

Trajectory Optimization and MPC Application for a
Building Model Identification
Optimization of Mechatronic Systems

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1 Introduction

The following report is done with the purpose of demonstrating the skills and techniques learned throughout the Optimization of Mechatronic Systems lecture. With this in mind, an investigation on the thermal behavior of an apartment located in Leuven, Belgium was conducted. Three goals were in mind while conducting this project. First, an identification for a suitable model of the apartment (referred to as the ‘thermal zone’ or simply ‘zone’) temperature was done by means of a trajectory optimization problem. For this, first a model was constructed and its constants were taken as a reference. Then, a model identification was conducted with an incorrect initial guess to demonstrate the utility of trajectory optimization. Once the model constants were identified, a model predictive control (MPC) application was made for the optimal deployment of the heating for the zone by means of a primal optimal problem statement. Finally, the same MPC application was developed using relaxed constraints by means of a lagrangian problem statement.

This section contains the description of the investigated thermal zone and the development of the zone model. Sections 2 and 3 contain the development, results and discussions over the problems while final comments and conclusions are discussed in section 4.

1.1 Thermal Zone

As mentioned in the previous paragraphs, an investigation is carried out for the thermal behavior and control of an apartment located in Leuven for the duration of the week of October 16 through 22, 2022. The inspiration for the apartment model is taken from the apartment pictured in Figure 1.



Figure 1: Inspiration for the parameter choice for the thermal zone model.

Here, it can be seen that the apartment is equipped with a large window as well as a single radiator as means of heating. The window faces south, maximizing the solar radiation throughout the day and has an area of 2.1 m^2 . The radiator has a maximal heating power of 1000 W and is equipped with a manual valve to regulate the heating output.

1.2 Zone Model

In order to approximate the thermal behavior of this apartment, first a model must be developed. This is achieved by lumping the thermal interactions of the apartment as a Resistance-Capacitance (RC) Thermal network. This is a common practice which leads to simplified models and accurate representations of the zone behaviors. Considering that the zone is relatively small in size ($\approx 25 \text{ m}^2$), a single zone model was used. Multiple lumped models with increasing number of zones and increasing complexity exist, nevertheless, they were deemed unnecessary. Figure 2 shows the RC-thermal network applied [1].

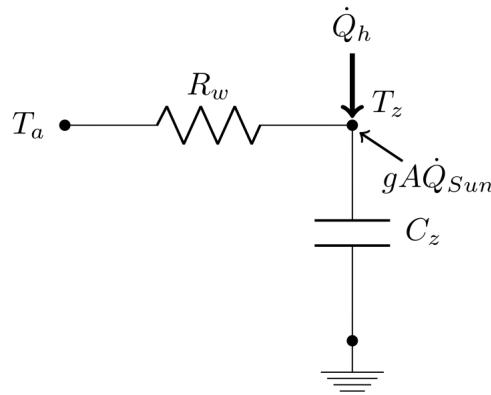


Figure 2: RC Thermal network for a single zone lumped model.

Moreover, an additional heating source \dot{Q}_g was introduced in order to account for the heat generated by the occupancy of the zone. Table 1 contains descriptions for all the above stated variables alongside their units.

Symbol	Variable	Units
T_z	Zone average temperature	K
T_a	Ambient temperature	K
R_w	Wall thermal resistance	K/W
C_z	Zone thermal capacitance	J/K
gA	Window glazing factor · window area	m^2
\dot{Q}_g	Heat input from occupancy	W
\dot{Q}_{sun}	Heat input from solar radiation	W/m^2
\dot{Q}_h	Heat input from radiator	W

Table 1: Nomenclature for the proposed variables for the zone model.

In order to describe the thermal interactions for the thermal network,a derivation for an energy balance was done.

$$C_z \cdot \frac{d}{dt}T_z = \dot{Q}_h + gA \cdot \dot{Q}_{sun} + \dot{Q}_g + \frac{T_z(t) - T_a(t)}{R_w} \quad (1)$$

This equation allows for a full description of the temperature profile of the zone based on input data (T_a , \dot{Q}_{sun} , \dot{Q}_g and \dot{Q}_h) and the zone constants (R_w , C_z and gA). Weather data for the week of October 16 to 22, 2022 was acquired from [2] and the solar radiance accounting for cloud coverage for Belgium (specifically the Brussels area, Leuven included) was acquired from [3] in order to achieve a realistic behavior for the zone temperature. A table containing this raw data is included in Appendix A. Finally, the heating output due to occupancy was applied based off of the average heating output of a human adult (100W) and traditional working schedules (not at home during weekdays from 07:00-18:00).

Furthermore, the zone constants were tuned until a realistic behavior was achieved. These can be seen in Table 2. These constants are hereon assumed to be correct and will be the goal for the convergence of the trajectory optimization problem discussed in the following sections. Further explanation for this reverse-engineering approach is given in section 2.

Constant	Value
C_z	5000000 J/K
R_w	0.01 K/W
gA	$0.45 \cdot 2.1 \text{ m}^2$

Table 2: Thermal zone constants.

Once the data was gathered and the constants were determined, the behavior for the zone was modeled following a simple heating strategy on which the heating was turned on to maximum power whenever someone was home and turned completely off whenever someone was not. Figure 3 shows the resulting behavior for the zone temperature. Ideally, the zone temperature should be within the range of 20-25°C (293.15-298.15K) to ensure thermal comfort for the users, pictured in the top subfigure in Figure 3 as the horizontal black lines. Finally, the running cost for the operation of the single radiator was calculated using the latest energy rate in Belgium (0.41 €/kWh) and is plotted for the entire week in the bottom subfigure of Figure 3.

When analyzing Figure 3, it is directly evident that the on/off strategy is not very effective economically and also in terms of thermal comfort. The temperature limits are crossed many times, reaching well over 300 K ($> 27^\circ\text{C}$) on the weekend. Moreover, by opening the radiator to the maximum, plenty of energy gets wasted since, in many cases, the zone temperature is already within the thermal comfort limits and does not need further heating, just maintaining the temperature range.

With this in mind, an optimized strategy for the appropriate heat deployment for the entire week is developed with two different approaches in section 3 after the model identification in section 2 is conducted.

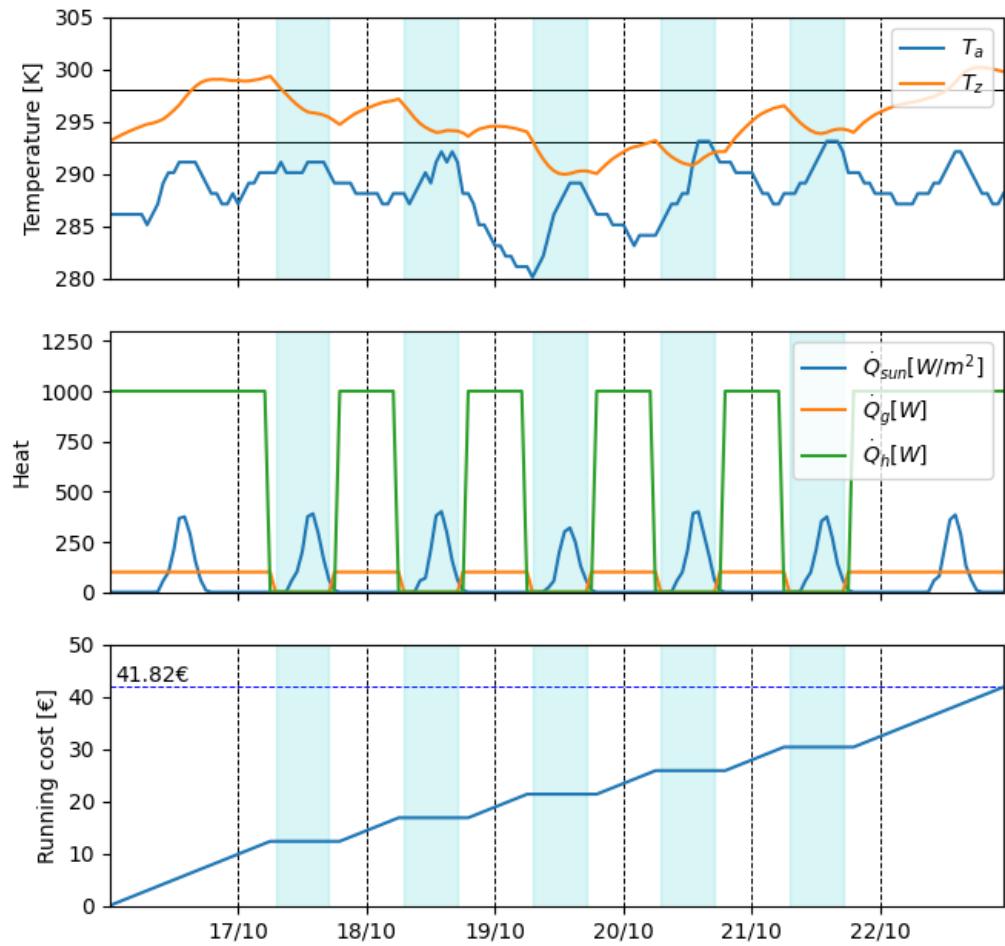


Figure 3: Zone temperature profile using a traditional on/off heating strategy.

2 Trajectory Optimization

A trajectory optimization is a set of mathematical techniques, which is used to find an ideal or the best behavior for a dynamic system, or also known as optimal trajectory. In order to describe mathematically what is understood as the "best" trajectory, an *objective function* should be defined [?]. Moreover, the optimization solver adjust a set of *decision variables* in order to minimize the objective function.

In the present section, it is described the process to identify the optimal values of the decision variables, with the objective of fitting the dynamics of the thermal system, into a model which is considered to be correct.

2.1 Objective function

As a first step, the temperature T_z , obtained with a finite difference approximation of the Equation 1, it is considered to be the ideal model of the room temperature, assuming that the values of C_z , R_w and gA presented in Table 2 are correct. The discretization processes is developed in the next equations

$$C_z \cdot \frac{T_{z,i+1} - T_{z,i}}{\Delta t} = \dot{Q}_{h,i} + gA \cdot \dot{Q}_{sun,i} + \dot{Q}_{g,i} + \frac{T_{z,i} - T_{a,i}}{R_w} \quad (2)$$

$$T_{z,i+1} = \Delta t \cdot \left(\frac{\dot{Q}_{h,i} + gA \cdot \dot{Q}_{sun,i} + \dot{Q}_{g,i}}{C_z} + \frac{T_{z,i} - T_{a,i}}{R_w \cdot C_z} \right) + T_{z,i} \quad (3)$$

The value $\Delta t = 3600s$ was selected based on the sampling time of historical data.

Subsequently, a model to optimize is presented, with C_z , R_w and gA selected as the decision variables. For that, an initial value of each, is proposed to be relatively close to the true values, with the intention of making the algorithm to converge faster and avoiding it to get stuck in local minima. The numerical values used as initial guess are shown in Table 3

Variable	Value
C_z	1000000 J/K
R_w	1 K/W
gA	$0.1 \cdot 1 \text{ m}^2$

Table 3: Initial guess of the decision variables.

To do: Describe the cost function/L2-norm.

$$\underset{C_z}{\text{minimize}} \sum_{i=1}^N (T_{z,i} - \hat{T}_{z,i})^2 \quad (4)$$

In which N is the number of samples, $\hat{T}_{z,i}$ is the the computed value to be updated by the optimization solver, and $T_{z,i}$ is the real value.

```

def minimize_function(Tz_a):
    N = len(Tz_a)
    delta_t = 3600 # s

    data = read_csv("leuven_october2022_16-22.csv")

    # Time dependent parameters
    time = data['time'].tolist()
    temp = data['temp'].tolist() # deg C
    for i in range(len(temp)):
        temp[i] = temp[i] + 273.15 # deg K

    Qg = np.zeros(len(time))
    Qh = np.zeros(len(time))
    for i in range(5):
        Qg[0 + 24 * (i + 1):7 + 24 * (i + 1)] = 100 # W. Human heat
        Qg[18 + 24 * (i + 1):24 + 24 * (i + 1)] = 100

        Qh[0 + 24 * (i + 1):6 + 24 * (i + 1)] = 1000 # W. Heater
        Qh[19 + 24 * (i + 1):24 + 24 * (i + 1)] = 1000

    Qg[0:24] = 100
    Qg[144:] = 100
    Qh[0:24] = 1000
    Qh[144:] = 1000

    Qsun = data['solrad'].tolist() # W/m2

    # Initiating optimization variables
    opti = Opti()
    R = opti.variable()
    C = opti.variable()
    gA = opti.variable()

    p = vertcat(R, C, gA) # parameter vector

    Tz = 293.15 # Initial temperature guess

    f = 0 # Error function initial value

    for i in range(N):
        f = f + (Tz - Tz_a[i]) ** 2
        Tz_next = delta_t * ((Qsun[i] * gA + Qh[i] + Qg[i]) / C + (temp[i] - Tz) / (R * C)) + Tz
        Tz = Tz_next

    f = f + (Tz - Tz_a[N - 1]) ** 2

    opti.minimize(f)

    opti.solver('ipopt')

    # filling initial guess parameter vector

```

```
p_hat = vertcat(R_guess, C_guess, gA_guess)

opti.set_initial(p, p_hat)

sol = opti.solve()

return sol.value(p)
```

3 Model Predictive Control

Following the identification of the model done in section 2, an optimal control strategy was developed for the deployment of the zone heating by means of model predictive control (MPC). First, a primal optimal problem was developed for the MPC application which resulted in a significant decrease in energy consumption and therefore energy costs. Nevertheless, due to the constraint nature of primal optimal problems, the robustness of the control was a matter of concern. Due to this, a second approach following a lagrangian problem statement was developed. This allowed for the relaxation of the constraints, leading to a more robust control. The details pertaining both approaches are thoroughly explained in their corresponding subsections in the following.

3.1 Primal MPC

As a first step, the calculated constants from section 2 were used to develop the model. In order to ensure a proper MPC development, model state and control variables were determined. For this, the zone temperature T_z , ambient temperature T_a , solar radiation \dot{Q}_{sun} and the heat input due to occupancy \dot{Q}_g were taken as the system states \mathbf{X} . Since the goal of the MPC is the optimal deployment of the zone heating \dot{Q}_h , it was taken as the control variable U . The following code shows how these were expressed.

```
# constants
N = len(time) # number of samples
delta_t = 3600 # s in 1 hour
R = R_opt
C = C_opt
gA = gA_opt

nx = 4 # number of states for system

# Initializing optimization problem
opti = Opti()

X = opti.variable(nx, N + 1) # states: Tz [K], Ta [K], Qsun [W/m2],
                             # Qg [W]. Multiple shooting

U = opti.variable(N, 1) # control variable: Qh [W]
```

Here, it can be seen that the state variable vector is initialized as a 4 by $N+1$ vector. This is since the transcription method used during this optimization is multiple shooting, which requires an additional state instance when compared to the control vector.

Moreover, the state vector was filled by means of a for-loop, following equation 3 and populating the rest of the states from the data collected in appendix A.

```
# Setting shooting constraints
for i in range(N - 1):
    opti.subject_to(X[0, i+1] == delta_t * ((X[2,i] * gA + U[i] + X[3,i]) /
                                              C + (X[1,i] - X[0,i])/(R*C)) + X[0,i])
```

```

opti.subject_to(X[1, i + 1] == temp[i + 1])
opti.subject_to(X[2, i + 1] == Qsun[i + 1])
opti.subject_to(X[3, i + 1] == Qg[i + 1])

```

Here, the first state is fully determined as a function of the control values, allowing for the optimization of its deployment. Additionally, the first instance for all states is purposefully skipped since the initial conditions are set at a later stage by means of the initial guess vector \mathbf{X}_0 .

Next, the matter of constraints is considered. For this, first the physical limits for the radiator are stated by setting the control variables to be within 0 and 1000 W (its maximal heating output). Furthermore, the thermal comfort limits were placed for the zone temperature for instances on which someone is occupying the zone. This allows for the reduction of heating output during non-occupation times, leading to lower electrical costs. For this, a typical occupational time range was used on which there is one person inside the zone during the entire weekend and the zone is not occupied in the weekdays from 07:00 to 18:00.

```

# setting bounded constraints (temp range for the zone whenever someone is
# home)
opti.subject_to(opti.bounded(293.15, X[0, 0:24], 298.15)) # weekend
opti.subject_to(opti.bounded(293.15, X[0, 144:], 298.15)) # weekend
for i in range(6): # weekdays
    opti.subject_to(opti.bounded(293.15, X[0, 0+24*(i+1):7+24*(i+1)], 298.15
                                ))
    opti.subject_to(opti.bounded(293.15, X[0, 18+24*(i+1):24+24*(i+1)], 298.
                                15))

# bounded constraints for max and min power output for the radiator
opti.subject_to(opti.bounded(0, U, 1000))

```

Next, initial conditions as well as the objective function were stated. Since the goal of the MPC is the reduction of energy consumption, the squared sum of the total heat deployed into the zone via the radiator $\sum \dot{Q}_h^2$ was declared as the cost function. The following snippet illustrates how both were introduced into CasADi.

```

# setting initial conditions
opti.subject_to(X[:, 0] == x0)

# setting minimization equation
opti.minimize(sumsqr(U))

opti.set_value(x0, vertcat(293.15, temp[0], Qsun[0], Qg[0]))

opti.solver('ipopt')
sol = opti.solve()

```

The optimal control problem is then ready to be solved by means of the IPOPT solver. In order to provide more clarity, equations 5 to 11 summarize the above stated code in equation form.

$$\text{minimize} \quad \sum_{i=1}^N \left(\dot{Q}_{h,i} \right)^2 \quad (5)$$

$$\text{subject to} \quad T_{z,i+1} - \Delta t \left(\frac{\dot{Q}_{h,i} + gA \cdot \dot{Q}_{sun,i} + \dot{Q}_{g,i}}{C_z} + \frac{T_{z,i} - T_{a,i}}{R_w \cdot C_z} \right) - T_{z,i} = 0 \quad (6)$$

$$\begin{bmatrix} T_{z,0}, T_{a,0}, \dot{Q}_{sun,0}, \dot{Q}_{g,0} \end{bmatrix}^\top - \mathbf{X}_0 = 0 \quad (7)$$

$$T_{z,i} - 298.15 \leq 0 \quad \forall i \in \text{occupied} \quad (8)$$

$$293.15 - T_{z,i} \leq 0 \quad \forall i \in \text{occupied} \quad (9)$$

$$\dot{Q}_{h,i} - 1000 \leq 0 \quad (10)$$

$$-\dot{Q}_{h,i} \leq 0 \quad (11)$$

Lastly, the above stated MPC results in the temperature and heating deployment profiles seen in Figure 4.

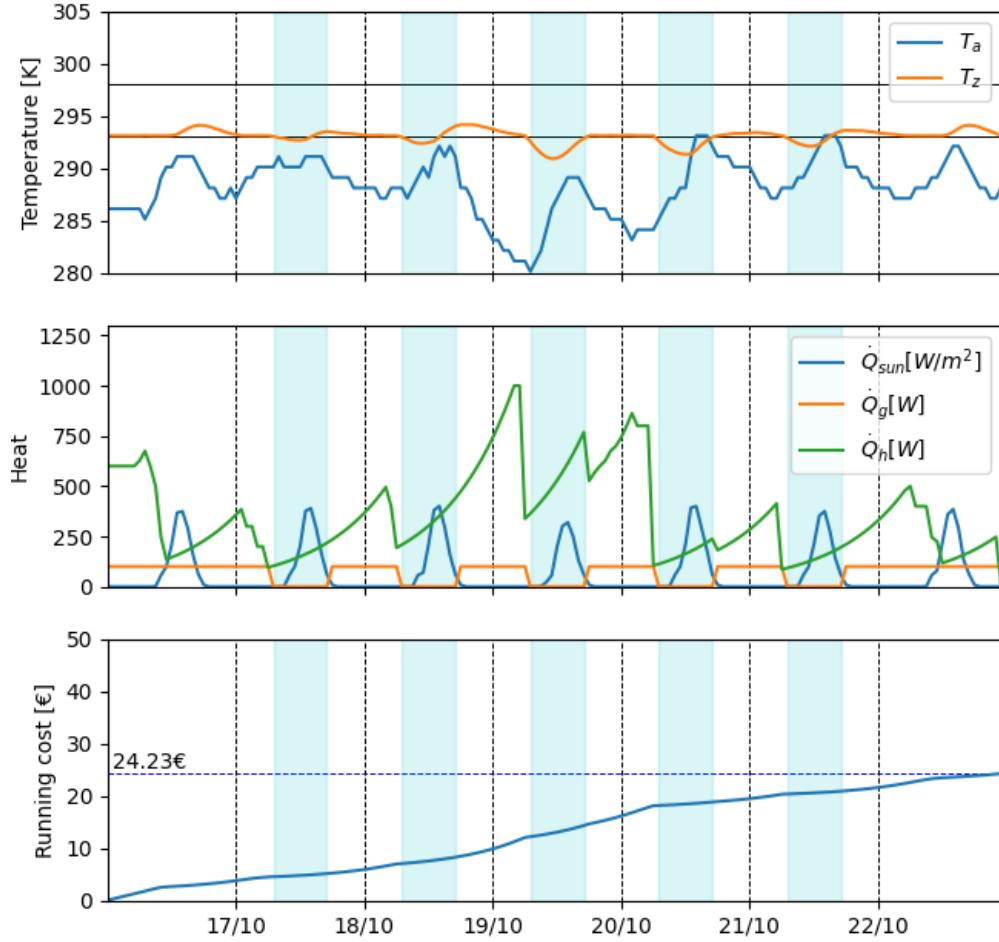


Figure 4: MPC by means of a primal optimal problem for the zone heat deployment.

Immediately, when comparing Figures 4 and 3 a decrease in weekly cost of about 42% can be seen. Additionally, this cost reduction comes with a more stable temperature profile for the zone, ensuring thermal comfort at all occupant times. It can also be noted that the heat deployment is maintained well below the maximum power output for most days, helping towards the reduction of energy use and the extension of the lifespan of the radiator.

While appreciating the benefits of the integrated MPC, the issue of robustness raises a large concern for the application of this system. This is due mainly to the strictness of the constraints for the zone temperature profile. By introducing the thermal comfort boundaries for the zone as a bounded constraint, we do not allow for considerations of exterior influences causing a drastic change in zone temperature and taking the zone outside of its comfort range (e.g. an open window, sudden rain, etc.). This effect is easily tested by varying the initial temperature for the zone since, at the first instance of the week, the thermal comfort constraint is valid. The following changes to the initial vector

```
opti.set_value(x0, vertcat(253.15, temp[0], Qsun[0], Qg[0]))  
  
opti.solver('ipopt')  
sol = opti.solve()
```

quickly back the hypothesis since, by enforcing a temperature outside of the thermal comfort range, the solver is unable to return a solution and instead gives the error `return_status` is '`Infeasible_Problem_Detected`'.

For this reason, it was decided that these constraints should be relaxed in order to increase the robustness of the system. This is done by means of a lagrangian problem statement, which is developed in the following subsection.

3.2 Lagrangian MPC

Considering the robustness issues discussed in subsection 3.1, a lagrangian approach was taken. For this, the same initial steps were taken as before. The distinction between both approaches is seen during the constraints setting portion of the code. When taking a lagrangian problem statement, the relaxed constraints are moved into the cost function alongside a weight factor for each constraint. Nevertheless, since some hard constraints (the maximum heating output for the radiator) are still necessary to maintain the physical limits of the system, not all constraints were introduced into the cost function.

```
# setting minimization equation in lagrangian form
mu1_val = 130
mu2_val = 150

# set the weights to a certain percentage for 'at work' hours
mu1 = np.ones(N) * mu1_val * 0.8
mu2 = np.ones(N) * mu2_val * 0.8

# values for 0.8mu whenever no one is home, mu_val whenever someone is
mu1[0:24] = mu1_val # weekend
mu1[144:] = mu1_val
mu2[0:24] = mu2_val
mu2[144:] = mu2_val
for i in range(6): # weekdays
    mu1[0 + 24 * (i + 1):7 + 24 * (i + 1)] = mu1_val
    mu2[0 + 24 * (i + 1):7 + 24 * (i + 1)] = mu2_val
    mu1[18 + 24 * (i + 1):24 + 24 * (i + 1)] = mu1_val
    mu1[18 + 24 * (i + 1):24 + 24 * (i + 1)] = mu1_val

temp_high = np.ones(N) * 298.15
temp_low = np.ones(N) * 293.15

opti.minimize(sumsqr(U + mu1*(Tz_var.T - temp_high) + mu2*(Tz_var.T - temp_low)))

opti.set_value(x0, vertcat(T_start, temp[0], Qsun[0], Qg[0]))

opti.solver('ipopt')
sol = opti.solve()
```

Here, the introduction of the lagrange multipliers μ_1 and μ_2 can be seen for the upper and lower thermal comfort boundaries, respectively. By varying these values, their weight (or importance) within the cost function varies, therefore these must be tuned depending on the preferences of the user. In the case lowering energy use is considered to be of highest importance, lower μ_i values would be used. On the other hand, if thermal comfort during occupancy times is the priority, higher μ_i values would be introduced. For the application shown here, a relative balance was attempted between both objectives: a maintenance of thermal comfort while taking into consideration energy use. Moreover, in order to account for ‘at work’ hours, the lagrangian multiplier values were decreased by 20% during those instances in order to reduce energy use while still allowing for the zone to pre-heat itself whenever someone is expected to come home.

The resulting optimal control problem can be stated mathematically as the following:

$$\text{minimize} \quad \sum_{i=1}^N \left(\dot{Q}_{h,i} + \mu_{1,i} (T_{z,i} - 298.15) + \mu_{2,i} (293.15 - T_{z,i}) \right)^2 \quad (12)$$

$$\text{subject to} \quad T_{z,i+1} - \Delta t \left(\frac{\dot{Q}_{h,i} + gA \cdot \dot{Q}_{sun,i} + \dot{Q}_{g,i}}{C_z} + \frac{T_{z,i} - T_{a,i}}{R_w \cdot C_z} \right) - T_{z,i} = 0 \quad (13)$$

$$\begin{bmatrix} T_{z,0}, T_{a,0}, \dot{Q}_{sun,0}, \dot{Q}_{g,0} \end{bmatrix}^\top - \mathbf{X}_0 = 0 \quad (14)$$

$$\dot{Q}_{h,i} - 1000 \leq 0 \quad (15)$$

$$-\dot{Q}_{h,i} \leq 0 \quad (16)$$

Finally, the results for this optimal control problem can be seen in Figure 5.

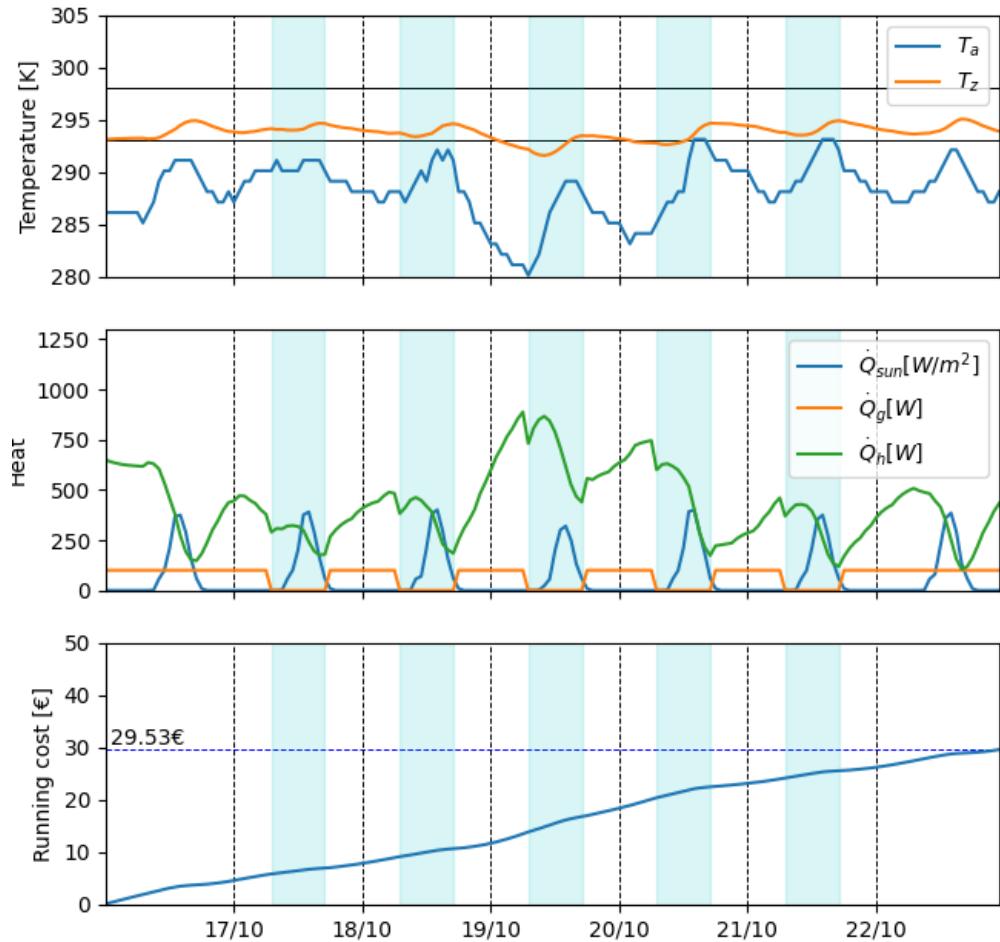


Figure 5: MPC by means of a lagrangian optimal problem for the zone heat deployment.

Similar to Figure 4, Figure 5 shows a decrease in energy costs when compared to Figure 3. Nevertheless, this is only represented by a 30% decrease instead of the 42% from before. This is due to the relaxation of the thermal boundary constraints and the weight balance applied in equation 12. This cost reduction could be set to match, or even surpass the 42% from the primal MPC but it would come at the cost of thermal comfort for the zone occupants. For this reason, this extra cost is tolerated to ensure thermal comfort.

More significantly, this MPC application follows reality more accurately than the one developed using a primal problem statement. By not forcing the zone temperature to be within the comfort boundaries at all moments, the system becomes robust towards outliers and sudden changes caused by third parties without crashing. Figure 6 shows the results for the same experiment done in subsection 3.1. Here, the robustness of the lagrangian problem statement becomes evident since, by relaxing the variables, the system allows for outliers without crashing while still penalizing them and quickly recovering.

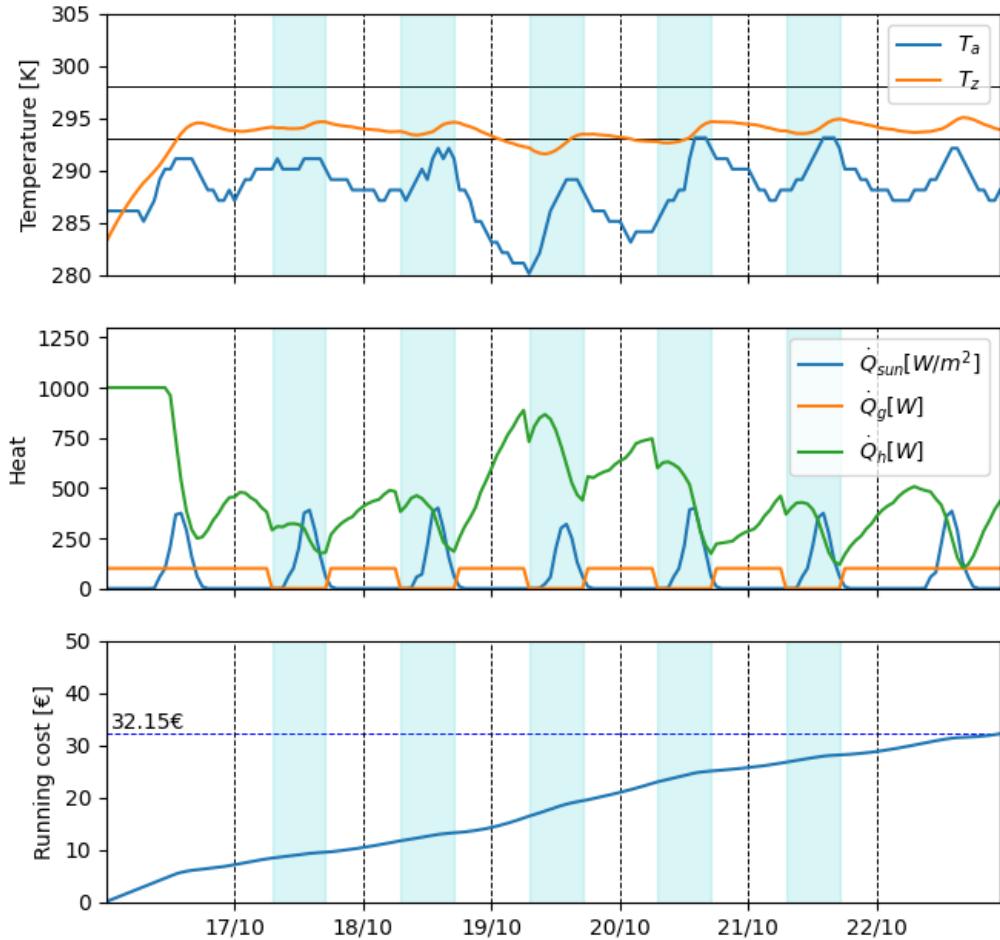


Figure 6: MPC by means of a lagrangian optimal problem for the zone heat deployment with deviated initial zone temperature.

4 Conclusions

A Appendix A

time	temp	rhum	prcp	wdir	wspd	pres	solrad
2022-10-16 00:00:00	13	82	0	190	13	1010	0
2022-10-16 01:00:00	13	82	0	190	13	1010	0
2022-10-16 02:00:00	13	82	0	210	15	1010	0
2022-10-16 03:00:00	13	82	0	210	13	1010	0
2022-10-16 04:00:00	13	82	0	210	17	1011	0
2022-10-16 05:00:00	13	88	0	200	15	1011	0
2022-10-16 06:00:00	13	82	0	200	15	1012	0
2022-10-16 07:00:00	12	88	0	200	17	1012	0
2022-10-16 08:00:00	13	88	0	200	17	1013	0
2022-10-16 09:00:00	14	82	0	220	19	1014	1.4
2022-10-16 10:00:00	16	77	0	220	20	1015	57
2022-10-16 11:00:00	17	72	0	240	13	1015	99.1
2022-10-16 12:00:00	17	68	0	240	11	1015	210.9
2022-10-16 13:00:00	18	60	0	190	9	1016	367.4
2022-10-16 14:00:00	18	56	0	200	11	1016	374.9
2022-10-16 15:00:00	18	64	0	150	7	1016	290.9
2022-10-16 16:00:00	18	64	0	120	6	1015	156.7
2022-10-16 17:00:00	17	72	0	100	4	1015	60.4
2022-10-16 18:00:00	16	77	0	110	4	1015	8.7
2022-10-16 19:00:00	15	88	0.1	170	2	1016	0
2022-10-16 20:00:00	15	88	0.3	90	4	1016	0
2022-10-16 21:00:00	14	94	0.5	70	4	1016	0
2022-10-16 22:00:00	14	94	0.2	90	6	1016	0
2022-10-16 23:00:00	15	88	0.7	120	7	1015	0
2022-10-17 00:00:00	14	94	0.2	130	9	1015	0
2022-10-17 01:00:00	15	94	0	160	13	1015	0
2022-10-17 02:00:00	16	88	0	170	22	1015	0
2022-10-17 03:00:00	16	88	0	180	20	1015	0
2022-10-17 04:00:00	17	83	0	180	17	1015	0
2022-10-17 05:00:00	17	88	0	180	20	1015	0
2022-10-17 06:00:00	17	88	0	180	17	1015	0
2022-10-17 07:00:00	17	88	0	180	19	1016	0
2022-10-17 08:00:00	18	83	0	200	20	1017	0
2022-10-17 09:00:00	17	94	2.6	250	17	1019	1.4
2022-10-17 10:00:00	17	94	3.6	180	7	1018	57
2022-10-17 11:00:00	17	88	1.1	230	7	1019	101
2022-10-17 12:00:00	17	88	0	230	7	1020	202
2022-10-17 13:00:00	18	83	0	240	15	1021	376
2022-10-17 14:00:00	18	83	0	240	15	1022	390.2
2022-10-17 15:00:00	18	83	0	240	15	1022	290.9

2022-10-17 16:00:00	18	83	0.5	230	13	1023	162
2022-10-17 17:00:00	17	88	0.7	190	9	1023	60.4
2022-10-17 18:00:00	16	88	0	180	6	1024	8.7
2022-10-17 19:00:00	16	88	0	180	13	1024	0
2022-10-17 20:00:00	16	88	0	180	13	1024	0
2022-10-17 21:00:00	16	82	0	200	7	1024	0
2022-10-17 22:00:00	15	88	0	230	4	1025	0
2022-10-17 23:00:00	15	88	0	190	6	1025	0
2022-10-18 00:00:00	15	88	0	190	6	1025	0
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2022-10-18 02:00:00	15	88	0	190	2	1025	0
2022-10-18 03:00:00	14	94	0	220	2	1026	0
2022-10-18 04:00:00	14	94	0	249	2	1025	0
2022-10-18 05:00:00	15	88	0	290	2	1026	0
2022-10-18 06:00:00	15	88	0	248	2	1026	0
2022-10-18 07:00:00	15	88	0	350	4	1026	0
2022-10-18 08:00:00	14	88	0	245	2	1027	0
2022-10-18 09:00:00	15	88	0.2	249	2	1027	1.4
2022-10-18 10:00:00	16	82	0	30	6	1028	57
2022-10-18 11:00:00	17	83	0	20	7	1028	70
2022-10-18 12:00:00	16	82	0	10	9	1028	210.9
2022-10-18 13:00:00	18	68	0	13	2	1028	380
2022-10-18 14:00:00	19	64	0	10	6	1028	401
2022-10-18 15:00:00	18	68	0	360	7	1028	297
2022-10-18 16:00:00	19	64	0	40	7	1028	156.7
2022-10-18 17:00:00	18	64	0	20	7	1028	60.4
2022-10-18 18:00:00	15	77	0	40	9	1028	8.7
2022-10-18 19:00:00	15	77	0	50	9	1028	0
2022-10-18 20:00:00	14	77	0	50	7	1028	0
2022-10-18 21:00:00	12	82	0	60	6	1028	0
2022-10-18 22:00:00	12	82	0	70	4	1028	0
2022-10-18 23:00:00	11	88	0	60	2	1028	0
2022-10-19 00:00:00	10	87	0	70	4	1028	0
2022-10-19 01:00:00	10	87	0	100	4	1028	0
2022-10-19 02:00:00	9	94	0	80	6	1027	0
2022-10-19 03:00:00	9	87	0	70	4	1027	0
2022-10-19 04:00:00	8	93	0	70	6	1027	0
2022-10-19 05:00:00	8	93	0	80	6	1026	0
2022-10-19 06:00:00	8	93	0	77	4	1026	0
2022-10-19 07:00:00	7	93	0	70	4	1026	0
2022-10-19 08:00:00	8	87	0	80	6	1026	0
2022-10-19 09:00:00	9	94	0	90	9	1026	1.4

2022-10-19 10:00:00	11	82	0	80	13	1025	23
2022-10-19 11:00:00	13	77	0	80	15	1025	56
2022-10-19 12:00:00	14	72	0	80	17	1024	198
2022-10-19 13:00:00	15	72	0	90	17	1023	301
2022-10-19 14:00:00	16	68	0	90	17	1022	320
2022-10-19 15:00:00	16	68	0	80	17	1022	250
2022-10-19 16:00:00	16	68	0	80	15	1021	130
2022-10-19 17:00:00	15	72	0	90	15	1020	60.4
2022-10-19 18:00:00	14	77	0	90	15	1019	8.7
2022-10-19 19:00:00	13	88	0	90	11	1019	0
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2022-10-19 21:00:00	13	82	0	90	11	1018	0
2022-10-19 22:00:00	12	88	0	100	9	1017	0
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2022-10-20 04:00:00	11	88	0	90	7	1013	0
2022-10-20 05:00:00	11	88	0	150	6	1013	0
2022-10-20 06:00:00	11	88	0.1	120	7	1012	0
2022-10-20 07:00:00	12	88	0	110	7	1011	0
2022-10-20 08:00:00	13	88	0	160	11	1011	0
2022-10-20 09:00:00	14	88	0	180	13	1012	1.4
2022-10-20 10:00:00	14	88	0	190	11	1011	57
2022-10-20 11:00:00	15	88	0	150	15	1011	99.1
2022-10-20 12:00:00	15	94	1	150	20	1010	210.9
2022-10-20 13:00:00	18	88	0	180	17	1011	392
2022-10-20 14:00:00	20	78	0	200	19	1010	400
2022-10-20 15:00:00	20	68	0	200	13	1010	290.9
2022-10-20 16:00:00	20	73	0	190	9	1009	182
2022-10-20 17:00:00	19	73	0	160	11	1009	60.4
2022-10-20 18:00:00	18	83	0	160	13	1009	8.7
2022-10-20 19:00:00	18	83	0	150	17	1008	0
2022-10-20 20:00:00	18	78	0	160	17	1009	0
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2022-10-20 22:00:00	17	83	0	170	13	1008	0
2022-10-20 23:00:00	17	83	0	160	15	1007	0
2022-10-21 00:00:00	17	83	0	170	20	1007	0
2022-10-21 01:00:00	16	82	0	200	19	1008	0
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2022-10-21 03:00:00	15	82	0	190	13	1006	0

2022-10-21 04:00:00	14	88	0	180	11	1006	0
2022-10-21 05:00:00	14	82	0	190	9	1006	0
2022-10-21 06:00:00	15	82	0	180	17	1006	0
2022-10-21 07:00:00	15	82	0	180	15	1005	0
2022-10-21 08:00:00	15	88	0	190	9	1006	0
2022-10-21 09:00:00	16	82	0	210	17	1007	1.4
2022-10-21 10:00:00	16	82	0	210	17	1007	57
2022-10-21 11:00:00	17	77	0.1	200	20	1007	99.1
2022-10-21 12:00:00	18	73	0	190	20	1007	210.9
2022-10-21 13:00:00	19	73	0	200	19	1007	353
2022-10-21 14:00:00	20	64	0	190	20	1007	374.9
2022-10-21 15:00:00	20	64	0	190	19	1007	274
2022-10-21 16:00:00	20	64	0	200	17	1007	140
2022-10-21 17:00:00	19	68	0	200	13	1007	60.4
2022-10-21 18:00:00	17	77	0	200	17	1007	8.7
2022-10-21 19:00:00	17	77	0	190	19	1008	0
2022-10-21 20:00:00	17	77	0	190	19	1008	0
2022-10-21 21:00:00	16	82	0	190	19	1008	0
2022-10-21 22:00:00	16	82	0	180	19	1008	0
2022-10-21 23:00:00	15	88	0	190	17	1009	0
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2022-10-22 10:00:00	16	77	0	230	24	1013	57
2022-10-22 11:00:00	16	77	0	240	24	1014	80
2022-10-22 12:00:00	17	72	0	230	22	1014	221
2022-10-22 13:00:00	18	68	0	220	19	1014	360
2022-10-22 14:00:00	19	64	0	220	19	1014	385
2022-10-22 15:00:00	19	60	0	210	19	1014	290.9
2022-10-22 16:00:00	18	64	0	220	9	1014	130
2022-10-22 17:00:00	17	72	0	190	6	1014	60.4
2022-10-22 18:00:00	16	77	0	170	6	1014	8.7
2022-10-22 19:00:00	15	82	0	170	6	1014	0
2022-10-22 20:00:00	15	82	0	130	4	1014	0
2022-10-22 21:00:00	14	88	0	120	6	1014	0

2022-10-22 22:00:00	14	88	0	160	4	1014	0
2022-10-22 23:00:00	15	82	0	170	7	1014	0

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