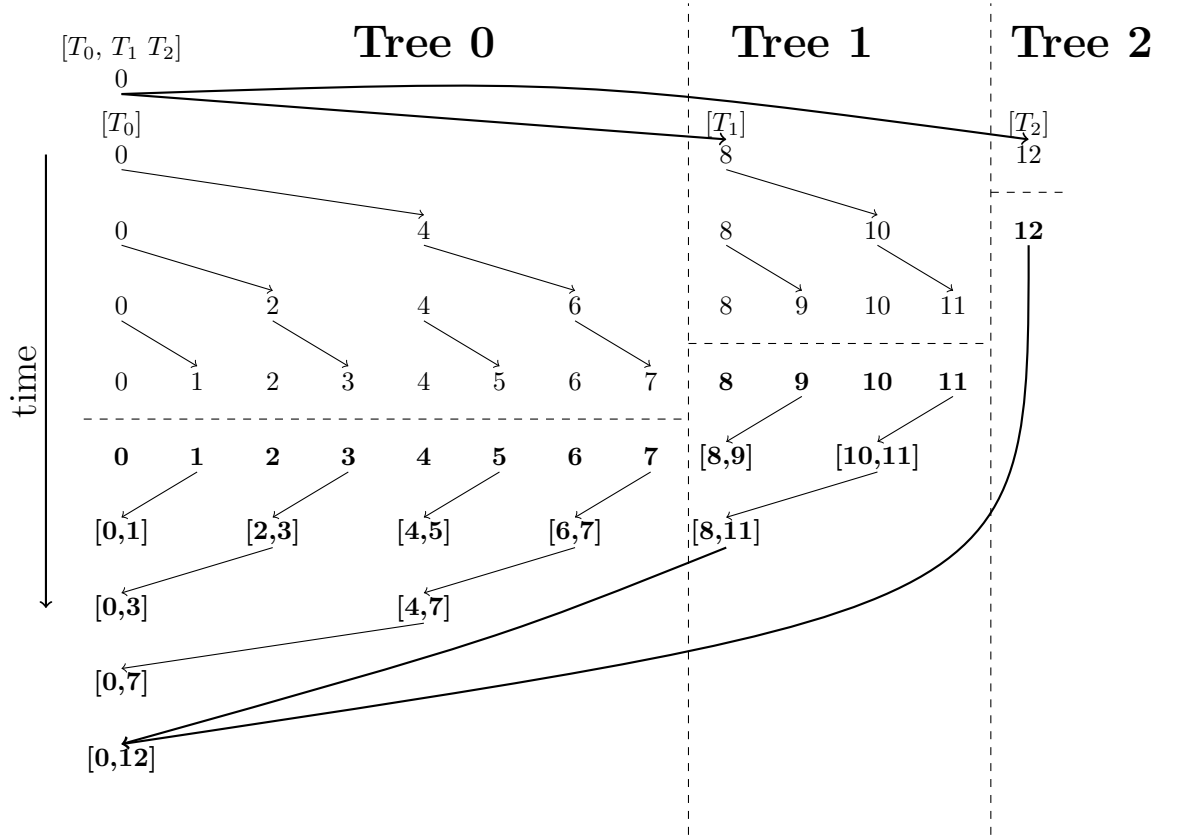


Figure 1: Communication involved in a 13 process computation (custom implementation)

two MPI.Recv on this unique tag, accumulating their sums along the way, and therefore has now the final integral value.

### 3 Performance Comparison

There are three implementations which we will compare. "native" is uses the native MPI collectives described in section 2, "main" is the implementation described in section 1, and "slow" is my original implementation, in which every process propagated data down to only two children (left and right). Then, it performed its integration and stood idle until its children responded with their sums, at which point the process would send *that* sum to its parent. Instead of waiting idle, the processes could instead be helping to propagate the data to not only 2 children, but as many as possible until all processes (in its tree) have its chunk of data. This is the reason "main" is faster than "slow". Even

# Procs	Billions of points	Times (sec)		
		native	main	slow
1	0.1	0.53	0.55	0.55
2	0.2	0.80	1.13	1.40
3	0.3	1.16	1.79	2.18
4	0.4	1.54	2.35	3.45
5	0.5	1.81	2.92	4.27
6	0.6	2.21	3.51	4.81
7	0.7	2.45	4.12	5.91
8	0.8	2.89	4.72	6.92
9	0.9	3.14	5.22	8.74
10	1.0	3.46	5.77	9.87
11	1.1	3.78	6.39	11.23
12	1.2	4.11	6.89	11.94
13	1.3	4.50	7.91	15.72

Table 1: Weak scaling analysis

though there are only two processes, I suspect that the huge amount of points (100 million per process in my tests) makes copying to MPI buffers quite slow, and therefore a communication protocol that takes more iterations to scatter data is significantly slower.

Table 1 shows the times for each implementation. I use weak scaling analysis by maintaining the points-per-process constant as I increase the processes of each test. Therefore, we can analyze the efficiency of parallelization. For example, communication overhead is evident in the fact that a single "native" process can integrate 100 million points in 0.53 seconds, but when communications with 12 other processes are involved, it needs 4.5 seconds to integrate 100 million points. Scaling efficiency is defined (for weak scaling) as  $\frac{t_1}{t_n}$ , where  $t_1$  is the time taken for a single process to complete a workload when no other processes exist, and  $t_n$  when  $n$  processes exist.

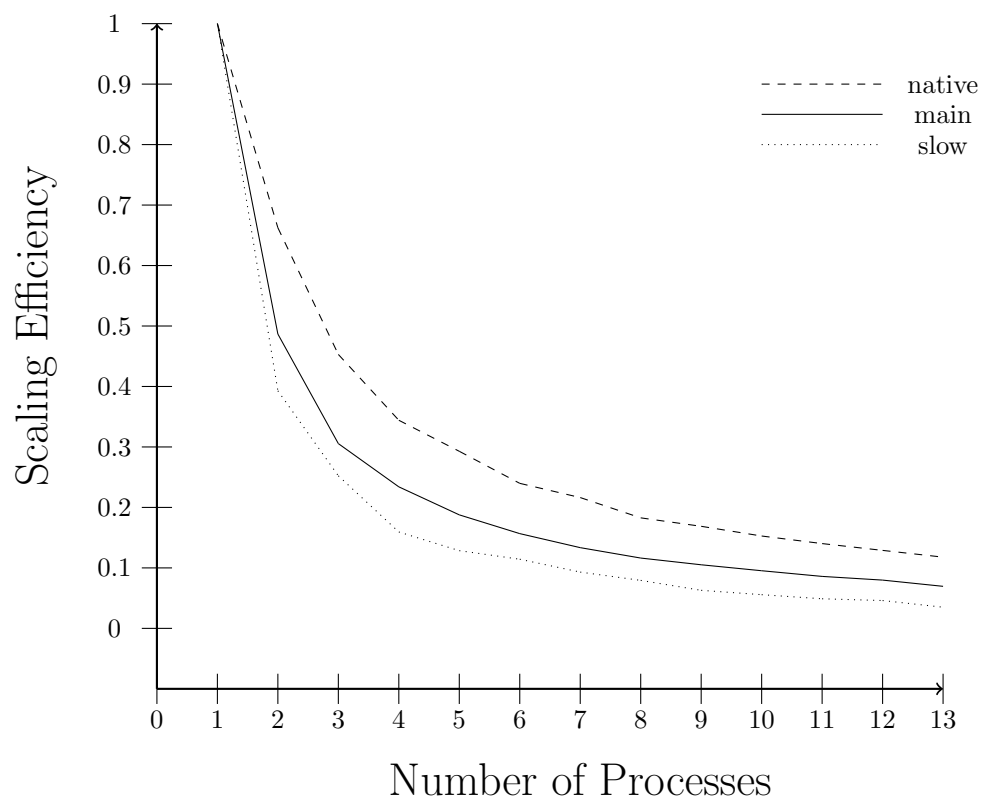


Figure 2: Communication overhead decreases the efficiency of each processes, even though each process has the same workload